

MIDDLE EAST TECHNICAL UNIVERSITY
DEPARTMENT OF MECHANICAL ENGINEERING
ME 310 NUMERICAL METHODS
FALL 2021
PROGRAMMING PROJECT 3

Assignment date : 04.01.2022
Due date : 14.01.2022
Prepared by :

The programming project will be submitted through METU-Class, as described in the “Programming Project Assignment Guidelines”, which is posted on METU-Class.

Given $n + 1$ data points x_1, x_2, \dots, x_{n+1} and corresponding function values y_1, y_2, \dots, y_{n+1} , it is desired to fit a cubic spline $S_k(x)$ for each interval.

Let the equation of the k -th spline is defined by the following polynomial.

$$S_k(x) = s_{k,1} + s_{k,2}(x - x_k) + s_{k,3}(x - x_k)^2 + s_{k,4}(x - x_k)^3$$

where $\mathbf{s} = [s_{k,1} \ s_{k,2} \ s_{k,3} \ s_{k,4}]^T$ are the unknown coefficients.

- Express the problem in matrix form as $\mathbf{A}\mathbf{s} = \mathbf{b}$ where \mathbf{s} is the unknown coefficients.
- Write a computer program that forms \mathbf{A} and \mathbf{b} matrices and solves for \mathbf{s} .
The input of your program should be $\mathbf{x} = [x_1 \ \dots \ x_{n+1}]^T$ and $\mathbf{y} = [y_1 \ \dots \ y_{n+1}]^T$ arrays.
The output should be $n \times 4$ coefficient matrix in the form of

$$\mathbf{C} = \begin{bmatrix} s_{1,1} & s_{1,2} & s_{1,3} & s_{1,4} \\ \vdots & \vdots & \vdots & \vdots \\ s_{k,1} & s_{k,2} & s_{k,3} & s_{k,4} \\ \vdots & \vdots & \vdots & \vdots \\ s_{n,1} & s_{n,2} & s_{n,3} & s_{n,4} \end{bmatrix}$$

Notes:

You are limited with the given polynomial description; any other forms will not be graded.

Your program should read the \mathbf{x} and \mathbf{y} arrays from a given “input.txt” file, output the coefficient matrix \mathbf{C} on screen and plot the x-y points and the splines (between the end points).

A sample “input.txt” is attached.

You may use readily available equation solvers.