# Build Survival Model: Cox Proportional Hazards Model

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<pre>library(tidyverse) library(survival) library(forestplot) library(glmnet) library(ggfortify) library(kableExtra) # include knitr automatically  source("/work/users/y/u/yuukias/BIOS-Material/BIOS992/utils/csv_utils.r") # * Don't use setwd() for Quarto documents! # setwd("/work/users/y/u/yuukias/BIOS-Material/BIOS992/data")</pre>	
adjust_type <- ifelse(exists("params"), params\$adjust_type, "minimal") #  options: "minimal", "partial", "full"	

```
# string of parameters
adjust_type_str <- switch(adjust_type,
    minimal = "minimal",
    partial = "partial",
    full = "full"
)
print(paste0("Model Adjustment Type: ", adjust_type_str))</pre>
```

[1] "Model Adjustment Type: minimal"

```
impute_type_str <- switch(impute_type,
    unimputed = "unimputed",
    imputed = "imputed"
)
print(paste0("Data Imputation Type: ", impute_type_str))</pre>
```

[1] "Data Imputation Type: unimputed"

## **Load Data**

```
if (include_statin == "yes") {
    data_train <-
    read.csv(paste0("/work/users/y/u/yuukias/BIOS-Material/BIOS992/data/train_data_",
    impute_type_str, "_statin.csv"),
        header = TRUE
    )
} else {
    data_train <-
    read.csv(paste0("/work/users/y/u/yuukias/BIOS-Material/BIOS992/data/train_data_",
    impute_type_str, ".csv"),
        header = TRUE
    )
}</pre>
```

#### [1] 28127 100

```
data <- select_subset(data_train, type = adjust_type)
(dim(data))</pre>
```

#### [1] 28127 48

#### colnames(data)

```
[1] "event"
                                      "time"
 [3] "HRV_SD1"
                                      "HRV_SD2"
 [5] "HRV_SD1SD2"
                                      "HRV_S"
 [7] "HRV_CSI"
                                      "HRV_CVI"
 [9] "HRV_CSI_Modified"
                                      "HRV_PIP"
                                      "HRV_PSS"
[11] "HRV_IALS"
[13] "HRV_PAS"
                                      "HRV_GI"
[15] "HRV_SI"
                                      "HRV_AI"
[17] "HRV_PI"
                                      "HRV_C1d"
[19] "HRV_C1a"
                                      "HRV_SD1d"
[21] "HRV_SD1a"
                                      "HRV_C2d"
[23] "HRV_C2a"
                                      "HRV SD2d"
[25] "HRV_SD2a"
                                      "HRV_Cd"
                                      "HRV_SDNNd"
[27] "HRV_Ca"
[29] "HRV_SDNNa"
                                      "HRV_ApEn"
                                      "HRV_FuzzyEn"
[31] "HRV_ShanEn"
[33] "HRV_MSEn"
                                      "HRV_CMSEn"
[35] "HRV_RCMSEn"
                                      "HRV_CD"
[37] "HRV_HFD"
                                      "HRV_KFD"
[39] "HRV_LZC"
                                      "HRV_DFA_alpha1"
[41] "HRV_MFDFA_alpha1_Width"
                                      "HRV_MFDFA_alpha1_Peak"
[43] "HRV_MFDFA_alpha1_Mean"
                                      "HRV_MFDFA_alpha1_Max"
[45] "HRV_MFDFA_alpha1_Delta"
                                      "HRV_MFDFA_alpha1_Asymmetry"
[47] "HRV_MFDFA_alpha1_Fluctuation" "HRV_MFDFA_alpha1_Increment"
```

```
data <- tibble::as_tibble(data)</pre>
```

Note now the interpretation of HR is different! For example, if HR=1.16 for the predictor in the univariate model fitted using scaled data, it means that each standard deviation increase is associated with 16% higher risk of event.

```
data_complete <- na.omit(data)</pre>
```

## **Univariate Cox Proportional Hazards Model**

```
upper_ci \leftarrow exp(coef + 1.96 * se)
    p_value <- summary(cox_model_single)$coefficients[5]</pre>
    return(
        data.frame(
             predictor = predictor,
             hr = hr,
             lower_ci = lower_ci,
             upper_ci = upper_ci,
            p_value = p_value
        )
    )
})
results_univariate$hr <- round(results_univariate$hr, 2)</pre>
results_univariate$lower_ci <- round(results_univariate$lower_ci, 2)</pre>
results_univariate$upper_ci <- round(results_univariate$upper_ci, 2)
results_univariate$ci <- paste0("(", results_univariate$lower_ci, ",",

¬ results_univariate$upper_ci, ")")

results_univariate$p_value <- round(results_univariate$p_value, 3)</pre>
results_univariate <- results_univariate %>% arrange(desc(hr)) # sort
\hookrightarrow descendingly by HR
```

```
# Create forest plot
results_univariate %>%
    forestplot(
       labeltext = c(predictor, hr, ci, p_value),
       mean = hr,
       lower = lower_ci,
       upper = upper_ci,
       xlab = "Hazard Ratio",
       title = "Univariate Cox Models",
       xlog = TRUE, # * Make sure the CI are not symmetric and need to be
        boxsize = 0.2,
       xticks = c(0.8, 0.9, 1.0, 1.1, 1.2),
       clip = c(0.8, 1.2),
       zero = 1
    ) %>%
    fp_set_style(
       box = "royalblue",
       line = "darkblue",
```

```
summary = "royalblue"
) %>%

fp_add_header(
    predictor = c("Predictor", ""),
    hr = c("Hazard Ratio", "per SD increase"),
    ci = c("95% CI", ""),
    p_value = c("p-value", "")
) %>%

fp_decorate_graph(
    box = gpar(lty = 2, col = "lightgray"),
    graph.pos = 4
) %>% # change the position of forest plot
fp_set_zebra_style("#f9f9f9")
```

Univariate Cox Models

Predictor	Hazard Ratio	95% CI		p-value
	per SD increase			
HRV_PIP	1.16	(1.12,1.2)	-	0
HRV_IALS	1.15	(1.11,1.19)		0
HRV_SD1SD2	1.14	(1.11,1.18)		0
HRV_HFD	1.14	(1.1,1.18)	-	0
HRV_PAS	1.12	(1.08,1.15)		0
HRV_GI	1.12	(1.08,1.16)	-	0
HRV_SI	1.12	(1.08,1.15)	-	0
HRV_PSS	1.11	(1.07,1.15)	-	0
HRV_AI	1.11	(1.07,1.16)		0
HRV_ApEn	1.1	(1.06,1.14)	+	0
HRV_CMSEn	1.1	(1.06,1.14)	+	0
HRV_C2d	1.09	(1.05,1.12)		0
HRV_Cd	1.09	(1.05,1.13)		0
HRV_RCMSEn	1.09	(1.05,1.13)		0
HRV_C1d	1.06	(1.02,1.1)		0.001
HRV_MFDFA_alpha1_Asymmetry	1.04	(1.01,1.08)	-	0.012
HRV_MSEn	1.03	(1,1.07)	-	0.075
HRV_KFD	1.02	(1,1.04)	•	0.05
HRV_ShanEn	1.01	(0.98,1.04)	+	0.621
HRV_MFDFA_alpha1_Width	1.01	(0.98,1.05)	+	0.429
HRV_MFDFA_alpha1_Fluctuation	1	(0.97,1.04)	+	0.914
HRV_MFDFA_alpha1_Increment	1	(0.97,1.04)	+	0.788
HRV_S	0.98	(0.95,1.02)	-	0.301
HRV_MFDFA_alpha1_Mean	0.98	(0.95,1.01)	-	0.181
HRV_FuzzyEn	0.96	(0.93,0.99)		0.011
HRV_C1a	0.95	(0.91,0.98)		0.001
HRV_SD1	0.93	(0.89,0.96)		0
HRV_SD1d	0.93	(0.9,0.97)	-	0
HRV_SD1a	0.92	(0.89,0.96)		0
HRV_C2a	0.92	(0.89,0.95)	-	0
HRV_Ca	0.92	(0.89,0.95)		0
HRV_MFDFA_alpha1_Max	0.92	(0.89,0.95)		0
HRV_MFDFA_alpha1_Delta	0.92	(0.89,0.95)		0
HRV_PI	0.91	(0.88,0.94)	+	0
HRV_SDNNd	0.91	(0.88,0.95)	-	0
HRV_CD	0.91	(0.88,0.94)		0
HRV_MFDFA_alpha1_Peak	0.91	(0.87,0.94)	-	0
HRV_SD2	0.9	(0.86,0.93)	-	0
HRV_SD2d	0.9	(0.87,0.94)	-1-	0
HRV_SDNNa	0.9	(0.87,0.94)	-	0
HRV_CSI_Modified	0.89	(0.85,0.93)		0
HRV_SD2a	0.89	(0.86,0.93)		0
HRV_LZC	0.89	(0.86,0.91)	-	0
HRV_DFA_alpha1	0.88	(0.85,0.91)	-	0
HRV_CVI	0.86	(0.83,0.89)	-	0
HRV_CSI	0.85	(0.82,0.88)	223 18 229 380	339
			Hazard Ratio 2.23 2.44 2.72 3.00	-

## Multivariate Cox Proportional Hazards Model

```
cox_model_full <- coxph(Surv(time, event) ~ ., data = data)
summary(cox_model_full)

cox_model_full_complete <- coxph(Surv(time, event) ~ ., data = data_complete)
summary(cox_model_full_complete)</pre>
```

## **PH Assumption Assessment**

```
cox.zph(cox_model_full)
```

	chisq	df	р
HRV_SD1	5.01e-01	1	0.48
HRV_SD2	3.96e-01	1	0.53
HRV_SD1SD2	5.07e-01	1	0.48
HRV_S	1.07e+00	1	0.30
HRV_CSI	5.14e-01	1	0.47
HRV_CVI	4.07e-03	1	0.95
HRV_CSI_Modified	3.06e-01	1	0.58
HRV_PIP	2.45e-02	1	0.88
HRV_IALS	7.94e-02	1	0.78
HRV_PSS	5.32e-02	1	0.82
HRV_PAS	2.08e+00	1	0.15
HRV_GI	5.67e-02	1	0.81
HRV_SI	5.29e-03	1	0.94
HRV_AI	9.58e-02	1	0.76
HRV_PI	6.22e-01	1	0.43
HRV_C1d	2.73e-02	1	0.87
HRV_SD1d	6.07e-01	1	0.44
HRV_SD1a	4.64e-01	1	0.50
HRV_C2d	1.41e-02	1	0.91
HRV_SD2d	3.69e-01	1	0.54
HRV_SD2a	3.71e-01	1	0.54
HRV_Cd	1.53e-01	1	0.70
HRV_SDNNd	5.35e-01	1	0.46
HRV_SDNNa	4.43e-01	1	0.51

```
HRV_ApEn
                            1.21e+00 1 0.27
HRV_ShanEn
                            1.52e-01 1 0.70
HRV_FuzzyEn
                            2.74e-01 1 0.60
HRV_MSEn
                            9.20e-02 1 0.76
HRV_CMSEn
                            9.87e-01 1 0.32
HRV_RCMSEn
                            3.57e-01 1 0.55
HRV_CD
                            9.40e-03 1 0.92
HRV_HFD
                            1.16e-01 1 0.73
HRV_KFD
                            9.12e-01 1 0.34
HRV_LZC
                            3.76e-04 1 0.98
HRV_DFA_alpha1
                            6.29e-01 1 0.43
HRV_MFDFA_alpha1_Width
                            4.90e-02 1 0.82
                            1.41e-01 1 0.71
HRV_MFDFA_alpha1_Peak
HRV_MFDFA_alpha1_Mean
                            3.71e-02 1 0.85
HRV_MFDFA_alpha1_Max
                            5.88e-01 1 0.44
HRV_MFDFA_alpha1_Delta
                            1.75e-01 1 0.68
HRV_MFDFA_alpha1_Asymmetry
                            5.36e-05 1 0.99
HRV_MFDFA_alpha1_Fluctuation 4.43e-01 1 0.51
HRV_MFDFA_alpha1_Increment
                            1.79e-01 1 0.67
GLOBAL
                            2.95e+01 43 0.94
```

## cox.zph(cox\_model\_full\_complete)

	chisq	df	р
HRV_SD1	5.01e-01	1	0.48
HRV_SD2	3.96e-01	1	0.53
HRV_SD1SD2	5.07e-01	1	0.48
HRV_S	1.07e+00	1	0.30
HRV_CSI	5.14e-01	1	0.47
HRV_CVI	4.07e-03	1	0.95
HRV_CSI_Modified	3.06e-01	1	0.58
HRV_PIP	2.45e-02	1	0.88
HRV_IALS	7.94e-02	1	0.78
HRV_PSS	5.32e-02	1	0.82
HRV_PAS	2.08e+00	1	0.15
HRV_GI	5.67e-02	1	0.81
HRV_SI	5.29e-03	1	0.94
HRV_AI	9.58e-02	1	0.76
HRV_PI	6.22e-01	1	0.43
HRV_C1d	2.73e-02	1	0.87
HRV_SD1d	6.07e-01	1	0.44
HRV_SD1a	4.64e-01	1	0.50

```
HRV_C2d
                             1.41e-02 1 0.91
HRV_SD2d
                             3.69e-01 1 0.54
HRV_SD2a
                             3.71e-01 1 0.54
HRV_Cd
                             1.53e-01 1 0.70
HRV SDNNd
                             5.35e-01 1 0.46
HRV_SDNNa
                             4.43e-01 1 0.51
HRV ApEn
                             1.21e+00 1 0.27
HRV_ShanEn
                             1.52e-01 1 0.70
                            2.74e-01 1 0.60
HRV_FuzzyEn
HRV_MSEn
                            9.20e-02 1 0.76
                            9.87e-01 1 0.32
HRV_CMSEn
                            3.57e-01 1 0.55
HRV_RCMSEn
HRV_CD
                            9.40e-03 1 0.92
HRV_HFD
                             1.16e-01 1 0.73
HRV_KFD
                            9.12e-01 1 0.34
HRV_LZC
                            3.76e-04 1 0.98
HRV_DFA_alpha1
                            6.29e-01 1 0.43
HRV_MFDFA_alpha1_Width
                            4.90e-02 1 0.82
HRV_MFDFA_alpha1_Peak
                            1.41e-01 1 0.71
HRV MFDFA alpha1 Mean
                            3.71e-02 1 0.85
HRV_MFDFA_alpha1_Max
                            5.88e-01 1 0.44
HRV MFDFA alpha1 Delta
                            1.75e-01 1 0.68
HRV_MFDFA_alpha1_Asymmetry 5.36e-05 1 0.99
HRV_MFDFA_alpha1_Fluctuation 4.43e-01 1 0.51
HRV_MFDFA_alpha1_Increment
                            1.79e-01 1 0.67
GLOBAL
                             2.95e+01 43 0.94
```

The proportional hazards assumption was tested using Schoenfeld residuals. None of the variables violated the PH assumption (all p > 0.05), indicating that the Cox proportional hazards model was appropriate for our analysis.

## Variable Selection

## **LASSO**

```
# * LASSO doesn't allow missing values
set.seed(1234)
x <- as.matrix(data_complete %>% select(-c(time, event)))
y <- Surv(data_complete$time, data_complete$event)
cox_model_lasso.cv <- cv.glmnet(</pre>
```

```
x,
y,
family = "cox",
alpha = 1, # 1 for LASSO, 0 for Ridge
nfolds = 10
)
# plot(cox_model_lasso.cv) # Plot partial likelihood deviance vs log(lambda)
print(cox_model_lasso.cv$lambda.min)
```

## [1] 0.0002914579

```
print(cox_model_lasso.cv$lambda.1se)
```

#### [1] 0.01592024

As mentioned in the paper, we will use the value of hyperparameter lambda.1se that gave the most shrunk model but still was within one standard error from the value that gave the lowest error. This is shown to produce consistently better performance than lambda.min.

```
cox_model_lasso <- glmnet(
    x,
    y,
    family = "cox",
    alpha = 1,
    lambda = cox_model_lasso.cv$lambda.1se
)
cox_model_lasso.coef <- coef(cox_model_lasso)
print(cox_model_lasso.coef)</pre>
```

```
46 x 1 sparse Matrix of class "dgCMatrix" s0

HRV_SD1 .

HRV_SD2 .

HRV_SD1SD2 .

HRV_S .

HRV_CSI -0.0009671365

HRV_CVI -0.0344744471

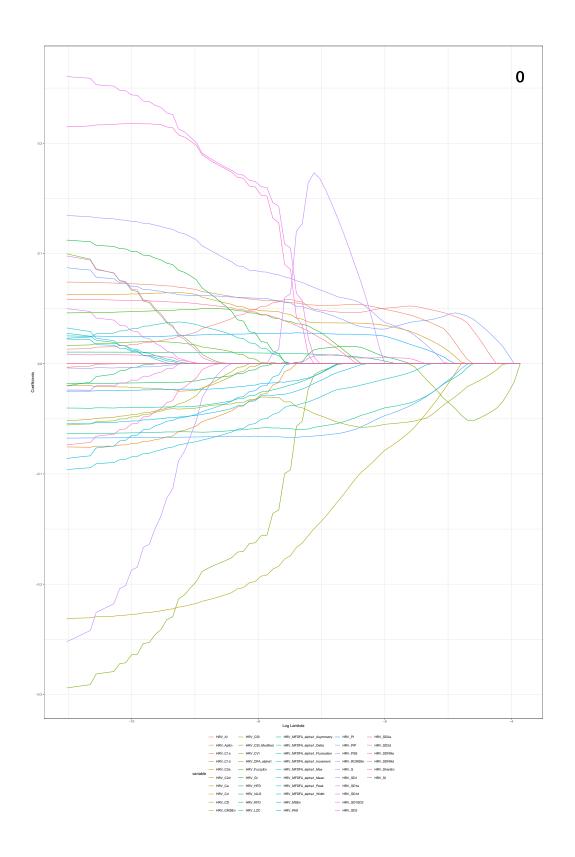
HRV_CSI_Modified .

HRV_PIP 0.0158238222
```

```
HRV_IALS
HRV_PSS
HRV_PAS
HRV_GI
HRV_SI
HRV_AI
HRV_PI
{\tt HRV\_C1d}
HRV_C1a
{\tt HRV\_SD1d}
HRV_SD1a
HRV_C2d
HRV_C2a
HRV_SD2d
HRV_SD2a
HRV_Cd
HRV_Ca
HRV_SDNNd
HRV_SDNNa
HRV_ApEn
HRV_ShanEn
HRV_FuzzyEn
HRV_MSEn
HRV_CMSEn
HRV_RCMSEn
HRV_CD
HRV_HFD
HRV_KFD
HRV_LZC
HRV_DFA_alpha1
HRV_MFDFA_alpha1_Width
HRV_MFDFA_alpha1_Peak
HRV_MFDFA_alpha1_Mean
HRV_MFDFA_alpha1_Max
HRV_MFDFA_alpha1_Delta
HRV_MFDFA_alpha1_Asymmetry
HRV_MFDFA_alpha1_Fluctuation .
HRV_MFDFA_alpha1_Increment
selected_vars <- rownames(cox_model_lasso.coef)[which(cox_model_lasso.coef !=</pre>
→ 0)]
print(selected_vars)
```

## [1] "HRV\_CSI" "HRV\_CVI" "HRV\_PIP"

```
# * To visualize the LASSO path, we should not supply lambda
cox_model_lasso_fullpath <- glmnet(
    x,
    y,
    family = "cox",
    alpha = 1
)</pre>
```



#### Stepwise Selection based on BIC

```
# * Stepwise selection doesn't allow missing values
cox_model_step <- MASS::stepAIC(cox_model_full_complete,</pre>
   direction = "both",
   k = log(nrow(data)), # Use BIC instead of AIC
   trace = FALSE
)
summary(cox_model_step)
Call:
coxph(formula = Surv(time, event) ~ HRV_SD1 + HRV_CVI + HRV_PIP +
   HRV_PI + HRV_RCMSEn + HRV_CD, data = data_complete)
 n= 27198, number of events= 3435
             coef exp(coef) se(coef) z Pr(>|z|)
                   1.45428 0.06154 6.086 1.16e-09 ***
HRV SD1
          0.37451
                   HRV_CVI
         -0.26757
HRV PIP
          0.09227 1.09666 0.02344 3.936 8.28e-05 ***
HRV_PI
         -0.12237
                   0.88482 0.02044 -5.986 2.15e-09 ***
                   1.14900 0.02187 6.350 2.15e-10 ***
HRV_RCMSEn 0.13889
                   HRV_CD
         -0.16319
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
         exp(coef) exp(-coef) lower .95 upper .95
HRV_SD1
            1.4543
                      0.6876
                               1.2890
                                       1.6407
HRV_CVI
            0.7652
                      1.3068 0.6990
                                       0.8378
            1.0967
HRV_PIP
                      0.9119 1.0474
                                       1.1482
HRV_PI
            0.8848
                      1.1302 0.8501 0.9210
HRV_RCMSEn
                      0.8703 1.1008 1.1993
            1.1490
                      1.1773 0.8099
HRV_CD
            0.8494
                                        0.8909
Concordance= 0.574 (se = 0.005)
Likelihood ratio test= 209.3 on 6 df, p=<2e-16
Wald test
                  = 195.1 on 6 df, p=<2e-16
```

Score (logrank) test = 195.8 on 6 df, p=<2e-16

## **Summary of Variable Selection**

We will compare the selection of variables from all models we have built.

```
# Obtain the selected variables from all models
variable_names_all <- colnames(data) %>%
    setdiff(c("time", "event"))
variable_names_univariate <- results_univariate %>%
    filter(p_value < 0.05) %>%
   pull(predictor)
variable_names_multivariate <- summary(cox_model_full_complete)$coefficients</pre>
as.data.frame() %>%
   rownames_to_column(var = "predictor") %>% # transpose, "predictor" will
    → now be the column name
   filter(Pr(>|z|) < 0.05) \%>\%
   pull(predictor)
variable_names_lasso <-
rownames(cox_model_lasso.coef)[which(cox_model_lasso.coef != 0)]
variable_names_step <- summary(cox_model_step)$coefficients %>%
    as.data.frame() %>%
   filter(`Pr(>|z|)` < 0.05) %>%
   rownames()
```

```
variable_selection_matrix <- matrix(
          0,
          nrow = length(variable_names_all),
          ncol = 4 # univariate, multivariate, lasso, stepwise
)

colnames(variable_selection_matrix) <- c("univariate", "multivariate",
          "lasso", "stepwise")

rownames(variable_selection_matrix) <- variable_names_all

for (variable in variable_names_all) {
    if (variable %in% variable_names_univariate) {
        variable_selection_matrix[variable, "univariate"] <- 1
    }
    if (variable %in% variable_names_multivariate) {</pre>
```

```
variable_selection_matrix[variable, "multivariate"] <- 1
}
if (variable %in% variable_names_lasso) {
   variable_selection_matrix[variable, "lasso"] <- 1
}
if (variable %in% variable_names_step) {
   variable_selection_matrix[variable, "stepwise"] <- 1
}</pre>
```

```
symbol_selected <- "*"
selection_table <- data.frame(</pre>
   Variable = variable names all,
   Univariate = ifelse(variable_selection_matrix[, "univariate"] == 1,

    symbol selected, ""),
   Multivariate = ifelse(variable_selection_matrix[, "multivariate"] == 1,

    symbol_selected, ""),
   LASSO = ifelse(variable_selection_matrix[, "lasso"] == 1,

    symbol_selected, ""),
    Stepwise = ifelse(variable_selection_matrix[, "stepwise"] == 1,

    symbol_selected, "")

) %>%
   mutate(Num_Selected = rowSums(variable_selection_matrix)) %>%
    arrange(desc(Num_Selected), Variable) %>%
    as.data.frame() %>%
    remove rownames()
variable_categories <- sapply(variable_names_all, determine_category)</pre>
category_colors <- c(</pre>
    "covariate" = "#FFB6C1", #
           = "#1E90FF", #
    "frequency" = "#32CD32", #
    "poincare" = "#FF4500", #
    "entropy" = "#FF8C00", #
    "fractal" = "#FFD700", #
    "unknown" = "#000000" #
category_colors_names <- c(</pre>
    "covariate" = "pink", #
    "time" = "blue", #
```

```
"frequency" = "green", #
    "poincare" = "red", #
    "entropy" = "orange", #
    "fractal"
                = "gold" #
category_legend <- sapply(names(category_colors_names), function(cat) {</pre>
    sprintf(
        "%s: %s",
        tools::toTitleCase(cat),
        tools::toTitleCase(category_colors_names[cat])
    )
}) %>%
   paste(collapse = "; ")
selection_table %>%
   kbl(
        caption = "Variable Selection by Different Models",
        align = c("|1", "c", "c", "c", "c", "c"),
        col.names = c("Variable", "Univariate", "Multivariate", "LASSO",

    "Stepwise", "Selected Times"),

        longtable = TRUE
    ) %>%
   kable styling(
        bootstrap_options = c("striped", "hover", "condensed", "responsive"),
        position = "center",
        font_size = 9,
        latex_options = c("repeat_header", "striped", "HOLD_position")
    ) %>%
    # Add color for different categories of variables
    column_spec(1,
        color =
        category_colors[variable_categories[selection_table$Variable]],
        bold = TRUE
    ) %>%
    # Add a header colname for four columns: Univariate, Multivariate, LASSO,

→ Stepwise

    add_header_above(c(
       " " = 1.
        "Selection Methods" = 4,
        " " = 1
    )) %>%
```

```
footnote(
    general = sprintf("%s", category_legend),
    general_title = "Note:"
)
```

```
Warning: 'xfun::attr()' is deprecated.
Use 'xfun::attr2()' instead.
See help("Deprecated")

Warning: 'xfun::attr()' is deprecated.
Use 'xfun::attr2()' instead.
See help("Deprecated")
```

Table 1: Variable Selection by Different Models

Variable	Univariate	Multivariate	LASSO	Stepwise	Selected Times
HRV_CVI	*	*	*	*	4
HRV_CD	*	*		*	3
HRV_PI	*	*		*	3
HRV_PIP	*		*	*	3
HRV_RCMSEn	*	*		*	3
HRV_ApEn	*	*			2
HRV_CSI	*		*		2
HRV_LZC	*	*			2
HRV_SD1	*			*	2
HRV_AI	*				1
HRV_C1a	*				1
HRV_C1d	*				1
HRV_C2a	*				1
HRV_C2d	*				1
HRV_CMSEn	*				1
HRV_CSI_Modified	*				1
HRV_Ca	*				1
HRV_Cd	*				1
HRV_DFA_alpha1	*				1
HRV_FuzzyEn	*				1
HRV_GI	*				1
HRV_HFD	*				1
HRV_IALS	*				1
HRV_MFDFA_alpha1_Asymmetry	*			_	1
HRV_MFDFA_alpha1_Delta	*				1
HRV_MFDFA_alpha1_Max	*				1
HRV_MFDFA_alpha1_Peak	*				1
HRV_PAS	*				1
HRV_PSS	*				1

Table 1: Variable Selection by Different Models (continued)

Variable	Univariate	Multivariate	LASSO	Stepwise	Selected Times
HRV_S		*			1
HRV_SD1SD2	*				1
HRV_SD1a	*				1
HRV_SD1d	*				1
HRV_SD2	*				1
HRV_SD2a	*				1
HRV_SD2d	*				1
HRV_SDNNa	*				1
HRV_SDNNd	*				1
HRV_SI	*				1
HRV_KFD					0
HRV_MFDFA_alpha1_Fluctuation					0
HRV_MFDFA_alpha1_Increment					0
HRV_MFDFA_alpha1_Mean					0
HRV_MFDFA_alpha1_Width					0
HRV_MSEn					0
HRV_ShanEn					0

Note:

Covariate: Pink; Time: Blue; Frequency: Green; Poincare: Red; Entropy: Orange; Fractal: Gold