



Programming in Python

Lecture 4- Functions

Plan for today

- Functions
 - What are they good for
 - Built-in Functions
 - Defining New Functions
 - Functions call functions
- Lambda
- Recursion

Reminder

- If statements
- For loop
- While loop

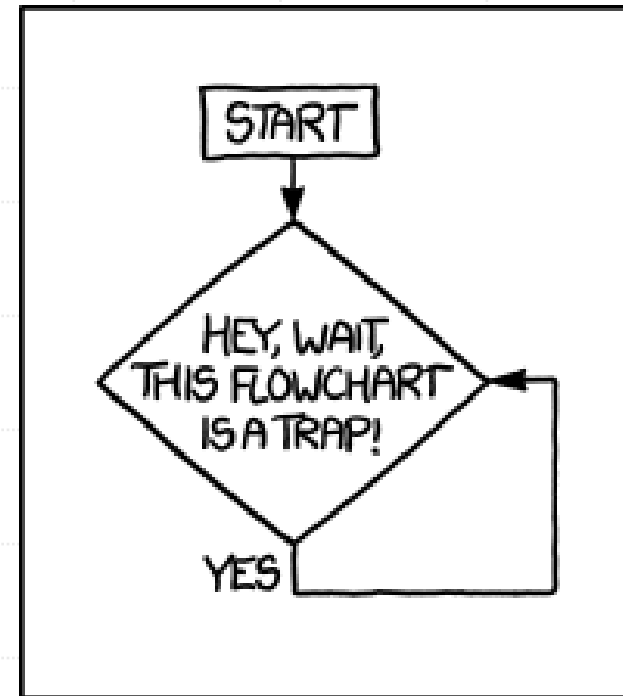
Flow Control

Different inputs → Different execution order

- Computer games
- Illegal input

Control structures

- **if-else**
- **for loop**
- **while loop**



<http://xkcd.com/1195/>

Conditional Statement: if

Used to execute statements conditionally

Syntax

if *condition*:

statement1

statement2

*If condition is **True**, statements are executed*

Condition = *expression that evaluates to a Boolean*

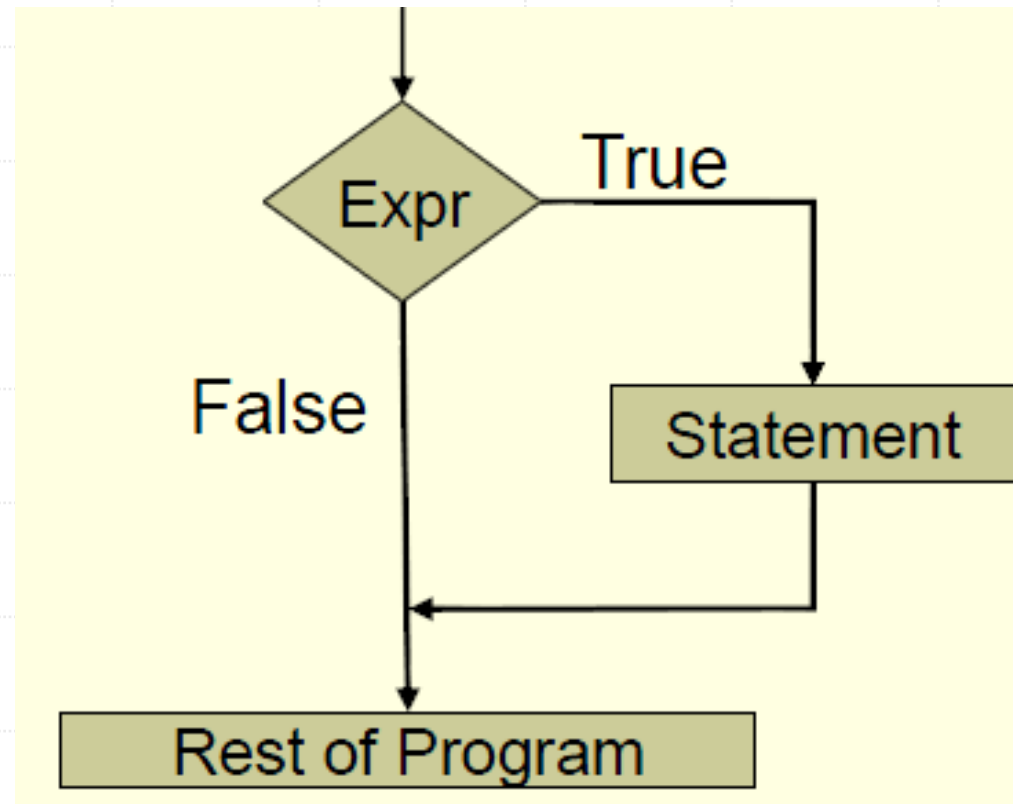
Indentation:

Following the if statement:

Open a new scope = one tab to the right.

Indicates the commands within the scope of this if.

Conditional Statements



elif

if condition1:

statement1

elif condition2:

statement2

else:

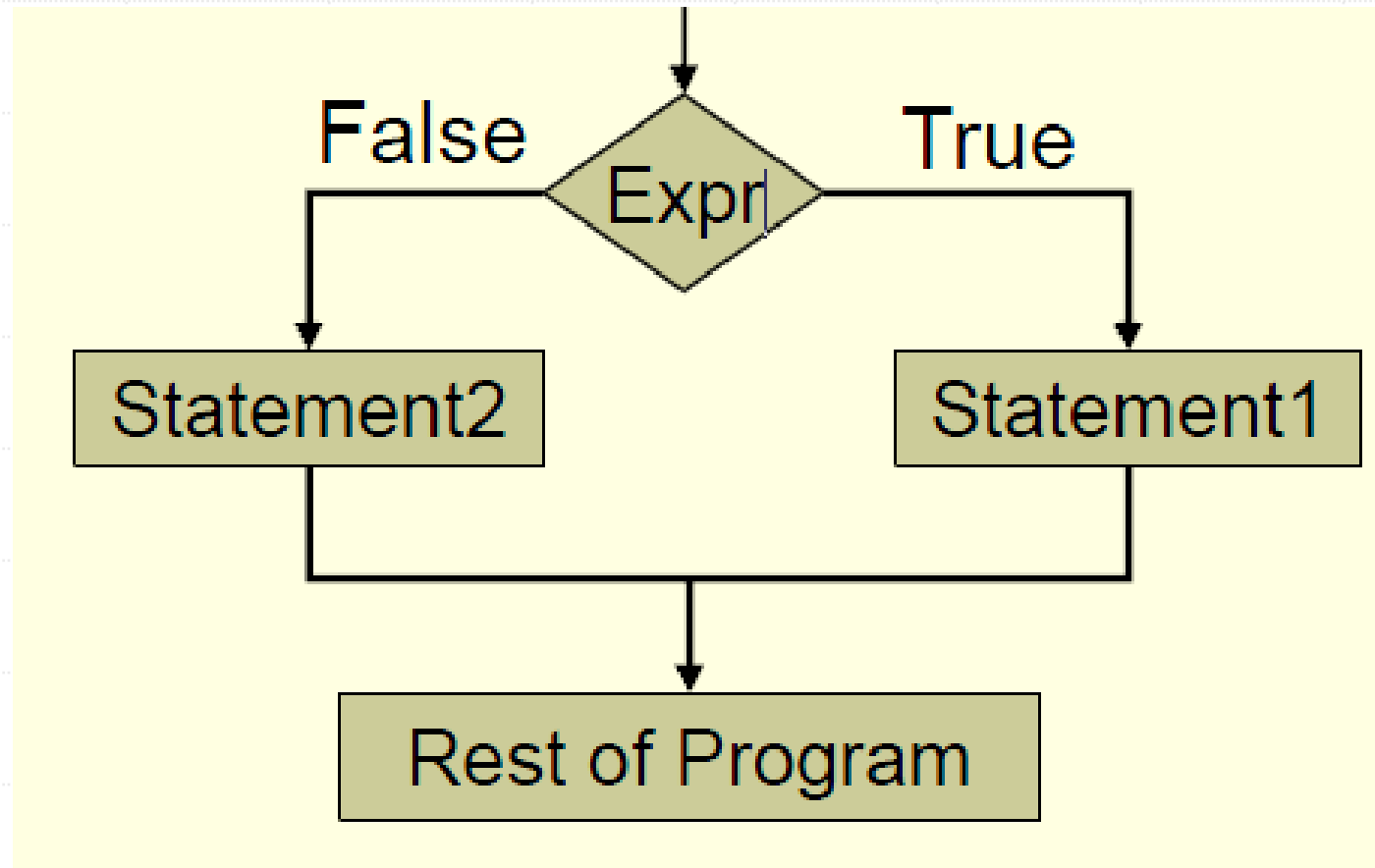
statement3

condition1 is true → execute *statement1*

condition1 false and **condition2** true → execute *statement2*

both conditions are false → execute *statement3*

elif



For Loop

for element **in** iterable:

statement1

statement2

...

Run over all elements in the object (list, string, etc.)

Iteration 0: Assign element = object[0]

- Execute the statements

Iteration 1: Assign *element* = object[1]

- Execute the statements

...

Range

An ordered list of integers in the range.

```
>>> range(10)
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

`range(from, to)` contains all integers k satisfying $\text{from} \leq k < \text{to}$.

`range(to)` is a shorthand for `range(0, to)`.

```
>>> range(2, 10)
[ 2, 3, 4, 5, 6, 7, 8, 9]
```

```
>>> range(-2, 2)
[-2, -1, 0, 1]
```

```
>>> range(4, 2)
[]
```

Range

```
>>> type(range(3))  
<type 'list'>
```

Step size:

range(from, to, step) returns:

*from, from+step, from+2*step, ..., from+i*step*
until *to* is reached, not including to itself.

```
>>> range(0, 10, 2)  
[0, 2, 4, 6, 8]  
>>> range(10, 0, -2)  
[10, 8, 6, 4, 2]
```

While Loop

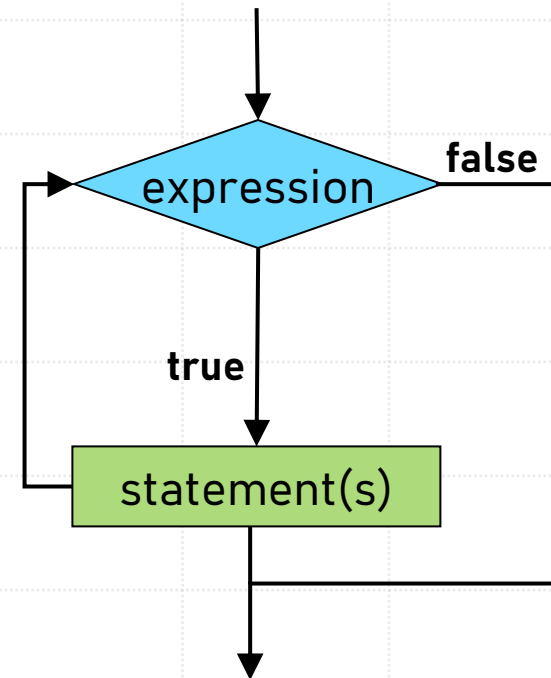
Used to repeat the same instructions until a stop criterion is met

while *expression*:

statement1

statement2

...



Homework

1. Create a Python program to get the largest/smallest number from a list

Input:

```
>>> s=[2,5,7,3,4,6]
```

Output:

```
>>> The max number is: 7
```

```
>>> The min number is: 2
```

2. Create a Python program to count the number of strings where the string length is 2 or more and the first and last character are same from a given list of strings

Input:

```
>>> words=['drd','1435','savg','11','sys','1321','10934','121']
```

Output:

```
>>> ['drd', 'sys', '1321', '121']
```

Homework

3. Create a Python program to count all the names that start with "M" from a given list

Input:

```
>>> names = ['Mor','Yuval', 'Many','Eli','Moshe']
```

Output:

```
>>> 3
```

4. Create a Python script to calculate to price of Apple, Milk and Meat

Input:

```
>>> Supermarket_list={"Apple":10,"Eggs":5,"Milk":5,"Bread":3,"Meat":20}
```

Output:

```
>>> 35
```

Plan for today

- **Functions**
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 - Functions call functions
- **Lambda**
- **Recursion**

What is a **function** in programming ?

- A function is a block of organized, reusable code that is used to perform a single, well defined action.
- Functions provide better modularity for your application and a high degree of code reusing

How to Calculate $4! + 7! + 9!$?

```
factorial4 = 1
```

```
factorial7 = 1
```

```
factorial9 = 1
```

```
for i in range(1, 5):
```

```
    factorial4 *= i
```

```
for i in range(1, 8):
```

```
    factorial7 *= i
```

```
for i in range(1, 10):
```

```
    factorial9 *= i
```

```
print ("4!+7!+9!=", factorial4 + factorial7 + factorial9)
```

Why use functions ?

- **We** wrote code calculating $4! + 7! + 9!$.

To use the code in 3 different calculations, he:

- copy & pasted
- assigned arguments

3 times.

The calculation took 0.0046 microseconds.

- There is a more efficient algorithm to calculate $4! + 7! + 9!$.
- To update the code, he went over the 3 calculations ☹️
- After the update, the calculation took only 0.0006 microseconds – over 7 times faster!

→ Don't duplicate code, use functions !

How to Calculate $4! + 7! + 9!$?

```
def factorial(n):
```

```
    fact = 1
```

```
    for i in range(1,n+1):
```

```
        fact *= i
```

```
    return fact
```

```
print ('4!+7!+9!=', factorial(4) + factorial(7) + factorial(9))
```

Modularity enables code reuse !

Definition

Modularity is the degree to which a system's components may be separated and recombined (Wikipedia).

- Top-down design
- Improves maintainability
- Enforces logical boundaries between components



Scope of a function

- Variables defined within a function are considered **local**, and can be used only within the function's block of code.
- Local variables can mask variables with the same name defined outside of a function (**Global** variables).

So – Why use functions?

- **Modularity** - Break a task into smaller sub-tasks (divide and conquer), enables code reuse
- **Abstraction** – Solve each problem once and wrap it in a function
- **Maintenance** - Solve bugs once
- **Readability** – Main code is shorter, implementation details are hidden within functions
- **Limited Variable Scope** - Temporary variables are restricted to the function's scope

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Built-in Functions

<http://docs.python.org/library/functions.html>

We already used built-in functions:

```
>>> type(5)
```

```
<type 'int'>
```

```
>>> len(range(8,100, 8))
```

```
12
```


Built-in Functions

Conversion functions:

```
>>> 5.__str__
```

```
'5'
```

```
>>> 3.2.__int__
```

```
3
```

```
>>> '3.14'.__float__
```

```
3.14
```

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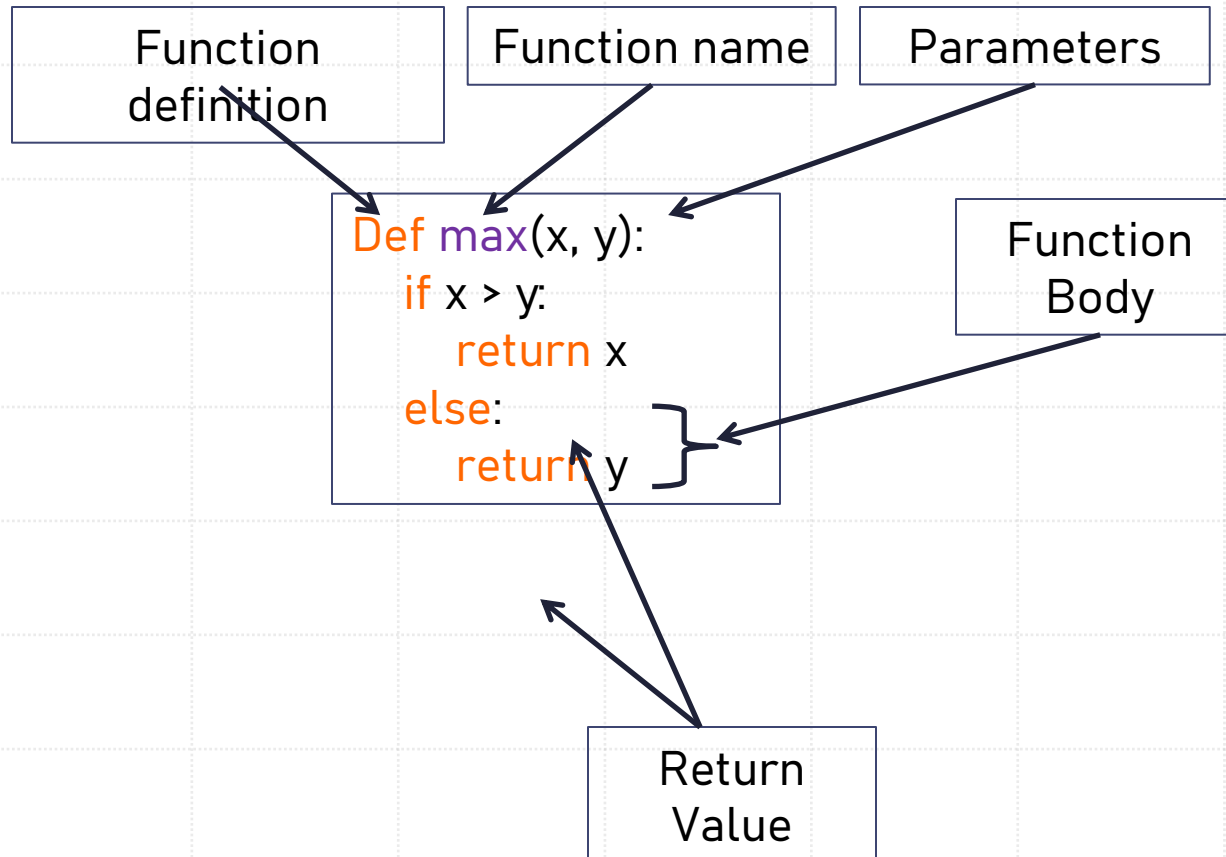
Functions

```
def function_name(argument1, argument2,...):  
    statement1  
    statement2  
    ...  
    return result1, result2, ... # optional, returns the  
                                constant None if not  
                                specified
```

Calling a function:

```
var1, var2,... = function_name(val1, val2,...)
```

Function Definition in Python



Function's Input / Output

Input: Arguments

Can be of any type - int / float / str / Boolean / list

Output: The *Return* statement

Returns a value to the function caller.

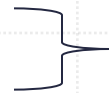
- Returned value can be any Python type
 - Multiple values are wrapped in list
- If no *Return* or no values is specified - returns *None*
- **Different from print**
- ***Return* stops the function's execution and returns to the caller**

Back to the factorial example...

Avoiding Code Duplication

Calculate $4! + 7! + 9!$ using a function:

```
def factorial(n):  
    fact = 1  
    for i in range(1,n+1):  
        fact *= i  
    return fact
```



Defining a new function

```
print "4!+7!+9!=", factorial(4) + factorial(7) + factorial(9)
```

Programming Style

- Comments: #
- Meaningful variables names

Why is it important?

Example - Palindromes

Palindromes are read the same way in either direction.

Examples

- 21.11.12
- Alula
- Anna
- Deified

Example - Palindromes

Pseudo-code

Translate a verbal description to code.

For every index in the string:

Check if the i^{th} letter is equal to the $(n-i)^{\text{th}}$ letter

If not return False (this is not a palindrome)

If all indexes were checked – this is a palindrome

Palindromes – Code

```
def is_palindrome(text):  
    for i in range(len(text) / 2):  
        if text[i] != text[- i - 1]:  
            return False  
    return True
```


```
def is_palindrome(text):  
    return text == text[::-1]
```

Passing Arguments to Functions

In a function call, **before** execution:
argument **values** are assigned to function arguments **by order**.

```
calculator(2, 3, '*')
```

```
def calculator(x, y, op):  
    if op == '+':  
        return x+y  
    elif ...  
    else:  
        return None
```



Questions?



Hands On

Example I

```
def add(a, b):  
    print "ADDING %d + %d" % (a, b)  
    return a + b  
  
def subtract(a, b):  
    print "SUBTRACTING %d - %d" % (a, b)  
    return a - b  
  
def multiply(a, b):  
    print "MULTIPLYING %d * %d" % (a, b)  
    return a * b  
  
def divide(a, b):  
    print "DIVIDING %d / %d" % (a, b)  
    return a / b  
  
print "Let's do some math with just functions!"  
  
age = add(30, 5)  
height = subtract(78, 4)  
weight = multiply(90, 2)  
iq = divide(100, 2)  
  
print "Age: %d, Height: %d, Weight: %d, IQ: %d" %  
      (age, height, weight, iq)
```

Let's do some math with just functions!

ADDING 30 + 5

SUBTRACTING 78 - 4

MULTIPLYING 90 * 2

DIVIDING 100 / 2

Age: 35, Height: 74, Weight: 180, IQ: 50

Example II

"The output of one function, is the input of another!"

```
def add(a, b):  
    print "ADDING %d + %d" % (a, b)  
    return a + b  
  
def subtract(a, b):  
    print "SUBTRACTING %d - %d" % (a, b)  
    return a - b  
  
def multiply(a, b):  
    print "MULTIPLYING %d * %d" % (a, b)  
    return a * b  
  
def divide(a, b):  
    print "DIVIDING %d / %d" % (a, b)  
    return a / b  
  
print "Here is a puzzle."  
  
what = add(age, subtract(height, multiply(weight, divide(iq, 2))))  
  
print "That becomes: ", what
```

Here is a puzzle.
DIVIDING 50 / 2
MULTIPLYING 180 * 25
SUBTRACTING 74 - 4500
ADDING 35 + -4426
That becomes: -4391

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Functions call functions

```
def print_text():  
    print "Is this the real life"  
    print "Is this the real life or it's just fantasy"  
  
def text_2():  
    print_text()  
    print_text()  
  
>>> text_2()
```

Is this the real life

Is this the real life or it's just fantasy

Is this the real life

Is this the real life or it's just fantasy

Default Arguments For Functions

- We can specify default values for the arguments of the function.
- The default value will be used only when the function is called **without** specifying a value for the argument.

```
def f1(x, y=1):  
    return x+y
```

```
>>> f1(1, 2)    # In this call: x = 1, y = 2
```

```
3
```

```
>>> f1(3)    # In this call: x = 3, y = 1 (the default value)
```

```
4
```

```
>>> f1()    # x doesn't have a default value, it must be specified
```

```
Traceback (most recent call last):
```

```
  File "<pyshell#12>", line 1, in <module>
```

```
    f1()
```

```
TypeError: f1() takes at least 1 argument (0 given)
```

More about a function's scope

Consider the following function, operating on two arguments:

```
def linear_combination(x, y):  
    y = 2 * y  
    return x + y
```

The formal parameters `x` and `y` are **local within the function's scope**, and their "life time" is just the execution of the function. They **disappear** when the function is returned.

Local vs. Global variables

- A **local** variable is defined within a function, and exists only within that function.
- A **global** variable is defined in the main script (outside of any function) and it is known globally (including within functions).

Global variables can be accessed within functions.

Defining a variable by the same name will create a local variable hiding the global variable

Local variables exist only with the function in which they were defined

```
def myFunc():  
    localVar = 5  
    print localVar  
    print globalVar
```

```
globalVar = 10  
myFunc()  
print globalVar+1  
# print localVar ### Error
```

The scope
of
variable
'localVar'

The scope
of variable
'globalVar'
is the
entire
program

5
10
11

Questions?



Hands On

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Lambda

- Lambda is a special command that is used to quickly create in-line functions for specific usecases.
- The lambda operator or lambda function is a way to create small anonymous functions, i.e. functions without a name .
- These functions are throw-away functions, i.e. they are just needed where they have been created.

Lambda

- Example
- a simple function that returns a number multiplied by itself

```
def num_func (num):
```

```
    result = num ** 2
```

```
    return result
```

```
print(num_func(8))
```

```
>>> 64
```

```
num_lamb = lambda num: num ** 2
```

```
print(num_lamb(8))
```

```
>>> 64
```

- The basic structure of a lambda statement – lambda input: output

Lambda

- lambda expression can accept multiple parameters

```
bigger = lambda num1, num2: num1 > num2
```

```
print(bigger(100,67))
```

```
>>> True
```

```
print(bigger(100,670))
```

```
>>> False
```

Lambda

- lambda with if statements, for loop and while loop

```
starts_with = lambda x: True if x[0]=='P' else False
```

```
print(starts_with('Python'))
```

```
>>> True
```

```
print(starts_with('Java'))
```

```
>>> False
```

Lambda

- lambda with if statements, for loop and while loop

```
starts_with = lambda x: True if x[0]=='P' else False
```

```
print(starts_with('Python'))
```

```
>>> True
```

```
print(starts_with('Java'))
```

```
>>> False
```

Lambda

- Filter()-offers an elegant way to filter out all the elements of a sequence "sequence", for which the function function returns True

```
nums = [2, 4, -6, -9, 11, -12, 14, -5, 17]
```

```
total_negative_nums = list(filter(lambda n:n<0,nums))
```

```
total_positive_nums = list(filter(lambda p:p>0,nums))
```

```
print("Sum of the positive numbers: ",sum(total_negative_nums))
```

```
print("Sum of the negative numbers: ",sum(total_positive_nums))
```

```
>>> Sum of the positive numbers: -32
```

```
>>> Sum of the negative numbers: 48
```

Questions?



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Recursion

Recursive function:

A function whose implementation calls itself (with different arguments).

Recursive Solution

A solution to a “large” problem using solutions to “small” problems that assemble it.

Recursion

- In every recursive call the problem is reduced.
- When the problem is small enough - solve directly (base case).

A divide and conquer
strategy

Iterative Versus Recursive

Step by step (iteratively):

$$n! = 1 * 2 * 3 * \dots * n$$

$$4! = 1 * 2 * 3 * 4 = 2 * 3 * 4 = 6 * 4 = 24$$

Recursively:

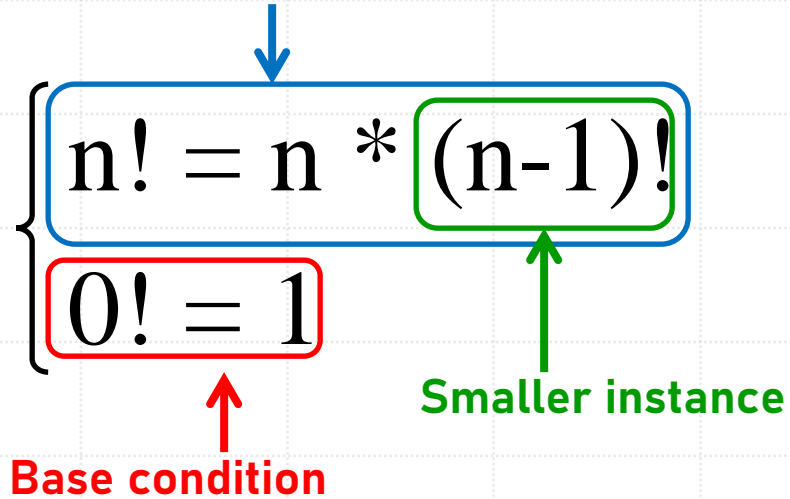
$$\begin{cases} n! = n * (n-1)! \\ 0! = 1 \end{cases}$$

$$\begin{aligned} 4! &= 4 * 3! \\ &= 4 * (3 * 2!) \\ &= 4 * (3 * (2 * 1!)) \\ &= 4 * (3 * (2 * (1 * 0!))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) = 4 * 6 = 24 \end{aligned}$$

Recursive Definition

Factorial

Calculate result using a recursive call



Pros and Cons

Pros

Short

Natural for
some problems



Cons

Computational inefficient

Hard to understand



Recursion Example in Python

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```

stop condition



calculate the result
using a recursive call

advance towards base case



Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```

factorial(4)

n

4

Returns...

Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```

factorial(4)

n

4

Returns...

Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```



factorial(4)

n

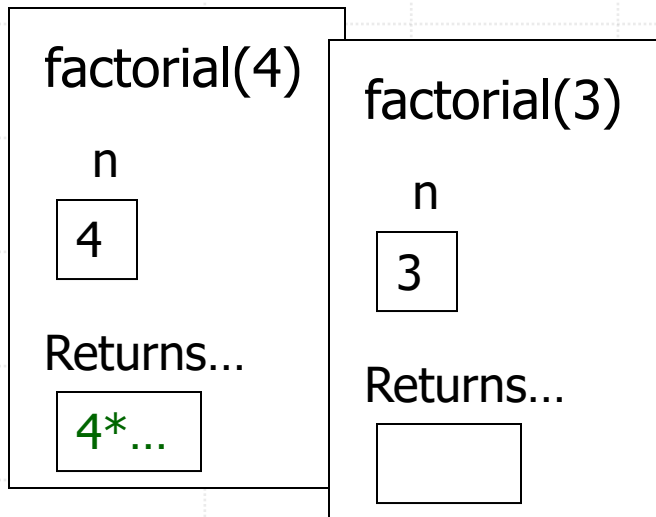
4

Returns...

4*...

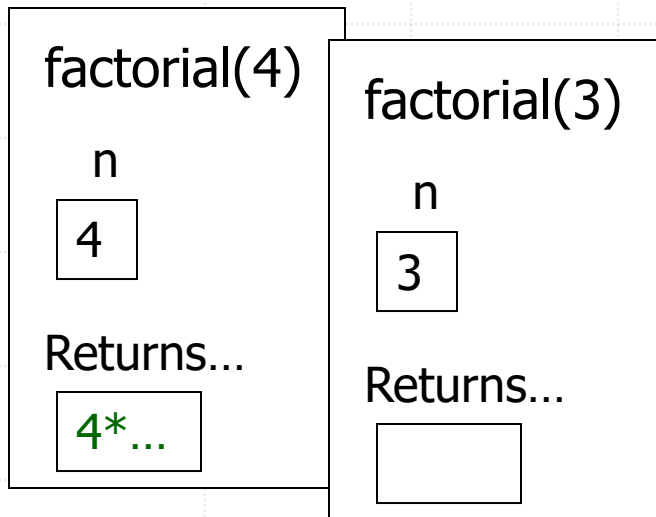
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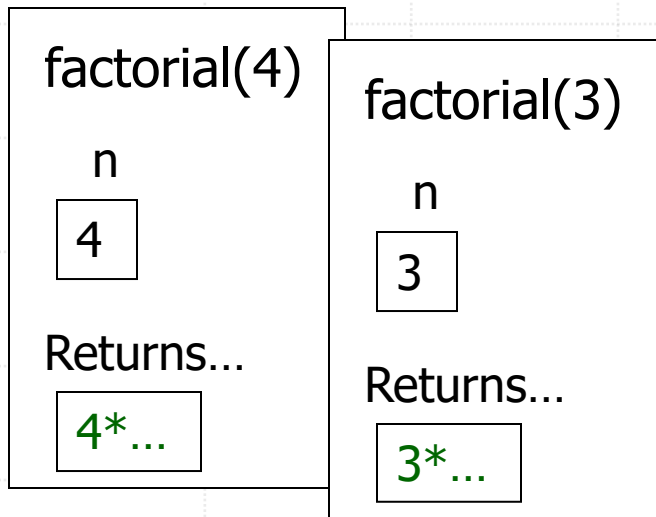
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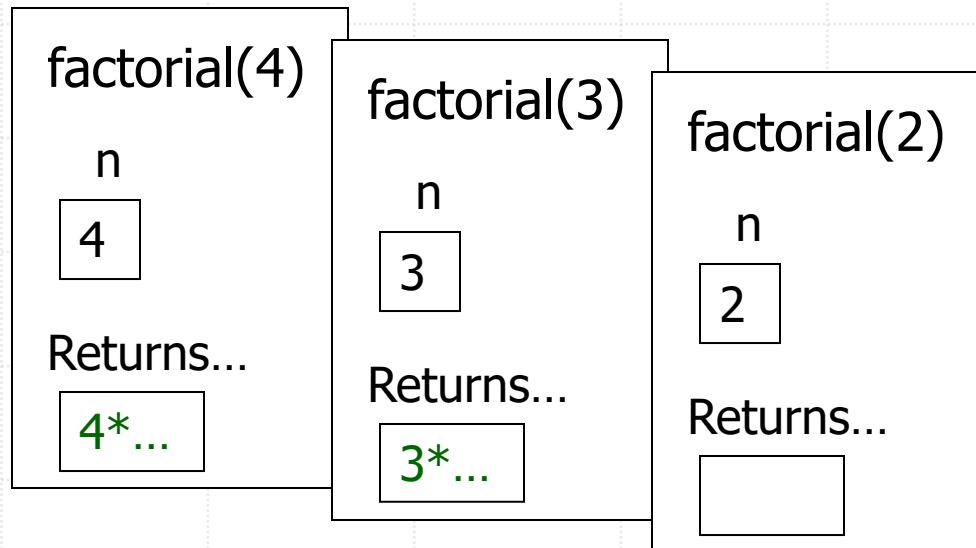
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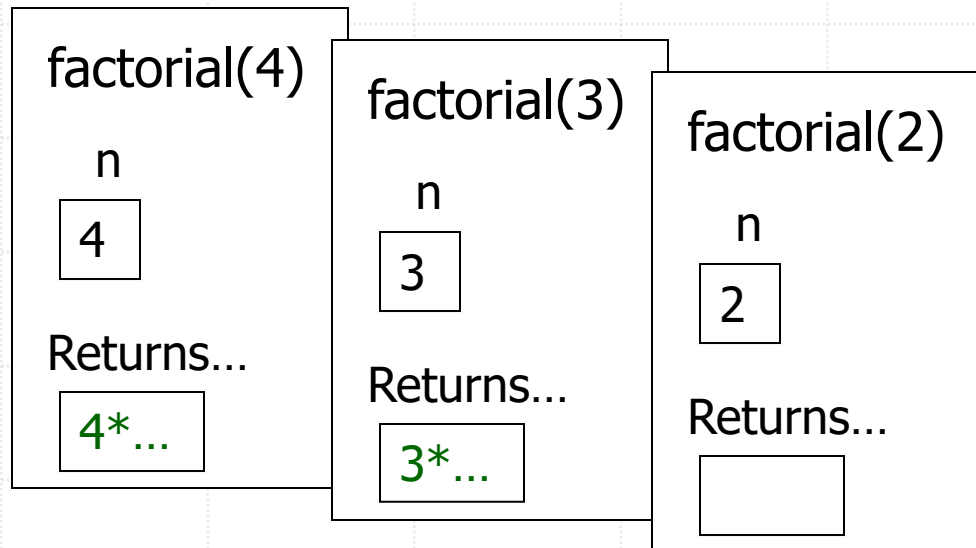
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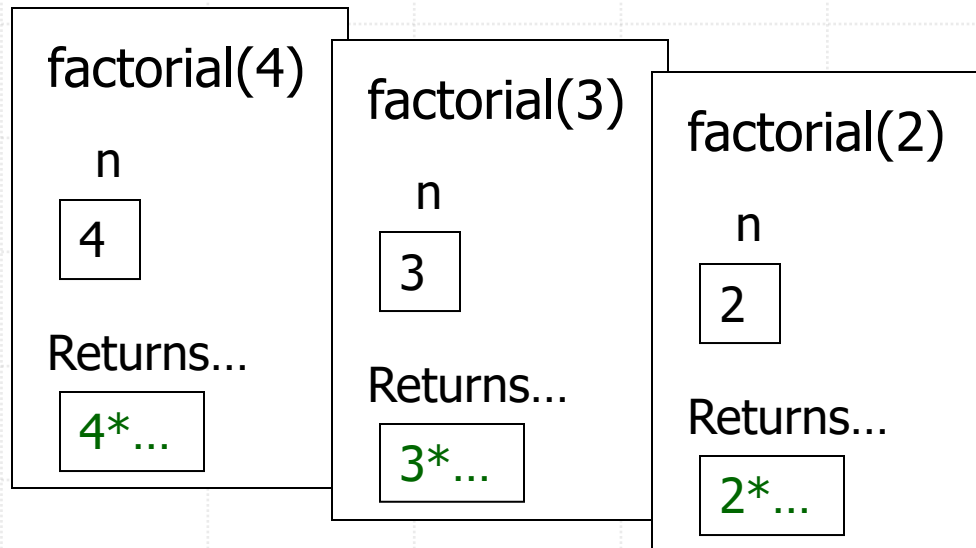
Recursive factorial – step by step

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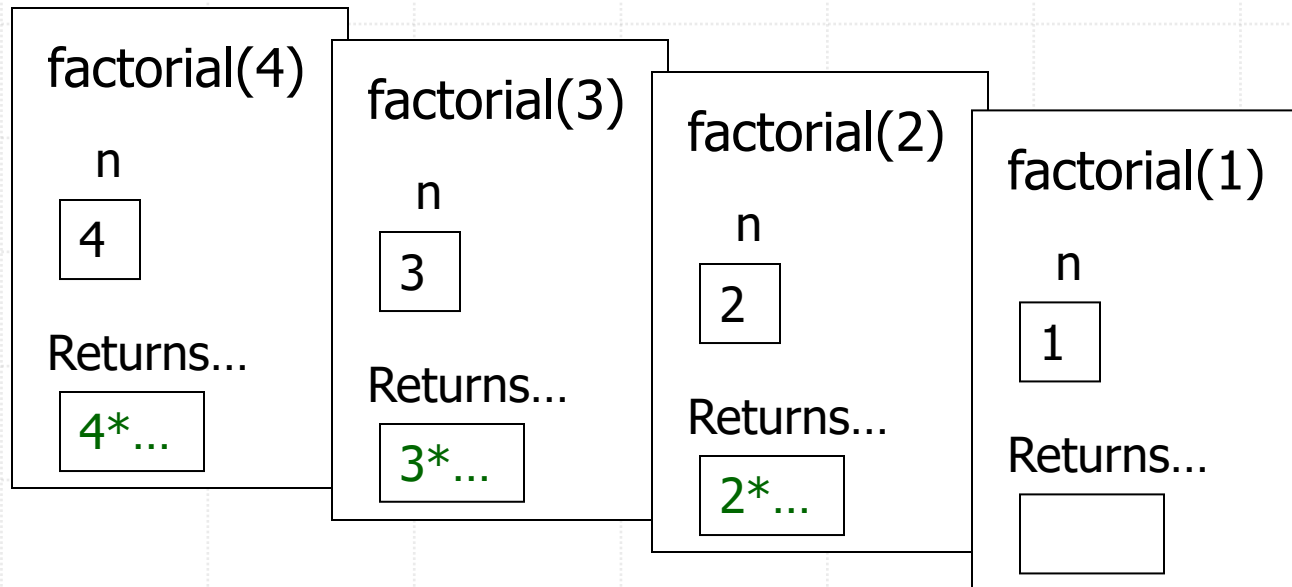
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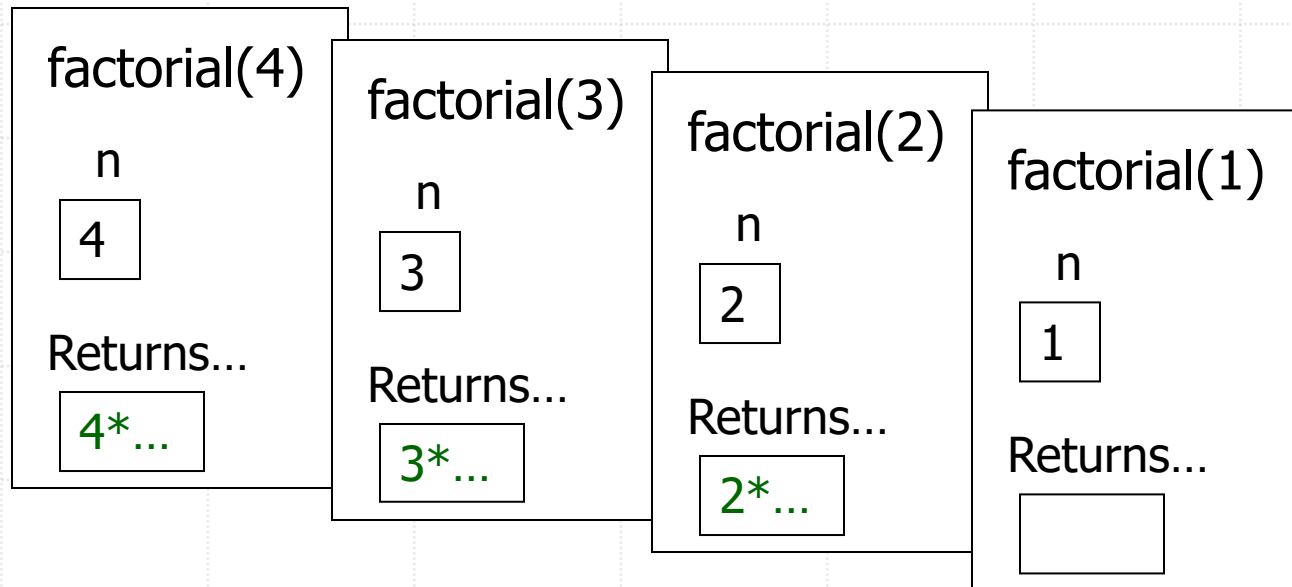
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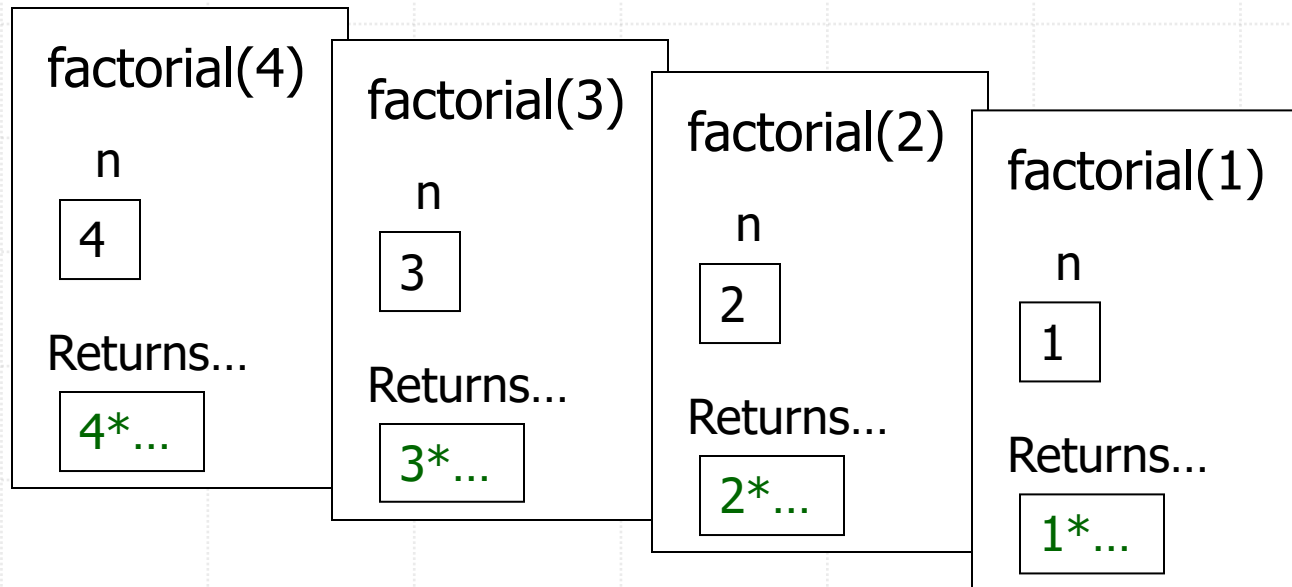
Recursive factorial – step by step

```
def factorial(n):  
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        return 1  
    return n * factorial(n-1)
```



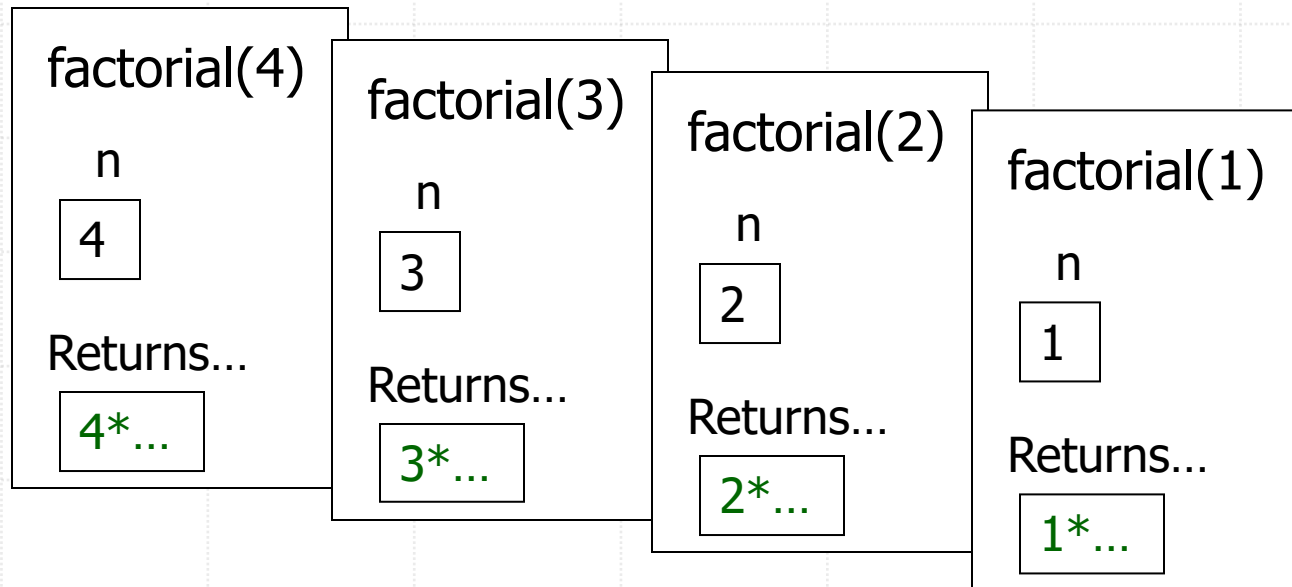
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```



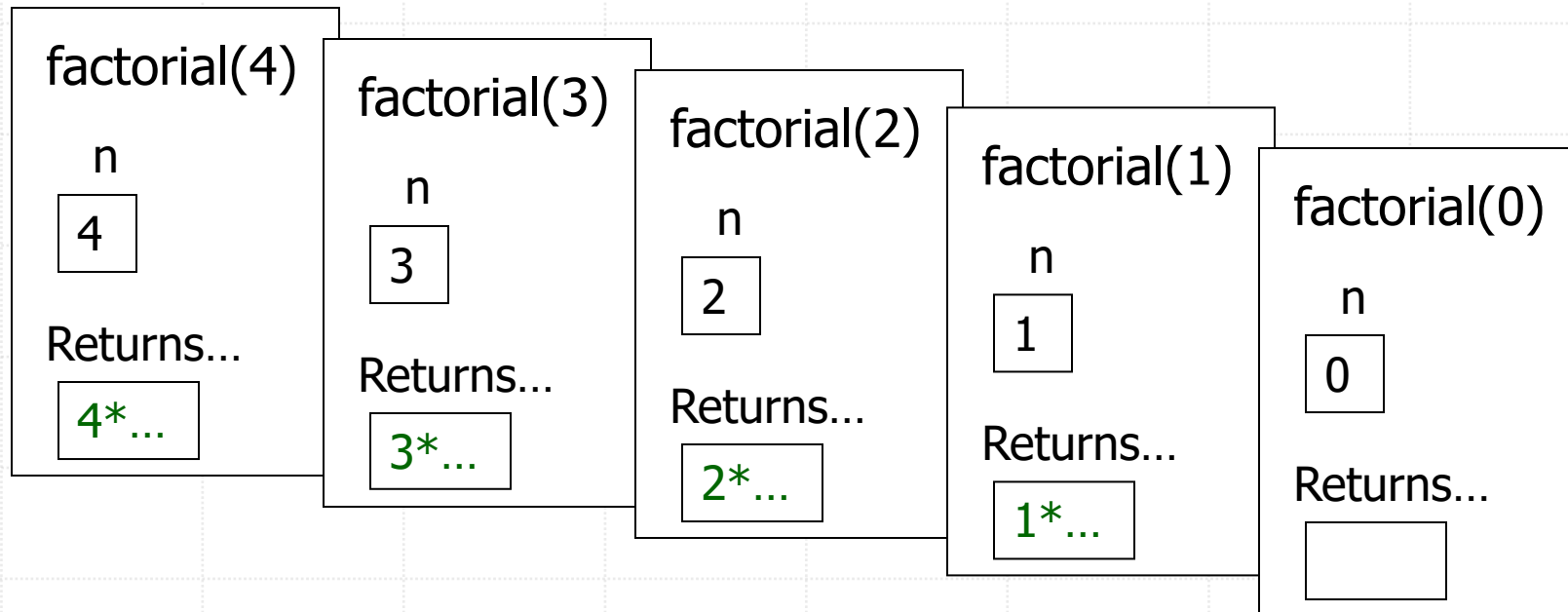
Recursive factorial – step by step

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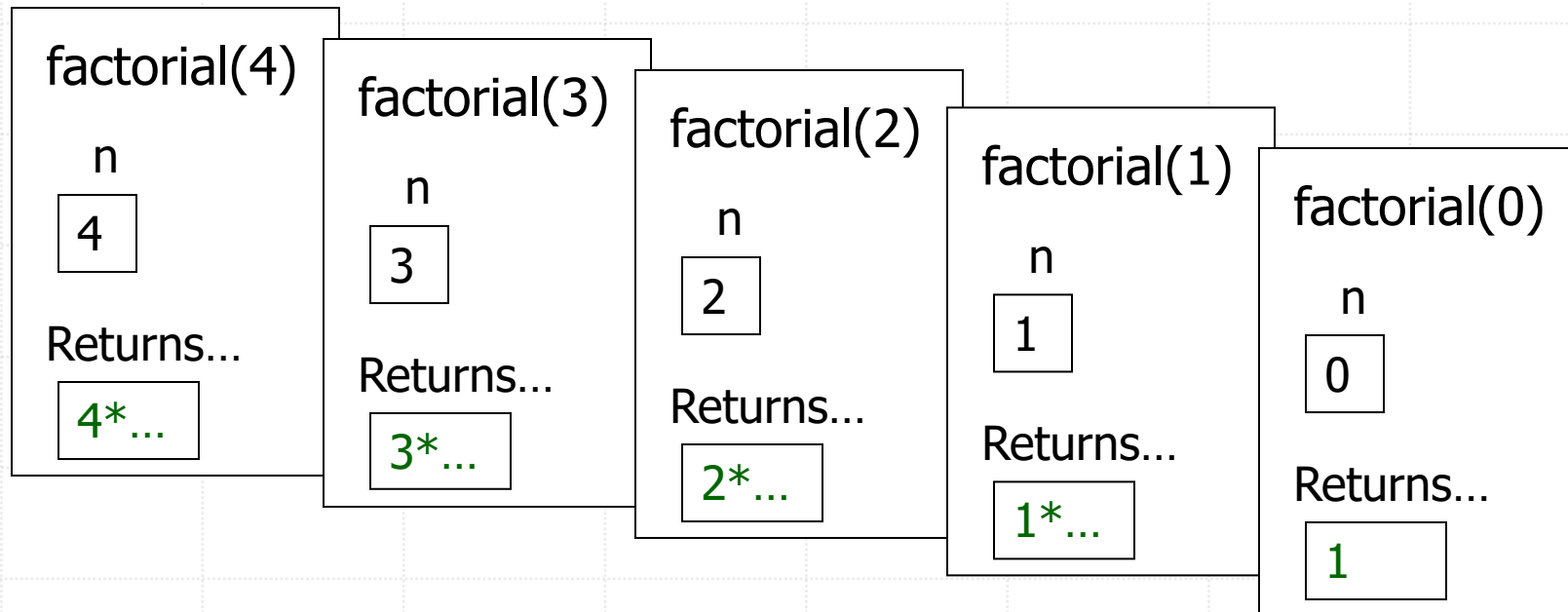
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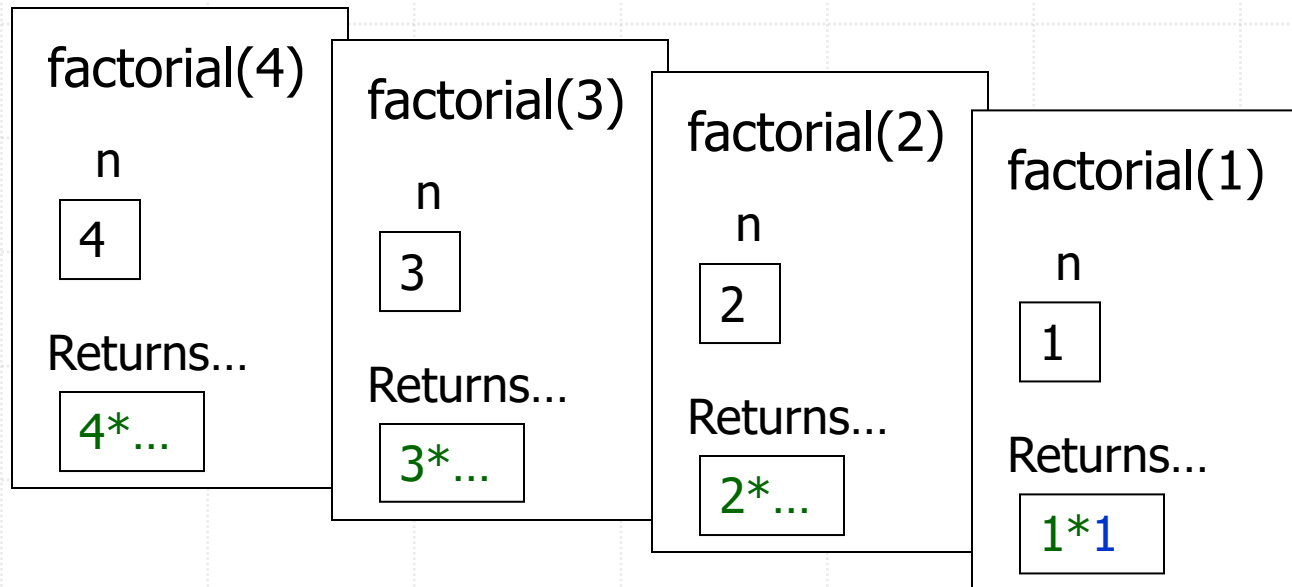
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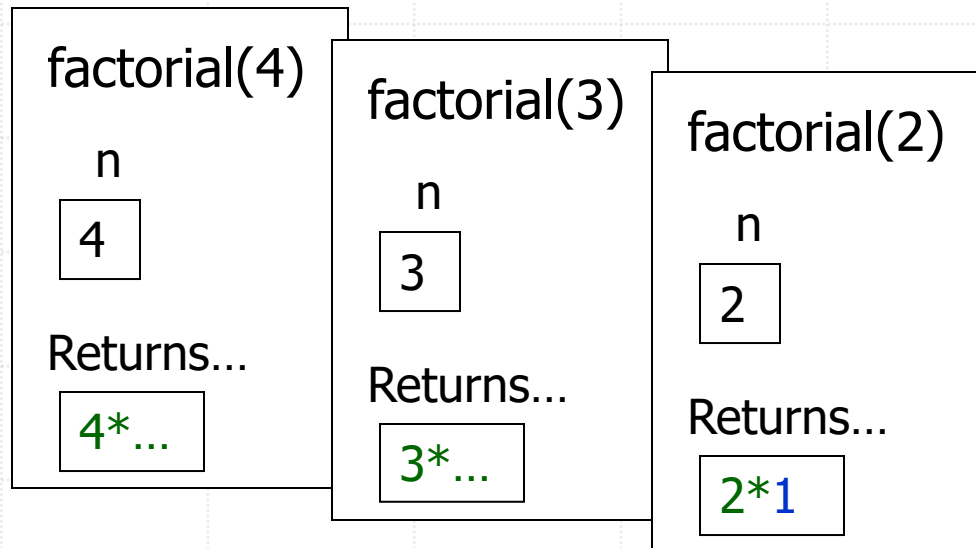
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    if n == 0:  
        return 1  
    return n * factorial(n-1)
```



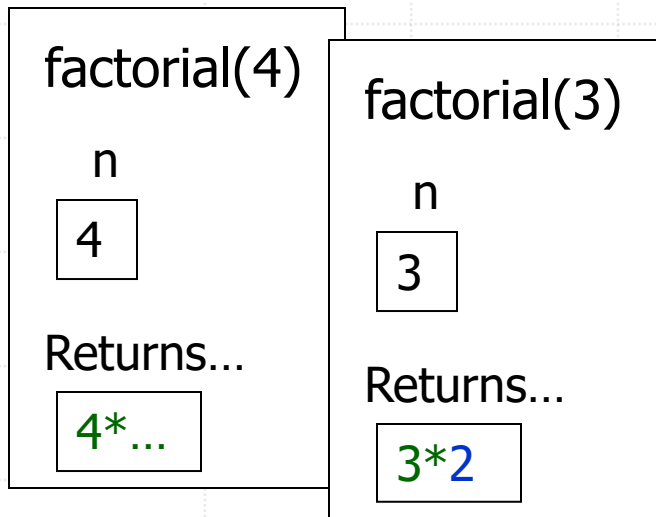
Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```



Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
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```



Recursive factorial – step by step

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```



factorial(4)

n

4

Returns...

4*6

General Form of Recursive Algorithms

```
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n-1)
```

Recursive case - decomposable problem.

Must be:

- at least one base case (the stop condition)
- at least one recursive call.

Short Summary

Design a recursive algorithm by

1. Breaking of big problems to smaller problems
2. Solving base cases directly.

Recursive algorithms have

1. Stopping criteria
2. Recursive call(s)
3. A solution that uses solutions of smaller cases

Example: Fibonacci Series

- Fibonacci series

0, 1, 1, 2, 3, 5, 8, 13, 21, 34

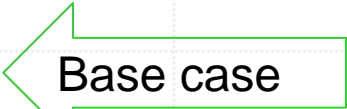



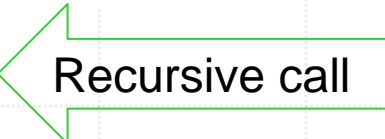


- Definition:

- $\text{fib}(0) = 0$
- $\text{fib}(1) = 1$
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$

Fibonacci

“Naturally” recursive

Therefore, the recursive definition is:

- $\text{fib}(0) = 0$  Base case 
- $\text{fib}(1) = 1$  Base case 
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$  Recursive call  + 

Summary

- Functions
 - What are they good for
 - Built-in Functions
 - Defining New Functions
 - Functions call functions
- Lambda
- Recursion

Homework

1. Create a Python script to create and print a list where the values are square of numbers between 1 and n (both included)

Input:

```
>>> 5
```

Output:

```
>>> [1, 4, 9, 16, 25]
```

2. -Create a Python script to find all keys in the provided dictionary that have the given value.

Input:

```
>>> students = {'Theodore': 19, 'Roxanne': 20, 'Mathew': 21, 'Betty': 20}
```

Output:

```
>>> ['Roxanne', 'Betty']
```

Homework

3. Create a Python script to calculate the value of the following expression by using lambda function. $(x*10+(y/2)*z)$

Input:

```
>>> x = 5, y = 5, z = 5
```

Output:

```
>>> 62.5
```

4. Create a Python script to create a lambda function that multiplies argument x with argument y and print the result

Input:

```
>>> a=4, b=12
```

Output:

```
>>> 48
```