# Tree Structure Analysis

#### **Combinations Tested**

- Constant tree:
  - Single input output
  - Multi input single output
  - Single input multi output
  - X inputs Y outputs (1 < X < Y)</li>
  - X inputs Y outputs (1 < Y < X)
- Linear tree:
  - Single input output
  - Multi input single output
  - Single input multi output
  - X inputs Y outputs (1 < X < Y)
  - X inputs Y outputs (1 < Y < X)
  - Single categorical input
  - Mixed numerical & categorical input
  - Multi categorical input

```
₹ 8:
                                                                                 "tree"
                                                name:
   tree index:
                       8
                                                version:
                                                                                "v4"
   num leaves:
                       21
                                                num_class:
   num cat:
    shrinkage:
                       0.05
                                                num_tree_per_iteration:
  ▼ tree_structure:
                                                label index:
                                                                                 0
      split_index:
                       0
                                                max feature idx:
                                                                                 0
      split_feature:
      split_gain:
                       0.10196000337600708
                                                                                "regression"
                                                objective:
     threshold:
                       0.32277838849773915
                                                average_output:
                                                                                false
                       "<="
      decision type:
                                             ▼ feature names:
     default_left:
                       true
     missing_type:
                       "None"
                                                   0:
                                                                                "Column 0"
      internal value:
                                                                                 monotone_constraints:
      internal weight:
      internal count:
                       632
                                             ▼ feature infos:
    ▶ left child:
                       {...}
                                                 ▶ Column 0:
                                                                                 {...}
                       {...}
    ▶ right child:
```

1 input 1 output numerical (constant)

```
₹ 8:
                                                                                "tree"
                                                   name:
    tree_index:
                         8
                                                                                "v4"
                                                   version:
    num leaves:
                         21
                                                   num class:
    num_cat:
                         0
                                                   num_tree_per_iteration:
    shrinkage:
                         0.05
                                                   label index:
                                                                                0
  ▼ tree_structure:
                                                   max feature idx:
                                                                                0
      split_index:
                         0
                                                   objective:
                                                                                "regression"
      split feature:
                                                   average output:
                                                                                false
      split gain:
                         0.10196000337600708
      threshold:
                         0.32277838849773915
                                                 feature names:
                         "<="
      decision_type:
                                                     0:
                                                                                "Column 0"
      default_left:
                         true
                                                   monotone_constraints:
                                                                                "None"
      missing_type:
                                                 ▼ feature_infos:
      internal value:
                         0
                                                   ▼ Column_0:
      internal_weight:
                                                        min value:
                                                                                0.00463202300460286
      internal count:
                         632
                                                        max_value:
                                                                                0.9997176732861306
    ▶ left_child:
                                                        values:
                         {...}
    ▶ right_child:
```

1 input 1 output numerical (linear)

```
▼ tree_info:
                                                                                              "tree"
                                                             name:
  ₹ 0:
                                                             version:
                                                                                              "v4"
      tree_index:
      num_leaves:
                           24
                                                             num class:
      num_cat:
                                                             num tree per iteration:
      shrinkage:
                                                             label index:
    ▼ tree_structure:
                                                             max_feature_idx:
         split_index:
                           0
                                                                                              "regression"
                                                             objective:
         split_feature:
                                                                                              false
                                                             average_output:
         split_gain:
                           0.9434239864349365
         threshold:
                           0.6665317632867276
                                                            feature names:
         decision_type:
                           "<="
                                                                0:
                                                                                              "Column 0"
        default_left:
                           true
                                                                1:
                                                                                              "Column 1"
                           "None"
         missing_type:
                                                                2:
                                                                                              "Column 2"
         internal_value:
                           0.484057
                                                                                              "Column 3"
                                                                3:
         internal weight:
                                                                4:
                                                                                              "Column_4"
         internal_count:
                           647
       ▶ left_child:
                           {...}
                                                             monotone constraints:
                                                                                               []
       ▶ right_child:
                           {...}
```

5 inputs 5 outputs numerical (linear)

```
"tree"
                                                               name:
▼ tree_info:
                                                                                             "v4"
                                                               version:
  ₹ 0:
      tree_index:
                                                               num class:
      num leaves:
                            26
                                                               num_tree_per_iteration:
                                                                                             1
      num cat:
                                                                label_index:
                                                                                             0
      shrinkage:
                                                               max feature idx:
    ▼ tree_structure:
                                                               objective:
                                                                                             "regression"
         split_index:
                                                               average output:
                                                                                             false
         split feature:
                                                             ▼ feature_names:
         split_gain:
                            0.2277749925851822
                                                                                             "Column 0"
         threshold:
                            0.9611304406466848
                                                                  0:
         decision type:
                            "<="
                                                                  1:
                                                                                             "Column 1"
         default_left:
                            true
                                                                                             "Column 2"
                                                                  2:
         missing_type:
                            "None"
                                                               monotone_constraints:
                                                                                             []
         internal value:
                            0.498222
                                                             ▼ feature infos:
         internal weight:
                                                                ▶ Column 0:
                                                                                             {...}
         internal_count:
                            647
                                                                                             {...}
                                                                ▶ Column_1:
       ▶ left_child:
                            {...}
                                                                                             {...}
                                                                ▶ Column 2:
       ▶ right child:
                            {...}
```

1 numerical 2 categorical inputs 5 outputs (linear)

```
"tree"
                                                                                                                  ▼ 3:
▼ feature_infos:
                                                       name:
  ▼ Column 0:
                                                                                                                       tree index:
                                                                                                                                             3
                                                       version:
                                                                                          "v4"
                          0.00013469300448532007
      min value:
                                                                                                                       num_leaves:
                                                                                                                                             26
                                                       num class:
      max value:
                          0.9997176732861306
                                                                                                                                             3
                                                                                                                       num cat:
      values:
                          \Gamma
                                                       num_tree_per_iteration:
                                                                                                                       shrinkage:
                                                                                                                                             0.05
  ▼ Column 1:
                                                                                                                     ▼ tree_structure:
                                                       label index:
                                                                                          0
                          0.000011634755366141114
      min value:
                                                                                                                          split index:
                                                                                                                                             0
                                                       max feature idx:
      max value:
                          0.9983475113929496
                                                                                                                         split_feature:
      values:
                          \mathbf{I}
                                                                                          "regression"
                                                       objective:
                                                                                                                         split gain:
                                                                                                                                             0.7711219787597656
  ▼ Column 2:
                                                       average output:
                                                                                          false
                                                                                                                          threshold:
                                                                                                                                             0.6388387594920623
      min value:
                          0.001353625715468154
                                                                                                                         decision_type:
                                                                                                                                             11<=11
      max value:
                          0.9966968538529769
                                                     ▼ feature names:
                                                                                                                         default_left:
                                                                                                                                             true
      values:
                          \Pi
                                                          0:
                                                                                          "Column 0"
                                                                                                                         missing type:
                                                                                                                                             "None"
  ▼ Column 3:
                                                                                          "Column 1"
                                                          1:
      min value:
                          -1
                                                                                                                          internal value:
                                                                                                                                             0
      max value:
                          2
                                                                                                                          internal_weight:
                                                                                                                                             0
                                                                                          "Column 2"
    values:
                          [...]
                                                                                                                          internal count:
                                                                                                                                             647
                                                          3:
                                                                                          "Column 3"
  ▼ Column 4:
                                                                                                                        ▶ left child:
                                                                                                                                             {...}
      min value:
                          -1
                                                                                          "Column 4"
                                                          4:
                                                                                                                        ▶ right_child:
                                                                                                                                             {...}
      max value:
                          2
                                                       monotone constraints:
                                                                                          ▶ values:
```

3 continuous 2 categorical inputs 5 outputs (linear)

## Summary

#### Cached Data:

- Name
- Version
- Num\_Class
- Num\_Tree\_Per\_Iteration
- Objective
- Max feature idx
- Monotone constraints
- Parent tree info:
  - Index
  - Num leaves
  - Num cat
  - Shrinkage
  - Decision type
- Weights and Values

#### Computed Data:

- min/max col value
- Leaf/child values
- Split indices
- Split gains
- Threshold
- Bounds