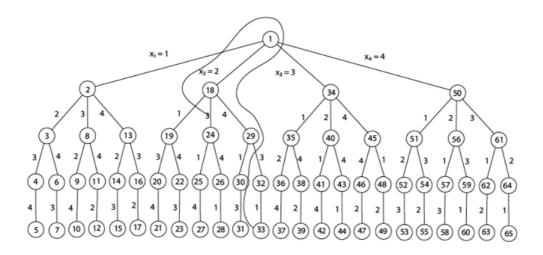
DAA MODULE 4

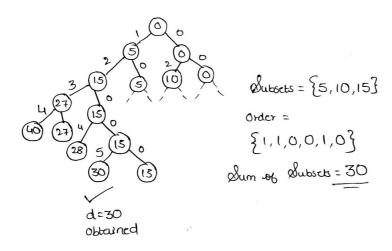
PART A

1) Build the state space tree generated by the 4 queen's problem.

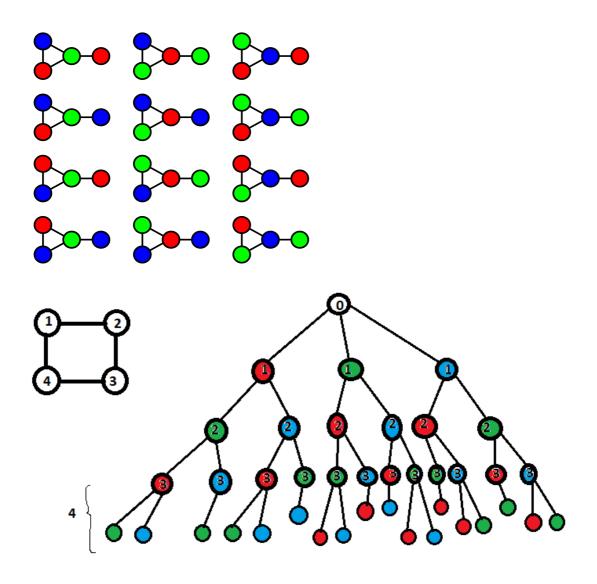
Answer is (2,4,1,3) or its mirror image (3,1,4,2)



2) Apply the backtracking algorithm to solve the following instance of the sum of subsets problem S=5,10,12,13,15,18 and d=30



3) Build the state space tree and generate all possible 3-color, 4-node graph.



- 4) Question incomplete
- 5) Solve the following instance of a travelling salesperson problem using Least Cost Branch and Bound.

Wrong values taken for Matrix from QB. The Procedure is correct. Please follow accordingly.

$$\begin{bmatrix} \infty & \infty & \infty & \infty \\ 8 & \infty & \infty & 1 \\ \infty & 4 & \infty & 12 \\ 8 & 0 & \infty & \infty \end{bmatrix} \Rightarrow (0st)$$

$$\Rightarrow ((1,3) + 3t + 37) \longrightarrow \begin{bmatrix} \infty & \infty & \infty & \infty \\ 0 & \infty & \infty & \infty \\ \infty & 4 & \infty & 12 \\ 0 & 0 & \infty & \infty \end{bmatrix}$$

$$\Rightarrow 0 + 17 + 9$$

$$\begin{cases} \infty & \infty & \infty & \infty \\ 0 & \infty & \infty \\ \infty & 4 & \infty \\ 0 & 0 & \infty \\ \infty & 0 & \infty \end{bmatrix}$$

$$\begin{bmatrix}
\infty & \infty & \infty & \infty \\
8 & \infty & 0 & \infty \\
0 & 4 & \infty & \infty \\
\infty & 0 & 0 & \infty
\end{bmatrix} \Rightarrow Cost$$

$$\Rightarrow C(1,4) + 34 + 34$$

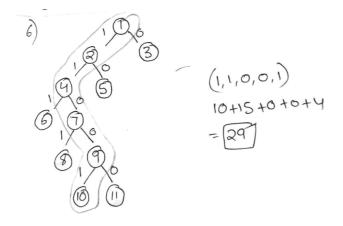
$$\Rightarrow Same Matrix$$

$$\Rightarrow 0 + 17 + 0$$

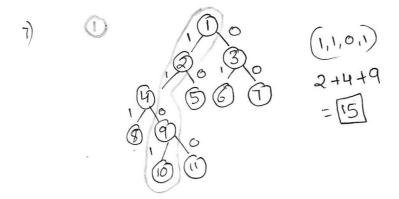
$$\Rightarrow 0 + 17 + 0$$

Answer with correct matrix values is 64

6) Build the state space tree generated by LCBB by the following knapsack problem n=5, (p1, p2, p3, p4, p5) = (10, 15, 6, 8,4), (w1, w2, w3, w4, w5) = (4, 6, 3, 4, 2) and m = 12.



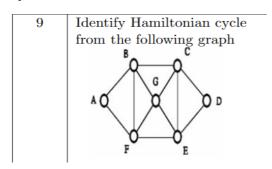
7) Build the state space tree generated by FIFO knapsack for the instance N=4, (P1, P2, P3, P4)=(10, 10, 12, 18), (w1, w2, w3, w4)=(2, 4, 6, 9), m=15



8) Solve the following instance of travelling salesperson problem using Least Cost Branch Bound

Same as 5th

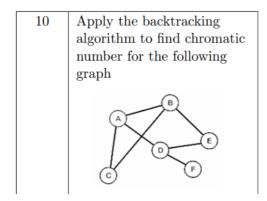
9)

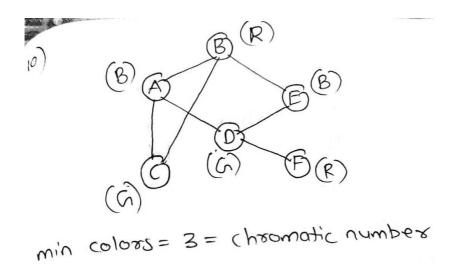


ABGCDEFA

etc

10)





PART B

1) Develop an algorithm for the N-queens problem using backtracking.

Refer Part B 11th q

2) Apply a backtracking method and solve subset-sum problems and discuss the possible solution strategies.

Same as Part A 2nd q

3) Apply graph colouring technique and write an algorithm for m-colouring problems.

In this problem, an undirected graph is given. There are also provided m colours. The problem is to find if it is possible to assign nodes with m different colours, such that no two adjacent vertices of the graph are of the same colours. If the solution exists, then display which colour is assigned on which vertex.

Starting from vertex 0, we will try to assign colours one by one to different nodes. But before assigning, we have to check whether the colour is safe or not. A colour is not safe whether adjacent vertices are containing the same colour.

Algorithm

isValid(vertex, colorList, col)

Input - Vertex, colorList to check, and color, which is trying to assign.

Output - True if the color assigning is valid, otherwise false.

```
Begin
  for all vertices v of the graph, do
    if there is an edge between v and i, and col = colorList[i], then
       return false
  done
  return true
End
```

4) Explain an algorithm for the Hamiltonian cycle with an example.

In an undirected graph, the Hamiltonian path is a path that visits each vertex exactly once, and the Hamiltonian cycle or circuit is a Hamiltonian path, where there is an edge from the last vertex to the first vertex.

In this problem, we will try to determine whether a graph contains a Hamiltonian cycle or not. And when a Hamiltonian cycle is present, also print the cycle.

Algorithm

isValid(v, k)

Input - Vertex v and position k.

Output - Checks whether placing v in the position k is valid or not.

```
Begin
  if there is no edge between node(k-1) to v, then
    return false
  if v is already taken, then
    return false
  return true; //otherwise it is valid
End
```

5) Explain properties of LC search.

- Least Cost Branch and Bound is a way of finding an optimal solution from the state space tree.
- The search for an answer node can be fastened by using an "intelligent" ranking function c(.) for live nodes. The next E-node is selected on the basis of a ranking function used in LC Search.
- The node x is assigned a rank using:

```
c(x) = f(h(x)) + g(x)
```

- where, c(x) is the cost of x.
- \circ h(x) is the cost of reaching x from the root and f(...) is any non-decreasing function.
- \circ g(x) is an estimate of the additional effort needed to reach an answer node from x.
- LC search terminates only when either an answer node is found or the entire state space tree has been generated and searched.
- An LC-search coupled with bounding functions is called an LC-branch and bound search.

6) Explain control abstraction for LC Search.

Control Abstraction for LC-search

Let \mathbf{t} be a state space tree and $\mathbf{c}()$ a cost function for the nodes in \mathbf{t} . If \mathbf{x} is a node in \mathbf{t} , then $\mathbf{c}(\mathbf{x})$ is the minimum cost of any answer node in the sub tree with root \mathbf{x} . Thus, $\mathbf{c}(\mathbf{t})$ is the cost of a minimum-cost answer node in \mathbf{t} .

LC search uses ĉ to find an answer node. The algorithm uses two functions

blog: anilkumarprathipati.wordpress.com

3

UNIT-V1

BRANCH AND BOUND

- 1. Least-cost()
- 2. Add_node().

Least-cost() finds a live node with least c(). This node is deleted from the list of live nodes and returned.

Add_node() to delete and add a live node from or to the list of live nodes.

Add_node(x) adds the new live node x to the list of live nodes. The list of live nodes be implemented as a min-heap.

7 and 8) Explain the principle of FIFO and LIFO branch and bound.

Branch and Bound is another method to systematically search a solution space. Just like backtracking, we will use bounding functions to avoid generating subtrees that do not contain an answer node.

However branch and Bound differs from backtracking in two ways:

- It has a branching function, which can be a depth first search, breadth first search or based on the bounding function.
- It has a bounding function, which goes far beyond the feasibility test as a means to prune efficiently the search tree.

Branch and Bound refers to all state space search methods in which all children of the E-node are generated before any other live node becomes the E-node Branch and Bound is the generalisation of both graph search strategies, BFS and DFS.

A BFS-like state space search is called a FIFO (First in first out) search as the list of live nodes in a first in first out list (or queue).

FIFO Branch and bound

- FIFO Branch and Bound is a BFS.
- In FIFO Branch and Bound , children of E-Node (or Live nodes) are inserted in a queue.
- Implementation of list of live nodes as a queue
 Least() Removes the head of the Queue
 Add() Adds the node to the end of the Queue

A DFS-like state space search is called a LIFO (Last in first out) search as the list of live nodes in a last in first out (or stack).

LIFO Branch and bound

LIFO Branch and Bound is a D-search (or DFS).

In LIFO Branch and Bound children of E-node (live nodes) are inserted in a stack Implementation of List of live nodes as a stack

Least() Removes the top of the stack

ADD() Adds the node to the top of the stack

9) Apply the method of reduction to solve travelling salesperson problems

using branches and bonds.

Refer this link: Travelling Salesman Problem | Branch & Bound | Gate Vidyalay

10) Explain TSP using branch and bound method with example

Same as the 9th question.

11) Explain the basic principle of Backtracking and list the applications of

Backtracking.

Backtracking is a technique based on algorithms to solve problems. It uses

recursive calling to find the solution by building a solution step by step

increasing values with time. It removes the solutions that don't give rise to the

solution of the problem based on the constraints given to solve the problem.

Backtracking algorithm is applied to some specific types of problems:

• Decision problem used to find a feasible solution of the problem.

• Optimisation problem used to find the best solution that can be applied.

Enumeration problem used to find the set of all feasible solutions of the

problem.

In a backtracking problem, the algorithm tries to find a sequence path to the

solution which has some small checkpoints from where the problem can

backtrack if no feasible solution is found for the problem.

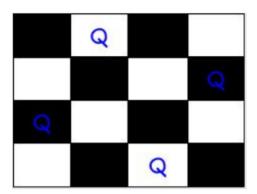
Example:

Let's use this backtracking problem to find the solution to the N-Queen

Problem.

In the N-Queen problem, we are given an NxN chessboard and we have to place n queens on the board in such a way that no two queens attack each other. A queen will attack another queen if it is placed in horizontal, vertical or diagonal points in its way. Here, we will do the 4-Queen problem.

Here, the solution is -



To solve the queen's problem, we will try placing the queen into different positions in one row. And checks if it clashes with other queens. Current positioning of queens if there are any two queens attacking each other. If they are attacking, we will backtrack to the previous location of the queen and change its positions. And check the clash of the queens again.

Algorithm

```
Step 1 - Start from 1st position in the array.
Step 2 - Place queens in the board and check. Do,
    Step 2.1 - After placing the queen, mark the position as a part of the solution and then recursively check if this will lead to a solution.
    Step 2.2 - Now, if placing the queen doesn't lead to a solution and trackback and go to step (a) and place queens to other rows.
    Step 2.3 - If placing queen returns a lead to solution return TRUE.
Step 3 - If all queens are placed return TRUE.
Step 4 - If all rows are tried and no solution is found, return FALSE.
```

12) Explain Backtracking technique and solve the following instance for the subset problem s=(1,3,4,5) and d=11.

Backtracking explained in the previous question.

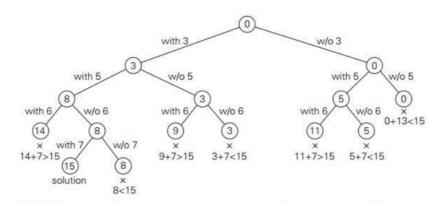


FIGURE 12.4 Complete state-space tree of the backtracking algorithm applied to the instance $A = \{3, 5, 6, 7\}$ and d = 15 of the subset-sum problem. The number inside a node is the sum of the elements already included in the subsets represented by the node. The inequality below a leaf indicates the reason for its termination.

Subsets do not add up to 11. Question seems incorrect. The above solution doesn't resonate with the above problem.

13) Construct the portion of the state space tree generated by LCBB for the knapsack instance: n=5, (p1, p2, p3, p4, p5) = (w1 w2, w3, w4, w5) = (4, 4, 5, 8, 9) and <math>m=15.

14) Explain an algorithm for 4-queens problem using backtracking

Refer Part B 11th q

15) Apply Backtracking technique to solve the following instance for the subset problem s=(6,5,3,7) and d=15.

Same as 12th question

- 16) Build the portion of state space tree generated by FIFOBB for the job sequencing with deadlines instance n=5, (p1,p2,...,p5) = (6,3,4,8,5), (t1,t2,...t5) = (2,1,2,1,1) and (d1,d2,...,d5)=(3,1,4,2,4). What is the penalty corresponding to an optimal solution?
- 17) Solve the solution for 0/1 knapsack problem using dynamic programming N=3, m=6 profits (p1,p2,p3) = (1,2,5) weights (w1,w2,w3) = (2,3,4)

Refer this link: 0/1 Knapsack Problem | Dynamic Programming | Example | Gate Vidyalay

18	Choose shortest distances
	using all pairs shortest path
	algorithm
	9 5 5 3 2

19) Solve knapsack problem by Dynamic Programming method n=6, (p1, p2,...p6)= (w1,w2,...w6)= (100,50,20,10,7,3) and m=165.

20) Define greedy methods.

A greedy algorithm is an approach for solving a problem by selecting the best option available at the moment. It doesn't worry whether the current best result will bring the overall optimal result.

The algorithm never reverses the earlier decision even if the choice is wrong. It works in a top-down approach.

This algorithm may not produce the best result for all the problems. It's because it always goes for the local best choice to produce the global best result.

Advantages of Greedy Approach

- The algorithm is easier to describe.
- This algorithm can perform better than other algorithms (but, not in all cases).

Greedy Approach

- 1. Let's start with the root node **20**. The weight of the right child is **3** and the weight of the left child is **2**.
- 2. Our problem is to find the largest path. And, the optimal solution at the moment is **3**. So, the greedy algorithm will choose **3**.
- 3. Finally the weight of an only child of **3** is **1**. This gives us our final result 20 + 3 + 1 = 24.

However, it is not the optimal solution. There is another path that carries more weight (20 + 2 + 10 = 32) as shown in the image below.

