

Theory of computation:

TOC: In theoretical Computer Science, the theory of computation is the branch that deals with whether and how efficiently problems can be solved on a model of computation, using an algorithm. This field is divided into three major branches:

① Automata Theory: Deals with definitions & properties of various mathematical models

② Computability Theory: Deals with what can, cannot be computed by the model.

③ Computational Complexity Theory: Deals with computable problems based on their hardness.

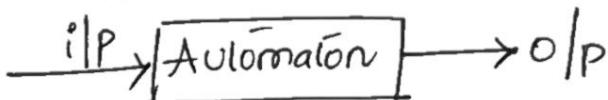
Automata Theory: Deals with definitions & properties of different types of "Computational models". Examples of such models:

→ Finite Automata

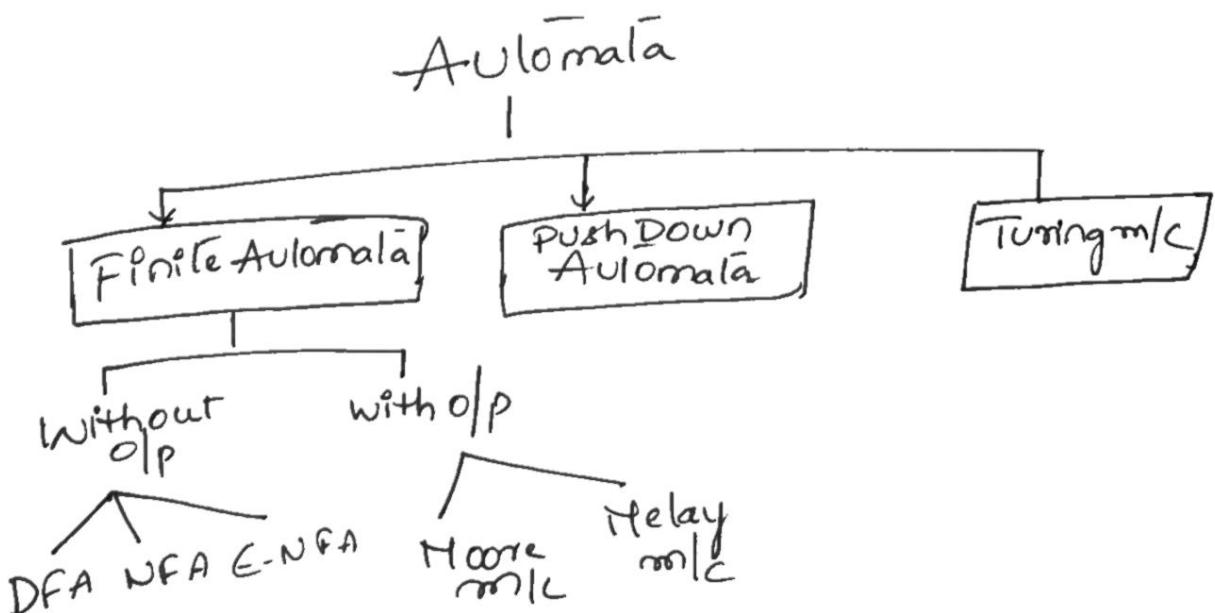
→ Context-Free Grammars

→ Turing Machines

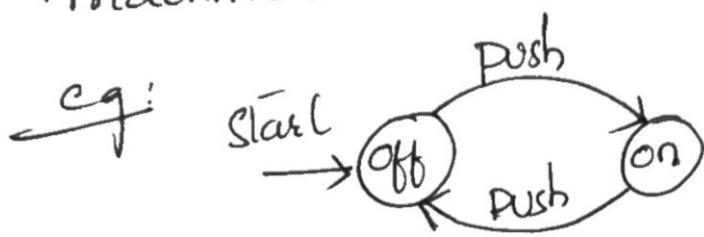
Autómata: An autómata is a system (abstract machine) which transforms information / data by performing some internal functions with different state at different instant of time and produce o/p without participation of human.



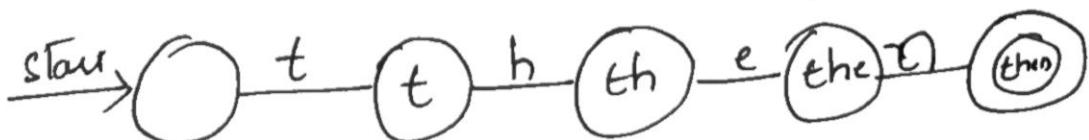
- Autómata means self-acting m/c ie; automatic.
- In TOC actual m/c is not designed but a mathematical model | abstract m/c is designed.
- Autómata
 - States (represented by circles)
 - Transitions (represented by arrows)



Finite Automata : "An Automaton with finite number of states is called Finite Automata / finite state machine."



- FA useful in both tt/w & s/w
- Remembers only finite amount of information
- Used in S/W for designing & checking the behaviour of digital circuits
- Used in "Lexical Analyzer" in a Compiler
- Used in S/W for scanning large bodies of text such as to find occurrences of words, phrases & other patterns.
- FA being a part of Lexical Analyzer. The job of automaton to recognize the keyword "then"



Symbol	Meaning
O	State
→○	Start State
○	End State or Accept State
→	Transition

Central Concepts of Automata Theory:

Symbol: The basic building block to build languages for machine.

→ If it is an individual part of input symbols or single character is known as a symbol

e.g.: digit 0, 1, 2 ... 9

alphabet a, b, c ... z

A, B, C ... Z

special symbols @, !, \$, <, > ...

Alphabet: Σ is a finite non-empty set

of symbols

$\rightarrow \Sigma$ is represented by sigma Σ

\rightarrow eg: $\Sigma = \{0, 1, 2\}$

$\Sigma = \{a, b\}$

String: Finite sequence of symbols from the
alphabet (Σ)

$\rightarrow \Sigma$ is represented by w

eg: $\Sigma = \{0, 1\}$

$w = 011010\dots$

$\Sigma = \{a, b\}$

$w = ababb$

\rightarrow Empty string denoted by epsilon ' ϵ '

\rightarrow In empty string no character is there &
its length is equal to zero.

\rightarrow Prefix \rightarrow a string is no: of leading symbols
of the string

Suffix \rightarrow a string is any no: of trailing
symbols of the string.

eg. "0011" prefix $\rightarrow 0, 00, 001$ eg. "Mango"
suffix $\rightarrow 1, 11, 011$ prefix man
suffix $\rightarrow 90$

Length of the string - It is equal to the number of symbols / characters in the string
→ It is represented by $|w| \text{ (mod of } w)$

e.g. $w = \text{hello}$

$$|w| = 5$$

$w = \epsilon$ (empty string)

$$|w| = 0$$

Operations on String:

i

Concatenation \rightarrow

$$\begin{aligned} w_1 &= ab \\ w_2 &= cd \\ w_1 w_2 &= abcd \end{aligned}$$

ii

Transpose \leftrightarrow

iii

palindrome $\rightarrow w = aba$ palindrome: aba

iv

substring $\rightarrow w = ab$ substring $\rightarrow \epsilon, a, b, ab$

v

union $\rightarrow w_1 = ab$ $w_2 = cd$ $w_1 \cup w_2 = \{ab, cd\}$

vi

Reverse of a string $\rightarrow w = ab$ $w^R = ba$

Language: A language is set of all strings that are chosen from an alphabet.

→ It is $L \subseteq \Sigma^*$, where L is a language.

eg:1 $\Sigma = \{a\}$

Language consist of any no. of a's over Σ

then $L = \{ \epsilon, a, aa, aaa \dots \}$

$$L = \{a^n \mid n \geq 0\}$$

eg:2 Describe the language consist of equal no. of 0's followed by equal no. of 1's over $\Sigma = \{0, 1\}$

$$\Sigma = \{0, 1\}$$

$$L = \{ \epsilon, 01, 0011, 000111 \dots \}$$

$$L = \{0^n 1^n \mid n \geq 0\}$$

Language $\xrightarrow{\text{finite language}} \Rightarrow$ contain finite no. of strings
 $\xrightarrow{\text{infinite language}} \Rightarrow$ contain infinite no. of strings

Ways to define a Language -

- ① Set-Former $\rightarrow \{ w \mid \text{something about } w \}$
e.g.: $L = \{ a^n \mid n \geq 0 \}$
[read as the set of a to the power n such that n is greater than or equal to 0]
- ② Roster | Tabular form $\rightarrow L = \{ \epsilon, a, aa, aaa \dots \}$
- ③ Regular Expression $\rightarrow L = a^*$

Operations on Languages: A = {1, 2} B = {2, 3}

① Concatenation of Two Languages

$$\text{eg } AB = \{(1,2)(1,3)(2,2)(2,3)\}$$

② Union of two Languages

$$A \cup B = \{1, 2, 3\}$$

③ Intersection $\rightarrow A \cap B = \{2\}$

④ Difference $\rightarrow A - B = \{1\}$

$$B - A = \{3\}$$

⑤ Complement

⑥ Kleene Closure (L^*)

⑦ Positive Closure (L^+)

Power of Alphabet

$\Sigma \rightarrow \text{Alphabet}$

$\Sigma^k \rightarrow \text{power of Alphabet}$

$k \rightarrow \text{Set of all strings of length } k$

$$\text{eg: } \Sigma = \{0, 1\}$$

$$\Sigma^0 = \{\epsilon\}$$

$$\Sigma^1 = \{0, 1\}$$

$$\Sigma^2 = \{00, 01, 10, 11\}$$

$$\Sigma^3 = \Sigma^2 \Sigma = \{00, 01, 10, 11\} \{0, 1\}$$

$$= \{000, 001, 010, 001, 100, \\ (a, 110, 111\}$$

Kleene Closure :- It consists of set of all strings including length '0'.

→ denoted by L^* , ie, Empty string is also included

~~q~~ → $L^* = L^0 \cup L^1 \cup L^2 \cup \dots$

Positive Closure :- It consists of set of all

strings except the empty string

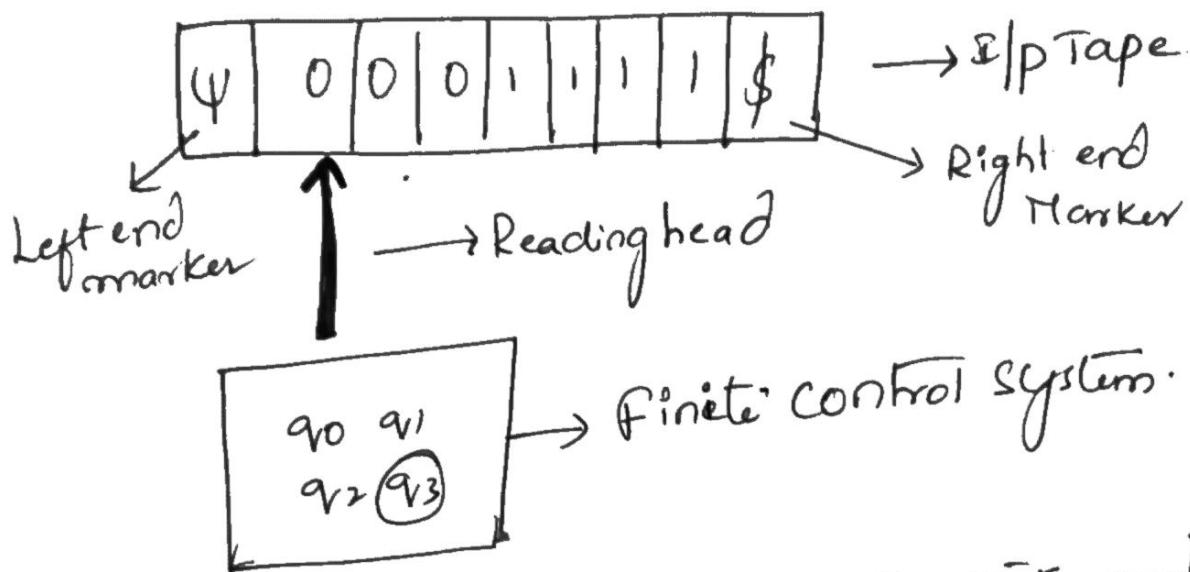
ie; (one or more occurrences).

→ represented by L^+

$$L^+ = L^* - \{\epsilon\}$$

(or) $L^1 \cup L^2 \cup L^3 \cup \dots$

Model & Behaviour of FSM or FA:



→ A FA consists of a finite set of states and a set of transitions from one state to another state that occurs on the I/P symbols (chosen from an alphabet 'S') & gives O/P

→ The read head is placed at 1st cell immediate right to left end marker and reads I/P symbol one by one till it gets right end marker (\$) & checks the current state of the FA if it belongs to final state. It represents the given string is valid otherwise not valid.

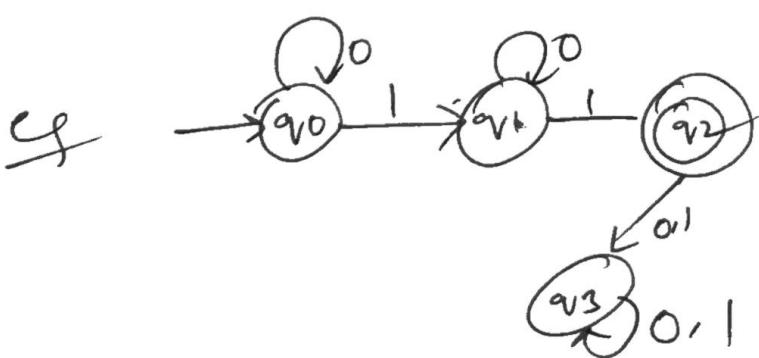
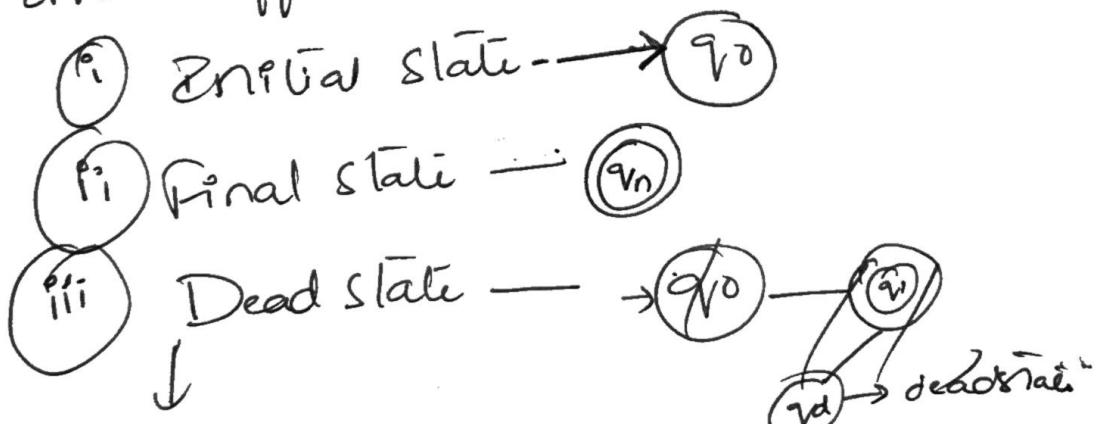
$$\delta(q_0, w) \in F$$

FA is mainly represented in two ways

- ① Transition Diagram
- ② Transition Table.

① Transition Diagram: In transition diagram set of vertices & edges are present.
The vertices of transition diagram are called "states" & "edges" are called input symbols of FA.

There are different types of states in FA



② Transition Table:- It consists of rows & columns

rows \rightarrow no. of states

columns \rightarrow set of I/P symbols

q_i	0	1
q_0	q_0	q_1
q_1	q_1	q_2
q_2	q_3	q_3
q_3	q_3	q_3

Formal Definition of FA :-

The FA is described as five Tuple notation
ie; Quintuple (5 elements in a tuple)

$$M = (Q, \Sigma, \delta, q_0, F)$$

Where $Q \rightarrow$ finite & non-empty set of states
 $\Sigma \rightarrow$ sequence of symbols from an Alphabet

$\delta \rightarrow$ Transition or mapping function

$q_0 \rightarrow$ Initial state

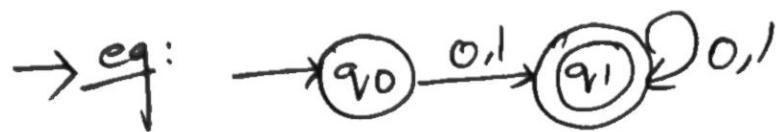
$F \rightarrow$ Set of final states

$$\delta = Q \times \Sigma \rightarrow Q$$

$$q_0 \rightarrow Q$$

$$q_0 \in Q$$

$$F \subseteq Q$$



$$Q = \{q_0, q_1\}$$

$$\Sigma = \{0, 1\}$$

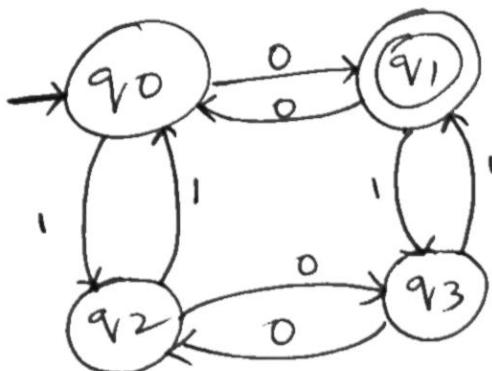
$q_0 \rightarrow$ initial state

$$F \rightarrow \{q_1\}$$

$$S: Q \times \Sigma \rightarrow Q$$

s	0	1
$\rightarrow q_0$	q_1	q_1
$\rightarrow q_1$	q_1	q_1

\rightarrow Consider the following transition diagram



i) Describe the given transition diagram using 5 tuple notation

ii) Draw Transition Table

iii) Check whether the following strings are accepted or not
 a) 01010110 b) 00110 c) 10101010

Sol? $\Rightarrow M = (Q, \Sigma, q_0, \delta, F)$

$$M = \left(\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \{q_0\}, \delta, \{q_3\} \right)$$

$$\delta(q_0, 0) = q_1$$

$$\delta(q_0, 1) = q_2$$

$$\delta(q_1, 0) = q_0$$

$$\delta(q_1, 1) = q_3$$

$$\delta(q_2, 0) = q_3$$

$$\delta(q_2, 1) = q_0$$

$$\delta(q_3, 0) = q_2$$

$$\delta(q_3, 1) = q_1$$

δ	0	1
q_0	q_1	q_2
q_1	q_0	q_3
q_2	q_3	q_0
q_3	q_2	q_1

iii) a, $\delta(q_0, 01010110)$

$$\delta(q_1, 1010110)$$

$$\delta(q_3, 010110)$$

$$\delta(q_2, 10110)$$

$$\delta(q_0, 0110)$$

$$\delta(q_1, 110)$$

$$\delta(q_3, 10) \quad \delta(q_1, 0) = q_0 \text{ } \cancel{\text{EF}}$$

$q_0 \cancel{\in F}$ so invalid step

$$\begin{aligned} & \Rightarrow 00110 \\ & \delta(q_0, 00110) \\ & \delta(q_1, 0110) \\ & \delta(q_0, 110) \\ & \delta(q_2, 10) \\ & \delta(q_0, 0) \\ & = q_1 \text{EF} \\ & \text{Valid step} \end{aligned}$$

→ Acceptance of string:- String ' α ' is accepted by FA if $\delta(q_0, \alpha) = p \in F$

e.g.: Find whether 1011 is accepted by following Automata or not.



$$\begin{aligned}
 \delta(q_0, 1011) &= \delta(q_1, 011) \\
 &= \delta(q_2, 11) \\
 &= \delta(q_2, 1) \\
 &= \emptyset q_2 \in F
 \end{aligned}$$

$q_0 \xrightarrow{1} q_1 \xrightarrow{0} q_2 \xrightarrow{1} q_2 \in F$
Valid or accepted.

Types of Finite Automata:

- (i) Deterministic FA (DFA)
- (ii) Non-Deterministic FA (NFA)

Defn: A FA is called as DFA if there is only one path from the current state to next state on every specific IP symbol

Formal Definition of DFA:

DFA can be described by using 5 tuple definition, i.e. $(Q, \Sigma, \delta, q_0, F)$

where Q = finite or non-empty set of states
 Σ = set of IP symbols

q_0 = initial state

F = set of final states

δ = transition or mapping function
 $\therefore \delta : Q \times \Sigma \rightarrow \mathcal{P}$

where \mathcal{P} is a set of final states

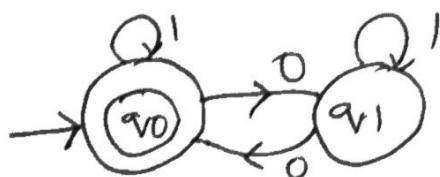
$F \subseteq \mathcal{P}$

Numericals on DFA:

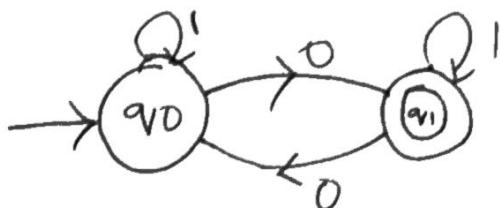
- ① Consider a DFA for even no. of zeros

$$L = \{\epsilon, 00, 001, 00001, 000\}$$

When 'ε' is there in language then
the start state will be the final state

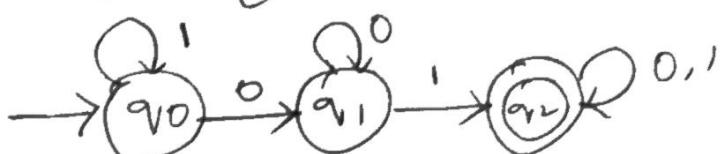


- ② odd no. of zeros



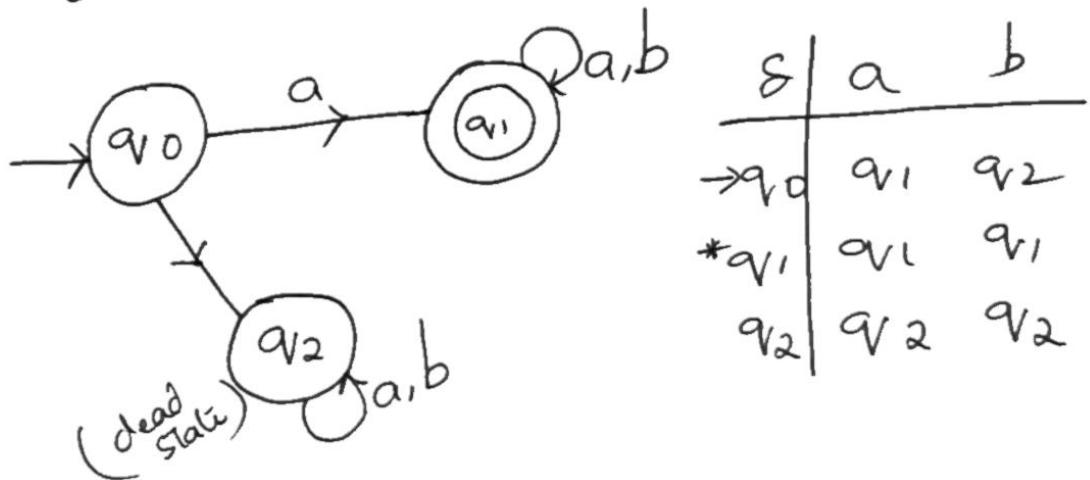
- ③ DFA for
Accept the string '01'

$$L = \{01, 010, 001, 0010, 0101, \dots\}$$

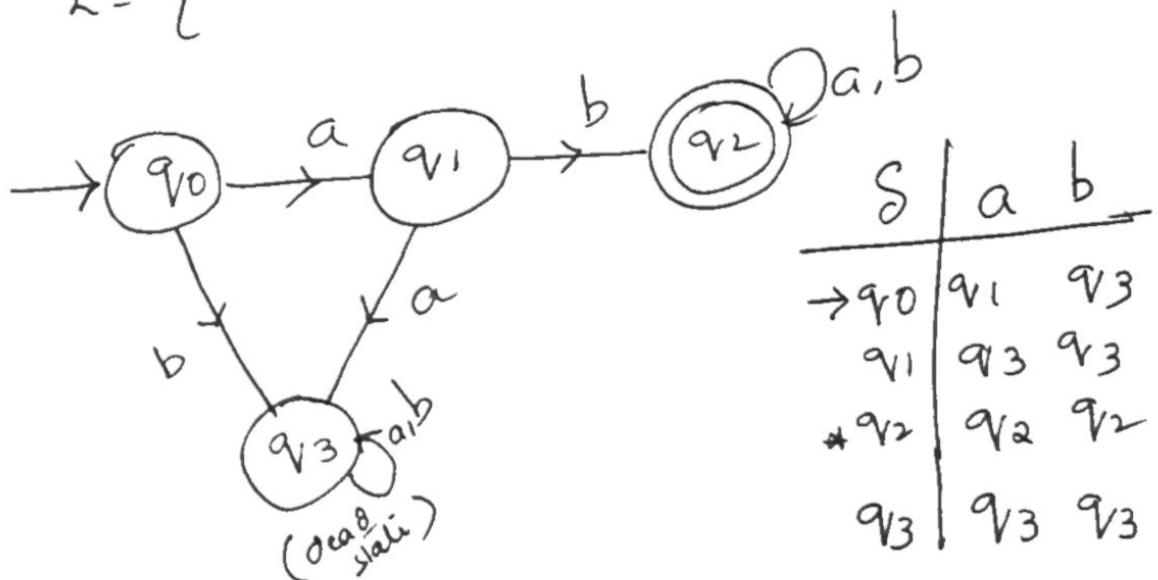


Start With: (^{Hint} Expect a dead state)

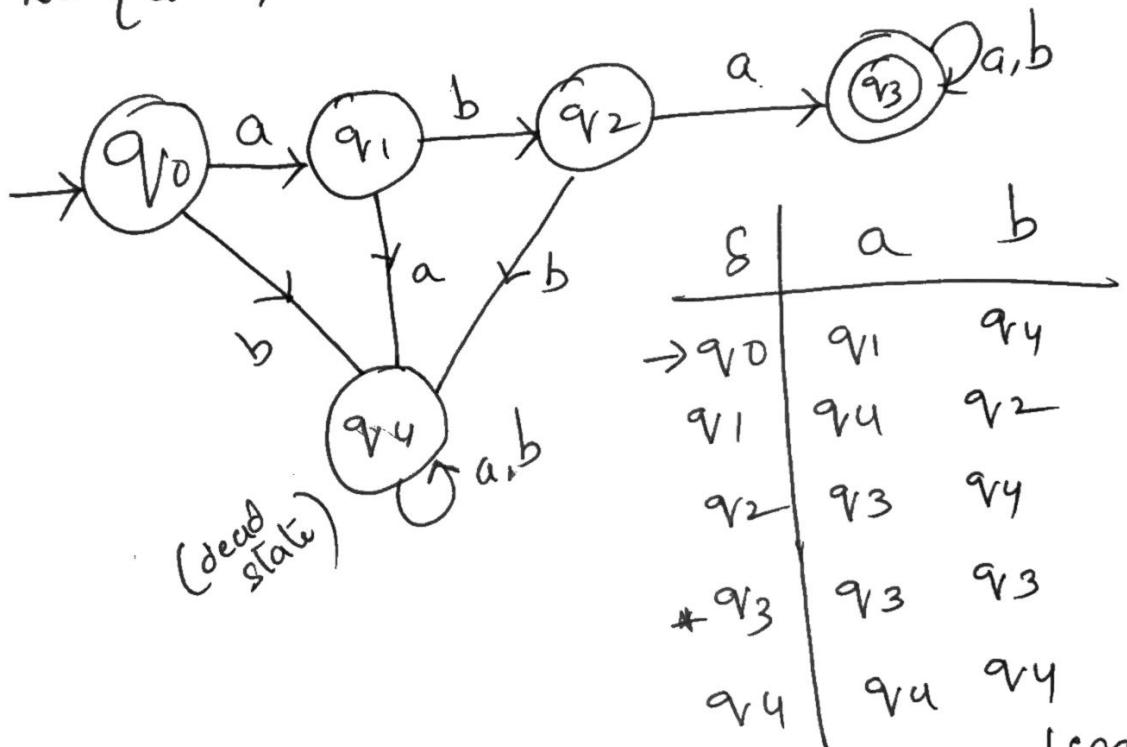
- ④ Construct DFA which accept set of all strings over $\{a, b\}$ which start with $i \geq 1$
- $$L = \{a, ab, aab, aba, aa, \dots\}$$



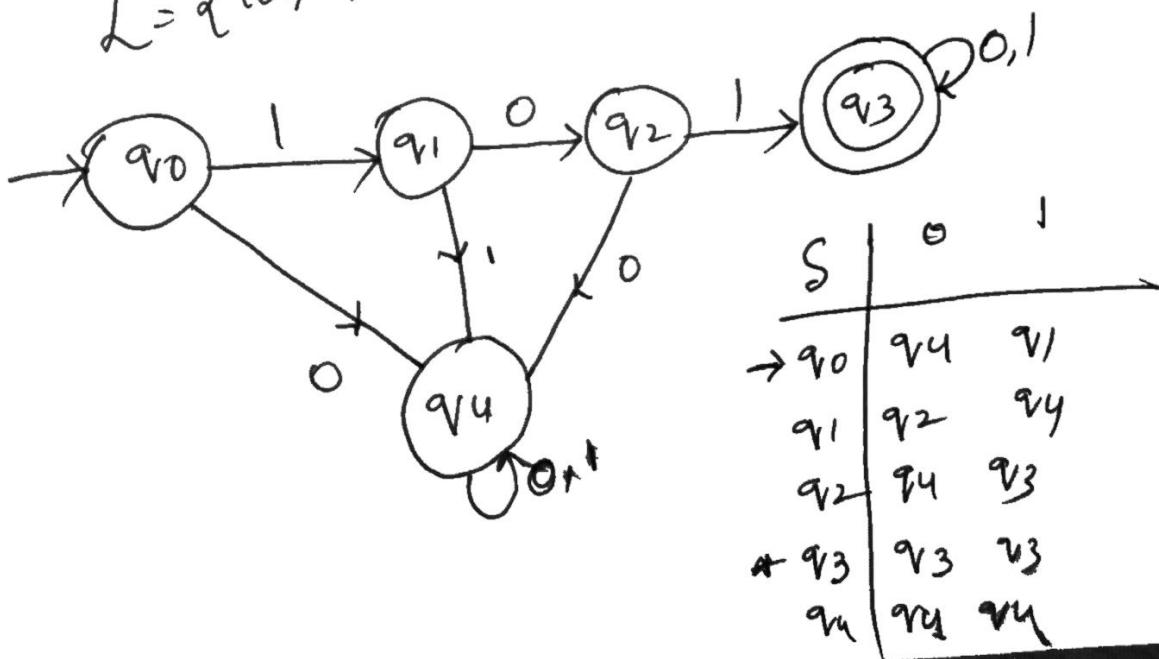
- ii) Start with 'ab'
- $$L = \{ab, aba, abb, abab, abaa, \dots\}$$



- iii) Start with 'aba'
 $L = \{aba, aba^a, abab, abaab\ldots\}$



- iv) Construct DFA which accepts set of binary strings begins with 101 $\subseteq \{0,1\}^*$
 $L = \{101, 1010, 1011, 10110, 101101\ldots\}$

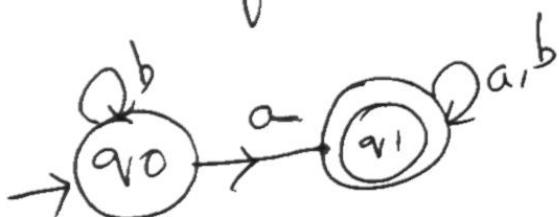


Substring:

5) Construct DFA which accept set of all strings over $\{a, b\}$ where each string contains

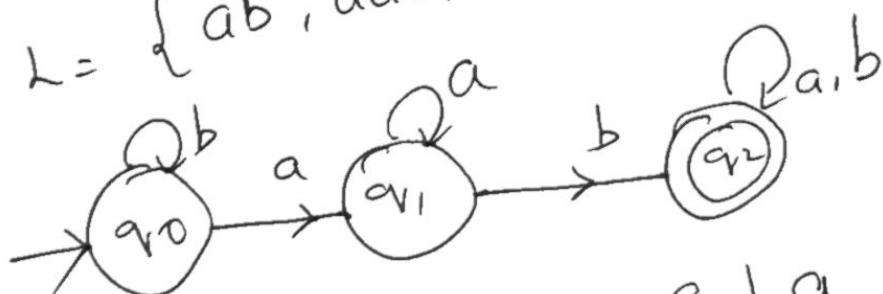
i) a
 $L = \{a, aa, ab, ba, bab, aba, aab, \dots\}$

min length = 1
 no. of states expected = 2



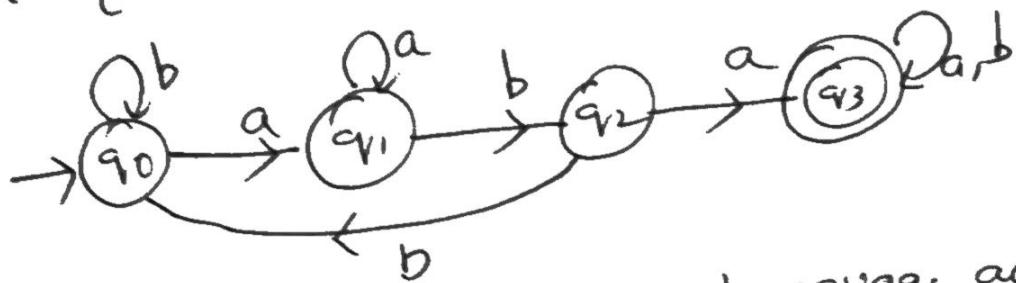
S	a	b
q0	q1	q0
q1	q1	q1

ii) 'ab' as substring
 $L = \{ab, aab, aba, bab, baab, \dots\}$

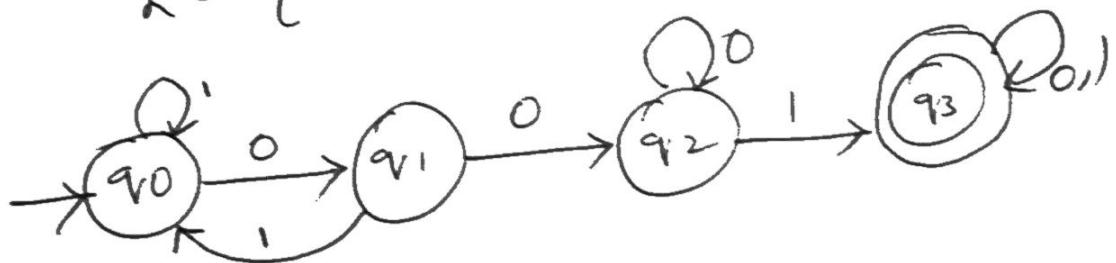


S	a	b
q0	q1	q0
q1	q1	q2
q2	q2	q2

iii) Contains 'aba'
 $L = \{ aba, aaba, ababa, baba, babaa \dots \}$

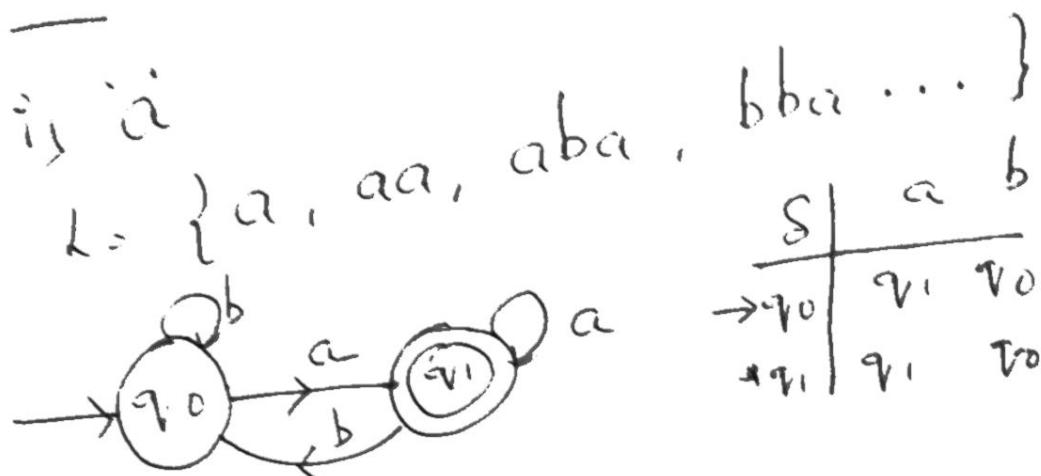


iv) Demonstrate DFA for language accepting strings which contains '001' as substring.
 $\Sigma = \{0, 1\}$
 $L = \{ 001, 1001, 0001, 0\ 0010 \dots \}$

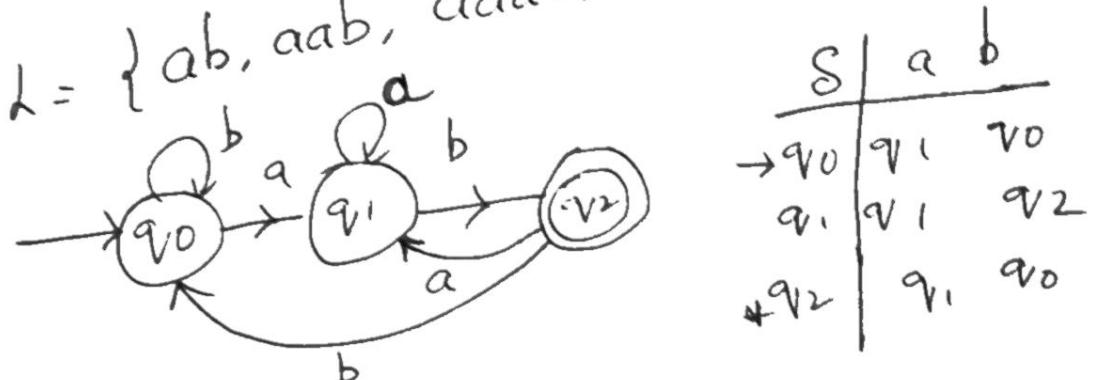


6. Ends with:

- (i) construct DFA which accepts set of all strings over $\{a, b\}$ where each string ends with



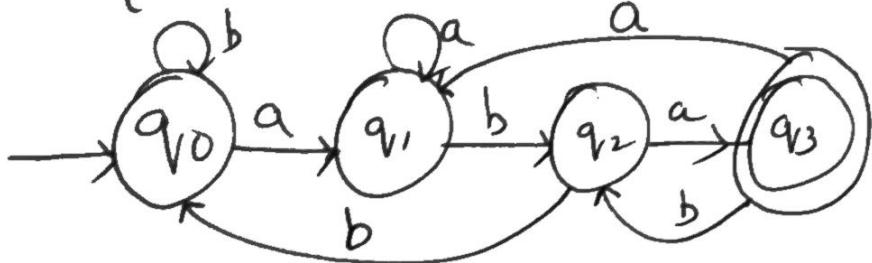
ii) 'ab' end with



iii) cod

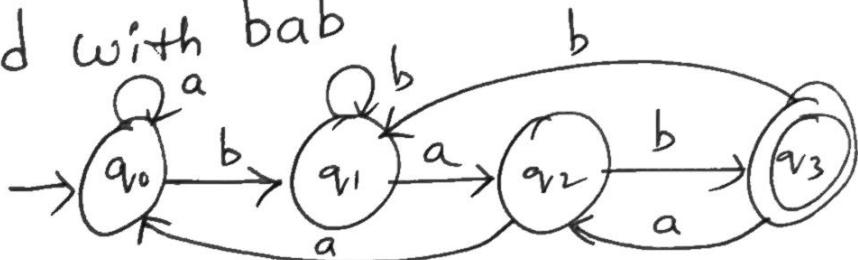
iii) end with aba

$$L = \{aba, aaba, baba \dots\}$$



δ	a	b
$\rightarrow q_{v0}$	q_{v1}	q_{v0}
q_{v1}	q_{v1}	q_{v2}
q_{v2}	q_{v3}	q_{v0}
$\leftarrow q_{v3}$	q_{v1}	q_{v2}

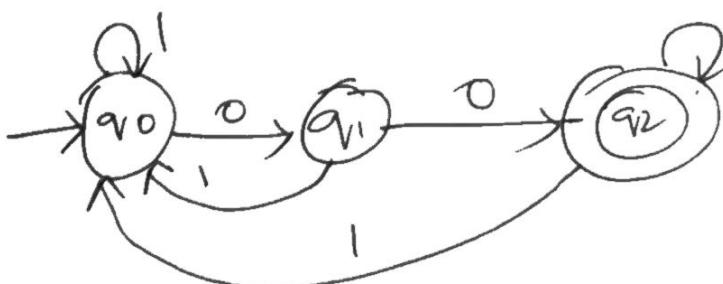
iv) end with bab



δ	a	b
$\rightarrow q_{v0}$	q_{v0}	q_{v1}
q_{v1}	q_{v2}	q_{v1}
q_{v2}	q_{v0}	q_{v3}
$\leftarrow q_{v3}$	q_{v2}	q_{v1}

v) Construct DFA to accept the strings ends with 00 only over $\Sigma = \{0,1\}$

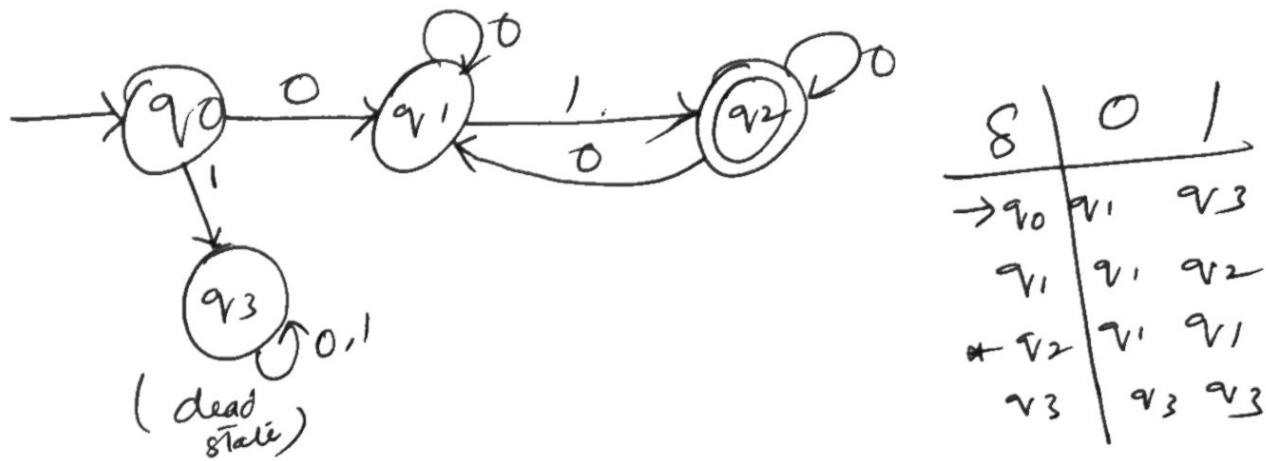
$$L = \{00, 000, 100, 0100, 1000 \dots\}$$



δ	0	1
$\rightarrow q_{v0}$	q_{v1}	q_{v0}
q_{v1}	q_{v2}	q_{v0}
$\leftarrow q_{v2}$	q_{v2}	q_{v0}

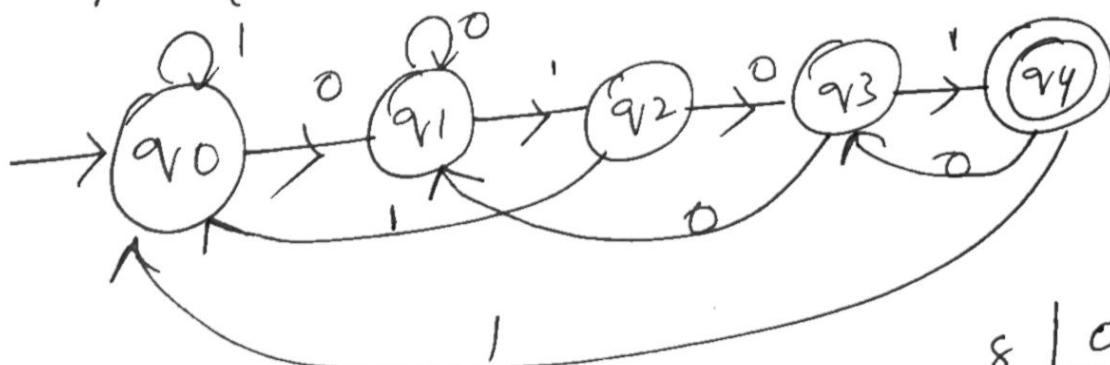
⑦ Construct DFA that start with '0' end with '1'
Over $\Sigma = \{0,1\}$

$$L = \{0011, \underline{01}, 001, 0101, 0011\cdots\}$$



⑧ Construct DFA which accept strings ending with 0101

$$L = \{0101, 10101, 00101, 100101, 01010\cdots\}$$



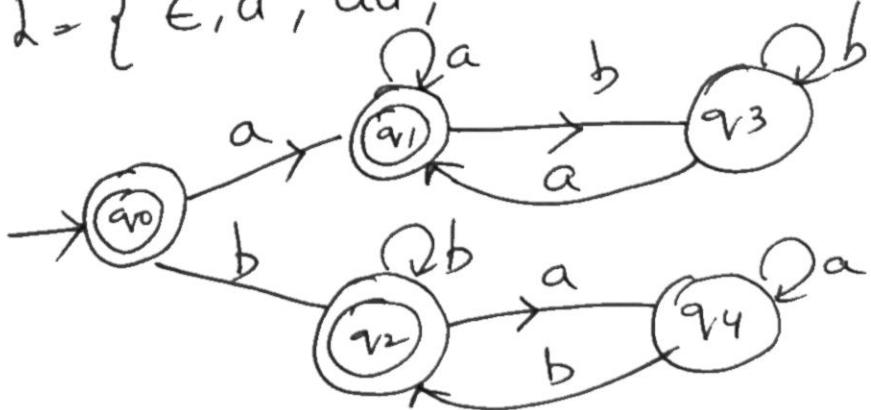
s	0	1
$\rightarrow q_0$	q_1	q_{10}
q_1	q_2	q_2
q_2	q_3	q_1
q_3	q_1	q_4
$\star q_4$	q_3	q_{10}

Q9 Construct a DFA for the following Lang's

i) $L = \{ w \mid w \text{ starts \& ends with same symbol, } w \in (a,b)^* \}$

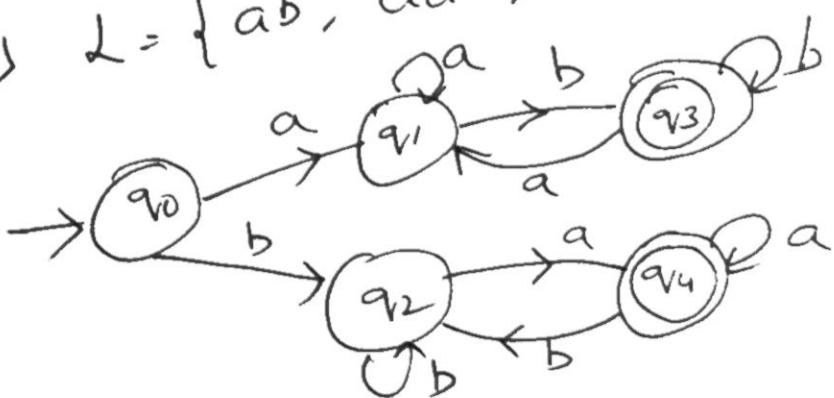
ii) $L = \{ w \mid w \text{ starts \& ends with different symbol, } w \in (a,b)^* \}$

sol i) $L = \{ \epsilon, a, aa, b, aba, aaba, bb \dots \}$



δ	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_4	q_2
q_3	q_1	q_3
q_4	q_4	q_2

sol ii) $L = \{ ab, aab, abb \dots \}$

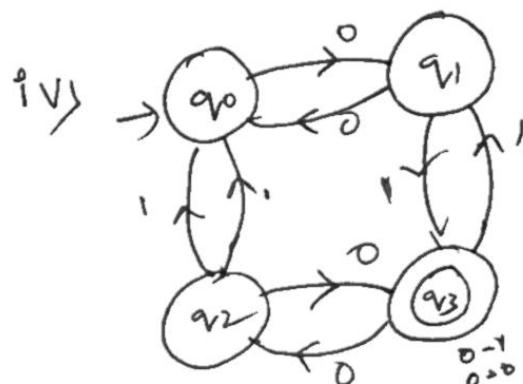
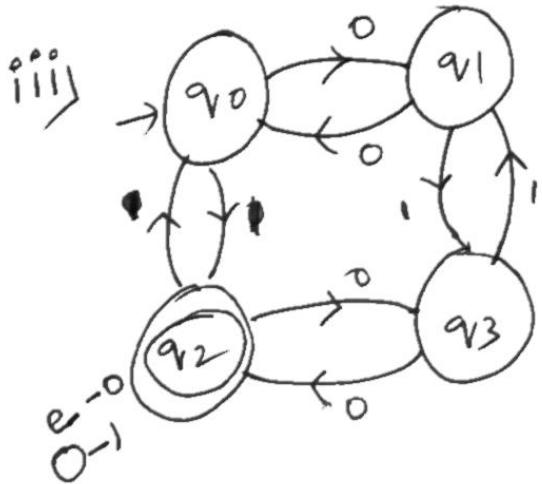
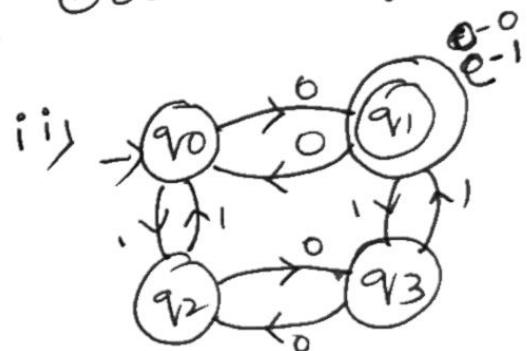
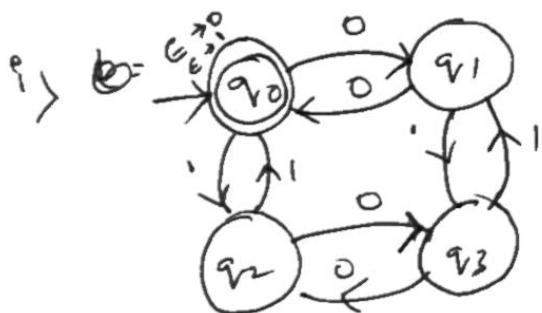


δ	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_4	q_3
q_3	q_1	q_2
q_4	q_4	q_2

⑩ Construct a DFA which accepts the strings on $\Sigma = \{0, 1\}$

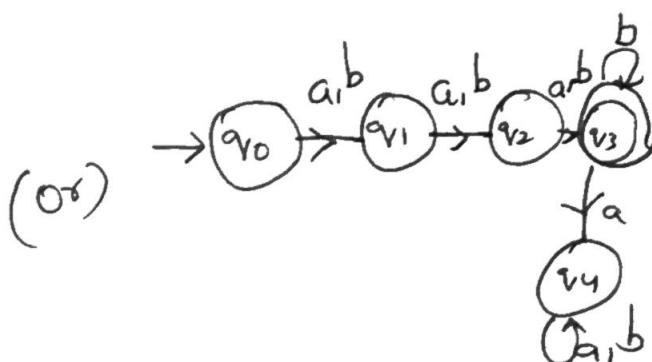
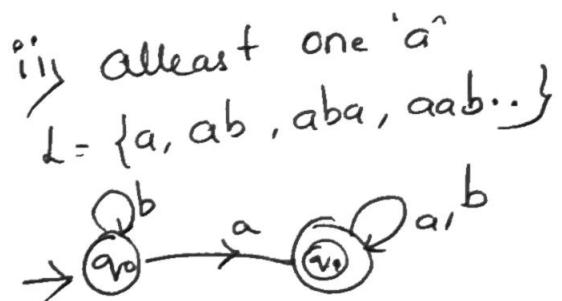
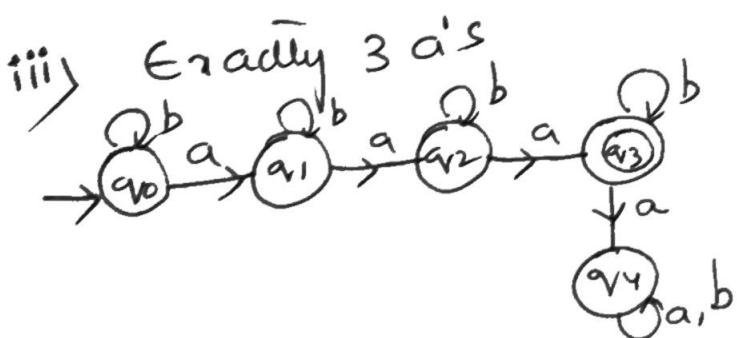
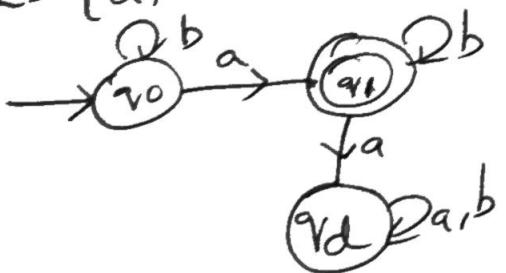
- i) Even no: of 0's
- ii) Even no: of 0's
- iii) Odd no: of 0's
- iv) Odd no: of 0's

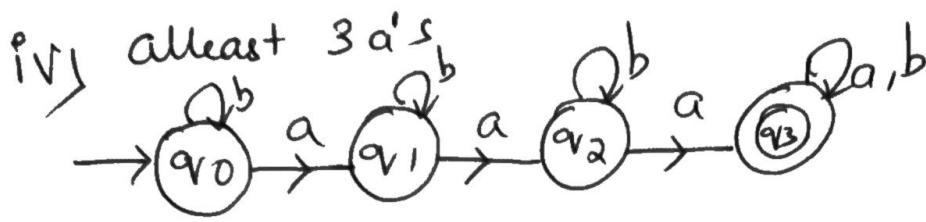
ϵ even no: of 1's
 ϵ odd no: of 1's
 ϵ even no: of 1's
 ϵ odd no: of 1's



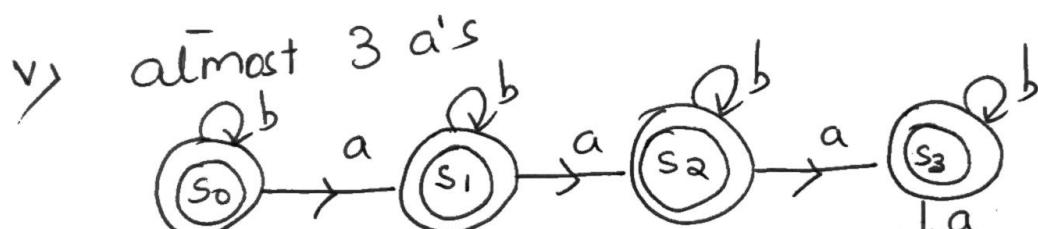
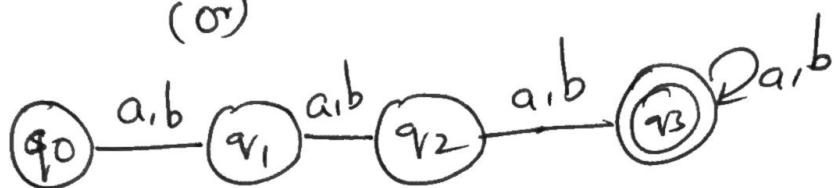
⑪ Construct a DFA to accept the strings
 $\Sigma = \{a, b\}$ having

- i) Exactly one 'a'
- ii) atleast one 'a'
- iii) Exactly 3 a's
- iv) atleast 3 a's
- v) almost 3 a's
- vi) almost 1 a
- vii) Exactly one 'a'
 $L = \{a, ab, abb, bab, \dots\}$



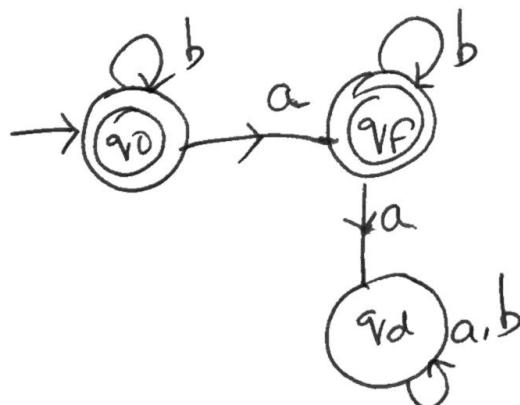


(or)



vi) almost 1 a

$$L = \{ \epsilon, bbb, a, ab \dots \}$$

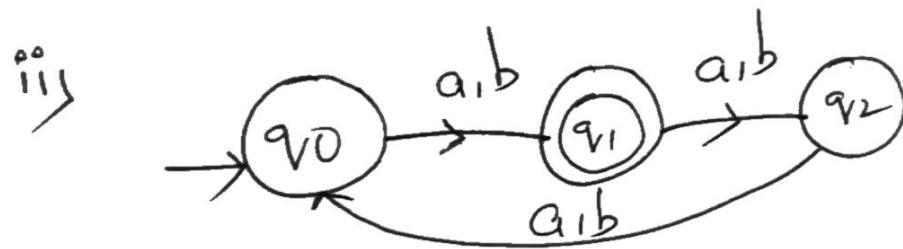
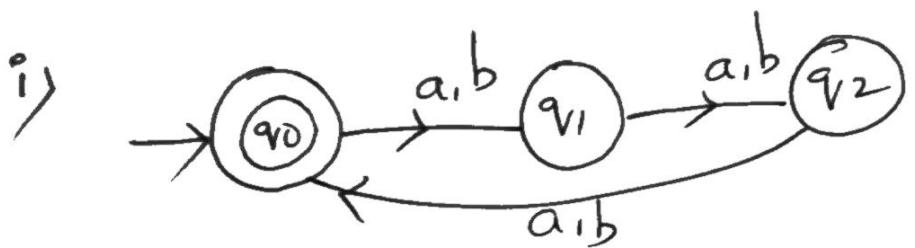


12) DFA for

i) $\{w \mid |w| \bmod 3 = 0\}$ for $(a, b)^*$

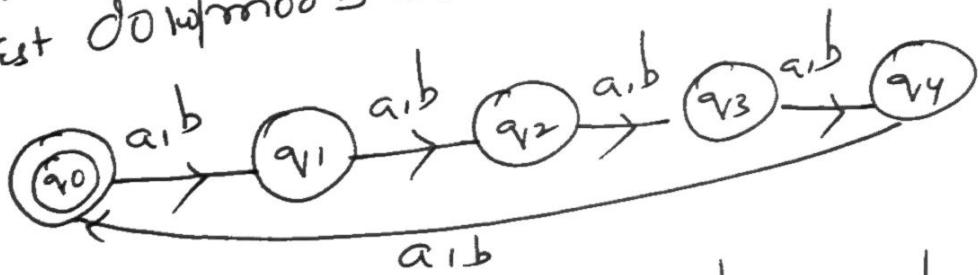
ii) $\{w \mid |w| \bmod 3 = 1\}$ for $(a, b)^*$

iii) $\{w \mid |w| \bmod 5 \neq 0\}$ for $(a, b)^*$

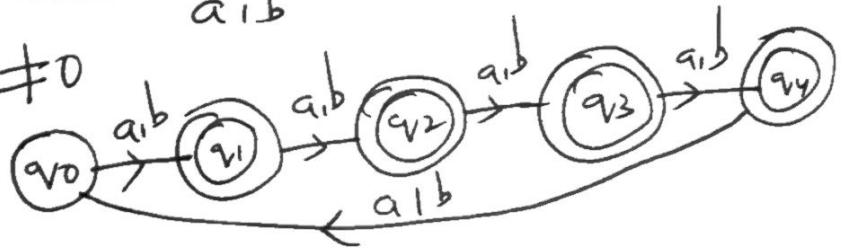


iii) $\{w \mid |w| \bmod 5 \neq 0\}$

first do $|w| \bmod 5 = 0$



Now reverse for $\neq 0$
~~+ accepting to non-accepting~~



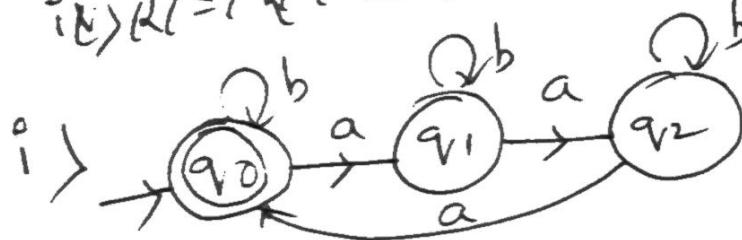
⑬ DFA for

$$\text{i)} L = \{ w \mid n_a(w) \bmod 3 = 0, w \in (a, b)^* \}$$

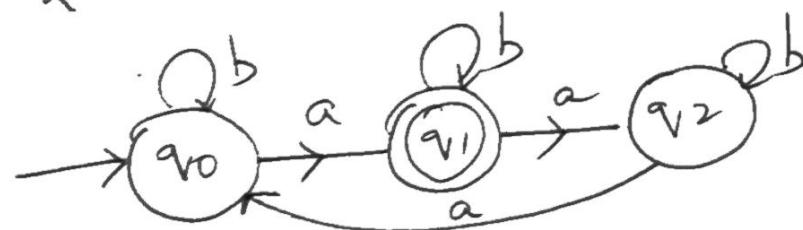
$$\text{ii)} L = \{ w \mid n_a(w) \bmod 3 = 1, w \in (a, b)^* \}$$

$$\text{iii)} L = \{ w \mid n_a(w) \bmod 3 = 2, w \in (a, b)^* \}$$

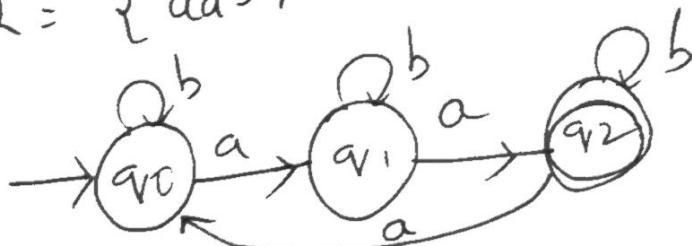
iv) $L = \{ \text{odd words} \}$



$$\text{v) } L = \{ \text{abb, aabbbbaa, aaab...} \}$$



$$\text{vi) } L = \{ \text{aab, aba, abbaaaaa...} \}$$

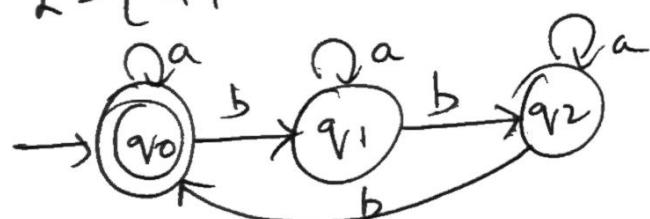


Q4 DFA for
 $L = \{w \mid n_b(w) \bmod 3 = 0, w \in (a, b)^*\}$

i) $L = \{w \mid n_b(w) \bmod 3 = 1, w \in (a, b)^*\}$

ii) $L = \{w \mid n_b(w) \bmod 3 = 2, w \in (a, b)^*\}$

iii) $L = \{a, bbb, abbb, aabb... \}$



iv) $L = \{b, ab, ba, abbb, bbaabb... \}$



v) $L = \{bb, abb, bba, ababab... \}$



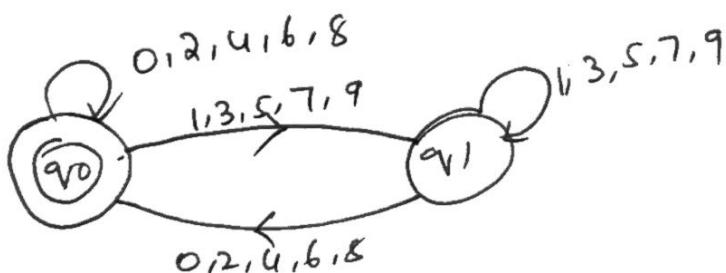
(15) Construct DFA for decimal no. divisible by

i) 2
ii) 3
iii) 5

$\Rightarrow q_0 \rightarrow n \% 2 = 0$

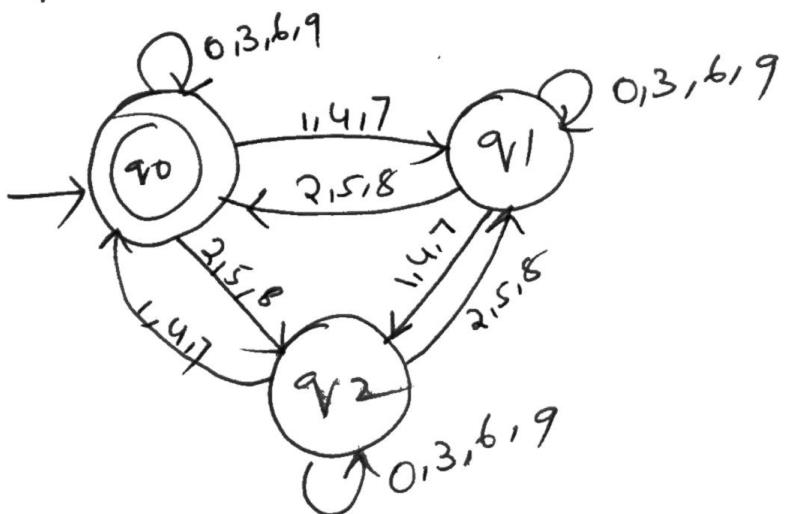
$q_1 \rightarrow n \% 2 = 1$

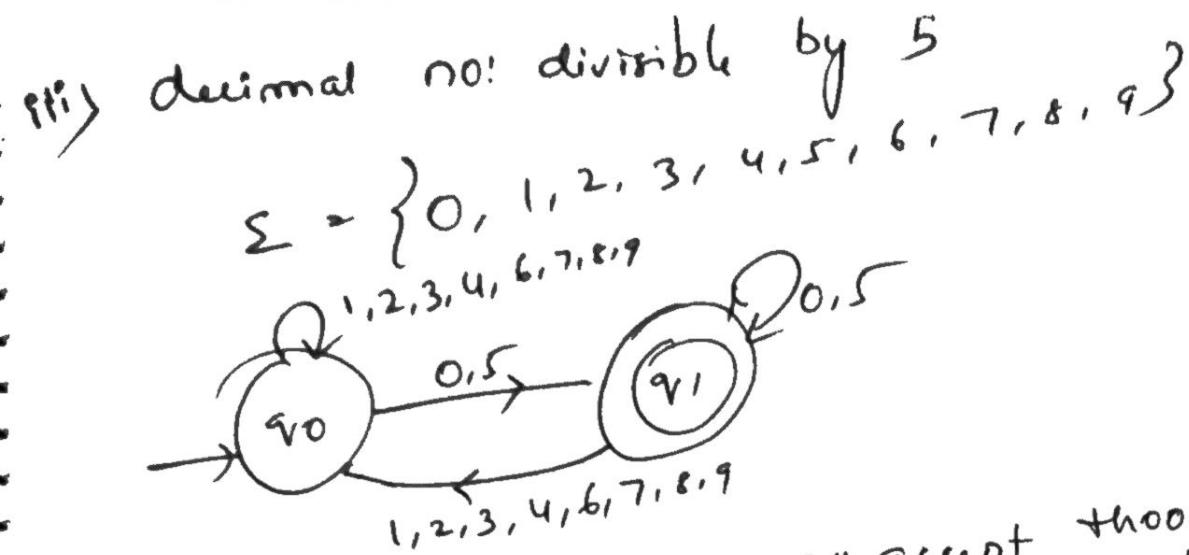
	$\{0, 2, 4, 6, 8\}$	$\{1, 3, 5, 7, 9\}$
$\rightarrow q_0$	q_0	q_1
$\rightarrow q_1$	q_0	q_1



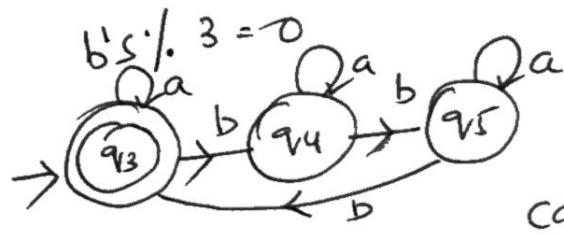
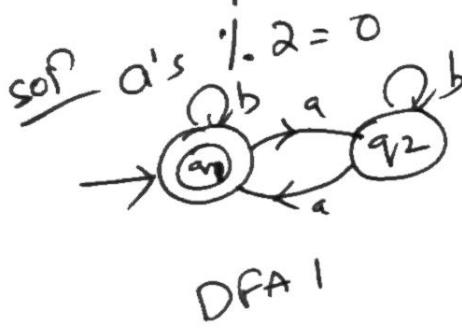
ii) $q_0 \rightarrow n \bmod 3 = 0$
 $q_1 \rightarrow n \bmod 3 = 1$
 $q_2 \rightarrow n \bmod 3 = 2$

	$\{0, 3, 6, 9\}$	$\{1, 4, 7\}$	$\{2, 5, 8\}$
q_0	q_0	q_1	q_2
q_1	q_1	q_2	q_0
q_2	q_2	q_0	q_1

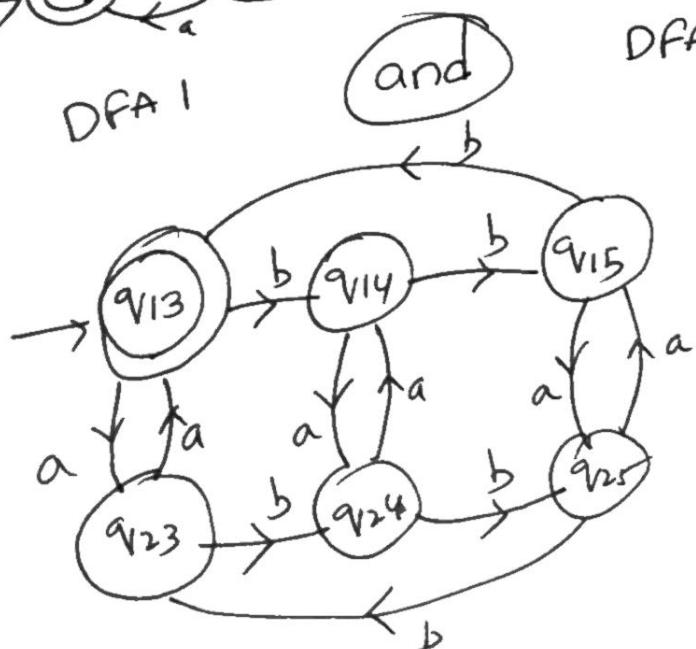




(16) Describe a DFA that will accept those no: of a's is divisible by 2 & b's divisible by 3. Sketch Transition table.



Cartesian product
 $q_1 \times q_2 = q_{12}$
 $q_1 \times q_4 = q_{14}$

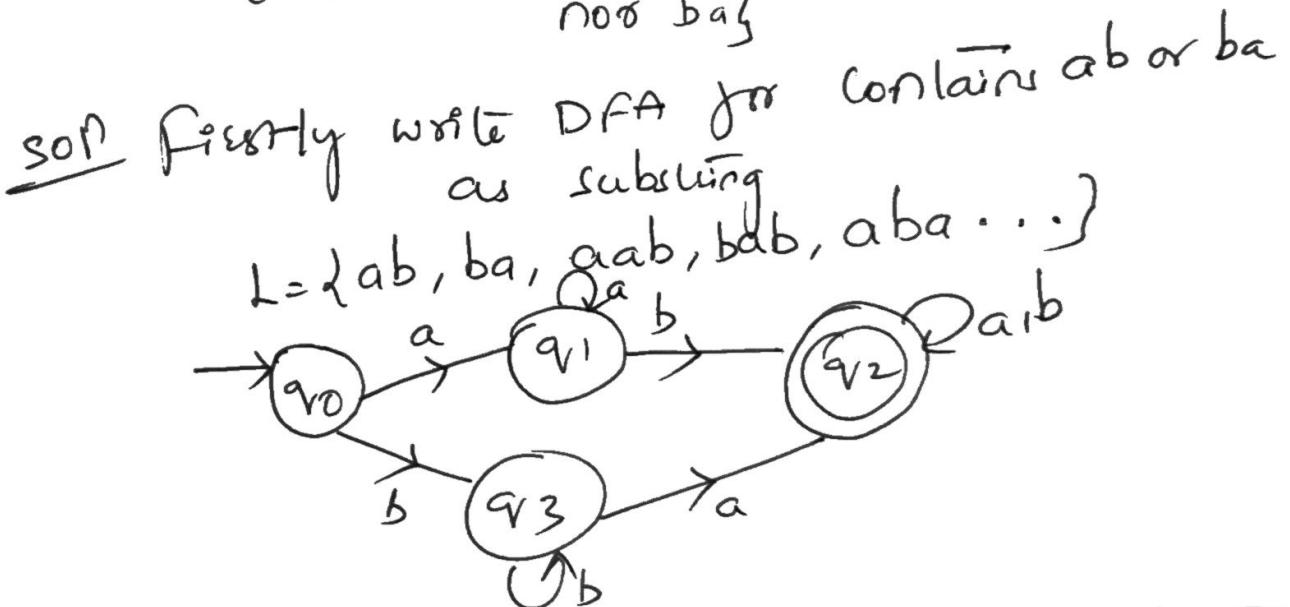


Transition table

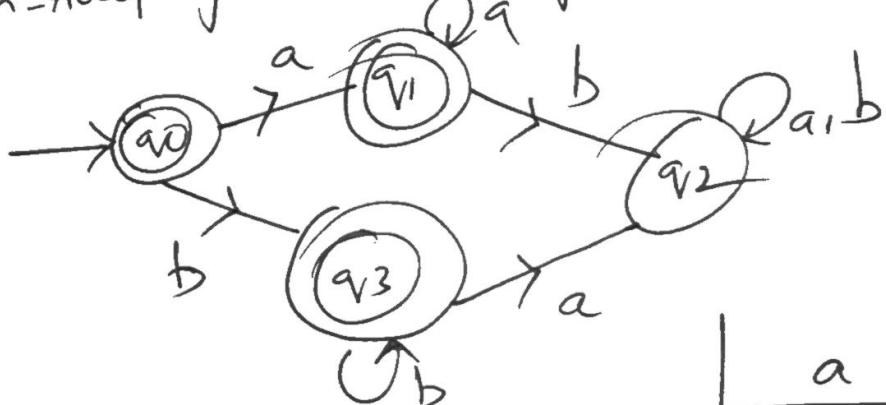
	a	b
q_{13}	q_{23}	q_{14}
q_{14}	q_{24}	q_{15}
q_{15}	q_{25}	q_{13}
q_{23}	q_{13}	q_{24}
q_{24}	q_{14}	q_{25}
q_{25}	q_{15}	q_{23}

Q17) Describe DFA, the language recognized by
the automaton being

$$L = \{ w \mid w \text{ contains neither the substring } ab \\ \text{ nor } ba \}$$



NOW reverse DFA i.e. Accepting to non-Accepting & non-Accepting to Accepting.



	a	b
*	$\rightarrow q_0$	q_1
q_1	q_1	q_2
q_2	q_2	q_2
q_3	q_2	q_3

Non-Deterministic Finite Automata (NFA)

A finite automata is called NFA if there exists one or more transitions from a state on the same input symbol (Choices of moves)

→ It is not compulsory that all states in NFA have to consume all the input symbols in Σ .

→ Formal Definition of NFA :-

$$M = (Q, \Sigma, \delta, q_0, F)$$

Q → Finite set of states

Σ → Finite set of symbols called the alphabet

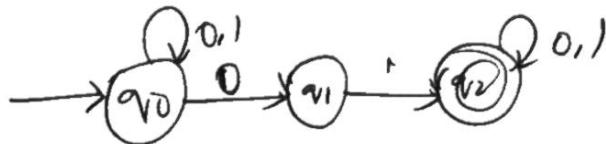
δ → Transition function where $\delta: Q \times \Sigma \rightarrow 2^Q$

q_0 → Initial state from where any input is $(q_0 \in Q)$

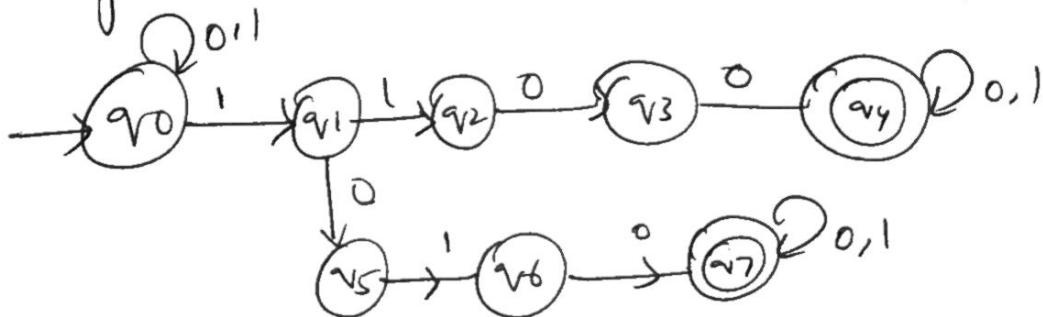
F → Set of final states $Q (F \subseteq Q)$

' δ ' is a Cartesian product of states & symbols giving a state in power set of Q .

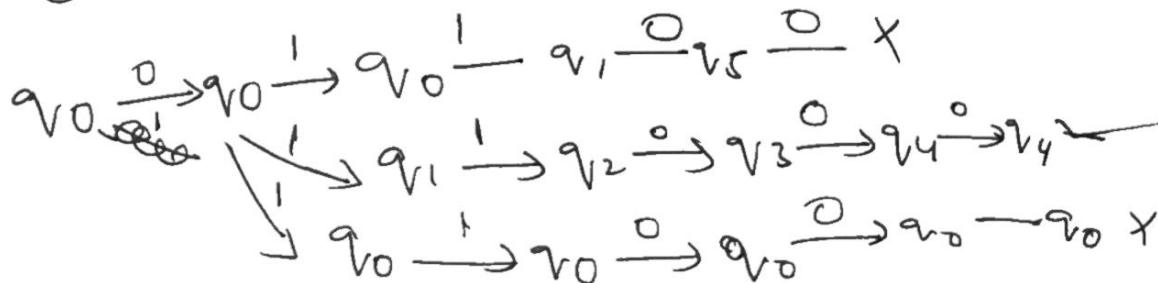
eg: let $w = X01Y$ where $x \& y$ are seq of 0's & 1's



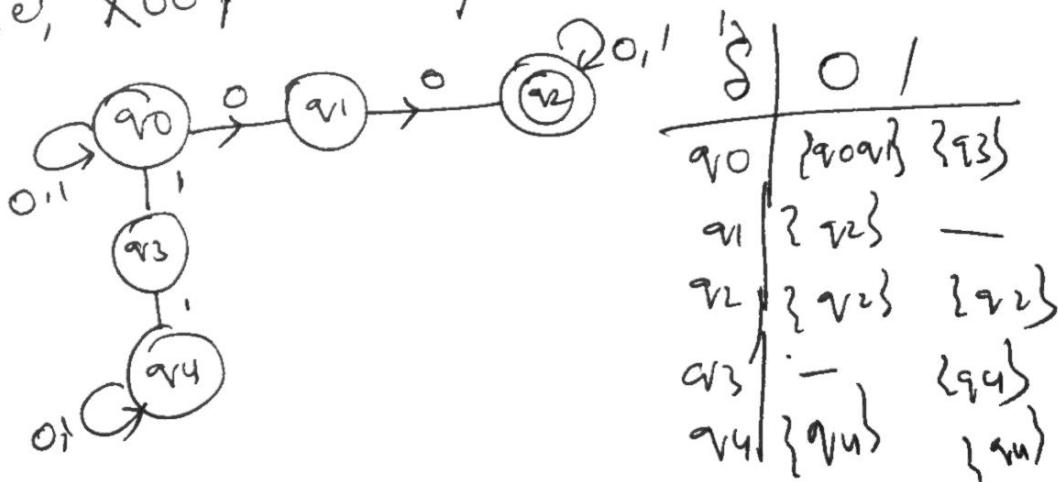
eg: construct an NFA which accept strings containing 1100 or 1010 as substring



ID 01100

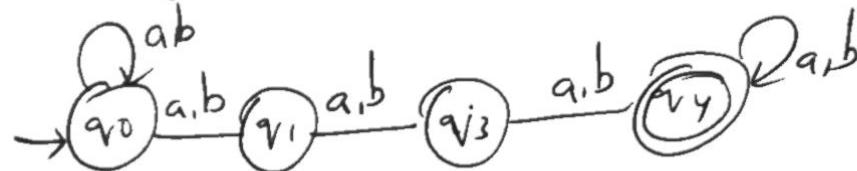


eg: string accepts two consecutive 0's OR
ie, X00Y or X11Y



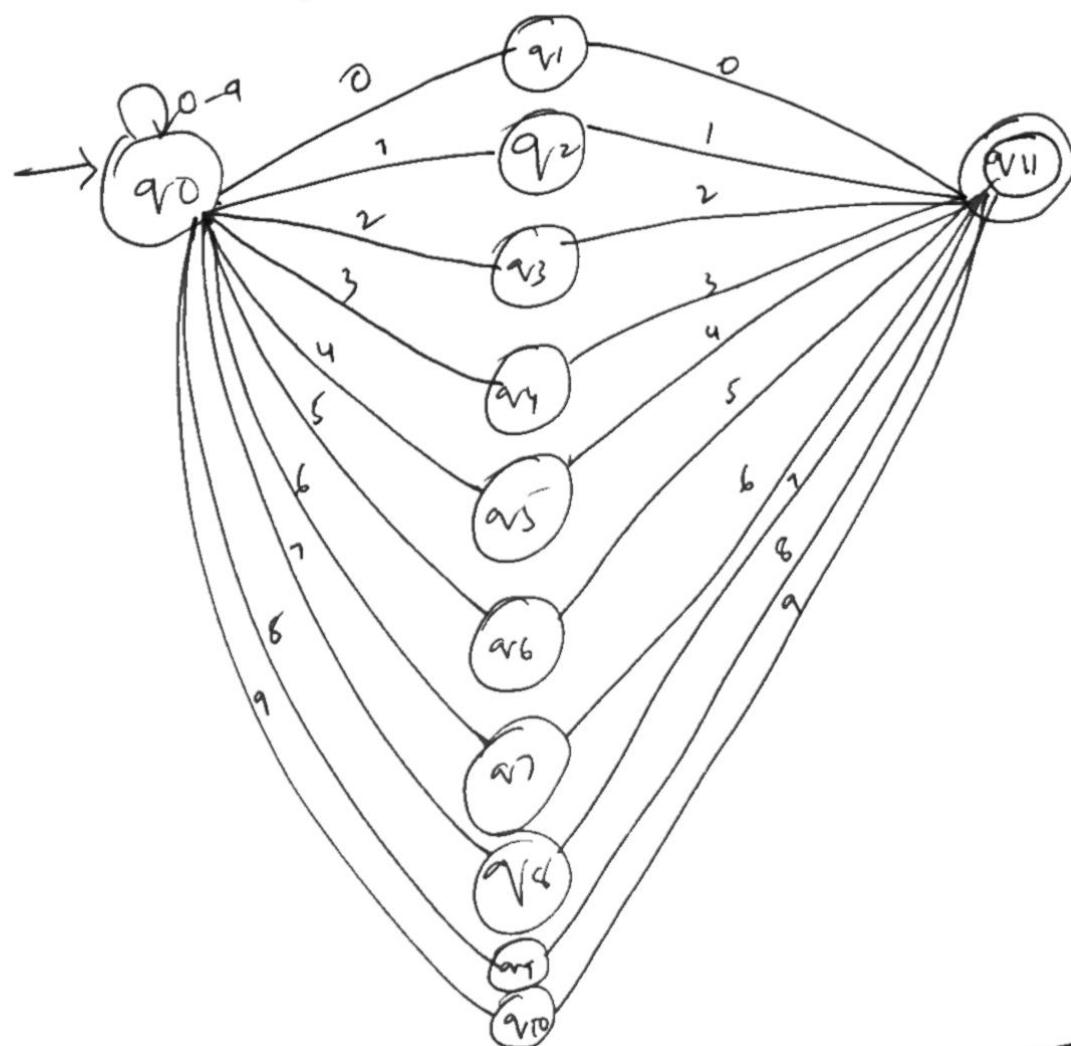
→ NFA for strings in which the 4th symbol from right end is always 'a' over $\Sigma = \{a, b\}$

$$L = \{abbb, aaaa, abab, abaabb \dots\}$$



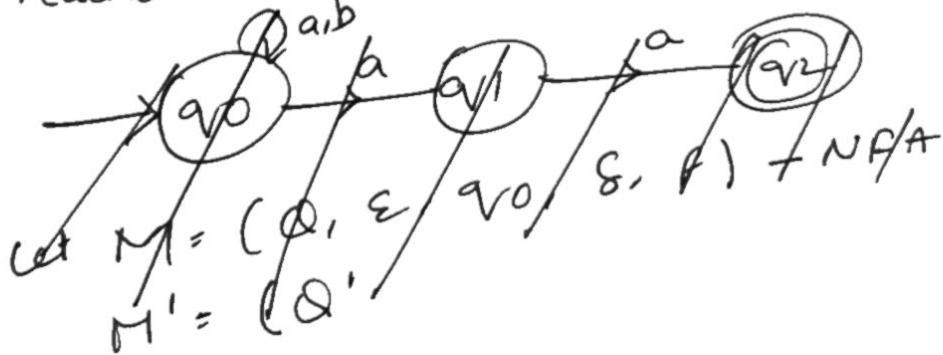
→ NFA for $\Sigma \{0 \dots 9\}$ such that final digit has appeared before.

$$L = \{010, 1\underline{2}13\underline{2}, 1\underline{2}34\underline{3}\}$$



Conversion of NFA to DFA

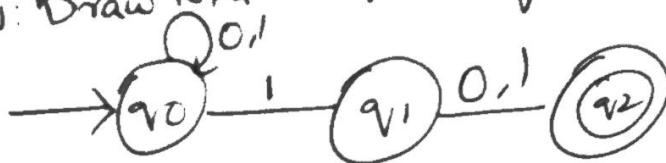
- A language that can be accepted by a DFA can be accepted by an NFA. Every DFA is an NFA.
- Conversion of NFA to DFA is called subset construction or powerset construction.
- Each state in the DFA is associated with a set of states in the NFA.
- The start state in the DFA corresponds to the start state of the NFA plus all states reachable via ϵ -transitions.



Conversion of NFA to DFA

NFA of all binary strings which 2nd last bit is '1'

so steps: Draw NFA



Step 2: first write Transition Table for NFA.

s	0	1
$\rightarrow q_0$	$q_0 \{q_0q_1\}$	
q_1	q_2	q_2
q_2	-	-

Step 3: Now write Transition Table for DFA
 → write first row as it is then expand all states

s	0	1
$\rightarrow q_0$	$q_0 \{q_0q_1\}$	
q_0q_1	$\{q_0q_1\} \{q_0q_2\} \{q_1q_2\}$	
q_0q_2	$q_0 \{q_0q_1\}$	
q_1q_2	$\{q_0q_2\} \{q_1q_2\}$	

→ ∵ q_2 is final state in NFA make q_2q_2 final wherever it is.



$\rightarrow L = \{ \text{Starts with 'a'} \} \quad \Sigma = \{a, b\}$



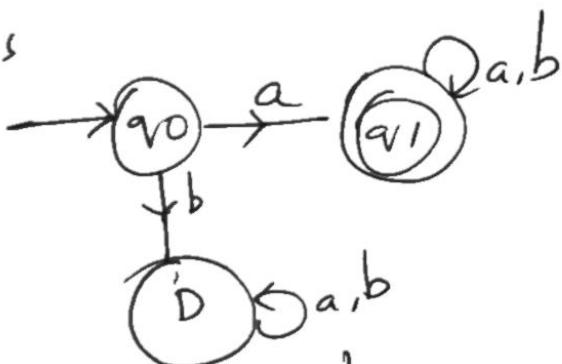
S	a	b
$\rightarrow q_0$	q_1	-
q_1	q_1	q_1

$\rightarrow \text{DFA}$

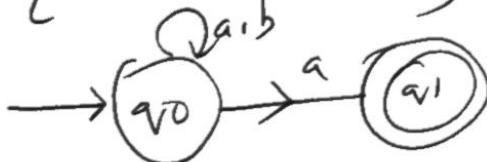
S	a	b
$\rightarrow q_0$	q_1	D
q_1	q_1	q_1
D	D	D

(\because NO Transition
it has to
redirect to dead
state)

$\therefore \text{DFA is}$

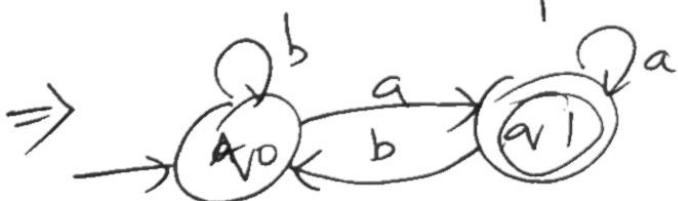


$\rightarrow L = \{ \text{ends with 'a'} \}$



S	a	b
q_0	$q_0 q_1$	q_0
q_1	-	-

S	a	b
q_0	$q_0 q_1$	q_0
q_1	$q_0 q_1$	q_0

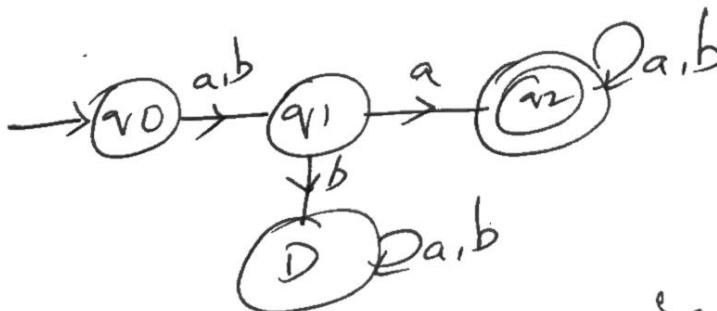


→ convert NFA to DFA for which NFA with second symbol from LHS is 'a'

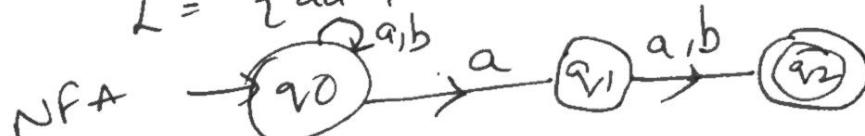


<u>NFA</u>	δ	a	b
→ q_0		$q_1 \ q_1$	
q_1		q_2	—
* q_2		$q_2 \ q_2$	

<u>DFA</u>	δ'	a	b
→ q_0		$q_1 \ q_1$	
q_1		$q_2 \ D$	
q_2		$q_2 \ q_2$	q_2
D		D	D

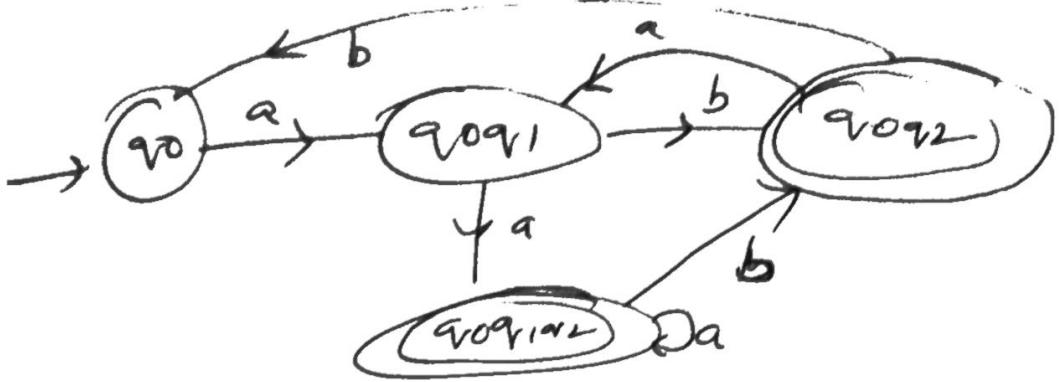


→ second symbol from RHS is 'a'
 $L = \{aa, ab, aaa, baa, bab\ldots\}$

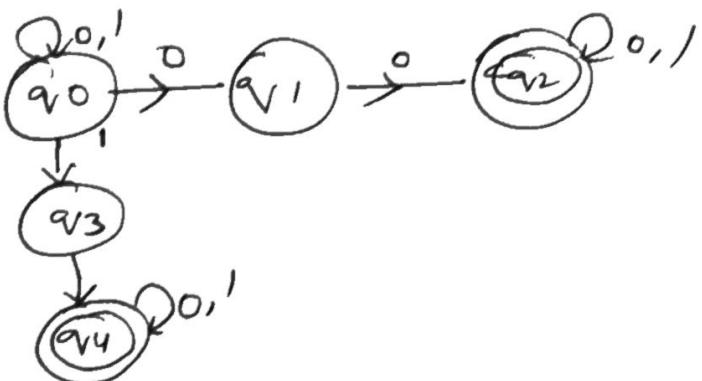


<u>NFA</u>	δ	a	b
→ q_0		$\{q_0q_1\} \ \{q_0\}$	
q_1		$\{q_2\} \ \{q_2\}$	
* q_2		—	—

<u>DFA_S</u>	δ	a	b
→ q_0		$[q_0q_1] \ [q_0]$	
$[q_0]$		$[q_0q_1q_2] \ [q_0q_2]$	
$[q_0q_2]$		$[q_0q_1q_2] \ [q_0q_2]$	
$[q_0q_1q_2]$		$[q_0q_1q_2] \ [q_0q_2]$	
$[q_0q_2]$		$[q_0q_1] \ [q_0]$	
$[q_0q_1]$		$[q_0q_1] \ [q_0]$	



Given NFA is



NFA

δ	0	1
$\rightarrow q_0$	$\{q_0q_1\}$	$\{q_0q_3\}$
q_1	$\{q_2\}$	-
q_2	$\{q_2\}$	$\{q_2\}$
q_3	-	q_4
$\rightarrow q_4$	$\{q_1\}$	$\{q_1\}$

DFA

δ'	0	1
$\rightarrow q_0$	$\{q_0q_1\}$	$\{q_3q_0\}$
$\{q_0q_1\}$	$\{q_0q_2q_1\}$	$\{q_0q_3q_0\}$
$\{q_0q_2q_1\}$	$\{q_0q_1q_2\}$	$\{q_0q_2q_3q_1\}$
$\{q_0q_3q_0\}$	$\{q_0q_1q_3\}$	$\{q_0q_2q_4\}$
$\{q_0q_1q_2\}$	$\{q_0q_1q_2q_1\}$	$\{q_0q_1q_3q_4\}$
$\{q_0q_2q_3q_1\}$	$\{q_0q_1q_2q_3\}$	$\{q_0q_2q_3q_4\}$
$\{q_0q_1q_3\}$	$\{q_0q_1q_2q_4\}$	$\{q_0q_2q_3q_4\}$
$\{q_0q_2q_4\}$	$\{q_0q_1q_2q_3q_4\}$	$\{q_0q_2q_3q_4\}$
$\{q_0q_1q_3q_4\}$	$\{q_0q_1q_2q_3q_4\}$	$\{q_0q_2q_3q_4\}$

