

Data_structure_note

Thursday, May 30, 2024 2:42 PM

1. Data Structure => is a way of organizing data different ways of storing data on your computer
EX: is like preparing for cooking you slice up vegetables

2. Algorithm => the process that does something to data to produce the output operations on different data structure

data structure + algorithm = programming

Steps to learn:

a.. Big O notation => is the language of analyzing algorithms and data structures.

b. Data structures list:

1. Arrays
2. Linked Lists
3. Queues and Stacks
4. Trees
5. Graphs
6. Hash Maps
7. pointers
8. Memory => 1 byte = 8 bits

c. Algorithms:

1. recursion
2. sorting algorithms
3. Graph search algorithms
4. Dynamic programming
5. common problem solving patterns

3. Memory (RAM) vs. Storage

After turning off the computer, Storage is permanent, and memory will disappear.

int a = 1; => 32 bits for int

4 bytes = 32 bits = 1 integer

4. classes and objects

```
//class
class Robot {
    string name;
    string color;
    int weight;
//constructors
    Robot(String n, String c, int w){
        this.name = n;
        this.color = c;
        this.weight = w;
    }
//function
    void introduceSelf(){
        system.out.println("My name is " + this.name);
    }
}
```

```

    }

}

//to use constructors and functions
Robot r1 = new robot("Leo", "Red", "37");
r1.introduceSelf();

```

5. Linked List

6 -> 3 -> 4 -> 2 -> 1 -> null

```

class Node{
    int data;
    Node next;
    Node prev;
    //constructor
    Node(int data){
        this.data = data;
    }
}

Node head = new Node(6);
Node nodeB = new Node(3);
Node nodeC = new Node(4);
...

head.next = nodeB
nodeB.next = nodeC
...

//count how many nodes we have
int countNodes(Node head){
    //assuming head != null
    int count = 1;
    Node current = head;
    while(current.next != null){
        current = current.next;
        count += 1;
    }
}

```

6. Recursion

```

//factorial
n! = n. (n-1)!    if n >= 1
    1            otherwise (if n = 0 )
Ex: 4! = 4 x 3 x 2 x 1 = 24

int fact(int n){
    //assume that n is a positive integer or 0
    if (n >= 1) {
        return n * fact(n-1);
    }
}

```

```

    } else {
        return 1;
    }
}

```

// Fibonacci sequence

Ex: 1, 1, 2, 3, 5, 8

```

int fib(int n){
    if (n >= 3){
        return fib(n-1) * fib(n-2);
    } else {
        return 1;
    }
}

```

google interview problem

Recursive staircase problem

num_way(N) = num_ways(N-1) + num_ways(N-2)

num_way(0) = 1

num_way(1) = 1

//python

//this wont work if n =2

```

def num_ways(n):
    if n == 0 or n == 1:
        return 1
    else:
        return num_ways(n-1) + num_ways(n-2)

```

//fixed

```

def num_ways_bottom_up(n):
    if n == 0 or n == 1:
        return 1
    nums = [0] * (n + 1)
    nums[0] = 1
    nums[1] = 1
    for i in range(2, n + 1):
        nums[i] = nums[i - 1] + nums[i - 2]
    return nums[n]

```

Example usage

total_feet = 11

print(f"Number of ways to jump {total_feet} feet: {num_ways_bottom_up(total_feet)}")

//variation problems

X = {1,3,5}

```

def num_ways_X(n):
    if n == 0:
        return 1
    total = 0;
    for each i in {1,3,5}:

```

```

        if n - i >= 0:
            total += num_ways_X(n-i)
    return total

```

```

//fixed
def num_ways_bottom_up_X(n):
    if n == 0:
        return 1
    nums = [0] * (n + 1)
    nums[0] = 1
    for i in range(1, n + 1):
        total = 0
        for j in {1, 3, 5}:
            if i - j >= 0:
                total += nums[i - j]
        nums[i] = total
    return nums[n]

```

7. Big O notation

a. runtime = time to takes to execute a piece of code

linear time = $O(n)$

constant time = $O(1)$

quadratic time = $O(n^2)$

1. find the fastest growing term

2. take out the coefficient

$T = an + b = O(n)$

$T = cn^2 + dn + e = O(n^2)$

The image shows a handwritten analysis of two Python functions, `stupid_function` and `find_sum`, with their corresponding Big O time complexities. The analysis is written on a dark background with white and yellow text.

Function 1: `stupid_function`

```

def stupid_function(given_array):
    total = 0
    return total

```

Annotations for `stupid_function`:

- `total = 0` is annotated with $O(1)$.
- `return total` is annotated with $O(1)$.

Complexity analysis for `stupid_function`:

$$T = O(1) + O(1) = c_1 + c_2 = c_3 = c_3 \times 1 = O(1)$$

Function 2: `find_sum`

```

def find_sum(given_array):
    total = 0
    for each i in given_array:
        total += i
    return total

```

Annotations for `find_sum`:

- `total = 0` is annotated with $O(1)$.
- `for each i in given_array:` is annotated with $O(n)$.
- `total += i` is annotated with $O(1)$.
- `return total` is annotated with $O(1)$.

Complexity analysis for `find_sum`:

$$T_2 = O(1) + n \times O(1) + O(1) = c_4 + n \times c_5 = O(n)$$

```
array_2d = [[1, 4, 3], [3, 1, 9], [0, 5, 2]]
```

```
[[1, 4, 3, 1], [3, 1, 9, 4], [0, 5, 2, 6], [4, 5, 7, 8]]
```

$$T_3 = O(1) + n^2 \times O(1) + O(1)$$

$$= c_6 + n^2 \times c_7 = O(n^2)$$

$$T_4 = \overset{0}{O}(2n^2) = \overset{c}{O}(n^2)$$

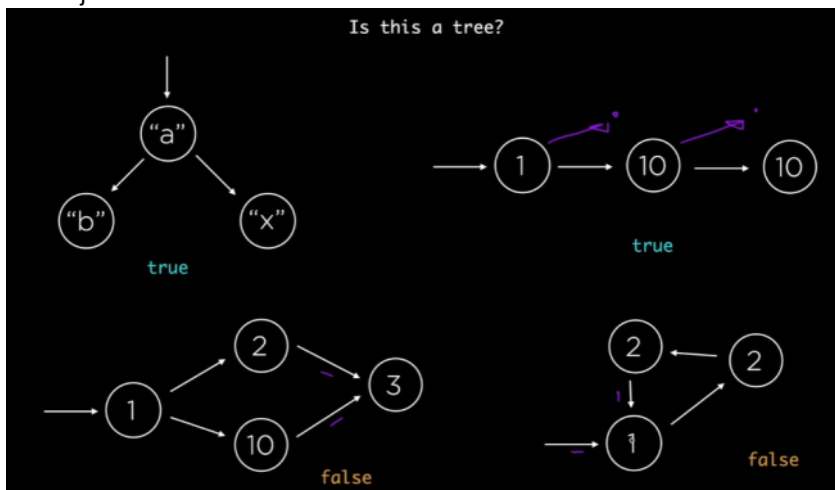
$$T_4 = 2n^2 \times c + \dots = 2n^2 \times c + c_2n + c_3$$

$$= (2c) \times n^2 + c_2n + c_3 = O(n^2)$$

```
def find_sum_2d(array_2d):
    total = 0 -> O(1)
    for each row in array_2d:
        for each i in row:
            total += i -> O(1)
    return total -> O(1)
```

8. Tree =>

```
Class Node{
    Int data
    Node left
    Node right
}
```



Binary Tree =>

is a data structure in which each node has at most two children, referred to as the left child and the right child.

9. Sorting

- a. **Linear search = $O(n)$ = $O(n/2)$** = It works by checking each element in the list, one by one, until the desired element is found or the end of the list is reached

```
def linear_search(arr, target):
    for i in range(len(arr)):
        if arr[i] == target:
            return i # Return the index of the target element
    return -1 # Return -1 if the target is not found
```

Example usage

```
arr = [34, 17, 23, 35, 45, 9, 1]
```

```

target = 23
result = linear_search(arr, target)

if result != -1:
    print(f"Element found at index {result}")
else:
    print("Element not found")

```

a. Binary search:

Arr[-50 ~ 50]

Target = 20

40 -> 20 -> 10 -> ... -> 1

$N \rightarrow \frac{n}{2} \rightarrow \frac{n}{4} \rightarrow \frac{n}{8} \rightarrow \dots \rightarrow 1$

$n \rightarrow \frac{n}{2} \rightarrow \frac{n}{2^2} \rightarrow \frac{n}{2^3} \rightarrow \dots \rightarrow \frac{n}{2^x} \approx 1$

$\frac{n}{2^x} \approx 1 \Rightarrow n = 2^x \Rightarrow \log_2(n) = x = \mathbf{O(\log(n))}$

```

def search(arr, target):
    left = 0
    right = len(arr) - 1
    while left <= right:
        mid = (left + right) // 2 # make sure to round it down
        if arr[mid] == target:
            return mid
        elif target < arr[mid]:
            right = mid - 1
        else:
            left = mid + 1
    return -1

arr1 = [-2, 3, 4, 7, 8, 9, 11, 13]
assert search(arr1, 11) == 6
assert search(arr1, 13) == 7
assert search(arr1, -2) == 0
assert search(arr1, 8) == 4
assert search(arr1, 6) == -1
assert search(arr1, 14) == -1
assert search(arr1, -4) == -1
arr2 = [3]
assert search(arr2, 6) == -1
assert search(arr2, 2) == -1
assert search(arr2, 3) == 0
print("If you didn't get an assertion error, this program has run
successfully.")

```

1. Quicksort is typically the fastest for large datasets due to its low overhead and excellent average-case performance.

2. Mergesort is a good choice when stability is required and for data that doesn't fit in memory (external sorting).

3. Heapsort provides reliable $O(n \log n)$ performance with in-place sorting but is generally

outperformed by quicksort and mergesort.

4. Timsort is highly efficient for real-world data and is used in many standard libraries due to its adaptive nature and stability.