#### **COMP 250 Midterm exam:**

When: Wednesday Feb 22nd, 6:00pm - 7:30pm Where:

- Last name starting with A to L: McIntyre room 522
- Last name starting with M to Z: McIntyre room 504

#### What to bring:

- 0) A couple of pencils (not pen) to fill the scantron sheets
- 1) Your student ID card
- 2) A 1-page double side crib sheet (8.5 inches x 11 inches)
- 3) Your brain and energy!

#### Java programming

- Everything we've covered in class could be on the exam
  - Methods
  - parameter passin g
  - object oriented programming

# Recursive algorithms

- To write a recursive algorithm:
  - Find how the problem can be broken up in one or more smaller problems of the same nature
  - Remember the base case!
- Usually, better running times are obtained when the size of the subproblems are approximately equal
  - power(a,n) = a \* power(a,n) ⇒ O(n)
  - power(a,n) = (power(a,n/2))<sup>2</sup> ⇒ O(log n)
- Fibonnaci, BinarySearch, Power, Integer multiplication, MergeSort



### Recursive algorithms

- Fibonnaci
- · BinarySearch
- Power
- Integer multiplication
- · MergeSort
- · QuickSort

# Induction proofs

- To prove that a proposition P(n) holds for all  $n \ge a$ :
  - Base case:

Prove that P(a) holds

- Induction step on n:

Induction Hypothesis: Assume P(k) holds Prove that I.H. implies that P(k+1) holds

# Proof of correctness of iterative algorithms

#### **Using Loop invariants:**

- 1. Initialization: It is true prior to the first iteration of the loop.
- 2. Maintenance: If it is true before an iteration of the loop, it remains true before the next iteration.
- 3. Termination: When the loop terminates, the invariant gives us a useful property that helps show that the algorithm is correct.

#### Running time

- · Primitive operations
  - Running time is constant, indep. of problem size

    - Assigning a value to a variable
      Calling a method; returning from a method
    - · Arithmetic operations, comparisons
    - Indexing into an array
    - · Following object reference Conditionals
- Running time = Number of primitive operations
- Loops: Sum the running time of each iteration
- · findMin, selectionSort, insertionSort

#### Recurrences

- For recursive algorithms, we express the running time T(n) for an input of size n as a function of T(a) for some a<n
- Example:
  - Binary search: T(n) = T(n/2) + a if  $n \ge 1$
  - RecursiveFastMult.: T(n) = 3 T(n/2) + c n + d



# Solving recurrences

- Solving recurrence = give explicit formula for T(n)
- Substitution method:
- Replace occurrences of T() by their value
- Repeat until pattern emerges
- Prove by induction that guess is correct

#### Big-Oh notation

- f(n) is O(g(n)) iff there exist constants c and N such that  $f(n) \le c g(n)$  for all  $n \ge N$
- Proving that f(n) of O(g(n)), or f(n) is not O(g(n))
- Tricks to establish if f(n) is O(g(n)):
  - Hierarchy of big-Oh classes, Simplification rules
  - Test of the limit of the ratio
- · NEW! Theta notation

f(n) is  $\Theta(g(n))$  iff f(n) is O(g(n)) and g(n) is  $\Theta$  (f(n))

- $\rightarrow$  f(n) and g(n) grow equally fast (within a multiplicative constant)
- NEW! Omega notation

f(n) is  $\Omega(g(n))$  iff g(n) is O(f(n))

#### List Abstract Data Type

- · Operations supported
- Two possible implementations
  - Array-based
  - Linked lists
- · Advantages and disadvantages of each implementations

#### Linked lists

- Implementation (node: value, next)
- Basic operations
  - getFirst(), get(n), getLast()
  - removeFirst(), removeLast(), remove(o)
  - addFirst(o), addLast(o), add(o)
  - empty(), size()
- · Advantages and disadvantages over arrays

# Stacks

- Last-in First-out data structure
- Operations: push(o), pop(), top()
- Applications:
  - Back button on browser
  - checking parentheses
  - evaluating expressions (homework #3)

# Queues

- Queue:
  - First-in First-out data structure
  - Operations: enqueue, dequeue, front
- Doubly-ended queue:
  - Elements can be accessed, added, or removed at both ends
- Rotating array implementation