

## Computers playing games

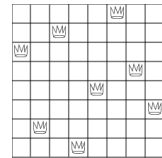


### One-player games

- Puzzle: Place 8 queens on a chess board so that no two queens attack each other (i.e. on the same row, same column, or same diagonal)

```

for  $i_1 \leftarrow 1$  to 8 // row of 1st queen
  for  $i_2 \leftarrow 1$  to 8 // row of 2nd queen
    ...
    for  $i_8 \leftarrow 1$  to 8 // row of 8th queen
      if (isValid( $i_1, i_2, \dots, i_8$ )) print  $i_1, i_2, \dots, i_8$ 
  
```



If we had a  $n \times n$  board, what would be the running time?



### Backtracking algorithm

- Idea: place queens from first row to last, but stop as soon as an invalid board is reached and backtrack to the last valid board

- Very similar to depth-first search

Algorithm placeQueens(partialBoard[8][8], row)

Input: A board with queens placed on rows 0...row-1

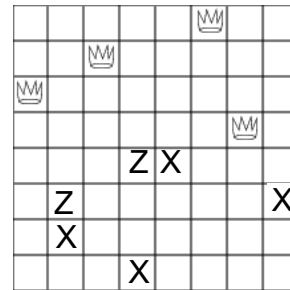
Output: Prints all valid configurations that can be reached from this board

```

if (row==8) print partialBoard;
else
  for  $i = 0$  to 8-1 do
    partialBoard[row][i] = QUEEN;
    if (isValid(partialBoard)) then placeQueens(partialBoard, row+1)
    partialBoard[row][i] = EMPTY; // reset board to original position
  
```



### Backtracking algorithms



Only 2057 partial boards are considered, compared to  $8^8 = 16\,777\,216$  for the original algorithm



### Two-player games

- Computers now beat humans in
  - backgammon (since 1980)
  - checkers (since 1994) (U. of Alberta)
  - chess (since 1997) (Prof. Monty Newborn)
  - bridge (since 2000 (?))
  - Go (since 2016)
- Human still beat computers in:
  - Rugby
- Human-computers are tied in:
  - 3x3 Tic-tac-toe
  - paper-scissor (but see <http://www.rpschamps.com>)



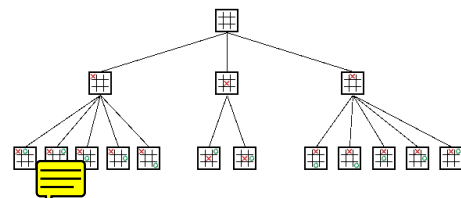
### Game trees

X's turn

O's turn

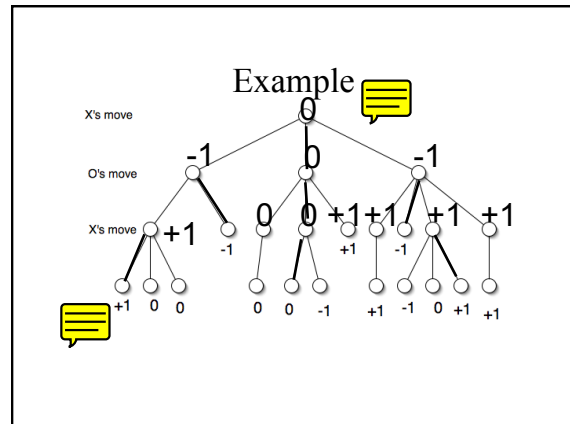
X's turn

...



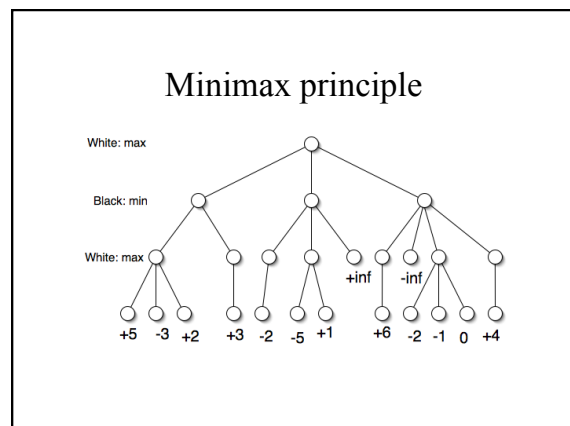
## Winning and Losing Positions

- A winning position for X is a position such that if X plays optimally, X wins even if O plays optimally
- A losing position for X is a position such that if O plays optimally, X loses even if it plays optimally.
- Recursive definition: *On X's move*,
  - a position P is winning for X if
    - P is an immediate win (Leaf of game tree), OR
    - There exists a move that leads to a winning position for X
  - a position P is losing for X if
    - P is an immediate loss (Leaf of game tree), OR
    - All moves available to X leads to losing positions for X
  - a position P is a tie if
    - P is an immediate tie (Leaf of game tree), OR
    - No moves available to X lead to a win, but at least one leads to a tie



## Evaluation functions

- Game trees are too big to be searched exhaustively!
  - Chess has  $10^{120}$  positions possible after 40 moves
- Idea: Look at most K moves ahead.
  - Tree has height K. Leaves are not final positions
  - Estimate the potential of the leaves
    - Good position for white: large positive score
    - Good position for black: large negative score
    - Undecided position: score near zero
    - For chess:
      - 1 point per pawn, 3 points for knights and bishops, ...
- Select the move that leads toward the most promising leaf.
- Start again next turn.



## Minimax principle

**Algorithm** white(board, depth)

**Input:** The current board and the depth of the game tree to explore

**Output:** The value of the current position

**if** (depth=0) **then return** eval(board)

**else**

**return** max { black(b', depth-1): b' is one move away from board }

**Algorithm** black(board, depth)

**if** (depth=0) **return** eval(board)

**else**

**return** min { white(b', depth-1): b' is one move away from board }