HomeWork

December 9, 2018

```
In [1]: from sqlalchemy import create_engine
    from sqlalchemy.exc import ResourceClosedError
    from sqlalchemy.types import VARCHAR
    from functools import partial
    import pandas as pd
    from scipy.spatial import distance
    from sklearn.neighbors import NearestNeighbors
    from IPython.display import display, HTML, Markdown, Latex
    from sklearn.utils.extmath import randomized_svd
    import numpy as np
```

0.1 Reading the data from database into a pandas dataframe

```
In [2]: #connection
         def DatabaseConnect(username, password, schema):
              conn_str = "mysql+pymysql://{username}:{password}@localhost/{schema}?charset=utf8&
                                            .format(username=username, password=password,schema=scheme
              engine = create_engine(conn_str, pool_recycle=1800)
              return engine
         RecSysConnect = partial(DatabaseConnect, 'root', 'mysql-password', 'recsys')
         e = RecSysConnect()
In [3]: #read ratings
         sql_cmt = "select userId, movieId, rating from ml100k_ratings;"
         raw_rating = pd.read_sql(sql_cmt, con=e)
         rating = raw_rating.pivot(index="userId", columns="movieId", values="rating")
         rating.head(10)
Out[3]: movieId 1
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                                  3
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         userId
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         [10 rows x 1682 columns]
In [4]: #read holdout data
         sql_cmt = "select userId from ml100k_ratings group by userId order by count(*) DESC lin
         user_100 = pd.read_sql(sql_cmt, con=e)['userId']
         sql_cmt = "select movieId from ml100k_ratings group by movieId order by count(*) DESC
         movie_10 = pd.read_sql(sql_cmt, con=e)['movieId']
         holdout = rating.loc[user_100,movie_10]
In [5]: rating.loc[user_100,movie_10]=np.nan
   Calculation of similarities
In [6]: import sklearn.metrics.pairwise
         def center(df):
              return df.sub( df.mean(axis=1), axis=0 )
         def cosine(df, axis=0):
              dff = df.fillna(0)
              if axis == 0: # Columns
                  return pd.DataFrame(sklearn.metrics.pairwise.cosine_similarity(dff.T), index=d.
              else:
                  return pd.DataFrame(sklearn.metrics.pairwise.cosine_similarity(dff),
                                                                                                      index=d
In [7]: r_cent = center(rating)
         userSim = rating.T.corr(method='pearson')
         \#userSim = cosine(r_cent, axis=1)
         itemSim = cosine(r_cent)
         display(userSim.head(),itemSim.head())
               1
                           2
                                      3
                                                  4
                                                              5
                                                                          6
                                                                                      7
                                                                                            \
userId
userId
```

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1.000000 0.156868 -0.069171 -0.666667 0.386678 0.298236 0.260460
1
2
        0.156868 1.000000 0.067420 0.148522 0.327327 0.446269 0.381875
3
       -0.069171 0.067420 1.000000 -0.262600
                                                      NaN -0.109109 0.104828
4
       -0.666667 0.148522 -0.262600
                                       1.000000
                                                1.000000 -0.581318 -0.660529
                                       1.000000
                                                 1.000000 0.241817 0.170291
5
        0.386678 0.327327
                                  {\tt NaN}
userId
             8
                       9
                                  10
                                                       934
                                                                 935
                                                                           936 \
userId
        0.694108 -0.301511 -0.124713
                                                 0.066802 -0.252820 0.435300
1
2
        0.585491 0.242536 0.668145
                                         . . .
                                                 0.021007 -0.271163 0.214017
3
        0.291937
                       NaN 0.311086
                                                                 NaN -0.045162
                                                       {\tt NaN}
4
        0.642938
                       NaN -0.301511
                                                 0.500000
                                                                 NaN -0.203653
5
        0.537400 0.577350 0.087343
                                                 0.229532 -0.500000 0.439286
                                         . . .
userId
             937
                       938
                                  939
                                            940
                                                       941
                                                                 942
                                                                           943
userId
1
       -0.044483 0.157353 0.584437 0.257908 0.000000 -0.202777 0.048947
2
        0.561645 0.331587 0.000000 -0.011682 -0.062017 0.085960 0.479702
3
        0.000000 -0.137523
                                  NaN -0.104678 1.000000 -0.011792
                                                                           NaN
4
             NaN 0.375000
                                  NaN 0.850992 1.000000 0.412568
                                                                           NaN
5
        0.608581 \quad 0.484211 \quad 0.880705 \quad 0.027038 \quad 0.468521 \quad 0.318163 \quad 0.346234
[5 rows x 943 columns]
movieId
             1
                       2
                                  3
                                            4
                                                      5
                                                                 6
movieId
1
         1.000000 - 0.023667 - 0.042012 \ 0.012120 \ 0.007037 - 0.002027 \ 0.020884
2
        -0.023667 1.000000 0.031568 0.030879 0.013452 -0.010600 -0.053574
3
        -0.042012 0.031568 1.000000 -0.118348 0.012564 0.054819 -0.087453
4
         0.012120 \quad 0.030879 \quad -0.118348 \quad 1.000000 \quad -0.149492 \quad -0.022921 \quad 0.005652
         0.007037 0.013452 0.012564 -0.149492 1.000000 -0.041295 -0.043651
5
movieId
                                  10
                                                       1673 1674
                                                                       1675 \
                                          . . .
movieId
                                           . . .
                                                              0.0 0.000000
        0.100244 -0.046859 0.002856
1
                                                  0.066344
                                          . . .
2
        -0.007358 -0.103660 -0.020773
                                                   0.000000
                                                              0.0 0.000000
                                          . . .
3
        -0.151500 -0.066376 -0.049901
                                                   0.000000
                                                              0.0 0.000000
4
        0.111663 0.029485 0.009932
                                                   0.000000
                                                              0.0 -0.114413
        0.012695 -0.061202 -0.033263
                                                              0.0 0.000000
                                                   0.000000
                                          . . .
movieId
             1676
                       1677 1678 1679
                                          1680
                                                    1681
                                                             1682
movieId
         0.000000 0.012261
                               0.0
                                     0.0
                                           0.0 0.000000 0.000000
1
2
         0.000000
                   0.000000
                               0.0
                                     0.0
                                           0.0 0.003661 0.034941
3
         0.000000
                   0.201111
                               0.0
                                     0.0
                                           0.0 0.000000
                                                           0.031866
4
                               0.0
                                     0.0
        -0.114413
                   0.090004
                                           0.0 0.002727 -0.048234
5
                                     0.0
        0.000000 0.000000
                               0.0
                                         0.0 0.000000 0.043673
```

0.3 Recommenders

0.3.1 - randomized_svd

```
In [8]: def svd_pred(rating,holdout):
            rating.columns = rating.columns.map(str)
           means = rating.mean(axis=1)
            cent = rating.sub( means, axis=0 )
            U_, Sigma, VT_ = randomized_svd(cent.to_sparse().to_coo().tocsc(), n_components=2,
           U = pd.DataFrame(U_, index=rating.index)
            VT = pd.DataFrame(VT_, columns=rating.columns)
            full = U.mul(Sigma).dot(VT)
            full.columns=full.columns.map(int)
           means = rating.mean(axis=1).loc[user_100]
           prediction = full.loc[user_100,movie_10].add(means,axis=0)
           y_true=[]
           y_predicted=[]
            for u in holdout.index:
               for m in holdout.columns:
                   if (holdout.isna().loc[u,m]==False):
                       y_true=y_true+[holdout.loc[u,m]]
                       y_predicted=y_predicted+[prediction.loc[u,m]]
            return y_true, y_predicted
In [9]: y_true_svd, y_pred_svd = svd_pred(rating,holdout)
In [10]: pd.DataFrame([y_true_svd,y_pred_svd])
Out[10]:
                0
                                    2
                                              3
                                                       4
                                                                 5
                           1
                                                                           6
                                                                                \
        0 5.000000 5.000000 5.000000 4.000000 2.00000 3.000000 3.000000
         1 3.969673 3.624942 2.092731 3.329952 2.95191 3.541682
                                                                     2.897582
                                                        745
                                                                  746
                                                                           747
         0 3.000000 3.000000 3.000000
                                                   5.000000 4.000000 5.00000
                                           . . .
         1 2.428885
                     2.977192 2.705344
                                                   3.488522 3.394138 3.49022
                                            . . .
                748
                         749
                                   750
                                             751
                                                      752
                                                                753
                                                                          754
        0 5.000000 5.00000 4.000000 4.000000 4.000000
                                                                     1.000000
         1 3.973007
                     3.68861 4.086564 3.667382 3.31407 3.672904
                                                                     3.285864
         [2 rows x 755 columns]
0.3.2 - user-based
In [11]: def recommendUser(df, user, item, k=3, weighted=True):
```

knn = userSim.loc[user].drop(user).nlargest(k)

```
norm = knn.sum()
            rating = 0
            for u in knn.index:
                rating += df.loc[u, item] * knn[u]
            rating = np.clip( rating / norm, 1, 5 )
            return (rating)
In [12]: def user_based(rating,holdout):
            rating.columns = rating.columns.map(int)
            v true=[]
            y_predicted=[]
            for u in holdout.index:
                 for i in holdout.columns:
                    if (holdout.isna().loc[u,i]==False):
                        y_true=y_true+[holdout.loc[u,i]]
                        y_predicted=y_predicted+[recommendUser(rating, u, i, 2)]
            return y_true,y_predicted
        y_true_user, y_pred_user = user_based(rating,holdout)
        df=pd.DataFrame([y_true_user,y_pred_user]).dropna(axis=1)
        y_true_user = df.iloc[0]
        y_pred_user = df.iloc[1]
        display(df)
  2
                      11
                                17
                                          18
                                                    21
                                                         27
                                                              28
                                                                        46
0 5.0
       3.000000 3.0 3.0 2.000000 3.000000 1.000000 4.0 4.0 4.000000
       3.989795 4.0 4.0 2.946724 3.579914 3.473362 3.0 4.0 4.463657
  3.0
       683 688 699 707
                          717 718 720 722 734 752
0 ...
       5.0
            3.0 5.0 5.0 3.0 5.0 3.0 4.0 3.0 4.0
1 ...
       3.5 2.0 3.0 3.5 3.0 3.0 2.5 4.5 3.5 2.5
[2 rows x 104 columns]
0.3.3 - item-based
In [13]: def recommendItem(df,user, item, k=2, weighted=True):
            knn = itemSim.loc[item][ df.loc[user].notnull() ]
            knn = knn[ knn> 0 ].drop(item, errors='ignore').nlargest(k)
            if weighted:
               norm = knn.sum()
            else:
               knn.values.fill(1/len(knn))
               norm = 1
            ratings = 0
            for i in knn.index:
                 ratings += df.loc[user,i] * knn[i]
            ratings = np.clip( ratings / norm, 1, 5 )
```

```
return (ratings)
        def item_based(rating,holdout):
            rating.columns = rating.columns.map(int)
            y_true=[]
            y_predicted=[]
            for u in holdout.index:
                for i in holdout.columns:
                    if (holdout.isna().loc[u,i]==False):
                        y_true=y_true+[holdout.loc[u,i]]
                        y_predicted=y_predicted+[recommendItem(rating, u, i)]
            return y_true,y_predicted
        y_true_item, y_pred_item = item_based(rating,holdout)
        pd.DataFrame([y_true_item,y_pred_item])
Out[13]:
           0
                1
                          2
                                                   5
                                                             6
                                                                      7
                                                                                8
        0 5.0 5.0 5.000000 4.000000 2.0 3.000000 3.000000 3.000000
        1 5.0 5.0 2.857781 3.531249 4.0 4.048189 3.601238 2.499696 2.429392
                9
                               745 746
                                              747
                                                        748
                                                                 749
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                       . . .
        0 3.000000
                               5.0 4.0 5.000000 5.000000 5.000000
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                       . . .
        1 2.587803
                               4.0 4.0 4.417514 3.531249 3.490975 4.551081
                751
                          752
                                    753
                                              754
        0 4.000000 4.000000 4.000000
                                        1.000000
        1 3.601238 3.473194 3.468862 2.835027
         [2 rows x 755 columns]
0.4 Evaluation: MSE MAE
In [14]: from sklearn.metrics import mean_squared_error,mean_absolute_error
        def evaluation(y_true, y_predicted):
            result=pd.DataFrame([y_true,y_predicted])
            print(result)
             \#MAE=np.mean(np.abs(result[0] - result[1]))/755
            MAE = mean_absolute_error(y_true,y_predicted)
            RMSE = np.sqrt(mean_squared_error(y_true,y_predicted))
             \#RMSE=np.mean((result[0] - result[1])**2)/755
            display("MAE", MAE, "RMSE", RMSE)
In [15]: evaluation(y_true_svd, y_pred_svd)
       0
                           2
                 1
                                     3
                                              4
                                                        5
                                                                  6
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0 5.000000 5.000000 5.000000 4.000000 2.00000 3.000000 3.000000
1 3.969673 3.624942 2.092731 3.329952 2.95191 3.541682 2.897582
       7
                                               745
                                                         746
                                                                  747
0 3.000000 3.000000 3.000000
                                          5.000000 4.000000 5.00000
                                  . . .
1 2.428885 2.977192 2.705344
                                          3.488522 3.394138 3.49022
                                  . . .
```

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748
               749
                         750
                                  751
                                           752
                                                    753
                                                             754
0 5.000000 5.00000 4.000000 4.000000 4.000000 1.000000
1 3.973007 3.68861 4.086564 3.667382 3.31407 3.672904 3.285864
[2 rows x 755 columns]
'MAE'
0.7386856980861768
'RMSE'
0.9117497430960818
In [16]: evaluation(y_true_item, y_pred_item)
  0
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                          3
                                        5
                                                           7
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       1
                                                 6
0 5.0 5.0 5.000000 4.000000 2.0 3.000000 3.000000 3.000000
1 5.0 5.0 2.857781 3.531249 4.0 4.048189 3.601238 2.499696 2.429392
                     745 746
                                   747
                                             748
                                                      749
                                                                750 \
              . . .
                     5.0 4.0 5.000000 5.000000 5.000000 4.000000
0 3.000000
              . . .
                     4.0 4.0 4.417514 3.531249 3.490975 4.551081
1 2.587803
              . . .
       751
                752
                          753
                                   754
0 4.000000 4.000000 4.000000 1.000000
1 3.601238 3.473194 3.468862 2.835027
[2 rows x 755 columns]
'MAE.'
0.6783970962926593
'RMSE'
0.9412219376564158
```

In [17]: evaluation(y_true_user, y_pred_user)

```
11
                                17
                                          18
                                                    21
                                                         27
                                                              28
0 5.0 3.000000 3.0 3.0 2.000000 3.000000
                                              1.000000 4.0 4.0 4.000000
                 4.0 4.0 2.946724 3.579914
                                               3.473362 3.0 4.0 4.463657
  3.0
       3.989795
       683
            688 699
                      707
                                     720
                                          722
                                               734
  . . .
                           717
                                718
                                                    752
0 ...
       5.0
            3.0 5.0 5.0
                           3.0
                                5.0
                                     3.0 4.0
                                               3.0
                                                    4.0
            2.0 3.0 3.5 3.0 3.0 2.5 4.5 3.5 2.5
1 ...
       3.5
[2 rows x 104 columns]
'MAE'
1.0512574811196467
'RMSE'
1.2742844501470791
In [14]: #Use suprise package
        from surprise import SVD
        from surprise.model_selection import cross_validate
        from surprise import Reader, Dataset
        reader = Reader(rating scale=(1, 5))
        # The columns must correspond to user id, item id and ratings (in that order).
        data = Dataset.load_from_df(raw_rating, reader)
        cross_validate(SVD(), data, measures=['RMSE', 'MAE'], cv=2, verbose=True)
Evaluating RMSE, MAE of algorithm SVD on 2 split(s).
                 Fold 1 Fold 2 Mean
                                         Std
RMSE (testset)
                 0.9598 0.9560 0.9579 0.0019
MAE (testset)
                 0.7583 0.7563 0.7573 0.0010
Fit time
                 3.38
                         4.16
                                 3.77
                                         0.39
Test time
                 0.66
                         0.59
                                 0.63
                                         0.04
Out[14]: {'fit_time': (3.375916004180908, 4.163803815841675),
          'test_mae': array([0.75829125, 0.7563168]),
          'test_rmse': array([0.95982148, 0.95600433]),
          'test_time': (0.6646459102630615, 0.5870378017425537)}
```