

$$6.1. a) \begin{aligned} 2150 &= 200x_1 + 150x_2 + 100x_3 \\ 470 &= 50x_1 + 30x_2 + 20x_3 \\ 150 &= 20x_1 + 10x_2 + 0x_3 \end{aligned} \Rightarrow \begin{array}{c|ccc} 2150 & 200 & 150 & 100 \\ 470 & 50 & 30 & 20 \\ 150 & 20 & 10 & 0 \end{array}$$

$$\Rightarrow \begin{array}{c|ccc} 21.5 & 2 & 1.5 & 1 \\ 47 & 50 & 30 & 20 \\ 150 & 20 & 10 & 0 \end{array} \xrightarrow{k = -\frac{20}{1}} \begin{array}{c|ccc} 21.5 & 2 & 1.5 & 1 \\ 47 & 10 & 0 & 0 \\ 150 & 20 & 10 & 0 \end{array} \Rightarrow \begin{array}{c|ccc} 21.5 & 2 & 1.5 & 1 \\ 150 & 20 & 10 & 0 \\ 47 & 10 & 0 & 0 \end{array}$$

$$\Rightarrow \frac{47}{2} = 2x_1 + \frac{3}{2}x_2 + x_3 \quad (1)$$

$$150 = 20x_1 + 10x_2 \quad (2)$$

$$40 = 10x_1 \quad (3)$$

$$3. \quad 40 = 10x_1$$

$$4 = x_1$$

$$2. \quad 150 = 20 \cdot 4 + 10x_2$$

$$150 = 80 + 10x_2$$

$$70 = 10x_2$$

$$7 = x_2$$

$$1. \quad \frac{47}{2} = 2 \cdot 4 + \frac{3}{2} \cdot 7 + x_3$$

$$\frac{47}{2} = 8 + \frac{21}{2} + x_3$$

$$\frac{47}{2} = \frac{37}{2} + x_3$$

$$3 = x_3$$

$$b) \begin{aligned} 1600 &= 200x_1 + 150x_2 + 100x_3 \\ 350 &= 50x_1 + 30x_2 + 20x_3 \\ 120 &= 20x_1 + 10x_2 + 0x_3 \end{aligned} \Rightarrow \begin{array}{c|ccc} 1600 & 200 & 150 & 100 \\ 350 & 50 & 30 & 20 \\ 120 & 20 & 10 & 0 \end{array} \Rightarrow \begin{array}{c|ccc} 16 & 2 & 1.5 & 1 \\ 350 & 50 & 30 & 20 \\ 120 & 20 & 10 & 0 \end{array} \xrightarrow{k = -\frac{20}{1}}$$

$$\Rightarrow \begin{array}{c|ccc} 16 & 2 & 1.5 & 1 \\ 30 & 10 & 0 & 0 \\ 120 & 20 & 10 & 0 \end{array} \Rightarrow \begin{array}{c|ccc} 16 & 2 & 1.5 & 1 \\ 120 & 20 & 10 & 0 \\ 30 & 10 & 0 & 0 \end{array} \Rightarrow \begin{array}{l} (1) \quad 16 = 2x_1 + 1.5x_2 + x_3 \\ (2) \quad 120 = 20x_1 + 10x_2 \\ (3) \quad 30 = 10x_1 \end{array}$$

$$3. \quad 30 = 10x_1$$

$$3 = x_1$$

$$2. \quad 120 = 20 \cdot 3 + 10x_2$$

$$120 = 60 + 10x_2$$

$$60 = 10x_2$$

$$6 = x_2$$

$$1. \quad 16 = 2 \cdot 3 + 1.5 \cdot 6 + x_3$$

$$16 = 6 + 9 + x_3$$

$$1 = x_3$$