

$$2. \quad z^4 + 4z^2 + 16 = 0$$

$$u = z^2 \Rightarrow u^2 + 4u + 16 = 0$$

$$u_{1,2} = \frac{-4 \pm \sqrt{(-4)^2 - (4 \cdot 16)}}{2 \cdot 1} = \frac{-4 \pm \sqrt{-48}}{2} \Rightarrow \frac{-4 \pm \sqrt{48}i}{2}$$

$$u_1 = \frac{-4 + \sqrt{48}i}{2} = \underbrace{-2}_a + \underbrace{\frac{\sqrt{48}}{2}i}_b = \sqrt{(-2)^2 + \left(\frac{\sqrt{48}}{2}\right)^2} \cdot \left(\cos\left(\tan^{-1}\left(\frac{\frac{\sqrt{48}}{2}}{-2}\right) + \pi\right) + i \sin\left(\tan^{-1}\left(\frac{\frac{\sqrt{48}}{2}}{-2}\right) + \pi\right) \right)$$

$$= 4 \cdot (\cos(2.094) + i \sin(2.094))$$

$$u_2 = \frac{-4 - \sqrt{48}i}{2} = -2 - \frac{\sqrt{48}}{2}i = 4 \cdot (\cos(5.236) + i \sin(5.236))$$

$$u = z^2$$

$$z = \sqrt{u}$$

$$z_1 = \sqrt{u_1} = \sqrt{-2 + \frac{\sqrt{48}}{2}i} \Rightarrow p + iq$$

$$p = \frac{1}{\sqrt{2}} \sqrt{(-2)^2 + \left(\frac{\sqrt{48}}{2}\right)^2} - 2 = 1$$

$$q = \frac{1}{\sqrt{2}} \sqrt{(-2)^2 + \left(\frac{\sqrt{48}}{2}\right)^2} - 2 = 1.732$$

$$\Rightarrow z_1 = 1 + 1.732i$$

$$z_2 = \sqrt{u_2} = \sqrt{-2 - \frac{\sqrt{48}}{2}i} \Rightarrow p + iq$$

$$p = \frac{1}{\sqrt{2}} \sqrt{(-2)^2 + \left(-\frac{\sqrt{48}}{2}\right)^2} - 2 = 1$$

$$q = -\frac{1}{\sqrt{2}} \sqrt{(-2)^2 + \left(-\frac{\sqrt{48}}{2}\right)^2} - 2 = -1.732$$

$$\Rightarrow z_2 = 1 - 1.732i$$