A FIRST COURSE

IN

STOCHASTIC DIFFERENTIAL EQUATION

A FIRST COURSE

IN

STOCHASTIC DIFFERENTIAL EQUAT

MAT4500 Notebook

Prof. Sang Hu

The Chinese University of Hongkong, Shenzhen

Contents

Ackno	owledgments	vii
Notat	ions	ix
1	Week1	1
1.1	Tuesday	1
1.1.1	News Vendor Problems	1
2	Week2	3
2.1	Tuesday	3
2.1.1	Optimal order quantity	3
2.1.2	Non-perishable Products	4
2.2	Thursday	6
2.2.1	Discrte Time Markov Chains	6

Acknowledgments

This book is from the MAT4001 in fall semester, 2018.

CUHK(SZ)

Notations and Conventions

 \mathbb{R}^n *n*-dimensional real space \mathbb{C}^n *n*-dimensional complex space $\mathbb{R}^{m \times n}$ set of all $m \times n$ real-valued matrices $\mathbb{C}^{m \times n}$ set of all $m \times n$ complex-valued matrices *i*th entry of column vector \boldsymbol{x} x_i (i,j)th entry of matrix \boldsymbol{A} a_{ij} *i*th column of matrix *A* \boldsymbol{a}_i $\boldsymbol{a}_{i}^{\mathrm{T}}$ *i*th row of matrix **A** set of all $n \times n$ real symmetric matrices, i.e., $\mathbf{A} \in \mathbb{R}^{n \times n}$ and $a_{ij} = a_{ji}$ \mathbb{S}^n for all *i*, *j* \mathbb{H}^n set of all $n \times n$ complex Hermitian matrices, i.e., $\mathbf{A} \in \mathbb{C}^{n \times n}$ and $\bar{a}_{ij} = a_{ji}$ for all i, j $\boldsymbol{A}^{\mathrm{T}}$ transpose of \boldsymbol{A} , i.e, $\boldsymbol{B} = \boldsymbol{A}^{\mathrm{T}}$ means $b_{ji} = a_{ij}$ for all i,jHermitian transpose of \boldsymbol{A} , i.e, $\boldsymbol{B} = \boldsymbol{A}^{H}$ means $b_{ji} = \bar{a}_{ij}$ for all i,j A^{H} trace(A)sum of diagonal entries of square matrix A1 A vector with all 1 entries 0 either a vector of all zeros, or a matrix of all zeros a unit vector with the nonzero element at the *i*th entry e_i C(A)the column space of \boldsymbol{A} $\mathcal{R}(\boldsymbol{A})$ the row space of \boldsymbol{A} $\mathcal{N}(\boldsymbol{A})$ the null space of \boldsymbol{A}

 $\operatorname{Proj}_{\mathcal{M}}(\mathbf{A})$ the projection of \mathbf{A} onto the set \mathcal{M}

Chapter 1

Week1

1.1. Tuesday