Using the Foundations and Trends® LATEX Class

Instructions for Creating an FnT Article

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Using the Foundations and Trends® LATEX Class

Alet Heezemans¹ and Mike Casey²

ABSTRACT

This document describes how to prepare a Foundations and Trends[®] article in LAT_EX . The accompanying LAT_EX source file FnTarticle.tex (that produces this output) is an example of such a file.

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Introduction to Linear Programming

1.1 Preliminaries

Standard Form We usually consider the standard linear programming (LP) model:

$$\max \sum_{j=1}^{n} c_{j} x_{j} \text{s.t.} \quad \sum_{j=1}^{n} a_{ij} x_{j} \leq b_{i}, \quad i = 1, \dots, m x_{j} \geq 0, j = 1, \dots, n$$
 (1.1)

Or more generally, the constraints with equalities:

$$\min \sum_{j=1}^{n} c_j x_j
\text{s.t.} \quad \sum_{j=1}^{n} a_{ij} x_j \leq b_i, \quad i \in I
\sum_{j=1}^{n} a_{ij} x_j = b_i, \quad i \in E
x_j \geq 0, j = 1, \dots, n$$

It's often convenient to write the LP (1.1) into the compact matrix form:

$$\begin{array}{ll}
\max & \boldsymbol{c}^{\mathrm{T}}\boldsymbol{x} \\
\text{s.t.} & \boldsymbol{A}\boldsymbol{x} \leq \boldsymbol{b} \\
& \boldsymbol{x} \geq \boldsymbol{0}
\end{array} \tag{1.2}$$

where $c \in \mathbb{R}^n$, $A \in \mathbb{R}^{m \times n}$, $b \in \mathbb{R}^m$.

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We also write \mathbf{A} as the column form:

$$A = \begin{pmatrix} a_1, & \cdots & a_n \end{pmatrix}$$

where a_i is the *i*-th column of A. We also express the submatrix of A, i.e., $A_I \subset A$ as:

$$\mathbf{A}_I := [a_i \mid i \in I],$$

where I is a subset of $\{1, 2, \ldots, n\}$.

Dictionaries of an LP We can introduce slack variables to transform (1.1) into LP with equalities:

$$x_{n+i} := b_i - \sum_{j=1}^n a_{ij} x_j, \quad i = 1, \dots, m$$

Let $z = \sum_{j=1}^{n} c_j x_j$ be the objective function, and therefore we obtain a dictionary for the LP (1.1):

$$x_{n+i} = b_i - \sum_{j=1}^n a_{ij} x_j, \quad i = 1, \dots, m$$

$$z = \sum_{j=1}^n c_j x_j$$
 Dictionary (1.3)

Assume that $b_i \geq 0$ for i = 1, ..., m. Therefore we obtain a feasible solution associated with the dictionary, say dictionary solution:

$$x_j = 0$$
, for $j = 1, ..., n$ $x_{n+i} = b_i$ for $i = 1, ..., m$

It's clear how to improve the current dictionary solution:

- If $c_j \leq 0, \forall j$, then we cannot possibly improve the dictionary solution
- If $c_j > 0$ for some $1 \le j \le n$, we increase the value for x_j from 0 into maximal value, while fixing $x_j = 0$ for $1 \le k (\ne j) \le n$. Keep implementing until $c_j \le 0, \forall j$.

Example 1.1. Consider the optimization problem

$$\max \quad 5x_1 + 4x_2 + 3x_3$$
s.t.
$$2x_1 + 3x_2 + x_3 \le 5$$

$$4x_1 + x_2 + 2x_3 \le 11$$

$$3x_1 + 4x_2 + 2x_3 \le 8$$

$$x_1 \ge 0, \ x_2 \ge 0, \ x_3 \ge 0$$

$$(1.4a)$$

We can find its dictionary:

$$x_{4} = 5 - 2x_{1} - 3x_{2} - x_{3}$$

$$x_{5} = 11 - 4x_{1} - x_{2} - 2x_{3}$$

$$x_{6} = 8 - 3x_{1} - 4x_{2} - 2x_{3}$$

$$z = 0 + 5x_{1} + 4x_{2} + 3x_{3}$$
(1.4b)

Since $c_1 > 0$, increasing value for x_1 suffices to consider the dictionary below instead:

$$x_{1} = \frac{5}{2} - \frac{3}{2}x_{2} - \frac{1}{2}x_{3} - \frac{1}{2}x_{4}$$

$$x_{5} = 11 - 4x_{1} - x_{2} - 2x_{3}$$

$$x_{6} = 8 - 3x_{1} - 4x_{2} - 2x_{3}$$

$$z = 0 + 5x_{1} + 4x_{2} + 3x_{3}$$

$$x_{1} = \frac{5}{2} - \frac{3}{2}x_{2} - \frac{1}{2}x_{3} - \frac{1}{2}x_{4}$$

$$x_{5} = 1 + 5x_{2} + 0x_{3} + 2x_{4}$$

$$x_{6} = \frac{1}{2} + \frac{1}{2}x_{2} - \frac{1}{2}x_{3} + \frac{3}{2}x_{4}$$

$$z = \frac{25}{2} - \frac{7}{2}x_{2} + \frac{1}{2}x_{3} - \frac{5}{2}x_{4}$$

$$(1.4c)$$

Also, since $c_3 > 0$, increasing value for x_3 suffices to consider the dictionary below instead:

$$x_{1} = \frac{5}{2} - \frac{3}{2}x_{2} - \frac{1}{2}x_{3} - \frac{1}{2}x_{4}$$

$$x_{3} = 1 + x_{2} + 3x_{4} - 2x_{6}$$

$$x_{5} = 1 + 5x_{2} + 0x_{3} + 2x_{4}$$

$$x_{3} = 1 + x_{2} + 3x_{4} - 2x_{6}$$

$$x_{5} = 1 + 5x_{2} + 2x_{4} + 2x_{6}$$

$$z = \frac{25}{2} - \frac{7}{2}x_{2} + \frac{1}{2}x_{3} - \frac{5}{2}x_{4}$$

$$z = 13 - 3x_{2} - x_{4} - x_{6}$$

$$(1.4d)$$

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1.2 Simplex Method

Notations The general dictionary for the problem (1.1) can be expressed as:

$$x_{i} = \bar{b}_{i} - \sum_{j \in N} \bar{a}_{ij} x_{j}, \quad i \in B$$

$$z = \zeta - \sum_{j \in N} \bar{c}_{j} x_{j}$$

$$(1.5)$$

where

- 1. the set B is called a basis, with |B| = m
- 2. the set N is called a non-basis, with |N| = n m. Moreover, $B \cup N = \{1, \dots, n\}$.
- 3. the basis B is said to be *primal feasible* if $\bar{b} \geq 0$, since in this case we can choose a primal feasible solution by setting non-basis variables to be zero and basis variables x_i to be \bar{b}_i .
- 4. the non-basis N is said to be *dual feasible* if $\bar{c} \leq 0$, since in this case we can choose a dual feasible solution by setting non-basis variables to be \bar{c}_i and other variables to be 0.

One can verify that in (1.5),

$$egin{aligned} ar{oldsymbol{b}} &= oldsymbol{A}_B^{-1} oldsymbol{b} \ ar{oldsymbol{c}}_N^{
m T} &= oldsymbol{c}_N^{
m T} - oldsymbol{c}_B^{
m T} oldsymbol{A}_D^{-1} oldsymbol{A}_N \ ar{oldsymbol{A}}_N &= oldsymbol{A}_B^{-1} oldsymbol{A}_N \ \zeta &= oldsymbol{c}_R^{
m T} oldsymbol{A}_B^{-1} oldsymbol{b} \end{aligned}$$

One can verify that $(x_B, x_N) = (A_B^{-1}b, 0)$ is a basic solution.

Simplex Method Algorithm The assumption for the working of simplex method is that we are given a primal feasible basic solution, i.e., $\bar{b} \geq 0$. The framework for obtaining an improved solution is summarized in (1).

Algorithm 1 Framework for the one step of the Simplex Method

Input:

Primal feasible basic solution;

Output:

Improved feasible basic solution;

- 1: Entering Basis Variable
 - Search for $j \in N$ such that $\bar{c}_j > 0$
 - If none exists then the current basic solution is optimal; otherwise choose one of such j.
- 2: Leaving Basis Variable
 - Search for $i \in B$ such that $\bar{a}_{ij} > 0$
 - If none exists then the problem is unbounded; otherwise choose

$$i \in \arg\min\left\{\frac{\bar{b}_i}{\bar{a}_{ij}} : \bar{a}_{ij} > 0, \ i \in B\right\}$$

3: Basis Update: $B \leftarrow B \cup \{j\} \setminus \{i\}$, and then form the corresponding basic solution.

Remark 1.1. The *one-step* of the simplex method is also called a *pivot step*, i.e., choose one pivot variable entering the basis and one leaving the basis.

The objective value for a successful pivot is improved by $\frac{\bar{c}_j b_i}{\bar{a}_{ij}}$. However, the simplex method may not necessarily increase the objective value at each pivot, e.g., the case $\bar{b}_i = 0$ coul happen. In this case, the basic solution is said to be degenerate.

Since there are no more than $\binom{n}{m}$ (finite) possible bases, the simplex method will stop on two cases: (a) declaring the problem is unbounded; (b) finding a basic optimal solution.

Pivot Rules The *simplex method* specializes into a *simplex algorithm* if one specifies a *pivot rule* to determine which one variable to enter

the basis and which one to leave, when there is a choice to make. Note that there exists some pivot rules that will make the problem face into cycling circumstance (see the example below), but here we list some examples of pivot rules that will be shown to definitely avoid cycling circumstance:

- Dantzig's pivot rule: choose the largest positive coefficient to enter the basis.
- The maximum improvement rule: try all the combinations and pick the pivot pair with the largest improvement.
- Bland's rule: Among the candidates always pick the one with the smallest index.

Example 1.2. This example shows that some pivot rules may let the problem face into cycling circumstance, i.e., the algorithm solves the problem in a loop and fails to go out:

$$x_5 = -0.5x_1 + 5.5x_2 + 2.5x_3 - 9x_4$$

$$x_6 = -0.5x_1 + 1.5x_2 + 0.5x_3 - x_4$$

$$x_7 = 1 - x_1$$

$$z = \mathbf{10}x_1 - 57x_2 - 9x_3 - 24x_4$$

Choosing x_1 to enter the basis and x_5 to leave gives:

$$x_1 = -2x_5 + 11x_2 + 5x_3 - 18x_4$$

$$x_6 = x_5 - 4x_2 - 2x_3 + 8x_4$$

$$x_7 = 1 + 2x_5 - 11x_2 - 5x_3 + 18x_4$$

$$z = -20x_5 + 53x_2 + 41x_3 - 204x_4$$

Choosing x_2 to enter the basis and x_6 to leave gives:

$$x_1 = 0.75x_5 - 2.75x_6 - 0.5x_3 + 4x_4$$

$$x_2 = 0.25x_5 - 0.25x_6 - 0.5x_3 + 2x_4$$

$$x_7 = 1 - 0.75x_5 - 13.25x_6 + 0.5x_3 - 4x_4$$

$$z = -6.75x_5 - 13.25x_6 + 14.5x_3 - 98x_4$$

Choosing x_3 to enter the basis and x_1 to leave gives:

$$x_3 = 1.5x_5 - 5.5x_5 - 2x_1 + 8x_4$$

$$x_2 = -0.5x_5 + 2.5x_5 + x_1 - 2x_4$$

$$x_7 = 1 - x_1$$

$$z = 15x_5 - 93x_5 - 29x_1 + 18x_4$$

Choosing x_4 to enter the basis and x_2 to leave gives:

$$x_3 = -0.5x_5 + 4.5x_5 + 2x_1 - 4x_2$$

$$x_4 = -0.25x_5 + 1.25x_5 + 0.5x_1 - 0.5x_2$$

$$x_7 = 1 - x_1$$

$$z = \mathbf{10.5}x_5 - 70.5x_5 - 20x_1 - 9x_2$$

Choosing x_5 to enter the basis and x_3 to leave gives:

$$x_5 = 9x_6 + 4x_1 - 8x_2 - 2x_3$$

$$x_4 = -x_6 - 0.5x_1 + 1.5x_2 + 0.5x_3$$

$$x_7 = 1 - x_1$$

$$z = 24x_6 + 22x_1 - 93x_2 - 21x_3$$

Choosing x_6 to enter the basis and x_4 to leave gives the *same dictionary* as we started:

$$x_5 = -0.5x_1 + 5.5x_2 + 2.5x_3 - 9x_4$$

$$x_6 = -0.5x_1 + 1.5x_2 + 0.5x_3 - x_4$$

$$x_7 = 1 - x_1$$

$$z = \mathbf{10}x_1 - 57x_2 - 9x_3 - 24x_4$$

Theorem 1.1. Bland's pivot rule would aviod cycling.

Proof. We show this claim by contradiction. If Bland's pivot rule produces cycling, let's study one cycle. For a sequence of dictionaries that form a cycle, let's delete all the variables that neither leave nor enter the basis, then it will remain a cycle.

In all these dictionaries, all \bar{b}_i will be zero, since otherwise the objective value will be strictly increased.

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Let's study the tablau of dictionaries. It's a matrix that stores all the coefficients of a dictionary:

Two vectors are of special interest. The last row of the tablau in left part can be written as

$$ar{oldsymbol{c}}^{ ext{T}} = oldsymbol{c} - oldsymbol{c}_{B}^{ ext{T}} oldsymbol{A}_{B}^{-1} oldsymbol{A}$$

For the chosen $j \in N$, the direction

$$d_i^{(j)} = \begin{cases} -\bar{a}_{ij}, & i \in B \\ 0, & i \neq j \\ 1, & i = j \end{cases}$$

It's clear that $\bar{\boldsymbol{c}}^{\mathrm{T}}\boldsymbol{d}^{(j)} = \bar{c}_j$.

Suppose that ℓ is the largest index of all variables that are involved in the cycle. Let (B,N) be the pivot where ℓ was about to enter the basis, $\boldsymbol{v}=\bar{\boldsymbol{c}}$ be the last row for that tableau at that point; let (B',N') be the pivot where ℓ was about to leave the basis, and k was to enter the basis at that point, $\boldsymbol{d}^{(k)}$ be the corresponding direction vector, \boldsymbol{u} the last row of that tableau.

It's clear that

- \boldsymbol{v} is everywhere non-positive except for one position $v_{\ell}>0$
- $\boldsymbol{d}^{(k)}$ is everywhere non-negative except for one position $d_{\ell}^{(k)} < 0$

Moreover, $\boldsymbol{v} - \boldsymbol{u} \in \mathcal{R}(\boldsymbol{A}^{\mathrm{T}})$ and $\boldsymbol{d}^{(k)} \in \mathcal{N}(\boldsymbol{A})$, which implies

$$0 = (\boldsymbol{v} - \boldsymbol{u})^{\mathrm{T}} \boldsymbol{d}^{(k)} = \boldsymbol{v}^{\mathrm{T}} \boldsymbol{d}^{(k)} - \boldsymbol{u}_k < 0,$$

which is a contradiction.

The Distribution and Installation

2.1 Pre-requisites

You will need a working LaTeX installation. We recomend using pdflatex to process the files. You will also need biber.exe installed. This is distributed as part of the latest versions of LiveTex and MikTex. If you have problems, please let us know.

2.2 The Distribution

The distribution contains 2 folders: nowfnt and nowfnttexmf.

2.2.1 Folder nowint

This folder contains the following files using a flat stucture required to compile a FnT issue:

- \bullet essence_logo.eps
- \bullet essence_logo.pdf
- $\bullet \ \ now_logo.eps$
- \bullet now_logo.pdf

2.3. Installation 11

- nowfnt.cls
- nowfnt-biblatex.sty
- NOWFnT-data.tex

It also contains the following folders:

journaldata A set of data files containing the journal-specific data for each journal. There are three files per journal:

- <jrnlcode>-editorialboard.tex
- <jrnlcode>-journaldata.tex
- <jrnlcode>-seriespage.tex

<jrnlcode> is the code given in Appendix A. You will need these three files to compile your article.

SampleArticle This folder contains this document as an example of an article typeset in our class file. The document is called FnTarticle.tex. It also contains this PDF file and the .bib file.

2.2.2 Folder nowfnttexmf

This folder contains all the files required in a texmf structure for easy installation.

2.3 Installation

If your LATEX installation uses a localtexmf folder, you can copy the nowtexmf folder to the localtexmf folder and make it known to your TEX installation. You can now proceed to use the class file as normal.

If you prefer to use the flat files, you will need to copy all the required files each time into the folder in which you are compiling the article. Do not forget to copy the three data files for the specific journal from the folder journaldata.

You may need to configure your TEX editor to be able to run the programs. If you have problems installing these files in your own system, please contact us. We use Computer Modern fonts for some of the

journals. You will need to make sure that these fonts are installed. Refer to your system documentation on how to do this.

Quick Start

The now-journal class file is designed is such a way that you should be able to use any commands you normally would. However, do **not** modify any class or style files included in our distribution. If you do so, we will reject your files.

The preamble contains a number of commands for use when making the final versions of your manuscript once it has been accepted and you have been instructed by our production team.

3.1 \documentclass

The options to this command enable you to choose the journal for which you producing content and to indicate the use of biber.

\documentclass[<jrnlcode>,biber]{nowfnt}.

<jrnlcode> is the pre-defined code identifying each journal. See Appendix A for the appropriate <jrnlcode>. 14 Quick Start

3.2 \issuesetup

These commands are only used in the final published version. Leave these as the default until our production team instructs you to change them.

3.3 \maintitleauthorlist

This is the authors list for the cover page. Use the name, affilliation and email address. Separate each line in the address by \\.

Separate authors by \and. Do not use verbatim or problematic symbols. _ (underscore) in email address should be entered as _. Pay attention to long email addresses.

If your author list is too long to fit on a single page you can use double column. In this case, precede the \maintitleauthorlist command with the following:

\booltrue{authortwocolumn}

3.4 \author and \affil

These commands are used to typeset the authors and the afilliations on the abstract page of the article and in the bibliographic data.

\author uses an optional number to match the author with the affiliation. The author name is written <surname>, <firstname>.

\affil uses an optional number to match the author with the author name. The content is <affiliation>; <email address>.

3.5 \addbibresource

Use this to identify the name of the bib file to be used.

Style Guidelines and LATEX Conventions

In this section, we outline guidelines for type setting and using IATEX that you should follow when preparing your document

4.1 Abstract

Ensure that the abstract is contained within the \begin{abstract}
environment.

4.2 Acknowledgements

Ensure that the acknowledgements are contained within the \begin{acknowledgements} environment.

4.3 References

now publishers uses two main reference styles. One is numeric and the other is author/year. The style for this is pre-defined in the LATEX

distribution and must not be altered. The style used for each journal is given in the table in Appendix A. Consult the sample-now.bib file for an example of different reference types.

The References section is generated by placing the following commands at the end of the file.

\backmatter \printbibliography

4.4 Citations

Use standard \cite, \citep and \citet commands to generate citations. Run biber on your file after compiling the article. This will automatically create the correct style and format for the References.

4.4.1 Example citations

This section cites some sample references for your convenience. These are in author/year format and the output is shown in the References at the end of this document.

Example output when using citet: arvolumenumber is a citation of reference 1 and Bertsekas (1995) is a citation of reference 2.

Example output when using citep: (beditorvolumenumber) is a citation of reference 3 and (inproceedings) is a citation of reference 4.

4.5 Preface and Other Special Chapters

If you want to include a preface, it should be defined as follows:

```
\chapter*{Preface}
\markboth{\sffamily\slshape Preface}
   {\sffamily\slshape Preface}
```

This ensures that the preface appears correctly in the running headings. You can follow a similar procedure if you want to include additional unnumbered chapters (e.g., a chapter on notation used in the paper), though all such chapters should precede Chapter 1.

Unnumbered chapters should not include numbered sections. If you want to break your preface into sections, use the starred versions of section, subsection, etc.

4.6 Long Chapter and Section Names

If you have a very long chapter or section name, it may not appear nicely in the table of contents, running heading, document body, or some subset of these. It is possible to have different text appear in all three places if needed using the following code:

\chapter[Table of Contents Name]{Body Text Name}
\chaptermark{Running Heading Name}

Sections can be handled similarly using the **sectionmark** command instead of **chaptermark**.

For example, the full name should always appear in the table of contents, but may need a manual line break to look good. For the running heading, an abbreviated version of the title should be provided. The appearance of the long title in the body may look fine with LATEX's default line breaking method or may need a manual line break somewhere, possibly in a different place from the contents listing.

Long titles for the article itself should be left as is, with no manual line breaks introduced. The article title is used automatically in a number of different places by the class file and manual line breaks will interfere with the output. If you have questions about how the title appears in the front matter, please contact us.

4.7 Internet Addresses

The class file includes the url package, so you should wrap email and web addresses with \url{}. This will also make these links clickable in the PDF.

Compiling Your FnT Article

During the first run using the class file, a number of new files will be created that are used to create the book and ebook versions during the final production stage. You can ignore these until preparing the final versions as described in Section 5.3. A complete list of the files produced are given in Appendix B.

5.1 Compiling Your Article Prior to Submission

To compile an article prior to submission proceed as follows:

- Step 1: Compile the LATEX file using pdflatex.
- Step 2: Run biber on your file.
- Step 3: Compile again using pdfLaTeX. Repeat this step.
- **Step 4:** Inspect the PDF for bad typesetting. The output PDF should be similar to FnTarticle.pdf. Work from the first page when making adjustments to resolve bad line breaks and bad page breaks. Rerun pdfLaTeX on the file to check the output after each change.

5.2 Preparing the Final Versions

If you choose the option to compile the final versions of your PDF for publication, you will receive a set of data from our production team upon final acceptance. With the exception of "lastpage", enter the data into the \issuesetup command in the preamble.

lastpage— This is the last page number in the sequential numbering of the journal volume. You will need to enter this once you have compiled the article once (see below).

5.3 Compiling The Final Versions

The final versions should be created once you received all the bibliographic data from our Production Team and you've entered it into the preamble. You will be creating a final online journal version pdf; a printed book version pdf; and an ebook version pdf.

- Step 1: Compile the LATEX file using pdfLaTeX.ArAuthor et al., 2014
- Step 2: Run biber on your file.
- Step 3: Compile again using pdfLaTeX. Repeat this step.
- **Step 4:** Inspect the PDF for bad typesetting. The output PDF should be similar to FnTarticle.pdf. Work from the first page when making adjustments to resolve bad line breaks and bad page breaks. Rerun pdfLaTeX on the file to check the output after each change.
- **Step 5:** When you are happy with the output make a note of the last page number and enter this in \issuesetup.
- Step 6: Compile the article again.
- **Step 7:** Open the file <YourFilename>-nowbook.tex. This will generate the printed book version pdf.
- Step 8: Compile the LATEX file using pdflatex.
- Step 9: Run biber on your file.

- Step 10: Compile again using pdfLaTeX. Repeat this step.
- **Step 11:** Repeat steps 7-10 on the file: <YourFilename>-nowebook.tex. This will generate the ebook version pdf.
- **Step 12:** Repeat steps 7-10 on the file: <YourFilename>-nowplain.tex. This will generate a plain version pdf of your article. If you intend to post your article in an online repository, please use this version.

5.4 Wednesday

Proposition 5.1. G is hamiltionian implies that for any nonempty $S \subseteq V$, G - S has at most |S| components.

Theorem 5.1. G is Hamiltionian if for any vetices v, w such that $(v, w) \notin E$,

$$\deg(v) + \deg(w) \ge n$$

Knapsacle Problem

$$\max \sum_{i=1}^{n} v_i u_i$$

such that
$$\sum_{i=1}^{n} w_i u_i \leq W$$
$$u_i \in \{0, 1\}, \ i = 1, \dots, n$$

This is the binary integer programming problem, which is NP-complete. We cannot find exact solution to this problem. There are 2^n possible solutions, which requires exponential time.

We can find some "pseudo"-polynomial algorithm. Assumption:

1. W is an integer.

State: remaining capacity, define as X_k .

Stage: iterm $1, \ldots, n$.

$$J_N(x_N) = \begin{cases} v_N & \text{if } N \le X_N \\ 0, & \text{if } w_N > X_N \end{cases}$$

$$J_N(x_{N-1}) = \begin{cases} 0 + J_N(X_N), & \text{if } w_{N-1} > X_{N-1}, \text{Here } X_N = \\ \max\{v_{N-1} + J_N(x_N), 0 + J_N(x_N)\}, & \text{if } w_{N-1} \le X_{N-1} \end{cases}$$

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Here why the DP has "pesduo"-polynomial time, and the w_i should be integer?

Let's list states $\{x_1, \ldots, x_N\}$. For each stage k, there would be W+1. Each iteration at most 2 computation, and therefore we face 2(W + $1) \cdot N$

5.4.1 **Label Correcting Methods**

Shortest Path. Back up some information.

The label refers to the intermediate information.

A*-algorithm; Bellman-Ford Algorithm

Benchmark: MILP, CPLEX, CVX.

5.4.2 DP problems with perfect state information

Linear Quadratic System Let $x_k \in \mathbb{R}^1$ be the state; $u_k \in \mathbb{R}^n$ be the control; $\omega_k \in \mathbb{R}^n$ be the disturbance.

System Dynamics.

$$x_{k+1} = A_k x_k + B_k u_k + \omega_k$$

Stage cost:

$$x_k'Q_kx_k + u_k'R_ku_k$$

Here Q_k is required to be positive-semi-definite symmetric matrix; R_k to be positive-definite symmetric matrix.

$$J_{n-1}(x_{n-1}) = \min_{u_{n-1}} \mathbb{E}_{\omega} \left\{ x'_{n-1} Q_{n-1} x_{n-1} + u'_{n-1} R_{n-1} u_{n-1} + J_n(x_n) \right\}$$

where

$$J_n(x_n) = (A_{n-1}x_{n-1} + Bu_{n-1} + \omega)'Q_n(A_{n-1}x_{n-1} + Bu_{n-1} + \omega)$$

5.4.3 Linear Quadratic

Dynamics:

$$x_{k+1} = A_k x_k + B_k u_k + \omega_k$$

Stage cost:

$$x_k'Q_kx_k + u_k'R_ku_k, \ Q_k \succeq 0, R_k \succ 0$$

Cost to go function:

$$J_k(x_k) = \min_{u_k} \mathbb{E}_{\omega_k} [x_k' Q_k x_k + u_k' R_k u_k + J_{k+1}(x_{k+1})]$$

The final cost is

$$J_N(x_N) = x_N' Q_N x_N$$

At N-1 stage

$$x'_{N-1}Q_{N-1}x_N + u'_{N-1}R_{N-1}u_{N-1} + \mathbb{E}[(A_{N-1}x_{N-1} + B_{N-1}u_{N-1} + \omega_{N-1})'Q_N(A_{N-1}x_{N-1} + B_{N-1}u_{N-1} + \omega_{N-1})]$$

Optimization model:

$$\frac{\partial}{\partial u}(u'Hu + 2r'u + c) = 2Hu + 2r \implies Hu = -r \implies u^* = -H^{-1}r$$

For N-1 stage, we have

$$H = R_{N-1} + B'_{N-1}Q_N B_{N-1}$$

$$r' = x'_{N-1}A'_{N-1}Q_N B_N$$

$$c = x'_{N-1}(Q_{N-1} + A'_{N-1}Q_N A_{N-1})x_{N-1} + \mathbb{E}_{\omega}(\omega'_{N-1}Q_N \omega_{N-1})$$

Therefore,

$$u_{N-1}^* = -(R_{N-1} + B_{N-1}'Q_N B_{N-1})^{-1} B_N Q_N A_{N-1} x_{N-1},$$

which is linear in terms of x_{N-1} , which is so called linear controller. Therefore,

$$J_{N-1}(x_{N-1}) = x'_{N-1}K_{N-1}x_{N-1} + \mathbb{E}(\omega'_{N-1}Q_N\omega_{N-1})$$

The linear controller will be tested during mid-term or final.

$$J_0(x_0) = x_0' K_0 x_0 + \sum_{k=0}^{N-1} \mathbb{E}_{\omega} \{ \omega_k' K_{k+1} \omega_k \}$$

$$K_{k-1} = f(K_k) \implies K_{k-1} = K_k$$
, for large k .

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Riccati Equation for stationary ststem, i.e., $A_k = A, B_k = B, Q_k =$ $Q, R_k = R.$

$$K = A'(K - KB(B'KB + R)^{-1}B'K)A + Q$$

Therefore as time goes long enough, the cost to go function $J_k(x_k)$ will be a constant plus over stages, such a constant K is called the optimal stationary controller.

Stability. For $u^* = Lx$, we imply

$$x_{k+1} = Ax_k + Bu_k + \omega_k = (A + BL)x_k + \omega_k$$

Care about $\lim_{k\to\infty} (A+BL)^k = 0$.

Here

$$L = -(B'KB + R)^{-1}B'KA$$

It suffices to solve

$$P_{k+1} = A^2 \left(P_k - \frac{B^2 P_k^2}{B^2 P_k + R} \right) + Q$$

Then consider the case that A_k, B_k are all random matrices, i.e., independent. $Q_k \succeq 0, R_k \succ 0$.

$$L_k = -(R_k + \mathbb{E}(B_k' K_{k+1} B_k))^{-1} \mathbb{E}(B_j' K_{k+1} A_k)$$

Note that

$$P_{\infty} = \frac{\mathbb{E}A^2RP}{R + EB^2P} + \frac{\mathbb{E}A^2\mathbb{E}B^2 - (\mathbb{E}A)^2(\mathbb{E}B)^2}{R + \mathbb{E}B^2P}$$

Certainty Equivalence

State: x_k , inventory level

Control: $u_k \geq 0$, number of orders placed

Disturbance: ω_k : damand

Dynamics:

$$x_{k+1} = (x_k + u_k - \omega_k)$$

Stage cost:

• Ordering cost: $c \cdot u_k$

• Maintaining cost: full backlog. $\mathbb{E}_{\omega_k}(r(x_k+u_k-\omega_k))$. where $r(z)=hz^++pz^-$ is a convex function. We imply the maintaining cost is $H(x_k+u_k)$, which is convex.

$$J_k(x_k) = \min_{u_k \ge 0} \left\{ cu_k + H(x_k + u_k) + \mathbb{E}[J_{k+1}(x_k + u_k - \omega_k)] \right\}$$

Define $Y = x_k + u_k$, and therefore

$$G(Y) = cY + H(Y) + \mathbb{E}[J(Y - \omega_k)]$$

Therefore, we can always set $Y = x_k + u_k = S_k$, where S_k minimizes G(Y).

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Appendices

A

Journal Codes

The table below shows the journal codes to be used in \documentclass. For Example: \documentclass[ACC,biber] {nowfnt}

${f J}$ ournal	<pre><jrnlcode></jrnlcode></pre>	Ref. Style
Annals of Corporate Governance	ACG	Author/Year
Annals of Science and Technology Policy	ASTP	Author/Year
FnT Accounting	ACC	Author/Year
FnT Comm. and Information Theory	CIT	Numeric
FnT Databases	DBS	Author/Year
FnT Econometrics	ECO	Author/Year
FnT Electronic Design Automation	EDA	Author/Year
FnT Electric Energy Systems	EES	Author/Year
FnT Entrepreneurship	ENT	Author/Year
FnT Finance	FIN	Author/Year
FnT Human-Computer Interaction	HCI	Author/Year
FnT Information Retrieval	INR	Author/Year
FnT Information Systems	ISY	Author/Year
FnT Machine Learning	MAL	Author/Year
FnT Management	MGT	Author/Year
FnT Marketing	MKT	Author/Year
FnT Networking	NET	Numeric
		Continues

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	Ref. Style
OPT	Numeric
PGL	Author/Year
ROB	Author/Year
SEC	Author/Year
SIG	Numeric
SYS	Author/Year
TCS	Numeric
TOM	Author/Year
WEB	Author/Year
	PGL ROB SEC SIG SYS TCS TOM

B

Files Produced During Compilation

The files that are created during compilation are listed below. The additional *.tex files are used during the final production process only. See Section 5.3.

```
<YourFilename>-nowbook.tex
<YourFilename>-nowchapter.tex
<YourFilename>-nowebook.tex
<YourFilename>-nowechapter.tex
<YourFilename>-nowsample.tex
<YourFilename>-nowplain.tex
<YourFilename>.aux
<YourFilename>.bbl
<YourFilename>.bcf
<YourFilename>.blg
<YourFilename>.log
<YourFilename>.out
<YourFilename>.pdf
<YourFilename>.run.xml
<YourFilename>.synctex.gz
<YourFilename>.tex
<YourFilename>.toc
```

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