

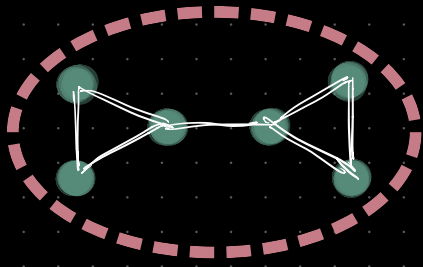
$$Q = \sum_{s=1}^{NM} \left[\frac{I_s}{L} - \left(\frac{\alpha_s}{2L} \right)^2 \right]$$

NM = number of modules in the network.

I_s = number of intra-modular links in module s .

α_s = sum of the degrees of the nodes in module s .

L = total number of links in the network.



$$Q = 0.$$

$$NM = 1$$

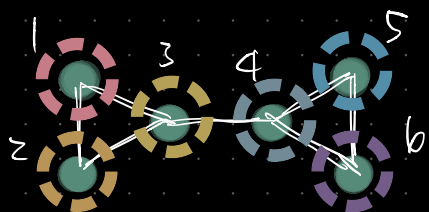
$$I_1 = 7$$

$$V_1 = 14$$

$$L = 7$$

$$\frac{7}{7} - \left(\frac{14}{14}\right)^2$$

$$= 1 - 1 = 0 \neq$$



$$Q = -0.1735,$$

$$NM = 7$$

$$I_1 = 0, I_2 = 0, I_3 = 0, I_4 = 0, I_5 = 0, I_6 = 0$$

$$\alpha_1 = 2, \alpha_2 = 2, \alpha_3 = 3, \alpha_4 = 3, \alpha_5 = 2, \alpha_6 = 2.$$

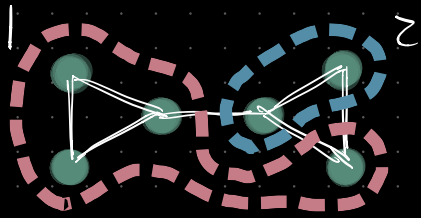
$$L = 7$$

$$\left[\frac{0}{7} - \left(\frac{2}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{2}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{3}{14} \right)^2 \right] \\ + \left[\frac{0}{7} - \left(\frac{3}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{2}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{2}{14} \right)^2 \right]$$

$$= -\frac{1}{49} + \left(-\frac{1}{49} \right) + \left(-\frac{9}{196} \right) + \left(-\frac{9}{196} \right)$$

$$+ \left(-\frac{1}{49} \right) + \left(-\frac{1}{49} \right) = -\frac{4}{49} + \left(-\frac{18}{196} \right)$$

$$= -\frac{4 \times 4 + 18}{196} = -\frac{34}{196} = -\frac{17}{98} = -0.1735$$



$$Q = 0.0306$$

$$NM = 2$$

$$I_1 = 3, I_2 = 1$$

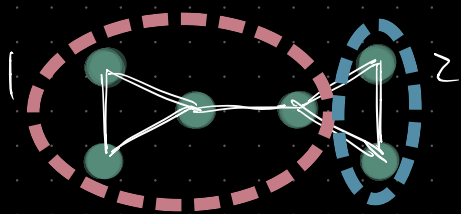
$$d_1 = 9, d_2 = 5$$

$$L = 7$$

$$\left[\frac{3}{7} - \left(\frac{9}{14} \right)^2 \right] + \left[\frac{1}{7} - \left(\frac{5}{14} \right)^2 \right]$$

$$= \frac{3 \times 28 - 81}{196} + \frac{1 \times 28 - 25}{196} = \frac{3 + 3}{196}$$

$$= \frac{6}{196} = \frac{3}{98} = 0.0306 \#$$



$$Q = 0.1224$$

$$NM = 2$$

$$I_1 = 4, I_2 = 1$$

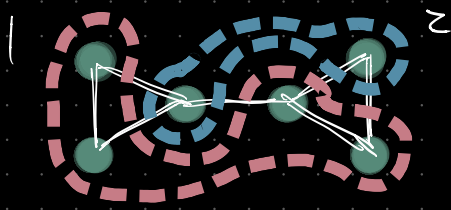
$$d_1 = 10, d_2 = 4$$

$$L = 7$$

$$\left[\frac{4}{7} - \left(\frac{10}{14} \right)^2 \right] + \left[\frac{1}{7} - \left(\frac{4}{14} \right)^2 \right]$$

$$= \frac{4 \times 28 - 100}{196} + \frac{1 \times 28 - 16}{196}$$

$$= \frac{12 + 12}{196} = \frac{24}{196} = 0.1224$$



$$Q = -0.2551.$$

$$NM = 2$$

$$I_1 = 2, \quad I_2 = 0$$

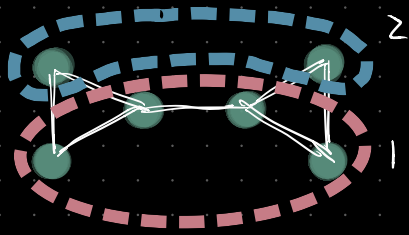
$$d_1 = 9, \quad d_2 = 5$$

$$L = 7$$

$$\left[\frac{2}{7} - \left(\frac{9}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{5}{14} \right)^2 \right]$$

$$= \frac{2 \times 28 - 81}{196} + \frac{0 - 25}{196} = \frac{-25 - 25}{196}$$

$$= \frac{-50}{196} = -0.2551$$



$$Q = -0.1633$$

$$NM = 2$$

$$I_1 = 3, I_2 = 0$$

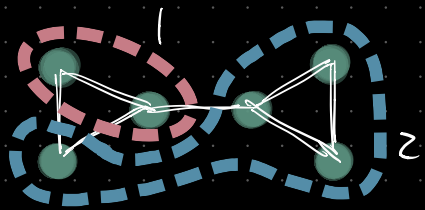
$$\alpha_1 = 10, \alpha_2 = 4$$

$$L = 7$$

$$\left[\frac{3}{7} - \left(\frac{10}{14} \right)^2 \right] + \left[\frac{0}{7} - \left(\frac{4}{14} \right)^2 \right]$$

$$= \frac{3 \times 28 - 100}{196} + \frac{0 - 16}{196} = \frac{-16 - 16}{196}$$

$$= \frac{-32}{196} = -0.1633$$



$$Q = 0.0306$$

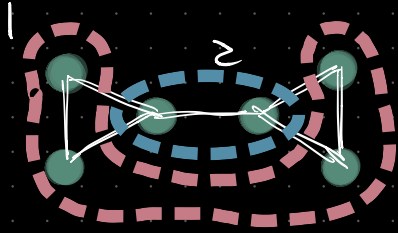
$$NM = 2$$

$$I_1 = 1, I_2 = 3$$

$$\alpha_1 = 5, \alpha_2 = 9$$

$$L = 7$$

$$\begin{aligned} & \left[\frac{1}{7} - \left(\frac{5}{14} \right)^2 \right] + \left[\frac{3}{7} - \left(\frac{9}{14} \right)^2 \right] \\ &= \frac{1 \times 28 - 25}{196} + \frac{3 \times 28 - 81}{196} = \frac{3 + 3}{196} \\ &= \frac{6}{196} = 0.0306 \end{aligned}$$



$$Q = -0,0816,$$

$$N_M = 2$$

$$I_1 = 2, I_2 = 1$$

$$\alpha_1 = 8, \alpha_2 = 6$$

$$L = 7$$

$$\begin{aligned} & \left[\frac{2}{7} - \left(\frac{8}{14} \right)^2 \right] + \left[\frac{1}{7} - \left(\frac{6}{14} \right)^2 \right] \\ &= \frac{2 \times 28 - 64}{196} + \frac{1 \times 28 - 36}{196} = \frac{-8 - 8}{196} \\ &= \frac{-16}{196} = -0,0816 \end{aligned}$$