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X SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                            File Edit Settings Run Debug Help
File Edit Settings Run Debug Help
Welcome to SWI-Frolog (threaded, 64 bits, version 7.6.3)
SWI-Frolog comes with ABSOLUTELY NO WARRANTY. This is free software.
Please run ?- license. for legal details.
                                                                                                                                            Welcome to SWI-Prolog (threaded, 64 bits, version 7.6.3)
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software.
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                                                                                                                                             For online help and background, visit http://www.swi-prolog.org
For built-in help, use ?- help(Topic). or ?- apropos(Word).
For online help and background, visit http://www.swi-prolog.org
For built-in help, use ?- help(Topic). or ?- apropos(Word).
?- prove([not,not,x], '|',lp, ['{',z,'V',y,'}','V',x]).notnotx,+ \{zVy\}Vx,-
                                                                                                                                            premises solving:
notnotx,+
x,+
premises solving:
notnota,+
conclusion solving:
{bVc}Va,-
aV{bVc},-
                                                                                                                                            conclusion solving: {zVy}Vx,-
xV{zVy},-
a,-
{bVc},-
                                                                                                                                             x,-
{z∀y},-
positive literals:
|a, + |
negative literals:
|a, - | b, - | c, - |
Closed branch lp has a,+ and a,-
true;
false.
                                                                                                                                            positive literals:

|x, + |
negative literals:

|x, - | z, - | y, - |
Closed branch lp has x, + and x, -
true;
false.
```

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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                               SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
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                                                                                                                                              File Edit Settings Run Debug Help
?- prove(['{',not,not,x,'&',not,y,'}'], '|',k3, [not,not,x,'V',z,'V',n
                                                                                                                                              ?- prove(['{',not,not,b,'&',not,e,'}',e], '|',k3, [not,not,c,'V',d,'V',not,f])
                                                                                                                                              ?- prove(['{',no
,not,f]).
{notnotb&note},+
notnotb&note,+
e,+
notnotcVdVnotf,-
ot,y]).
{notnotx&noty},+
notnotx&noty,+
notnotxVzVnoty,-
premises solving
notnotx&noty,+
                                                                                                                                             premises solving:
notnotb&note,+
notnotb,+
note,+
b,+
notnotx,+
notv.+
conclusion solving:
notnotxVzVnoty,-
notnotx,-
                                                                                                                                              conclusion solving
notnoteVdVnotf,-
notnote,-
d,-
z,-
noty,-
                                                                                                                                              notf,-
positive literals: 
|x, + | not y, + |
negative literals: 
|x, - | z, - | not y, - |
Closed branch k3 has x,+ and x,-
closed branch k3 has not y,+ and not y,-
                                                                                                                                              positive literals:

|e, + | b, + | not e, + |

negative literals:

|c, - | d, - | not f, - |

Closed branch k3 has not e,+ and e,+
true ; false.
                                                                                                                                               true ; false.
?-
```

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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                             SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
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File Edit Settings Run Debug Help
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 ?- prove([not,'{',p,'V',not,q,'}'], '|',fde, [r,'V','{',p,'&',q,'}']).
                                                                                                                                                                                             ?-\ prove([not, `\{`,b,`V',not,d,`\}'],\ `|`,fde,\ [c,`V',`\{`,b,`&',d,`\}'])\ .
 \begin{array}{l} \text{not}\{p \forall n \text{ot} q\}, + \\ r \forall \{p \& q\}, - \end{array} 
                                                                                                                                                                                             not{bVnotd},+
cV{b&d},-
premises solving:
not{pVnotq},+
notp&notnotq,+
                                                                                                                                                                                            premises solving:
not{bVnotd},+
notb&notnotd,+
notb,+
notnotd,+
d,+
 notp,+
notnotq,+
g.+
inferences solving:
rV{p&q},-
                                                                                                                                                                                             inferences solving cV{b&d},-
                                                                                                                                                                                            c,-
{b&d},-
^b&d,-
b,-
 r,-
{p&q},-
//p&q,-
p,- OR q,-
                                                                                                                                                                                            positive literals:
|not b, + | d, + |
negative literals:
|c, - | b, - |
fde branch is open, counter-example found fde:
not b, + d, + c, - b, -
p+? set pr1, notp+? set pr0
Set b related to false (b rho 0)
Set d related to true (d rho 1)
No other facts about rho obtain
true;
positive literals:
|not p. + | q. + |
negative literals:
|r. - | p. - |
branch #1 fde is open, counter-example found fde:
not p.+ q.+ r.- p.-
p+? set pr1, notp+? set pr0
Set p related to false (p rho 0)
Set q related to true (q rho 1)
No other facts about rho obtain
true;
No other facts about rho obtain true;
positive literals:
| not p, + | q, + |
negative literals:
| r, - | q, - |
Closed branch fde #2 has q,+ and q,-
                                                                                                                                                                                            positive literals:
|not b, + | d, + |
negative literals:
|c, - | d, - |
Closed branch fde has d,+ and d,-
 true ; false.
                                                                                                                                                                                             true ; false.
```

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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                    SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                                                                                                                                                                           File Edit Settings Run Debug Help
                                                                                                                                                                                   File Edit Settings Run Debug Help
 ?- prove([not, s,'&',t], '|',lp, [not,t]).
                                                                                                                                                                                   ?- prove([c,'&',not,f], '|',lp, [f])
c&notf,+
f,-
 nots&t,+
conclusion solving:
nots&t,+
nots,+
t,+
                                                                                                                                                                                   conclusion solving:
                                                                                                                                                                                    c,+
notf,+
 positive literals:

|not s, + | t, + |

|nogative literals:

|not t, - | sopen, counter-example found lp:

|not s, + t, + | not t, - |

|nop - | set pr1, |no | notp-| set pr0

| set s related to false (s rho 0)

| set t related to true (t rho 1)

| No other facts about rho obtain
                                                                                                                                                                                   positive literals:
                                                                                                                                                                                   positive literals:
|c, +| not f, +|
negative literals:
|f, -|
|p branch is open, counter-example found lp:
c,+ not f,+ f,-
no p-7 set prl, no notp-7 set pr0
Set c related to true (c rho 1)
Set f related to false (f rho 0)
No other facts about rho obtain
true;
false.
                                                                                                                                                                                    ?- ■
 ?-
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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                        SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
File Edit Settings Run Debug Help
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                                                                                                                                                                        ?- prove([not,not,'{',x,'&',r,'}'], '|',k3, [not,r,'&',not,not,q,'&',p]).
    ]).
notnot{x&r},+
                                                                                                                                                                            otnot{q&h},+
   x&r,+
notr&notnotq&p,-
                                                                                                                                                                        g&h,+
notf&notnotg&i,-
  premises solving: x&r,+ x,+ r,+
                                                                                                                                                                    premises solving:
g&h,+
[g,+
h,+
   conclusion solving 

^notr&notnotq&p,-
                                                                                                                                                                        conclusion solving:
notf&notnotg&i,-
^notf&notnotg&i,-
notf,-
  //notr&notnotq&p,-
notr,- OR notnotq,- OR p,-
notr,- OR q,- OR p,-
                                                                                                                                                                   positive literals:
|g, + | h, + |
|nsqative literals:
|not f, - |
|k & branch | is open, counter-example found k3:
g, + h, + not f, -
p+? set pr1, notp+? set pr0
Set g related to true (g rho 1)
Set h related to true (h rho 1)
No other facts about rho obtain
true;
  positive literals:

|x + | r + |
negative literals:
|not r, - |
brench #1 k3 is open, counter-example found k3:

x,+r,+ not r,-
p+? set pr1. notp+? set pr0

Set x related to true (x rho 1)

Set r related to true (r rho 1)

No other facts about rho obtain

true:
   no other facts about rho obtain true;
positive literals:
|x, + | r, + |
negative literals:
|q, - |
branch #2 k3 is open, counter-example found k3:
                                                                                                                                                                        notnotg,-
g,-
                                                                                                                                                                        positive literals:
|g, + | h, + |
negative literals:
|g. - |
  x,+r,+q,-
p+? set pr1, notp+? set pr0
Set x related to true (x rho 1)
Set r related to true (r rho 1)
No other facts about rho obtain
                                                                                                                                                                        |g, - |
Closed branch k3 has g,+ and g,-
   true ;
positive literals:
                                                                                                                                                                    true;
positive literals:
|x, + | r, + |
negative literals:
|p, - |
branch #3 k3 is open, counter-example found k3:
x,+ r,+ p.-
p+? set pr1, notp+? set pr0
Set x related to true (x rho 1)
Set related to true (r rho 1)
No other facts about rho obtain
true;
                                                                                                                                                                         true ; false.
   ?-
                                                                                                                                                                        2-
```

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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                 SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            File Edit Settings Run Debug Help
                                                                                                                                                                                                                                                                                                                                                                                                                                                  File Edit Settings Run Debug Help
           ?- prove([not,t,'&','{',not,w,'&',q,'}'], '|',fde, [not,not,'{',not,w,'&',q,'}'], '|',fde, [not,not,'{',not,w,'nott&(notw&q),+
notnot(notw&q),-
                                                                                                                                                                                                                                                                                                                                                                                                                                                  ?- prove([not,c,'&','{',e,'&',not,f,'}'], '|',fde, [not,not,'{',e,'&',not,f,'}']), not.6,'e&notf),+ notnot(e&notf),+
           premises solving
nott&{notv&q},+
nott,+
{notv&q},+
notw,+
                                                                                                                                                                                                                                                                                                                                                                                                                                                  premises solving
notc&{e&notf},+
notc,+
{e&notf},+
                                                                                                                                                                                                                                                                                                                                                                                                                                                   e,+
notf,+
                                                                                                                                                                                                                                                                                                                                                                                                                                               conclusion solving
notnot{e&notf},-
{e&notf},-
~e&notf,-
           conclusion solving:
notnot{notw&q},-
{notw&q},-
^notw&q,-
              //notw&q,-
notw,- OR q,-
                                                                                                                                                                                                                                                                                                                                                                                                                                                 positive literals:
|not c, + | e, + | not f, + |
negative literals:
|e, - |
Closed branch fde has e,+ and e,-
         positive literals:
|not t, + | not w, + | q, + |
|not w, - |
Closed branch fde #1 has not w,+ and not w,-
true;
positive literals:
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not t, + | not w, + | q, + |
|not w, + | not w, + | q, + |
|not w, + | not w, + | q, + |
|not w, + | not w, + | q, + |
|not w, + | not w, + | q, + |
|not w, + | not w, + | q, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + | not w, + |
|not w, + | not w, + |
|not w, + | not w, + |
                                                                                                                                                                                                                                                                                                                                                                                                                                                     true :
                                                                                                                                                                                                                                                                                                                                                                                                                                                   notf,-
                                                                                                                                                                                                                                                                                                                                                                                                                                                  positive literals:
|not c, + | e, + | not f, + |
negative literals:
|not f, - |
Closed branch fde has not f,+ and not f,-
                                                                                                                                                                                                                                                                                                                                                                                                                                                     true ;
false.
             ?-
                                                                                                                                                                                                                                                                                                                                                                                                                                                 ?- ■
```