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SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                    SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
File Edit Settings Run Debug Help
Welcome to SVI-Prolog (threaded, 64 bits, version 7.6.3)
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                                                                                                                                                                   File Edit Settings Run Debug Help
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                                                                                                                                                                    For online help and background, visit http://www.swi-prolog.org
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?- prove([not,not,a], '|',lp, ['{',b,'V',c,'}','V',a]).
notnota,+
{bVc}Va,-
                                                                                                                                                                    ?-prove([not,not,x], '|',lp, ['{',z,'V',y,'}','V',x]).
notnotx,+
{zVy}Vx,-
premises solving:
notnota,+
a,+
                                                                                                                                                                    premises solving:
notnotx,+
conclusion solving:
{bVc}Va,-
aV{bVc},-
                                                                                                                                                                    conclusion solving:
{zVy}Vx,-
xV{zVy},-
                                                                                                                                                                    x,-
{z∀y},-
 a,-
{bVc},-
                                                                                                                                                                  positive literals:

|x, +|

negative literals:

|x, -| z, -| y, -|

Closed branch lp has x,+ and x,-

true;

false.
positive literals:
|a, + |
negative literals:
|a, - | b, - | c, - |
Closed branch lp has a,+ and a,-
true;
false.
                                                                                                                                                                    ?-
?-
```

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                                                                                                                                                                                                                                                                                                               SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
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                                                                                                                                                                                                                                                                                                               File Edit Settings Run Debug Help
                                                                                                                                                                                                                                                                                                              ?- prove(['{',not,not,b,'&',not,e,'}',e], '|',k3, [not,not,c,'V',d,'V' ^,not,f]), {notnotb&note,+ notnotb&note,+
          ?- prove(['{',not,not,x,'&',not,y,'}'], '|',k3, [not,not,x,'V',z,'V',not,y]).
{notnotx&noty},+
          notnotx&noty,+
notnotxVzVnoty,-
                                                                                                                                                                                                                                                                                                                e,+
notnotcVdVnotf,-
         premises solving:
notnotx&noty,+
notnotx,+
noty,+
                                                                                                                                                                                                                                                                                                              premises solving
notnotb&note,+
notnotb,+
note,+
b,+
         inferences solv
notnotxVzVnoty
notnotx,-
                                                                                                                                                                                                                                                                                                              inferences solving:
notnotcVdVnotf,-
notnotc,-
d,-
          z,-
noty,-
      positive literals:
|x, + | not y, + |
negative literals:
|x, - | z, - | not y, - |
Closed branch k3 has x,+ and x,-
Closed branch k3 has not y,+ and not y,-
true;
false;
                                                                                                                                                                                                                                                                                                               notf,-
                                                                                                                                                                                                                                                                                                              positive literals:

|e, + | b, + | not e, + |

negative literals:

|c, - | d, - | not f, - |

Closed branch k3 has not e,+ and e,+
                                                                                                                                                                                                                                                                                                                true ; false.
                                                                                                                                                                                                                                                                                                               2-
                     p_{x} p_{y} p_{y
                                                                                                                                                                                                                                                                                                                  r- prove([noc, { ,b, * ,noc,α, } ], | ,tae, [c, * , { ,D, α ,α, , ] } ])
          not{pVnotq},+
rV{p&q},-
                                                                                                                                                                                                                                                                                                               not{bVnotd},+
cV{b&d},-
        premises solving:
not{pVnotq},+
notp&notnotq,+
notp,+
notnotq,+
                                                                                                                                                                                                                                                                                                              premises solving:
not{bVnotd},+
notb&notnotd,+
notb,+
notnotd,+
d,+
         inferences solving:
rV{p&q},-
                                                                                                                                                                                                                                                                                                               inferences solving: cV{b&d},-
                                                                                                                                                                                                                                                                                                              c,-
{b&d},-
^b&d,-
          -, {p&q}, -
                                                                                                                                                                                                                                                                                                               Ъ,-
          //p&q,-
p,- OR q,-
                                                                                                                                                                                                                                                                                                             positive literals:
|not b, + | d, + |
negative literals:
|c, - | b, - |
fde branch is open, counter-example found fde:
not b, + d, + c, - b, -
p+? set pr1, notp+? set pr0
Set b related to false (b rho 0)
Set d related to true (d rho 1)
No other facts about rho obtain
true;
        positive literals:
|not p, + | q, + |
negative literals:
|r, - | p, - |
branch #1 fde is open, counter-example found fde:
not p.+ q,+ r,- p,-
p+? set pr1, notp+? set pr0
Set p related to false (p rho 0)
Set q related to true (q rho 1)
No other facts about rho obtain
true;
       No other recording true;
positive literals:
|not p, + | q, + |
negative literals:
|r, - | q, - |
Closed branch fde #2 has q,+ and q,-
                                                                                                                                                                                                                                                                                                               d.-
                                                                                                                                                                                                                                                                                                              positive literals:
|not b, + | d, + |
|negative literals:
|c, - | d, - |
|Closed branch fde has d,+ and d,-
```

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                                                                                                                                                                                 SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
   File Edit Settings Run Debug Help
                                                                                                                                                                                File Edit Settings Run Debug Help
                                                                                                                                                                                ?- prove([c,'&',not,f], '|',lp, [f]).c&notf,+
f,-
    ?- prove([not. s.'&'.t]. '|'.lp. [not.t]).
    nots&t,+
nott,-
                                                                                                                                                                                premises solving:
c&notf,+
c,+
notf,+
    premises solving:
nots&t,+
    nots,+
                                                                                                                                                                                positive literals:

|c, + | not f, + |

negative literals:

|f, - |
   positive literals:
|not s, + | t, + |
|not s, + | t, + |
|nogative literals:
|not t, - |
|branch is open, counter-example found lp:
|not s, + t, + not t, - |
|nop-7 set pr1, no notp-7 set pr0
|Set s related to false (s rho 0)
|Set t related to true (t rho 1)
|No other facts about rho obtain
                                                                                                                                                                                |f, -|
|p branch is open, counter-example found lp:
c,+ not f,+ f,-
no p-7 set prl, no notp-7 set pr0
Set c related to true (c rho 1)
Set f related to false (f rho 0)
No other facts about rho obtain
true;
false.
                                                                                                                                                                                 ?-■
    2-
    SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                  SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
File Edit Settings Run Debug Help
                                                                                                                                                                                 File Edit Settings Run Debug Help
                                                                                                                                                                                  ?- prove([not,not,'{',g,'&',h,'}'], '|',k3, [not,f,'&',not,not,g,'&',i-
]);
    ?- prove([not,not,'{',x,'&',r,'}'], '|',k3, [not,r,'&',not,not,q,'&',p]
       ).
otnot{x&r}.+
                                                                                                                                                                                      otnot{g&h},+
    x&r,+
notr&notnotq&p,-
                                                                                                                                                                                  g&h,+
notf&notnotg&i,-
    premises solving:
x&r,+
x,+
r,+
                                                                                                                                                                             premises solving:
g&h,+
[g,+
h,+
                                                                                                                                                                                 inferences solving:
    //notr&notnotq&p,-
notr,- OR notnotq,- OR p,-
notr,- OR q,- OR p,-
                                                                                                                                                                                positive literals:
|g, + | h, + |
negative literals:
|not f, - |
| k3 brench is open, counter-example found k3:
g,+ h,+ not f,-
p+? set pr1. notp+? set pr0
Set g related to true (g rho 1)
Set h related to true (h rho 1)
No other facts about rho obtain
true;
   positive literals:
|x, + | r, + |
| negative literals:
|x, + | r, - |
| branch #1 k3 is open, counter-example found k3:
x, + r, + not r. -
| p+? set pr1, notp+? set pr0
Set x related to true (x rho 1)
Set r related to true (r rho 1)
No other facts about rho obtain
true;
| positive literals:
|x, + | r, + |
| negative literals:
| q, - |
| branch #2 k3 is open, counter-example found k3:
x, + r, + q, -
                                                                                                                                                                                  notnotq.-
                                                                                                                                                                                 positive literals:
|g, + | h, + |
negative literals:
    |g, - |
Closed branch k3 has g,+ and g,-
    true;
positive literals:
|x, + | r, + |
negative literals:
                                                                                                                                                                                  positive literals:
|g, + | h, + |
negative literals:
    negative literals:

|p. - | branch #5 k3 is open, counter-example found k3:

x.+ r.+ p.-

p+? set pr1, notp+? set pr0

Set x related to true (x rho 1)

Set r related to true (r rho 1)

No other facts about rho obtain

true:
                                                                                                                                                                                   g,+h,+ i,-
p+? set pr1, notp+? set pr0
Set g related to true (g rho 1)
Set h related to true (h rho 1)
No other facts about rho obtain
                                                                                                                                                                                   true ;
false.
    ?-
                                                                                                                                                                                   2-
    SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
                                                                                                                                                                                 SWI-Prolog (AMD64, Multi-threaded, version 7.6.3)
   File Edit Settings Run Debug Help
                                                                                                                                                                                File Edit Settings Run Debug Help
    ?- prove([not,t,'&','{',not,w,'&',q,'}'], '|',fde, [not,not,'{',not,w,'&',q,'}'], '|'not,w,'a(not,w,',+);
                                                                                                                                                                                ?- prove([not,c,'&','{',e,'&',not,f,'}'], '|',fde, [not,not,'{',e,'&',not,f,'}']), notck(e&notf),+ notnot(e&notf),-
                                                                                                                                                                                premises solving
notc&{e&notf},+
notc,+
{e&notf},+
e,+
notf,+
    premises solving
nott&{notv&q},+
    nott&{notwo
nott,+
{notw&q},+
notw,+
    inferences solving
notnot{notw&q},-
{notw&q},-
^notw&q,-
                                                                                                                                                                                inferences solving:
notnot{e&notf},-
{e&notf},-
^e&notf,-
e.-
    //notw&q,-
notw,- OR q,-
                                                                                                                                                                                positive literals:
|not c, + | e, + | not f, + |
negative literals:
|e, - |
Closed branch fde has e,+ and e,-
   notw,— ox q,—
positive literals:
|not t, + | not w, + | q, + |
negative literals:
|not w, - |
Closed branch fde #1 has not w,+ and not w,-
true;
positive literals:
|not t, + | not w, + | q, + |
negative literals:
|q, - |
Closed branch fde #2 has q,+ and q,-
true;
                                                                                                                                                                                 true :
                                                                                                                                                                                positive literals:
|not c, + | e, + | not f, + |
negative literals:
|not f, - |
Closed branch fde has not f,+ and not f,-
    true ;
                                                                                                                                                                                true ; false.
                                                                                                                                                                                ?- ■
```