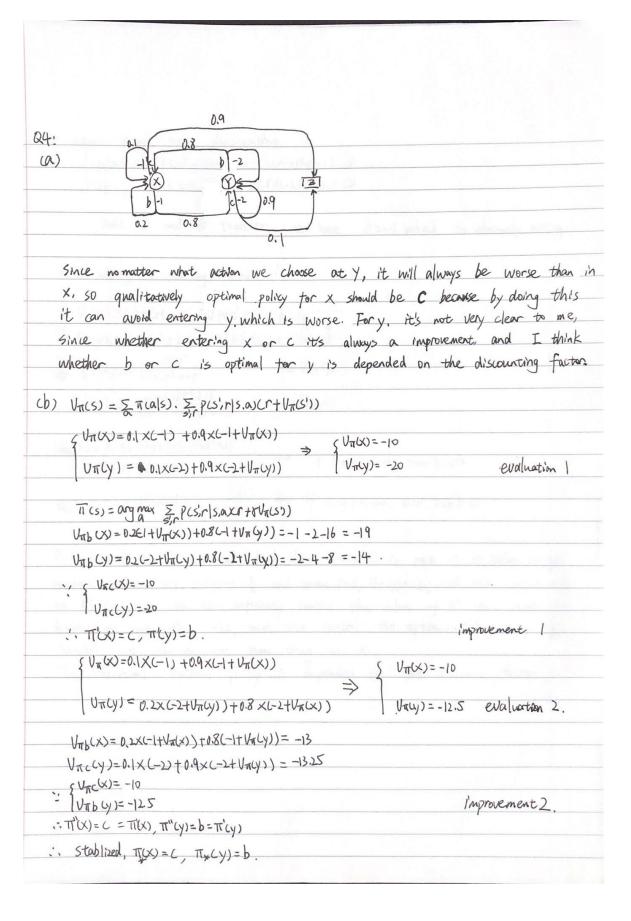
QO: (A) Yes. Either anonymized or not is okay
(b) Same for EXO and EXI
QI:
(a)
$V_{\chi}(s) = \max_{\alpha} q_{\chi}(s, \alpha)$
(b) 9*(a,s)= = Pcs',rls,a)(r+8V*(s'))
(C) $T_{*}(s) = \underset{\alpha}{\operatorname{arg max}} q_{*}(s, \alpha)$
(d) $T(x(s)) = \underset{a}{\operatorname{arg max}} \sum_{s,r} p(s',r s,a)(r+t)V_{x}(s')$
(e) VT(s) = \(\frac{2}{a}\pi(a s)\)[\(\frac{\sigma}{s',r}\pi(s',r s,a)\cdot r+\(\frac{2}{s',r}\pi(s',r s,a)\cdot \sigma'\cdot \sigma'\s
= = = T(a s) (r(s,a) + = P(s' s,a).8V_T(s'))
$V_{*}(s) = \max_{\alpha} (r(s,\alpha) + \sum_{s} p(s' s,\alpha) \cdot \gamma V_{*}(s'))$
$q_{\pi(s, \omega)} = r(s, \alpha) + \sum_{s} p(s' s, \alpha) \cdot \sum_{a} \pi(a' s) \cdot q(s', a')$
$q_{*}(s,a) = r(s,a) + \sum_{s} p(s s,a) r max q_{*}(s',a')$
Q2:
(a). The policy keeps switching between two optimal ones because the original
pseudo code use actions as criteria to Judge stobility of the policy, while actually we should stop the iteration when we know we already have an optimal one
tix: change the second line from the last to:
if \$\frac{5}{5},r\s,o\d_action)(r+rv(s')) \div \frac{5}{5},r\sigma(s',r\sigma)(r+rv(s')), policy-stable false
(b). There isn't, because value iteration derives the optimal V* first, and then calculate the policy, so there isn't switching action.

03:	
(a) 1. Initialization	
QCS, a) = R and TICS) = A(S) arbitarily for all SES	
2 policy evaluation	
Loop:	
4-0	
Loop for each s ES	
$\alpha \leftarrow \pi(S)$	
q < Q(S,a)	
QC,Q) = Sin P(s,r,s,a)[r+8 Sitt(a' s)(Q(s,a')]	
$\Delta = \max(\Delta, q - Q(S, \alpha))$	
until $\Delta < \theta$ ca small value for accuracy)	
3. policy improvement	
policy_stable < true	
For each s ES	
old_action < TT(S)	
$\pi(s) \leftarrow \underset{\alpha}{\operatorname{arg max}} q(s, \alpha)$	
a de la companya de l	
If STO PCSINISTICATED EN+ & STICALS') 9 (OU) SINIF STOPS, Old action) [r+8 STICALS') 90	alss"
then policy_stable - talse	,
If policy_stable, then 5top and return Q2qx, and T2TIx; nelse go to 2	
Cb)int: threshold 0>0; QCS,a), for all SESt, arbitanily QCS,a)=0 when s is term	ilnal.
Loop:	
'△←0	
Loop for each SES: a growing (S,a)	
$q \leftarrow Q(S, A)$	
QCS, W- Fpcs; Ms, a)[n+8 max qcs', a')]	
$\Delta \leftarrow \max(s, q - Q(s, a))$	
until 6<0.	
Output deterministic policy, T&Tx, such that	
T(S) = argmax \(\frac{1}{2}\) P(S', r\S, a) Ert \(\frac{1}{2}\) Q(S, \(\pi S')) \(\frac{1}{2}\)	
~ IA 5.4	



(C) when there isn't discounting Q Uπ(x) = 0.2 x C-1 + Uπ(x) + α8 x C-1 + Uπ(y)) Φ VT (y) = 0.2x (-2+UT(y)) +0.8x(-2+UT(x)) @ add D and D together, we have 0=-3, which is obviously wrong. After adding discounting factor 8: Un(x) =0.2x(-1+xVn(x)+0.8x(-1+ xVn(y)) Uny) = 0.2x(-2+1=Uny))+0.8x(-2+ YVn(x)) $\Rightarrow \begin{cases} V_{\pi}(y) = \frac{-2 - 0.48}{1 - 0.68^2 - 0.48} \\ V_{\pi}(x) = \frac{-1 + 0.288^2 - 1.28}{(1 - 0.68^2 - 0.48 \times 1 - 0.28)} \end{cases}$ = VTTB (4) = 4xb(X) Vac(x) = 0.1x(-1)+0.9x(-1+Vn(x)) it VIW<-10, then TIW=C =- 1+09 UT (X) Vac(y) = -2+0.9Un(y) -> if Unity) <-10, then Tity)= C. By observing Unb(y), we can find that (-90,-2) is part of it value range, because when $r \to 1$, $V_{\pi}(y) \to -\frac{2}{6}$, and when r = 0, $V_{\pi}(y) = -2$, and it's continuous on recoil), so we can definitely control the value of r to make it higher or lower than -20, and thus control the optimal policy for y. Similarly, we can do the same thing on X. In conclution, optimal policy is depended on the discount factor.

(a)

```
[[ 3.31 8.79 4.43 5.32 1.49]
[ 1.52 2.99 2.25 1.91 0.55]
[ 0.05 0.74 0.67 0.36 -0.4 ]
[-0.97 -0.43 -0.35 -0.58 -1.18]
[-1.86 -1.34 -1.23 -1.42 -1.97]]
```

Same as Figure 3.2

(b)

```
[[21.98 24.42 21.98 19.42 17.48]
[19.78 21.98 19.78 17.8 16.02]
[17.8 19.78 17.8 16.02 14.42]
[16.02 17.8 16.02 14.42 12.98]
[14.42 16.02 14.42 12.98 11.68]]
{'[0, 0]': ['r'], '[0, 1]': ['u', 'd', 'l', 'r'], '[0, 2]': ['l'], '[0, 3]': ['u', 'd', 'l', 'l'], '[1, 0]': ['u', 'r'], '[1, 1]': ['u'], '[1, 2]': ['u', 'l'], '[1, 3]': ['l'], '[1, 4]': ['l'], '[2, 0]': ['u', 'r'], '[2, 1]': ['u'], '[3, 0]': ['u', 'l'], '[3, 3]': ['u', 'l'], '[3, 4]': ['u', 'l'], '[4, 0]': ['u', 'r'], '[4, 1]': ['u'], '[4, 2]': ['u', 'l'], '[4, 4]': ['u', 'l']}
```

Same as Figure 3.5. The dictionary contains derived optimal policy, which key is state and value is action.

(c)

```
[[21.98 24.42 21.98 19.42 17.48]
[19.78 21.98 19.78 17.8 16.02]
[17.8 19.78 17.8 16.02 14.42]
[16.02 17.8 16.02 14.42 12.98]
[14.42 16.02 14.42 12.98 11.68]]
{'[0, 0]': ['r'], '[0, 1]': ['u', 'd', 'l', 'r'], '[0, 2]': ['l'], '[0, 3]': ['u', 'd', 'l', 'l'], '[1, 0]': ['u', 'r'], '[1, 1]': ['u'], '[1, 2]': ['u', 'l'], '[1, 3]': ['l'], '[1, 4]': ['l'], '[2, 0]': ['u', 'r'], '[2, 1]': ['u'], '[3, 0]': ['u', 'r'], '[3, 1]': ['u'], '[3, 2]': ['u', 'r'], '[4, 1]': ['u'], '[4, 2]': ['u', 'l'], '[4, 4]': ['u', 'l'], '[4, 2]': ['u', 'l'], '[4, 4]': ['u', 'l'], '[4, 5]': ['u', 'l'], '[4, 4]': ['u', 'l']]
```

- (a) I wrote the code but fail to implement it.
- (b) The reward will change when making those modifications. When a employee is able to help switching cars the cost on switching will decrease from num_movedCars to (num_movedCars -1), in this case the optimal policy should be tend to switch more cars. And when the parking lot charge for extra fees there will be an extra cost which result in lower reward, so the optimal policy should be tend to keep less cars in both locations.

Q7. (a). it max tra - max g (a) 30: |max + (a) - max g(a)| = max + (a) - max g(a)" maxga>> g(x) for all x : $\max + (a) - \max_{x} g(x) \leq \max_{x} + (a) - g(x)$, tor all x, . max + (a) - max g cas < max + (a) - g (a) (Say, a = argmax +(a), a = argmax(+(a) - gco) then $f(a_1) - g(a_1) \le f(a_2) - g(a_2)$ (2) could be easily proved (2) 0: where +(0,)-g(a) = max f(a)-g(a), t(a2)-g(a2) = max (t(a)-g(a)) \Rightarrow max +(a) -g(a) \leq max (+(a) -g(a)) when mox+(a)-maxg(a) <0 substitute flax = g(a) , and g(a) = + (w), and we can prove it in the same vby. : (max + (a) - max gras) < max + (a) - gras). | BV:(S) -BV:(S) = | max \(\sum_{\text{p}} \sum_{\text{s},r} \sum (b) use equation proved from (a) (i) ≤ max | ₹ P(s',r|sa)[r+t/k(s')] - ₹ P(s',r|s,a)[r+t/k(s')] | = max | F p(s), r|s, a) Cr+ tVk(s') - r- tVk'(s') = max | = p(s,r|s,ox. r(VKS) - Vk(S)) | hold for all S & S for n-length vector V: and Vi': 11BV; -BV; 11= max { 1BV; (S,) -BV; (S,) } } | 1 BViGN-BViGN) max = p(s,r/s,a) r(U; (S,n-V:(S,N)) -

(2) < max { max \(\subseteq \text{PCS', rls, a} \) - \(\subseteq \subseteq \limits \) \(\superits \) \(\superi	
,	
dupliate. Xn.	
I by many was the a second district.	
max = -PCS, r S, a) - } Vi - Vi	
$ \langle \sigma V_i - V_i^* \rangle$	
$= \max \left\{ \frac{\left \left V_{i}-V_{i}^{*}\right \right }{\left \left V_{i}-V_{i}^{*}\right \right } \right\} = \left \left \left V_{k}-V_{k}^{*}\right \right .$	
×n	
$V_{i} = V_{i} $	
". proved.	
(C) Barach fixed point therom: d(T(X), T(y)) = qd(X, y)	
in our case: dexy) = 11x-y11,	
$T(X) = \beta X$, B is contracting mapping	
$q = 8$ Use equation from (b), $ BV_i - BV_i _{\infty} \leq x V_i - V_i _{\infty}$	
use equation from (b): BV:-BV: = \(\frac{1}{2} \rightarrow \frac{1}{2} \ri	
proof:	
first for any positive integer n; Vn+- Vn \le \sign^n V1-Vo Cue	3)
then, ter any m,n!	
11 Um - Vall = Vm - Vm 1 + Vm - Vm 2 + + Vn+1, Vall	-
< 3m-1 11V, -Val, + 8m-2 11V, -Val) + 7m 11V, Vol)	
= 81 IIV, -Voll E=0 8th	
< 5" V, -Vo ≥ 7k.	
= 0 11 V V. 11 1- x	
We can find a large N that $qN < \frac{E(1-q)}{ V_1-V_0 }$ $E > 0$ is an	bitary value
: Vm-Vn ≤ 8 n tv - Vo 1 - 8 < €	

_'、	the sequence Vi is Cauchy, and thus must have a fix point.
V	At = 1m Vn = 1m BUn-1 = B(1m Vn-1) = BVX
八	it conveges to a fix point.
My	que: if it has two fix point, V_1 , V_2 then. $V_1 = \beta V_2$, $V_2 = \beta V_2$.
	$ \beta V_1 - \beta V_2 = V_1 - V_2 = V_1 - V_2 _{\infty}$
	-1 Le (0'1)
	-1. unique. tix point.
acce	BV(S) = max ECRt+1 + &V*(St+1) St=S,At=a]
	= mox 9 (5, a)
	= V _* (s)
	so this unique tixed point satisfied Bellman optimal equation
	or equivalent to