

Variables (Alphabetical By Variable)

a	Constant; distance
A, B, C, ...	Forces; reactions
A, B, C, \dots	Points
A, \mathcal{A}	Area
b	Distance; width
c	Constant; distance; radius
C	Centroid
C_1, C_2, \dots	Constants of integration
C_p	Column stability factor
d	Distance; diameter; depth
D	Diameter
e	Distance; eccentricity; dilatation
E	Modulus of elasticity
f	Frequency; function
F	Force
$F.S.$	Factor of safety
G	Modulus of rigidity; shear modulus
h	Distance; height
H	Force
H, J, K	Points
I, I_x, \dots	Moment of inertia
I_{xy}, \dots	Product of inertia
J	Polar moment of inertia
k	Spring constant; shape factor; bulk modulus; constant
K	Stress concentration factor; torsional spring constant
l	Length; span
L	Length; span
L_e	Effective length
m	Mass
M	Couple
M, M_x, \dots	Bending moment
M_D	Bending moment, dead load (LRFD)
M_L	Bending moment, live load (LRFD)
M_U	Bending moment, ultimate load (LRFD)
n	Number; ratio of moduli of elasticity; normal direction
p	Pressure
P	Force; concentrated load
P_D	Dead load (LRFD)
P_L	Live load (LRFD)

P_U	Ultimate load (LRFD)
q	Shearing force per unit length; shear flow
Q	Force
Q	First moment of area
r	Radius; radius of gyration
R	Force; reaction
R	Radius; modulus of rupture
s	Length
S	Elastic section modulus
t	Thickness; distance; tangential deviation
T	Torque
T	Temperature
u, v	Rectangular coordinates
u	Strain-energy density
U	Strain energy; work
v	Velocity
V	Shearing force
V	Volume; shear
w	Width; distance; load per unit length
W, W	Weight, load
V	Shearing force
V	Volume; shear
w	Width; distance; load per unit length
W, W	Weight, load
x, y, z	Rectangular coordinates; distance; displacements; deflections
$\bar{x}, \bar{y}, \bar{z}$	Coordinates of centroid
Z	Plastic section modulus
α, β, γ	Angles
α	Coefficient of thermal expansion; influence coefficient
γ	Shearing strain; specific weight
γ_D	Load factor, dead load (LRFD)
γ_L	Load factor, live load (LRFD)
δ	Deformation; displacement
ϵ	Normal strain
θ	Angle; slope
λ	Direction cosine
ν	Poisson's ratio
ρ	Radius of curvature; distance; density
σ	Normal stress
τ	Shearing stress
ϕ	Angle; angle of twist; resistance factor
ω	Angular velocity

Conversion Factors

$$1\text{hp} = 550\text{ft}\cdot\text{lb/s} = 6600\text{ in}\cdot\text{lb/s} \quad (1)$$

General

SI Prefixes

Multiplication Factor	Prefix†	Symbol
1 000 000 000 000 = 10^{12}	tera	T
1 000 000 000 = 10^9	giga	G
1 000 000 = 10^6	mega	M
1 000 = 10^3	kilo	k
100 = 10^2	hecto‡	h
10 = 10^1	deka‡	da
0.1 = 10^{-1}	deci‡	d
0.01 = 10^{-2}	centi‡	c
0.001 = 10^{-3}	milli	m
0.000 001 = 10^{-6}	micro	μ
0.000 000 001 = 10^{-9}	nano	n
0.000 000 000 001 = 10^{-12}	pico	p
0.000 000 000 000 001 = 10^{-15}	femto	f
0.000 000 000 000 000 001 = 10^{-18}	atto	a

Chapter 1 - Concept of stress

Axial Loading: Normal Stress

$$\sigma = \frac{P}{A} \quad (2)$$

Transverse Forces and Shearing Stress

$$\tau_{\text{ave}} = \frac{P}{A} \quad (3)$$

Single and Double Shear

Single Shear

$$\tau_{\text{avg}} = \frac{P}{A} = \frac{F}{A} \quad (4)$$

Double Shear

$$\tau_{\text{avg}} = \frac{P}{A} = \frac{F/2}{A} = \frac{F}{2A} \quad (5)$$

Bearing Stress

$$\sigma_b = \frac{P}{A} = \frac{P}{td} \quad (6)$$

Method of Solution

1. Clear and precise statement of problem
2. Draw one or several free-body diagrams; used to write equilibrium equations
3. Think SMART. Strategy, Modeling, Analysis, and Reflect & Think

Stresses on an Oblique Section

$$\sigma = \frac{P}{A_0} \cos^2 \theta \quad (7)$$

$$\tau = \frac{P}{A_0} \sin \theta \cos \theta \quad (8)$$

Stress Under General Loading

Factor of Safety

$$\text{Factor of safety} = \text{F.S.} = \frac{\text{ultimate load}}{\text{allowable load}} \quad (9)$$

Chapter 2 - Stress and Strain - Axial Loading

Normal Strain

$$\epsilon = \frac{\delta}{L} \quad (10)$$

Hooke's Law and Modulus of Elasticity

$$\sigma = E\epsilon \quad (11)$$

Elastic Deformation Under Axial Loading

$$\delta = \frac{PL}{AE} \quad (12)$$

$$\delta = \Sigma = \frac{P_i L_i}{A_i E_i} \quad (13)$$

Problems with Temperature Change

$$\delta_T = \alpha(\Delta T)L \quad (14)$$

$$\epsilon_T = \alpha\Delta T \quad (15)$$

Lateral Strain and Poisson's Ratio

$$v = -\frac{\text{lateral strain}}{\text{axial strain}} \quad (16)$$

Multiaxial Loading

$$\epsilon_x = \frac{\sigma_x}{E} \quad (17)$$

$$\sigma_y = \sigma_x = -\frac{v\sigma_x}{E} \quad (18)$$

Generalized Hooke's law for multiaxial loading

$$\sigma_x = +\frac{\sigma_x}{E} - \frac{v\sigma_y}{E} - \frac{v\sigma_z}{E} \quad (19)$$

$$\sigma_y = -\frac{\sigma_x}{E} + \frac{v\sigma_y}{E} - \frac{v\sigma_z}{E} \quad (20)$$

$$\sigma_z = -\frac{\sigma_x}{E} - \frac{v\sigma_y}{E} + \frac{v\sigma_z}{E} \quad (21)$$

Dilation

$$e = \frac{1-2v}{E}(\sigma_x + \sigma_y + \sigma_z) \quad (22)$$

Bulk Modulus

p : Hydrostatic Pressure

$$e = -\frac{p}{k} \quad (23)$$

k : bulk modulus of the material

$$k = \frac{E}{3(1-2v)} \quad (24)$$

Shearing Strain: Modulus of Rigidity

$$\tau_{xy} = G\gamma_{xy} \quad (25)$$

$$\tau_{yz} = G\gamma_{yz} \quad (26)$$

$$\tau_{zx} = G\gamma_{zx} \quad (27)$$

$$\frac{E}{2G} = 1 + v \quad (28)$$

Stress Concentrations

$$K = \frac{\sigma_{\max}}{\sigma_{\text{avg}}} \quad (29)$$

Chapter 3 - Torsion

General

Deformation in Circular Shafts

$$\gamma = \frac{\rho\phi}{L} \quad (30)$$

$$\gamma_{\max} = \frac{c\phi}{L} \quad (31)$$

$$\gamma = \frac{\rho}{c} * \gamma_{\max} \quad (32)$$

Shearing Stresses in Elastic Range

$$\tau = \frac{\rho}{c} \tau_{\max} \quad (33)$$

$$\tau_{\max} = \frac{Tc}{J} \quad (34)$$

$$\tau = \frac{T\rho}{J} \quad (35)$$

Polar Moment of Inertia Solid Shaft

$$J = \frac{1}{2} \pi c^4 \quad (36)$$

c = radius

Polar Moment of Inertia of a Hollow Shaft inner radius c_1 , outer radius c_2

$$J = \frac{1}{2} \pi (c_2^4 - c_1^4) \quad (37)$$

Angle of Twist

$$\phi = \frac{TL}{JG} \quad (38)$$

$$\phi = \Sigma \frac{TL}{JG} \quad (39)$$

Statically Indeterminante Shafts

Transmission Shafts

Power P is transmitted as:

$$P = 2\pi fT \quad (40)$$

T is the torque exerted at each end of the shaft
 f the frequency (hz or s^{-1})

Stress Concentrations

$$\tau_{\max} = K \frac{Tc}{J} \quad (41)$$

K = Stress concentration factor
stress $\frac{Tc}{J}$ is computed for the smaller-diameter shaft

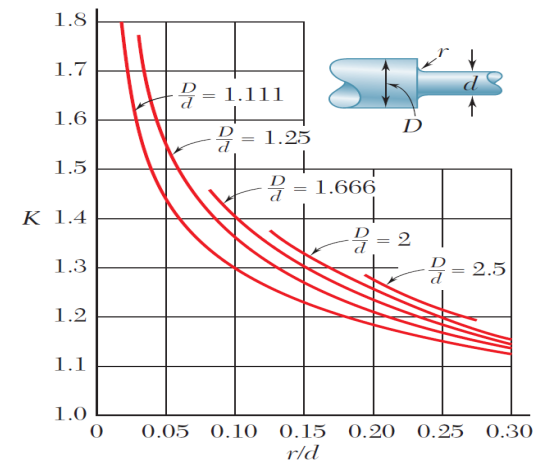


Fig. 3.28 Plot of stress concentration factors for fillets in circular shafts. (Source: W. D. Pilkey and D. F. Pilkey, *Peterson's Stress Concentration Factors*, 3rd ed., John Wiley & Sons, New York, 2008.)

Plastic Deformations

$$T = \int_0^c \rho\tau(2\pi d\rho) = 2\pi \int_0^c \rho^2 \tau d\rho \quad (42)$$

Modulus of Rupture

This is a ficticious value.

R_t = \frac{T_u c}{j} (43)

Solid Shaft of Elastoplastic Material

Maximum Elastic Torque; Solid Circular Shaft, Radius c

\tau_y = \frac{1}{2} \pi c^3 \tau Y (44)

Torque Related to \rho_y

T = \frac{4}{3} T_y (1 - \frac{1}{4} \rho \rho^3 y c^3) (45)

Plastic Torque

T_p = \frac{4}{3} T_y (46)

Plastic Torque Vs. Angle of Twist

T = \frac{4}{3} T_y (1 - \frac{1}{4} \frac{\phi^3 y}{\phi^3}) (47)

Torsional Loading or Shaft Cross-Section Changes Along Length

\phi = \sum_i \frac{T_i L_i}{J_i G_i} (48)

Thin-Walled Hollow Shafts

Shear Flow

q = \tau t (49)

Average Shearing Stress \tau at any given point in cross section

\tau = \frac{T}{2 t A} (50)

Chapter 4 - Pure Bending

1 - Symmetric Members in Pure Bending

\epsilon_x = -\frac{y}{\rho} (51)

\rho - Radius of curvature of the neutral surface
y - Distance from neutral surface

2 - Stresses and Deformatoins in the Elastic Range

\sigma_x = -\frac{y}{c} \sigma_m (52)

c - largest distance from the neutral axis to a point in the section

Elastic Flexture formula

\sigma_m = \frac{M c}{I} (53)

\sigma_x = -\frac{M y}{I} (54)

Eleastic Section Modulus

S = \frac{I}{c} (55)

\sigma_m = \frac{M}{S} (56)

Curvature of Member

\frac{1}{\rho} = \frac{M}{EI} (57)

Eccentric Axial Loading

\sigma_x = \frac{P}{A} - \frac{M_y}{I} (58)

Unsymmetric Bending

\sigma_x = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y} (59)

General Eccentric Axial Loading

\sigma_x = \frac{P}{A} - \frac{M_z y}{I_z} + \frac{M_y Z}{I_y} (60)

Curved Members

R = \frac{A}{\int \frac{dA}{r}} (61)

\sigma_x = -\frac{M y}{A e (R - y)} (62)

Additional Notes

Area, width, and moment of inertia for W shapes should be given on a test or found in appendix c of textbook.