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**AUTOMATIC DOCUMENT SEGMENTATION AND SUMMARIZATION USING NLP-BASED METHODS**

Student name: Lương Trí Vỹ (ITITIU20359)

Advisor: Dr. Nguyễn Thị Thanh Sang

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**AUTOMATIC DOCUMENT SEGMENTATION AND SUMMARIZATION USING NLP-BASED METHOD**

APPROVED BY: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_   
Dr. Nguyễn Thị Thúy Loan

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_   
Dr. Mai Hoàng Bảo Ân

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_   
Dr. Nguyễn Thị Thanh Sang

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_   
Dr. Hồ Long Văn

THESIS COMMITTEE

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# ABSTRACT

In today’s exceedingly information-rich world, the efficiency with which humans can absorb, consume, and integrate information into their own repertoire of knowledge is dependent upon one’s reading speed and their own understanding of said information. As a result, one solution to said problem is for text to be summarized and information to be condensed into forms that can be quickly absorbed. For the solution to be viable, the PDF file of a research paper must be successfully converted into a document containing the summary of each segment of the paper. The main structure of the project, therefore, can be separated into two different sections: PDF segmentation and text summarization of each segment.

Although information from a PDF can easily be extracted using tools such as PyPDF2, the structure of each paper remains an issue due to the wide variety in which research papers are formatted. As such, traditional methods cannot be relied upon but require the use of machine learning models.

The process of text summarization is more varied, as many approaches are available. In general, text summarization can be achieved either through extractive or abstractive methods. An extractive method can only generate a summary using the provided text. On the other hand, the abstractive method’s output is a summary that is made using text that is not present in the document itself.

This thesis’s aim is to test multiple different approaches to text summaries, attempt to improve said methods, and determine the most suitable approach and a final product that can demonstrate said result.

# INTRODUCTION

## Background

As the speed at which information is generated increases in the age of digitalization, the speed of information consumption and digestion must also be improved through the use of tools and techniques. As such, the development of a tool that can help with that issue is the focus of the thesis.

## Problem Statement

Due to the tremendous amount of information that each research paper holds, the potential and possibilities with which a research paper can make an impact on the world can be lost. With topics ranging from physics, medicine, psychology, etc., the potential loss of valuable insights that could be gleamed from research papers or papers that are overlooked is immense.

Although methods to improve reading speed, such as speed reading, skimming, active reading, etc., exist, all these methods aim to improve the person who is acquiring information. Even though this method is viable and can improve efficiency, much time is required to be spent for one person to acquire said skill. Human beings, innately, improve their existence and society through the development of tools. As such, developing a tool that can be used to assist said endeavor is this project's main purpose.

## Scope and Objectives

For the thesis to be considered completed, the development of a tool that can be used to parse a PDF file, turn it into a document of different segments, and then automatically summarize the information must be completed and presented as the result of the thesis.

## Structure of thesis

The main structure of the paper can be divided into six different chapters, with each chapter having its own purpose in providing full coverage of the topic. Chapter 1 serves as the paper's introduction, as the problem and aim of the thesis are introduced. Chapter 2 gives an overview of the information and knowledge used in the paper. Moving onto Chapter 3, the methodologies and techniques used for the implementation are discussed in detail. The results of the project are shown and displayed in Chapter 4. The results are then evaluated and compared based on predefined measurements to determine the effectiveness of the model itself. Lastly, chapter 6 is the summary of the project, including the strengths, weaknesses, and improvements that could be made to the thesis.

# LITERATURE REVIEW



## Overview of Automatic Document Segmentation

The general goal of Automatic Documentation Segmentation (ADS) is to scan through a document (in the form of a PDF file), identify each segment of the document, and then output the result into a well-defined form for further use cases.

As most scientific texts in online databases, which are well-defined and documented, are in the form of a PDF file, this has become the priority in terms of input format. This choice is further enhanced due to an estimate of around 50 million research papers [1] that were stored as PDF files in 2008. Since then, the number of research papers has only grown ceaselessly, further enhancing the decision to use PDFs as inputs.

Segments of a document refer to each part of a paper that is frequently required to be a part of any research paper, such as the *abstract*, *introduction*, *methodologies*, etc. However, the number of segments that are presented in the paper should not have any severe effects on the functionality of the tool itself. As the aim of the application is not to adhere to a certain principle or guideline regarding the writing style, but to effectively summarize a paper, all segments of a paper are treated as equal, and can equally influence the reader.

The act of identifying each segment of the document referred to the process of acquiring the texts that are available in the paper, classifying them accordingly based on their segment, and formatting and storing them in a predefined form of storage. The process of text acquisition can be achieved by using multiple different methods. It can be as simple as extracting the text from the PDF as is, without regard for the structure of the paper, by making use of tools such as the PyPDF2 package in Python. The structure of a paper can be difficult to acquire due to the variety of methods and standards by which it is written. For example, whether the content is divided into two columns or one, or whether the spacing on each line is 1.5 or double, all aspects of a PDF can influence the way that the text is perceived by the machine. Currently, two methods by which the structure can be parsed are using **O**ptical **C**haracter **R**ecognition (OCR) and classification of content into predefined categories using machine learning. While the first method is viable, its output is highly dependent on how the document is rendered. It is, therefore, the second method that will be the focus of the paper. To achieve this, **G**ene**R**ation **O**f **B**ibliographic **D**ata (or GROBID) is the tool of choice according to the criteria that have been set. Since GROBID integrates with a third-party file conversion tool called **pdftoxml** to convert files from PDF to XML, XML is chosen as the form of storage for the output of the extraction process.

### GROBID

GROBID [2] makes use of a cascade of sequence labeling models to parse its documents. This means that a document must go through multiple different models, each specializing in a specific task, to achieve the result. In the case of extracting the segments of the entire document, the model must first go through each layer and get the result, then pass said result to the next layer. Each of these layers is then combined and formatted accordingly. The GROBID cascade of the sequencing model can be seen in Figure 2‑1.

A diagram of a reference

Description automatically generated

Figure 2‑1 - GROBID cascade of the sequencing model [3]

Although each model can create output from the original text, some models’ purpose is only to provide the lower layer with input, creating a *cascade* of information. As a result, the accuracy of the model is highly dependent on the combination of multiple models. However, any errors that result from the higher layer will have a negative effect on the final output.

Although GROBID’s implementation supports the use of both a Deep Learning model and a **C**onditional **R**andom **F**ield (CRF) model, for the purpose of segmenting a scientific PDF paper, only the CRF model can be utilized as the number of parameters that are needed for processing the entire document exceeds the limit of what the deep learning model is currently capable of. Although the CRF model is lacking in terms of accuracy in comparison to the Deep Learning model, it makes up for it through the speed with which it processes each PDF.



## Overview of Natural Language Processing

Natural Language Processing (NLP) is an interdisciplinary field that focuses on the process of comprehending and manipulating human language. The general goal is to achieve a better understanding of natural language using simple and durable techniques for fast text processing.

Although differences exist in the function and usage of NLP between different use cases, the common natural language process typically includes seven steps, which are sentence segmentation, word tokenization, stemming, lemmatization, stop-word analysis, dependency parsing, and part-of-speech tagging.

The first step of the process is to retrieve the list of sentences from the provided text through the process known as sentence segmentation. In most cases, a sentence ends with a dot, which can make processing this step simple as that is the most common separator in a sentence. Only sentences that end with an “e.g.”, “?”, and “etc.” should be taken note of as the that can happen occasionally.

Another different method on the list is word tokenization. This step’s main purpose is to segment the sentences into separate words. These words are separated by a white space, comma, dash, dot, etc. This process can be achieved simply by storing each word of a sentence in a data structure, then proceeding to filter out unwanted whitespace words.

Stemming is the process of stripping the words of their prefixes and suffixes, allowing the algorithm to obtain the basic form of a word. As an example, by stemming the word “improvement", “improve” is the result of this step. Multiple different words can result in the same result through the stemming process, as can be seen when applying this process to both “improvement” and “improvise.”. An implementation of this process can be implemented through the Porter-Stemmer algorithm, the Lancaster-Stemmer algorithm, etc. The output of the process, however, does not bear resemblance to an English word.

Input from the stemming function is then piped into the lemmatization function. This process improved upon the stemming process by turning it into a lemma, which is the canonical form of a word. Instead of “improve", which is not a proper word, “improve” is returned instead.

After the word list has been refined and reduced to contain a list of lemmas, words that are not considered important to the linguistic analysis process are removed from the list through the process of stop-word filtering. Words such as “a”, “the”, “an”, etc., appear frequently throughout the content of a document, and are considered stop words since they do not contribute any additional meaning or context to the document. Filtering these values can improve the accuracy of the overall process.

Through filtering stop words, the word list can now be considered clean, as it contains only lemmas that influence the meaning of the document and can be used for the dependency parsing process. During the process, the structure of a sentence can be broken down into its basic form, from sentences to noun phrases and verb phrases to verbs and determiners, etc. The sentence is parsed, creating a tree-like structure with each lower layer being more specific than the one above it.

Part-of-speech tagging improves the dependency parsing functionality by assigning a part-of-speech label to each sequence of words [4]. Tags can be divided into closed class words, which are frequent and ambiguous, and open-class words, which are divided differently depending on the set of tags that is being used. Typically, a tag set can include tags such as nouns, verbs, adjectives, etc. The result from both dependency parsing and part-of-speech tagging can be seen in Figure 2‑2.

A diagram of a tree

Description automatically generated

Figure 2‑2 - Dependency style parse tree [4]

## Overview of Text Summarization

Text summarization, as the name suggests, is the process of parsing a single or multiple documents and constructing a summary for each respective document. Applications of this system are widely available, from the summarization of news, opinion, sentiment, stories, and novels to scientific paper summaries in all fields.

The general framework of the system involves a pre-processing step, a processing step, and a post-processing step, with the final step being optional in some cases. Text summarization systems can be classified based on many aspects, including input size (single-document or multi-document), approach (extractive, subtractive, or hybrid), nature of output summary (generic-based or query-based), language (monolingual, multilingual, or cross-lingual), type (headline, sentence-level, highlights, or full summary), and domain (generic or domain-specific) [5]. The framework’s visualization can be seen in Figure 2‑3*.*

A diagram of a process

Description automatically generated

Figure 2‑3 - Text summarization general framework [5]

### Extractive text summarization

The *extractive text summarization* approach selects the most important sentence using one approach amongst many to create the output. Among the available methods, approaches that have proven to produce positive results include statistical-based methods, concept-based methods, graph-based methods, deep-learning methods, etc.

Due to only reusing words from the original text, some advantages that this approach may provide include faster response times in comparison with abstractive text summarization techniques and higher accuracy in its output. However, for the same reason, some disadvantages to the techniques were created. The resulting text can contain redundancy due to having two closely related-in-meaning sentences included. Chosen sentences may also be too lengthy to serve as a summary, or the chosen sentence may lack the required context that is necessary for the reader to fully comprehend the summary. Additionally, sentences with different temporal statuses may conflict with each other when included in the same paragraph. Some notable extractive methods include TextRank (which made use of a graph-based system to determine the importance of words) [6] and Latent Semantic Analysis (LSA) (which made use of Single Value Decomposition technique to analyze the relationship between documents) [7]

The general framework of a text summarization system in the previous section can then be updated to include general steps in an extractive system. These changes can be seen in Figure 2‑4*.*

Diagram of a process

Description automatically generated

Figure 2‑4 - Extractive text summarization general framework [5]

#### TextRank

TextRank is an unsupervised graph-based ranking algorithm for the particular use case of keyword extraction in Natural Language Processing. It came into existence when the author was inspired by the PageRank algorithm that Google used to rank web pages for their search engines. The general process of TextRank includes:

1. Graph construction: The algorithm first constructed a graph with each node being a sentence and each edge representing the similarity score between sentences. The similarity score can be calculated using cosine similarity or any other method.
2. Edge weighting: Calculate the similarity score and applies it to the graph constructed.
3. Node Ranking: The PageRank algorithm [6] is applied to the graph, which apply a score for each node based on its connection to other nodes and the weights of these connections.
4. Keyword extraction: The top-ranking sentences are selected. This is dependent on the user’s input.
5. Text summarization: The extracted sentences are combined with each other, creating the summary.

#### Latent Semantic Analysis

Latent Semantic Analysis makes use of term-document matrix and Singular Value Decomposition to analyze and retrieve relationships between a set of sentences and words that the document contains. The general process of the algorithm involves:

1. Constructing a term-document matrix: The relationship is represented through a matrix between the sentences and the important words (after removing stop words) from the documents.
2. Apply singular value decomposition: Decompose the term-document matrix into 3 matrices: (left singular matrix), (singular matrix), and (right singular matrix).
3. Matrix dimensionality reduction: Keep only the top n singular values from each matrix to reduce the dimensions while retaining important concepts.
4. Compute sentence ranking: Using the reduced matrices, the ranking of each sentence is computed [8].
5. Summarize text: Choose the top sentences based on the ranking in order to construct the summary by concatenating each sentence with each other.

### Abstractive text summarization

Abstractive text summarization differs from the extractive method in that before the input is processed, it is turned into one of the intermediate forms that will then be the input of the summarization process. Similar to extractive text summarization, multiple different approaches can be used in the summary generation process, ranging from graph-based, tree-based, template-based, machine-learning-based, etc.

An abstractive text summarization system can generate a greater summary with words that do not belong to the original text. For a summary generation system, the ability to create new sentences defines what an abstractive text summary is. The output of this type of system is generally more similar to a summary created by humans in comparison to the extractive type. However, due to the highly advanced and complex nature of this system, creating one is typically difficult and can require the use of natural language generation or machine learning, which is still a growing field.

A new version of the general framework containing the architecture of an abstractive text summarization can then be visualized, resulting in Figure 2‑5.

A diagram of a process

Description automatically generated

Figure 2‑5 - Abstractive text summarization general framework [5]

#### Machine-learning-based Summary Generation

Due to the recent advancements in the progress of improving Artificial Intelligence (AI), techniques that make use of AI models have increasingly become both more effective and efficient at a rapid rate. Models such as **B**idirectional and **A**uto-**R**egressive **T**ransformers (**BART**) [9] or **T**ext-**t**o-**T**ext **T**ransfer **T**ransformer (**T5**) [10] have continuously improved the process of text summarization.

Following the development of pretrained models, utilizing trained and optimized models has become trivial due to the reduction in training time required for these models. This is especially relevant in cases where resources are limited, such as laptops or lightweight servers. The primary method by which this is achieved is through a method known as transferred learning [11]. Inspired by how humans acquire new knowledge by applying and adapting old ones, AI models are trained in a two-phase framework [12], with the first being pre-training, allowing the model to obtain knowledge from large labeled datasets, and the second being fine-tuning, which allows a model to adjust to a specific task with less data required.

Amongst the models, three, which are possible to run in a local environment efficiently, were chosen for this purpose. This includes **Falcon AI’s Text Summarization model** [13] (a T5-based model) and **Facebook’s BART Large CNN model** [14] (a BART-based model). Even though another model is not suitable for this use case, a relatively large model was chosen for the benchmark, which was **Stability AI’s Stable LM 2 1.6B model** [15].

As these models are pretrained, the dataset that was used also differs between each model. While some models were trained mostly on one dataset, others used multiple simultaneously. For instance, Facebook’s BART Large CNN model’s base BART model was pretrained on a large corpus using a denoising autoencoder method, which is then fine-tuned using the CNN Dailymail Dataset ([16], [17]). Falcon AI’s Text Summarization model, on the other hand, is fine-tuned using a variety of documents and their generated summaries. Since Text Summarization model is fine-tuned based on Google’s T5 Small model [10], the model is pre-trained on many datasets. Some important datasets include:

* **C4** [10]: A cleaned version of Common Crawls’ web crawl corpus.
* **Wiki-DPR** [18]: contains 21 million passages from Wikipedia.

As for Stable LM 2 1.6B, three main datasets were used for the pre-training process, including:

* **UltraChat 200k** [19], [20]: Consisting of 1.4 million dialogues generated by ChatGPT.
* **MetaMathQA** [21]: Containing questions and answers related to math.
* **Orca DPO Pairs**: A modified version of the OpenOrca dataset ([22], [23], [24], [25], [26])

# METHODOLOGY

## Overview

Although this project does have exposed APIs and a minimal web user interface, the application only lacks refinement that can effectively serve its purpose. Currently, most core sections of the project are well defined, resulting in a fully featured tool that can be utilized, albeit not very user-friendly. The general structure of the desired application can be surmised to be the combination of the document segmentation system and the text summarization system, with the output of the first system being the input of the next, with pre-processing being applied to the segmented text between the two systems. The original input of the system should take into consideration both single document and multiple document situations. As such, the general structure of the application can be described in Figure 3‑1.

A diagram of a document segmentation

Description automatically generated

Figure 3‑1 - General structure of the application

Since many summarization techniques can be utilized in this situation, five were chosen to be used as the summarization methods. These methods would then be compared using specific benchmarks to determine which was most suitable for this specific use case. Amongst them, aside from LSA and TextRank, which is an extractive method, two previously mentioned pretrained machine learning models are utilized to achieve abstractive results, including Falcon AI’s Text Summarization and Facebook’s BART Large CNN.

Additionally, an improvement to the summarization method can be observed through the Pre-processing section, potentially improving both the efficiency of the system and the quality of the created summaries.

## System design

Although Figure 3‑1 depicts a multitude of steps involved in the process, the whole system can be condensed into two different parts, which are the segmentation subsystem, and the text summarization subsystem, which includes all steps after segmenting the documents. The first subsystem contains the data path and logic behind the segmenting of a document using GROBID. Following this, the output of the first subsystem is then preprocessed, summarized, and postprocessed in the second subsystem. The subsystem would then deliver the response to the corresponding request, completing all tasks required. The overall design of the system can be expressed through the component diagram in Figure 3‑2.

The system is heavily dependent on the use of Docker as a method to ensure system stability and interoperability. The usage of containers can decrease unforeseen errors caused by operating systems or package dependencies by having Dockerfiles predefining steps that are required to be completed before each container starts. Through these steps, both the version of the operating system and the project’s dependencies can be defined, ensuring that the system will work for as long as these packages are supported and available.

The entire system is defined through the use of Docker Compose since each container on its own would not be able to communicate with each other. While each subsystem can be initialized easily through Docker, the act of connecting these containers repeatedly for either debugging purposes or deployment is both inefficient and tedious, making the whole process error prone. As such, by utilizing Docker Compose, the connectivity and prerequisites between all related containers can be defined, allowing Docker to construct each container orderly through predefined steps.

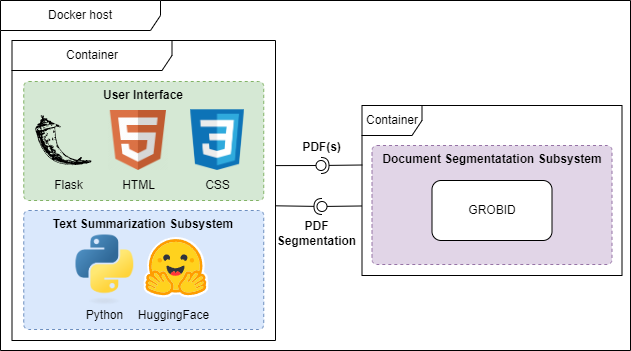


Figure 3‑2 – The component diagram of the system

### Data format

The use of Docker as the main method for cross-platform compatibility is inevitable, as the application needs to be flexible and adaptable to new system requirements. In addition, as each subsystem is designated as a different container, communication between each container is limited to HTTP requests. Due to this, the application must, therefore, be data-driven, controlling its logic through changes made to the data. As a result, the JSON file format was chosen as the common interface between each of the subsystems and processes.

Although the original output of the GROBID subsystem is an XML file, which can act as the interface for the overall system, a large amount of unnecessary data is included due to its highly generalized nature. Among the included data, tags containing header information and reference information, for instance, are of no use for the current application. Therefore, the truncation of said file is necessary to declutter and isolate the important information for further use. The resulting truncation is then reformatted into a JSON file due to the necessity of moving data between containers.

For the purposes of this application, a research paper can be divided into many sections, with each section being the header (i.e., Header 1. Introduction) of the paper. Each sub-header’s content (i.e., Header 1.1’s content) will be consolidated and appended to the parent header, creating a section. A section’s name, however, is defined only by the parent header. This process can be visualized in Figure 3‑3.

A diagram of a company

Description automatically generated

Figure 3‑3 – Data condensing process

Since each paper can be divided into sections based on the section’s content, the necessary information for each paper includes the name of the header and the content of each header. The name of the file is also included in the final summary JSON file due to the need for differentiation between different files when multiple PDFs are uploaded. However, the abstract section is included in the JSON file due to its usefulness for testing purposes. As such, the JSON file may contain the abstract section, depending on the current setup of the system, and the section list, which includes multiple headers and content.

### Document Segmentation Subsystem

As explained in the Literature Review chapter, GROBID has been chosen due to its high compatibility with the needs of the project. As a result, most classes and functionalities of this subsystem are for integrating the GROBID’s functionalities with the main application. One of its main purposes is to initialize and configure the basic GROBID settings, such as the GROBID home (the GROBID source location), changing the input PDF file into an appropriate format, and getting the result after parsing. Said result, which is in the form of an XML file, then became the input for the XMLParser class and YAMLParser class, creating the final output of the subsystem, which is a YAML file containing the segmentation of the provided PDF.

GROBID is set up as a separate Docker container in which a PDF file or a whole PDF can be used as an input to the system. Since GROBID provides prebuilt Docker containers that can help users build and use them on both Windows and Linux, building the entire system from source is not necessary, as you would be forced to use Linux to develop the entire system. Communicating with said container is simply done through the use of the provided APIs. Since wrapper libraries are provided to users for quick integration of their system with GROBID, the act of utilizing these APIs is trivialized.

### Text Summarization Subsystem

As the text summarization subsystem is not only responsible for the text summarizer but also both the pre-processing and post-processing of the input and output, this subsystem is further divided into three main modules, with each being pre-processing, summary, and post-processing correspondingly. Additionally, a wrapper module is used to encapsulate the whole subsystem, wiring everything together, and exposing the appropriate APIs and web interface.

#### Pre-processing module

In the pre-processing module, each section’s content from the segmented paper is first trimmed and normalized. During the trimming process, excess white space from both between, before, and after words is removed, cleaning the text syntactically. After said process, all capitalized characters are lowercased in the word normalization process, allowing the model to read the text more effectively. Each section and its name are then stored in a custom data object called Paper. Each paper contains the name of the currently processing PDFs and a list containing the multiple data objects called sections. A section is responsible for containing the section’s name and content. Utilizing the custom data object can help move data more effectively between each module.

A diagram of a diagram

Description automatically generated

Figure 3‑4 – Pre-processing module diagram

#### Text summarization module

Moving to the text summarization module, although many different pre-processing and summarization options are available, only a few options are included in the final product due to the speed at which these methods process the provided data. Especially noteworthy are the text summarization methods involving the use of pretrained machine learning models, as these methods not only consume a significant amount of resource while running but also during their start-up. Amongst the aforementioned models, only Facebook’s BART Large CNN and Falcon AI’s Text Summarization are suitable for running in production, while Stability AI’s Stable LM 2 1.6B can only be used for testing purposes. This can be observed more clearly through the execution time in the evaluation section. Therefore, a list of available options for summarizing text includes: TextRank, LSA, Text Summarization model, and BART Large CNN model. These methods are then connected to the overall system to produce the corresponding summaries.

The input text is simply passed into the system in the case of extractive summarization methods (LSA and TextRank). However, since all chosen subjective summarization methods use machine learning methods, a corresponding prompt needs to be constructed, instructing the model on what to do. The input would also need to be tokenized and calculated for the total number of tokens. This is due to some models having a limit on the number of tokens they can accept with each prompt, requiring the input to be truncated before being passed into the model. With BART Large CNN model, 1024 tokens are the limit, while for Stable LM 2 1.6B, the model can handle up to 2048 tokens. As for text summarization, it boasts a 2048 token limit despite being lightweight.

A diagram of a method

Description automatically generated

Figure 3‑5 – Text summarization module diagram

#### Post-processing module

Since the resulting summaries are formatted in different ways depending on the method by which they were produced, For example, Stable LM 2 1.6B’s output will start with “<|im\_end>\n<|endoftext|>”, which needs to be removed. As such, it is the post-processing module’s responsibility to reformat the resulting text according to the corresponding summarization method. Furthermore, since each section of a paper is passed through the summarization method individually, the module must recompile all these sections and add them under the correct section header for the result, which is in the form of a JSON file. In order to display the results on the web interface, the JSON result is required to be translated into HTML with the correct format and CSS style class, which would then be used to display the result through the web interface.

Amongst the results from each subtractive summarization model, only BART Large CNN model does not require any additional processing, the remaining 2 methods would require cleaning, as the Text Summarization model would have “Summarize the following segment into 1 sentence:” (which was part of the prompt) at the start of the result, and Stable LM 2 1.6B would start with “<|im\_end>\n<|endoftext|>”.

#### Wrapper module

As for the final module, which is the application wrapper, Flask is used as the main library to construct and host the website due to its simplicity and ease of use. The APIs are constructed as the main method for communication with the system. Of note are two APIs, including a method for uploading a file and a method for summarizing the provided files. Port 5000 is also available by default as a method of choice for the system to be more accessible through a simple Web UI. Overall, an overview of the system can be observed through Figure 3‑6.

A diagram of a process

Description automatically generated

Figure 3‑6 – The application’s activity diagram

## Utilizing Extractive summarization methods in Pre-processing

### Overview

During the normal pre-processing procedure for text, methods such as text normalization, whitespace trimming, etc. are frequently used. Although these methods can improve the input to the summarization system and clean up the input text, the remaining paragraphs can be exceedingly lengthy, spanning more than 1000 words each, which can include unnecessary information, as well as, possibly exceeding the token limit of the model. As such, filtering important sentences from the others can potentially improve the output of the whole system.

### Detailed Description

Extractive summarization methods such as LSA and TextRank have been decided to be used as methods for extracting the specified number of sentences to be passed into another summarization model. For this approach, the top five sentences from each section’s content are chosen for further summarization through the abstractive method.

Since both LSA and TextRank use different approaches to rank sentences, the result can change drastically. Although with the addition of this step, only subtractive summarization methods can utilize this method, applying the same method to itself does not make sense and would not yield a meaningful result. When comparing the process of Figure 3‑8 to Figure 3‑3, changes made to the original text can be seen clearly. In this specific case, the phrase “*Donec sed dui quis nunc lacinia maximus id vitae lectus.*” is determined to be the lowest ranking sentences amongst the condensed sentences as an example, causing the sentence to be filtered after being passed through the process. Through Figure 3‑7**Error! Reference source not found.**, the flow of the data in the pre-processing section can further be dissected, allowing for a clearer view of the data pipeline.

In the first step, which is to rank each sentence, each summarization has its own way to do so, either by calculating the distance between each sentence using Levensthein distance in the case of TextRank or by constructing a matrix of term frequency in the case of LSA. As such, the biggest difference between each method would be in this step since each method can contain multiple steps within themselves, causing each one to be different from one another. In theory, a ranking can be made using other methods besides the provided extractive methods, as the only requirement is providing a method to compare the sentences with each other, allowing for automatic ranking between each sentence. Some examples of this can be seen by utilizing an embedded AI model to vectorize each sentence and then comparing them. Moving on to the second step, the list provided in the first step is simply sorted, permitting the top sentences to be picked.

A diagram of a diagram

Description automatically generated

Figure 3‑7- Proposed pre-processing module diagram

Due to changes made to the data pipeline, it follows that changes must also be made to the overall design of the pre-processing subsystem. These changes to the layout can be seen in Figure 3‑7, in comparison with Figure 3‑4. Even though a new step was added to the process, no significant changes were made as the results from the segmentation system still required cleaning and compilation before becoming usable. Since the system is only utilized when the user chooses an abstractive method, the proposed pre-processing method will not be used if extractive methods are chosen. This would mean that in cases where TextRank and LSA are chosen as the main summarization methods, the ranking sentence step and top sentence selection step are ignored, stopping only at normalizing the text content.

A diagram with text and images

Description automatically generated with medium confidence

Figure 3‑8 – Pre-processing data processing

### Rationale

When implementing and executing the system while utilizing the abstractive summarization method, none of the available models would be practical enough to be used as an application practically due to their long inference times. This is especially true in cases where users have no access to a powerful GPU but can only make use of the computer's CPU. A possible solution to this issue is to set the system up as a cloud service, allowing for ease of access for users, and to scale the entire system horizontally to make use of powerful GPUs through cloud providers. Although this method is technically viable, the cost involved with running an AI model through cloud services can be tremendous, especially when powerful GPUs are involved.

As such, the second method, which is to allow users to host their own application node, is more preferable. This requires the system to somehow be able to optimize the time of inference, while maintaining a good enough result that a low-end machine can effectively utilize the application locally. Therefore, a hybrid approach in which extractive summarization methods are utilized to reduce the provided input, which in turn would reduce the amount of time required to process the summaries.

Although the method makes sense in theory, it is unknown whether these changes to the data pipeline can improve the results in terms of their effectiveness. This is due to the possibility of preprocessed text losing important information from the process instead of filtering unnecessary ones.

Since each method executes both methods in different ways, the combination of each method with an abstractive summarization method must be examined and evaluated. Effectively, after implementing this change, the entire system would execute the summarization process twice, with the first pass going through an extractive summarization process while producing five sentences. These five sentences would then be passed through the extractive summarization system, finalizing the result of the system. Presumably, by reducing the input to the abstractive system, the provided prompt would become shorter, which would ultimately reduce the time needed for the model to infer the result from the input text. Additionally, it can potentially increase the overall quality of the resulting prompt, which may improve in comparison to its non-pre-processed counterpart.

## User interface

Due to the system’s structure being constructed as a composition of Docker modules, the project lent itself well to using a Web User Interface as its default method of presenting information to users. Since cross-compatibility and flexibility have been some of the project’s main concerns since its conception, utilizing a web browser as the method of choice for communicating with the UI. The design and implementation of the UI can be seen in Figure 3‑9.

By default, the home directory of the website would direct the user to the Web UI interface of the application, The UI includes simple but important settings that can help with configuring the whole summarization process, which include the choice of two important aspects of the system. The choice of which can greatly change the length, quality of the output and the total time it takes to summarize one paper.

The first option is closely related to the previously proposed method of pre-processing the provided condensed and summarized segment. The user is allowed to choose one of three available pre-processing options, including “**None**” (which skips the use of extractive summarization in the pre-processing step), “**TextRank**”, and “**Latent Semantic Analysis**”. By default, “**None**” is chosen in case user does not choose any method.

As for the summarization method, this option is controlled through the use of the second radio option. Since the Stable LM 2 1.6B model is unsuitable for production environment due to reasons previously stated, only the **Text Summarization model** and **the BART Large CNN model** are available. Along with the subtractive model, both **TextRank** and **LSA** are available as choices for users.

The user would then be required to choose a file that would be processed. This action can either be done by dragging and dropping the file into the designated zone or by simply clicking on the zone, allowing the user to choose a file from the file explorer. In order to prevent unintended consequences from users’ actions, some simple failsafes are implemented, including checking the file extension for any combination of the phrase “.pdf”, filtering the file’s name from including inappropriate keywords for certain operating systems through the provided *secure\_filename* function from Flask, and providing extensive error messages in various other cases.

A screenshot of a web page

Description automatically generated

Figure 3‑9– Web user interface

# IMPLEMENT AND RESULTS

## Overview

This chapter provides explanations and descriptions of the work that has been done. Amongst them, most of the work can be divided into two distinct parts, which are implementing document segmentation using GROBID and developing the text summarization capabilities along with the multitude of summarization methods. Since the whole system is encapsulated in a cluster of Docker nodes, configured through the use of Docker Compose, the whole system can be reproduced easily.

## Implementation

Some code snippets explaining what has been discussed in Chapter 3 for each subsystem can be found in the following part of this chapter. By providing these code sections, the method in which the application is implemented can be better understood.

### Document Segmentation

As GROBID is a machine learning approach to the segmentation problem, its initialization requires the initialization of the GROBID container. The code snippet in Figure 4‑1 is the function through which the initialization is made.

Since this method would find all PDF files available in the specified UPLOAD FOLDER, no additional set up is required except for having to upload the corresponding files to the correct folder. Toward that end, users can directly upload the PDF file by submitting it from the Web UI or by utilizing the folder-uploading request, an example of which can be found inFigure 4‑2.

After the file content as well as its name are checked sufficiently, including the file extension, the content of the file, and the filename. Additionally, the *secure\_filename* function also provides a method to adjust the file name so that it does not violate any rules regarding the naming scheme of files on any operating system. The file is then saved to the corresponding folder, awaiting further usage.

async def **parse\_pdf**() -> **bool**:

    """

    Connect to the GROBID and summarize the PDF in the folder.

    """

    with **app**.app.**app\_context**():

        with **concurrent**.**futures**.**ThreadPoolExecutor**(max\_workers=1):

            try:

                client = **GrobidClient**(config\_path=GROBID\_CONFIG\_PATH)

                client.**process**(

                    "processFulltextDocument",

                    UPLOAD\_FOLDER,

                    output=SEGMENT\_FOLDER,

                    consolidate\_citations=False,

                    tei\_coordinates=False,

                    verbose=True

                )

            except:

                return False

    return True

Figure 4‑1 – GROBID initialization code snippet

### Text summarization

As both LSA and TextRank are used during the development process, implementation of both systems is available. Even though TextRank was implemented through the use of a library, its implementation is worth mentioning as some parameters and its choice have effects on the result of the summary. LSA, however, does not have a library that supports it from the start, so it needs to be implemented step by step. As for the pretrained models, HuggingFace [27] was utilized as the library of choice for implementation due to the large number of tools, support, and models available.

**@app.route**("/upload", methods=['POST'])

def **upload**():

    if (request.method != 'POST'):

        return "No GET method", 404

    if 'files' not in request.files:

        return "No 'files' header in payload.", 404

    pdf\_file = request.files['files')

    if pdf\_file.filename == '':

        return "File has no name.", 404

    if not pdf\_file:

        return "File does not exist.", 404

    if not **allowed\_file**(pdf\_file.filename):

        return "File does not end with .pdf", 404

    filename = **secure\_filename**(pdf\_file.filename)

    pdf\_file.**save**(**os**.path.**join**(app.config['UPLOAD\_FOLDER'], filename))

    return 'Successfully send files', 200

Figure 4‑2 – PDF-uploading method

#### LSA

The LSA summarization approach goes through seven steps in total, including tokenizing, NGram generation, stop-word filtering, word frequency sorting, sentence detection, word searching, and finally summarization. While the first 3 steps are part of the *\_create\_dictionary* function, the remaining steps are distributed among the remaining function calls due to their complexity. The summary is then generated by using the output from the steps above. This can be seen in Figure 4‑3.

def **lsa** (text:**str**, sent\_num:**int**=SENT\_NUM) -> **str**:

    if(**len**(text) == 0):

        return ""

    dictionary = **\_create\_dictionary**(text)

    sentences = **sent\_tokenize**(text)

    matrix = **\_create\_matrix**(text, dictionary)

    matrix = **\_compute\_term\_frequency**(matrix)

    u, sigma, v = **singular\_value\_decomposition**(matrix, full\_matrices=False)

    ranks = **iter**(**\_compute\_ranks**(sigma, v))

    result = **\_get\_best\_sentences**(

        sentences,

        sent\_num,

        lambda s: **next**(ranks)

    )

    result\_str = ''

    for sentence in result:

        result\_str += sentence

    return result\_str

Figure 4‑3 – LSA Implementation

The summarization process above works by looping through each summary sentence, conducting word searching on it, and storing the results in a list. The summary is then concatenated and constructed from said list.

#### TextRank

As mentioned, the TextRank implementation is made using a library called *summa*, this can be seen in Figure 4‑4, where the summarization function is defined.

def **summarize\_text**(text:**str**, sent\_num:**int**=SENT\_NUM) -> **str**:

    return **summarize**(

        text = text,

        words = sent\_num \* (**\_get\_max\_length\_sentence**(text) + 5),

        additional\_stopwords= **summary**.**get\_stop\_word\_list**()

    )

Figure 4‑4 – TextRank summarization function

In said function, “text” refers to each PDF segment that the user wants to summarize. “words” is the upper word limit of the resulting summary, and “additional\_stopwords” refers to the list of words that need to be filtered out before processing the summary. In order to control the number of sentences the resulting summary will have, the length of the longest sentence in the provided text must be calculated, which is the responsibility of the \_get\_max\_length\_sentence function. Utilizing this, only the text that needs to be summarized and the number of sentences need to be passed in as parameters.

#### Pretrained models

Even though small differences exist when implementing different models with regards to how each one is initialized and utilized, a familiar structure can be distilled. Due to loading a model requiring an extended amount of time, it is preloaded and cached, allowing for subsequent usage requiring less memory and time to complete a task. An example of preloading the model can be found inFigure 4‑5.

async def **preload\_stable\_lm\_chat\_1\_6b**():

    global tokenizer

    global model

    tokenizer = **AutoTokenizer**.**from\_pretrained**(

        'stabilityai/stablelm-2-1\_6b-chat'

   )

    model = **AutoModelForCausalLM**.**from\_pretrained**(

        'stabilityai/stablelm-2-1\_6b-chat',

        device\_map="auto",

    )

Figure 4‑5 – Model preloading

The text is then passed into the chosen model and further processed to be suitable for the required text generation. The input is first passed into a prompt constructor, where it will instruct the model for the required text generation. The prompt would then be tokenized in some models, such as Stable LM 2 1.6B, as per the requirements of each model. Finally, the text is passed into the model, where it is processed, and the result can be obtained. The process can be seen in Figure 4‑6 in the case of Stable LM 2 1.6B.

async def **stable\_lm\_chat\_1\_6b**(content:**str**) -> **str**:

    prompt = [{'role': 'user', 'content': **prompt\_constructor**(content)}]

    inputs = tokenizer.**apply\_chat\_template**(

        prompt,

        add\_generation\_prompt=True,

        return\_tensors='pt'

    )

    tokens = model.generate(

        inputs.**to**(model.device),

        max\_new\_tokens=**get\_max\_length**(content),

        temperature=0.01,

        do\_sample=True

    )

    output = tokenizer.**decode**(

        tokens[:, inputs.shape[-1]:][0], skip\_special\_tokens=False)

    return output.**rstrip**("<|im\_end|>\n<|endoftext|>")

Figure 4‑6 – Model text generation

## Results

The results from the process of the entire system can be condensed into two different JSON files, with the first being the document segmentation result and the second being the summary. As an example, one research paper has been chosen. As a result of the document segmentation being the content of the entire paper, only the first header will be showcased in Figure 4‑7. Since many different methods of summarization were used, only LSA and TextRank are shown as examples of the data format, which can be seen in Figure 4‑8 andFigure 4‑9.

{

  "name": "Hansen\_et\_al.\_-\_2024\_-\_Productivity\_and\_quality-adjusted\_life\_years\_QALY.grobid.tei.xml",

  "segments": [

    {

      "header": "Introduction",

      "content": "few aspects concern human beings more than health. but resources are scarce and, as we face demographic changes, with increased demand from retirees and a constrained labour market due to shrinking working age share of the population, there is a pressing need to protect the health and productivity of the economically active population. therefore, critical decisions on health care interventions, as well as occupational health and safety policies, have to be made constantly. the evidence from clinical trials and observational studies, in addition to assessments about the productivity consequences, are crucial to make those decisions. the purpose of this paper is to develop a unified framework for the measurement and valuation of outcomes of such programmes and policies.it is widely accepted that the health benefit a patient derives from a particular health care intervention can be defined according to two natural dimensions: quality of life and quantity of life.pioneered in multiattribute utility theory the axiomatic foundations of the so-called quality-adjusted life years (in short, qalys), which offer a straightforward procedure to combine the two natural dimensions. together with the so-called disability-adjusted life years (in short, dalys), a primary focus of the landmark global burden of disease studies, they are arguably the most frequently employed methodologies in the evaluation of health outcomes nowadays (e.g.,.an alternative to qalys is the so-called productivity-adjusted life years (in short, palys), which are calculated by multiplying a productivity index by years lived. the productivity index ranges from 0 (completely unproductive) to 1 (completely productive), and may take into consideration factors such as absence from work due to ill health (absenteeism), reduced productivity while at work (presenteeism) and premature exit from the workforce (e.g.,.economic evaluation of policies to improve occupational health and safety is one field of research where productivity outcome measures following the broader paly idea are applied extensively (e.g.,. similar to standard health economic evaluation, this involves measuring costs and effects of working environment interventions except that many studies in this field concentrate on measuring changes in productivity as the most important intervention effect while leaving health effects out (e.g.,. productivity effects of interventions are often operationalised and measured for each individual employee as sickness absence and reduced productivity while the employees are at work. many studies are performed as a cost-benefit analysis from an employer's perspective where the purpose of the analysis is to assess if the costs of an intervention can be covered entirely or to a degree through the value of improved productivity. however, from a societal perspective, it seems too narrow to focus exclusively on productivity effects, as working environment interventions will often have wider benefits including effects on employee health. now, productivity effects are also often taken into account in the evaluation of health care itself (not just workplace safety). the traditional approach has been to net indirect earnings effects out of the cost of treatment (on the basis of the present value of the additional stream of lifetime income for an individual, possibly involving realistic situations such as involuntary unemployment) and keep the qaly outcome measure …"

    },…

}

Figure 4‑7 – Segmentation result

{

  "name": "Hansen\_et\_al.\_-\_2024\_-\_Productivity\_and\_quality-adjusted\_life\_years\_QALY.grobid.tei.xml",

  "segments": [

    {

      "header": "Introduction",

      "content": "therein, classical evaluation functions, such as the (time linear) qaly and hye (acronym for healthy years equivalent) measures are characterized axiomatically.our generalization of that framework allows us to characterize not only those evaluation functions but also others including a concern for productivity, such as the (time linear) paly evaluation function, and also appealing hybrids between qalys and palys.we shall refer to the simplest one as productivity-andquality-adjusted life years (in short, pqalys)."

    },…

}

Figure 4‑8 – TextRank summarization result

{

  "id": "Hansen\_e",

  "name": "Hansen\_et\_al.\_-\_2024\_-\_Productivity\_and\_quality-adjusted\_life\_years\_QALY.grobid.tei.xml",

  "segments": [

    {

      "header": "Introduction",

      "content": "we shall also characterize even more general evaluations functions, around the notion of healthy productive years equivalent we introduce in this setting.we conclude this introduction stressing that our model treats health and productivity as different individual attributes."

    },…

}

Figure 4‑9 – LSA summarization result

# DISCUSSION AND EVALUATION

## Evaluation

Text segmentation utilized GROBID, which is a tool that has been used and benchmarked through multiple sources ([28], [29], [30], [31]). As such, the main focus of the evaluation section would be on the summarization method.

Evaluating and comparing the chosen summarization methods an important task so as to choose the appropriate sentences for the product to be adaptable for a range of topics that can be covered by a research paper. Additionally, the provided summarization methods must be efficient enough to be able to be executed by an average user. As such, additional information such as the evaluation method, the dataset, the specification of the test machine, and the evaluation results will be included in the following sections.

### Evaluation methods

Due to text summarization being highly dependent on the perspective and knowledge of the reader, As such, having testers with the appropriate knowledge to evaluate the result is the most desirable outcome, as this can realistically reflect the opinion of normal readers. Otherwise, a dataset containing a reference summary result can also be used to compare the generated text of the system being tested.

However, due to the high specificity of the current summarization use case, we were unable to find any dataset that contained the necessary referenced summary. Since most open-sourced datasets focus on summarizing the entire paper’s content into a small paragraph, this could not be applied for this current use case since the PDF is segmented and each segment is further summarized. Additionally, many datasets were rejected due to their being based on sources that were not research papers, including newspapers and books. This can be seen among the list of frequently used datasets for this purpose [5] as most of them are from the news and book domains.

As such, the only available option is to utilize a statistical calculation in order to determine the value of each summary. The calculation of choice was ROUGE-1, ROUGE-2, and ROUGE-L [32]. Although some traditional measures such as Recall (Equation 5‑1), Precision (Equation 5‑2), and F-Measure (Equation 5‑3) can be used to calculate quantitatively how much of the summary has recaptured the context of the original text and how much of that context is relevant, ROUGE measure provides more granularity as it has the benefits of the simpler measures, but also applies it to the n-gram and longest matching sequence. Using these measures, the process of evaluating text summarization can be done automatically, allowing for faster feedback and improvement to the system.

Equation 5‑1 – Precision equation

Equation 5‑2 – Recall equation

Equation 5‑3 – F-Measure equation

ROUGE measures build upon the existing methods of Recall, Precision, and F-Measure. In the case of ROUGE-1 and ROUGE-2, Recall and Precision for the unigram and bigram are calculated, respectively. Afterwards, F-Measure is calculated, resulting in the final product. As for ROUGE-L, instead of N-Gram, the longest common subsequence is used to calculate Recall and Precision. From which, the corresponding F-Measure is the result of ROUGE-L measure. In essence, ROUGE measures make use of F-Measure and add small additional improvements to help account for many situations.

### Dataset

In order to evaluate the system, a random set, including 10 research papers in PDF format relating to multiple topics (medicine, astrophysics, machine learning, etc.). With an average page number of 26.3, detailed information regarding these papers can be found in Table 5‑1.

|  |  |  |
| --- | --- | --- |
| **Category** | **Paper** | **Page No.** |
| Astrophysics | Accretion and Uneven Depletion of the Main Asteroid Belt [33] | 23 |
| General Economics | Karma: An Experimental Study [34] | 17 |
| Theoretical Economics | Productivity and quality-adjusted life years: QALYs, PALYs and beyond [35] | 41 |
| Artificial Intelligence | AI and the Problem of Knowledge Collapse [36] | 16 |
| Quantitative Biology | The rules of multiplayer cooperation in networks of communities [37] | 28 |
| Machine Learning | Mixture-of-Depths: Dynamically allocating compute in transformer-based language models [38] | 14 |
| Statistics | Sequential Monte Carlo Bandits [39] | 66 |
| Computer Science | History Trees and Their Applications [40] | 20 |
| Quantitative Finance | Portfolio optimization: bridging the gap between theory and practice [41] | 33 |
| Electrical and Engineering | Source Tracing of Audio Deepfake Systems [42] | 5 |

Table 5‑1 - Papers chosen for Evaluation dataset

These papers were all randomly chosen by browsing through Arvix, finding different topics, and choosing a paper at random. By having a more diversified list of PDFs, the dataset can be less biased overall. These papers are first segmented through GROBID, then condensed by removing sub-headers. The condensed content would then be summarized individually, resulting in a reference version of the summary of each paper.

### Evaluation results and Environment Settings

The machine being used to evaluate the system is currently an AMD RYZEN 5 5600 with 16 GB of RAM. After running ROUGE-1, ROUGE-2, and ROUGE-L measures, the results are tabulated inTable 5‑2.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Pre-processing method | Summarization method | **ROUGE-1** | **ROUGE-2** | **ROUGE-L** |
| None | **TextRank** | 0.427682 | 0.115167 | 0.168592 |
| None | **LSA** | 0.472785 | 0.091069 | 0.150404 |
| None | **Falcon AI’s Text Summarization** | 0.459338 | 0.114218 | 0.202763 |
| None | **Facebook’s BART Large CNN** | 0.477966 | 0.131873 | 0.223863 |
| TextRank | **Falcon AI’s Text Summarization** | 0.519981 | 0.176081 | 0.222811 |
| TextRank | **Facebook’s BART Large CNN** | **0.560178** | **0.195771** | **0.243939** |
| LSA | **Falcon AI’s Text Summarization** | 0.462003 | 0.106761 | 0.174480 |
| LSA | **Facebook’s BART Large CNN** | 0.519516 | 0.126529 | 0.194028 |
| None | **Stability AI’s Stable LM 2 1.6B** | 0.500416 | 0.188832 | 0.264923 |
| TextRank | **Stability AI’s Stable LM 2 1.6B** | **0.571027** | **0.248053** | **0.352087** |
| LSA | **Stability AI’s Stable LM 2 1.6B** | 0.488266 | 0.164300 | 0.247764 |

Table 5‑2 - ROUGE-1, ROUGE-2, and ROUGE-L evaluation n results.

Since **Stable LM 2 1.6B** is selected as an example of some of the latest models, it is not surprising to see that its performance is ranked among the top of the benchmark results. Interestingly, while using TextRank as a pre-processing method increases the performance of the model on all measures, using LSA for the same purpose would decrease the performance on all testing measurements.

Amongst the evaluation results of the remaining methods, the combination of having TextRank as the pre-processing method and using the resulting sentences to be summarized by Facebook’s BART Large CNN model obtained the most positive result, being the top ROUGE-1, ROUGE-2, and ROUGE-L measure. The combination between TextRank and Falcon AI’s Text Summarization model also yields positive results since it claims 2nd place amongst the ROUGE-2 and ROUGE-L measures. Noticeably, all summarization methods being pre-processed by the use of an extractive summarization model would increase the evaluation results over the executing just base summarization method.

Additionally, in order to measure the efficiency of each method, the total time required to generate the summaries for ten chosen PDFs was documented inTable 5‑3.

|  |  |  |  |
| --- | --- | --- | --- |
| Summarization method | **Pre-processing method** | | |
| **None** | **TextRank** | **LSA** |
| **TextRank** | 0.885442 | - | - |
| **LSA** | 8.959388 | - | - |
| **Falcon AI’s Text Summarization** | 571.973681 | 318.815027 | **288.749598** |
| **Facebook’s BART Large CNN** | 828.024041 | 719.341524 | **681.081772** |
| **Stability AI’s Stable LM 2 1.6B** | 11332.362937 | **6656.221096** | 7058.812489 |

Table 5‑3 – Summarization time (in second) of each combination

Two observations can be obtained from the data above, with the first being that passing the provided text through a layer of pre-processing can significantly reduce the total text generation time across all summarization methods, aside from the two extractive summarization methods, which serve as an example. In the case of Falcon AI’s text summarization, a 43% decrease in execution time was observed for the TextRank pre-processing and a 49% decrease when using LSA. However, time saved does not appear to be consistent between methods, with only a peak of 17% in the case of Facebook’s BART Large CNN model and 41% in the case of Stable LM 2 1.6B. Another observation is that while LSA on its own requires more time than TextRank to complete the task, using it as the pre-processing method will save more time in comparison to TextRank, with the exception of Stable LM 2 1.6B. The reason for the reduction in execution time is possibly due to the input being truncated to only maintain 5 sentences. This cuts down on the time needed to process the input for each model, allowing them to finish significantly quicker.

Conclusively, using an extractive summarization method for pre-processing resulted in a decrease in summarization time. Amongst these, aside from the extractive models, the Text Summarization model finished executing the quickest, followed closely by BART Large CNN model. As Stable LM 2 1.6B takes hours to complete on average, it is not suitable for any application that requires low processing time. When considering the performance of each model, BART Large CNN model remains the summarization method of choice for this task, with Text Summarization being in second place and both models’ input being processed by TextRank. Overall, the system of choice for the current application would be GROBID segmenting the PDF file, TextRank choosing the important sentences, and BART Large CNN model summarizing the sentences.

# CONCLUSION AND FUTURE WORK

## Conclusion

Although the project can be considered functional, much is left to be desired as the project does not consider much of the user experience. Additionally, even though pre-trained models were used, fine-tuning the model to fit with the current use case was not possible due to limited time and resources. Overall, the project can be considered a steppingstone for future improvements.

## Future work

Ideas for improving the current work that can be done in the future:

1. Fine-tuning the model may allow for better summarization results, which can further improve the evaluation metrics.
2. A self-developed model can be considered a simple model that is tailored to the current task and can improve both the application’s efficiency and output if done correctly.

Additional possible evaluation metrics:

1. Alternating the number of sentences extracted during the pre-processing methods that utilize the extractive summarization method (currently extracting 5 sentences) to a variety of different paragraph lengths to effectively determine the sentence number’s effect on the summarization results.
2. Utilizing a larger open-source dataset containing paragraphs from research papers as an additional evaluation metric in tandem with human generated summaries that are currently being used.

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# APPENDIX

The full result from the Segmentation process

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life.pioneered in multiattribute utility theory the axiomatic foundations of the so-called quality-adjusted life years (in short, qalys), which offer a straightforward procedure to combine the two natural dimensions. together with the so-called disability-adjusted life years (in short, dalys), a primary focus of the landmark global burden of disease studies, they are arguably the most frequently employed methodologies in the evaluation of health outcomes nowadays (e.g.,.an alternative to qalys is the so-called productivity-adjusted life years (in short, palys), which are calculated by multiplying a productivity index by years lived. the productivity index ranges from 0 (completely unproductive) to 1 (completely productive), and may take into consideration factors such as absence from work due to ill health (absenteeism), reduced productivity while at work (presenteeism) and premature exit from the workforce (e.g.,.economic evaluation of policies to improve occupational health and safety is one field of research where productivity outcome measures following the broader paly idea are applied extensively (e.g.,. similar to standard health economic evaluation, this involves measuring costs and effects of working environment interventions except that many studies in this field concentrate on measuring changes in productivity as the most important intervention effect while leaving health effects out (e.g.,. productivity effects of interventions are often operationalised and measured for each individual employee as sickness absence and reduced productivity while the employees are at work. many studies are performed as a cost-benefit analysis from an employer's perspective where the purpose of the analysis is to assess if the costs of an intervention can be covered entirely or to a degree through the value of improved productivity. however, from a societal perspective, it seems too narrow to focus exclusively on productivity effects, as working environment interventions will often have wider benefits including effects on employee health. now, productivity effects are also often taken into account in the evaluation of health care itself (not just workplace safety). the traditional approach has been to net indirect earnings effects out of the cost of treatment (on the basis of the present value of the additional stream of lifetime income for an individual, possibly involving realistic situations such as involuntary unemployment) and keep the qaly outcome measure (e.g.,. another more recent approach, which is growing rapidly to the extent of becoming a new development in health economic evaluation, is precisely to switch from qalys or dalys to palys as the outcome measure. a sizable number of healthcare applications are lately endorsing this approach (see, for instance,and the references cited therein). nevertheless, palys as an outcome measure lack a proper theoretical justification. an aim of this paper is to fill that gap in this emerging literature by providing axiomatic foundations of this newly proposed outcome measure. furthermore, rather than replacing qalys by palys, one could conceivably think about compromising between both, as they can each be seen as partial measures to evaluate outcomes of health care interventions or occupational health and safety policies. qalys dismiss productivity, whereas palys dismiss quality-of-life (morbidity) concerns. more general evaluation functions encompassing both concerns would be more complete and thus more appropriate from a societal perspective. we also provide in this paper axiomatic foundations for evaluation functions allowing for compromises among qalys and palys within a unified framework. in order to do that, we present a stylized model in which individuals are described by profiles of (representative) health states, productivity and lifetime spans. the aim is to derive measures to evaluate the distribution of those profiles in a population. and to do so by means of specific combinations of axioms that characterize different evaluation measures.our approach builds upon the framework introduced in hougaard et al.. therein, classical evaluation functions, such as the (time linear) qaly and hye (acronym for healthy years equivalent) measures are characterized axiomatically.our generalization of that framework allows us to characterize not only those evaluation functions but also others including a concern for productivity, such as the (time linear) paly evaluation function, and also appealing hybrids between qalys and palys.we shall refer to the simplest one as productivity-andquality-adjusted life years (in short, pqalys). we shall characterize other hybrids as well, combining qalys with palys or pqalys, in an additive way. we shall also characterize even more general evaluations functions, around the notion of healthy productive years equivalent we introduce in this setting.we conclude this introduction stressing that our model treats health and productivity as different individual attributes. in doing so, we obviously depart from the literature that considers only one of them, but also from the simplistic assumption that both concepts are perfectly correlated (which would allow to use a reduced model). the precise relationship between health and productivity is complex and the anticipated correlation might actually be positive or negative, depending on the viewpoint. for instance,reviews a literature which suggests that \"chronic and acute physical and mental conditions, as well as health-related behaviours, explain a significant portion of sickness absence (a proxy for productivity)\". on the other hand,recently studied the effect of rising workload on health and found that it wears down an individual worker's health capital, leading to an increased likelihood of sickness. this is also in line with the classical human capital model of the demand for health (e.g.,, which concludes that health does not affect productivity (it affects an individual's annual salary but not the individual's hourly wage).the rest of the paper is organized as follows. in section 2, we introduce the framework and the basic common axioms that all our evaluation functions will satisfy. in section 3, we characterize the focal (and somewhat polar) evaluation functions qalys and palys. in section 4, we characterize classes of evaluation functions which compromise among the previous two. in section 5, we characterize more general functional forms, that evolve around the notion of healthy productive years equivalent. in section 6, we discuss our contribution with a special emphasis on the choice among the different evaluation functions we characterize. finally, in section 7, we provide some concluding remarks providing further connections to related literature and pointing out possible extensions of our work. for a smooth passage, we defer all proofs to the appendix."

    },

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measure could be chosen that reflects the value of the work contributed by the individuals, as would (very roughly) be the case if measured by e.g., (relative) earnings (e.g.,).however, our primary interpretation of productivity will be the broad one, as taking into account the monetary value of individuals (to society) is ethically questionable, as well as potentially more difficult to measure.finally, there are two plausible interpretations of time in our model. on the one hand, it could be identifying the individual total lifetime. on the other hand, it could be identifying incremental individual lifetime from a given status quo up to the end of life or retirement.let d = (d 1 , ..., d n ) denote a distribution of individual profiles, as described above, and let d denote the set of possible distributions. we now give an example in which two hypothetical distributions are presented. we shall return to this example later in the text several times to illustrate how these two hypothetical distributions can be (relatively) evaluated, by means of various evaluation functions we consider.example 1 consider the following two distributions, involving five individuals each (that could be interpreted as representative agents of five different groups).in the first distribution (d ∆ ), all individuals are experiencing full health. the first one is also experiencing maximum productivity as well as forty years of lifetime (until retirement, or the end of life), i.e., d ∆ 1 = (a \* , 1, 40). the second individual is experiencing 50% of maximum productivity and forty years of lifetime, i.e., d ∆ 2 = (a \* , 0.5, 40). the third individual is experiencing zero productivity and forty years of lifetime, i.e., d ∆ 3 = (a \* , 0, 40). the fourth individual is experiencing 50% of maximum productivity and ten years of lifetime, i.e., d ∆ 4 = (a \* , 0.5, 10). the last individual is experiencing zero productivity and lifetime, i.e., d ∆ 5 = (a \* , 0, 0). in the second distribution (d λ ), the first individual is also experiencing full health and maximum productivity as well as forty years of lifetime, i.e.,. the remaining individuals are experiencing a worse health state, which we denote by a.the second individual is also experiencing maximum productivity and forty years of lifetime, i.e., d λ 2 = (a, 1, 40). the third individual is experiencing 50% of maximum productivity and forty years of lifetime, i.e., e : d → r. we say that e represents ifnote that if e represents then any strictly increasing transformation of e would also do so.an evaluation function e may be interpreted as an effect measure if it is used for the economic evaluation of health care or working environment interventions.in what follows, we present some basic axioms for social preferences in the current context, that will be common to all the evaluation functions we consider in this paper.in this section, we present a set of seven axioms that forms the necessary conditions for the theorems presented in the remaining sections of this paper. these are termed the common axioms. the axioms reflect basic principles adapted to our framework that are widely accepted in economics. in the following sections, additional axioms are presented, which together with the common axioms close the characterizations of the evaluation functions we highlight.the first three common axioms apply to all three attributes in the same way; whereas the latter four common axioms introduce some conditions on time which distinguish it from the other two attributes.the first axiom, anonymity, reflects the principle of impartiality, with a long tradition in the theory of justice (e.g.,. it says that the identities of individuals do not matter in the evaluation of distributions. formally, permuting triples does not alter preferences. the second axiom, separability, also has a long tradition of use in models of welfare economics (e.g.,. it says that if the profiles change only for a subgroup of individuals, then the relative evaluation of the two distributions should only depend on this subgroup.the third axiom, continuity, is the adaptation of a standard operational condition to our context. it says that small changes in productivity or life years should only produce small changes in the evaluation of the distribution.cont: let d, d ′ ∈ d, and d (k) be a sequence such that for each i ∈ n, di , twe then move to the second group of common axioms. first, the social zero condition, which is reminiscent of a well-known condition for individual utility functions on health (e.g.,. it says that if an individual has zero lifetime, then the health state and productivity of that individual does not influence the evaluation of the distribution.zero: for each d ∈ d and each i ∈ n such that t i = 0, and each a ′ i ∈ a, and each the following axiom, lifetime monotonicity at full health and productivity, says that if an individual enjoys full health and maximum productivity then increasing life years is strictly better.lmfhp: for each d ∈ d and each i ∈ n, such that (a i , p i ) = (a \* , 1) and eachwhere q : a → [0, 1] is a function satisfying 0 ≤ q(a i ) ≤ q(a \* ) = 1, for each a i ∈ a.the unweighted aggregation of individual qalys, as specified in, is the preferred evaluation function in the majority of cost-utility analyses performed for health care interventions (e.g.,.this evaluation function ignores productivity. more precisely, it satisfies the following axiom, productivity independence, which states that for a fixed health state and lifetime, the productivity is irrelevant for the evaluation of the distribution.it also satisfies the time invariance at common health and full productivity axiom, which states that for two individuals at common health and maximum productivity, extra life years are interchangeable. that is, it does not matter to the social planner which individual (among those with common health and maximum productivity) gets extra life years.tichfp: for each d ∈ d, each pair i, j ∈ n with a i = a j = a and p i = p j = 1, and eachour first result states the qaly evaluation function is characterized by the combination of the previous two axioms and the common axioms. 10   theorem 1 the following statements are equivalent:1. is represented by a qaly evaluation function (1).a possible interpretation of theorem 1 could be a situation where a social planner decides to evaluate and prioritise among a set of interventions using the qaly evaluation function. this social planner will thus agree to the value choices that productivity changes among individuals do not matter for the evaluation of interventions (axiom pi) and that an extension of life of a specific length of any two individuals is of equal value as long as they enjoy a common health state and maximum productivity (axiom tichfp). in addition, the social planner subscribes to a set of assumptions that are largely technical and uncontroversial (thea counterpart axiom of productivity independence is health independence, which states that, for fixed productivity and lifetime, the health state of an individual is irrelevant for the evaluation.and, likewise, a counterpart of time invariance at common health and full productivity is time invariance at full health and common productivity, which states that for two individuals at full health and common productivity, it does not matter to the social planner who receives the extra life years. 11 as all theorems in this paper require the common axioms, these will not be mentioned again in the interpretations of the remaining theorems.tifhcp: for each d ∈ d, each pair i, j ∈ n with a i = a j = a \* and p i = p j = p, and eachas the next result states, if the previous two axioms replace their counterparts at theorem 1, we characterize the following generalized paly evaluation function, which evaluates distributions by means of the aggregation of individual palys in society, when submitted first to a continuous function (v). formally,wherethe following statements are equivalent:1. is represented by a generalized paly evaluation function (2).the generalized paly evaluation function is a counterpart of the qaly evaluation function.as such, neither the v function nor the q function (in their respective functional forms) has a monotonic structure. this makes sense in the latter case because the domain of health statesa does not have a mathematical structure. but the domain of productivity levels is naturally ordered and, therefore, it would make sense to impose v a non-decreasing structure. the following axiom will guarantee such a feature as a byproduct.the axiom productivity invariance at full health and common time states that, for any two individuals with common lifetime and full health, it makes no difference who gains in productivity.pifhct: for each d ∈ d, each pair i, j ∈ n with a i = a j = a \* and t i = t j = t, and eachas the next result states, adding this axiom to those in theorem 2 we characterize the affine paly evaluation function, which evaluates distributions by means of the aggregation of individual palys in society, when submitted first to an affine and non-decreasing function.formally,where α ∈ [0, 1].the following statements are equivalent:1. is represented by an affine paly evaluation function (3).satisfies common, hi, tifhcp, and pifhct.the previous families are obvious generalizations of the focal linear paly evaluation function, which evaluates distributions by means of the unweighted aggregation of individual palys in society, or, in other words, by the weighted (through productivity levels) aggregate time span the distribution yields. formally,the unweighted aggregation of individual palys as specified in (this evaluation function is characterized when we add the time independence for unproductive individuals axiom, which states that if an individual has zero productivity, then the lifetime of that individual does not influence the evaluation of the distribution.tiup: for each d ∈ d and each i ∈ n such that p i = 0, and eachthe following statements are equivalent:1. is represented by a paly evaluation function (4).satisfies common, hi, tifhcp, pifhct, and tiup.according to theorem 4, a social planner wishing to conduct an economic evaluation of working environment interventions using the paly evaluation function (4) will also hold a number of specific values in the process of priority setting. these value choices include, for example, that changes in health among individuals following an intervention (axiom hi) and that increases in lifetime among unproductive individuals (axiom tiup) both have no influence on the choice of intervention.we conclude this section applying the evaluation functions characterized in this section to the distributions from example 1. more precisely, we summarize the computations in the next table. we infer from there that the first distribution is preferred from the viewpoint of qalys, whereas the second distribution is preferred from the viewpoint of the palys-based evaluation functions."

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      "header": "Compromising between QALYs and PALYs",

      "content": "as mentioned above, the evaluation functions characterized in the previous section ignore one dimension of our model. in other words, they all rely on a very demanding axiom of (productivity or health) independence. the purpose of this section is to dismiss those axioms, while obtaining characterizations of natural compromises between those focal (albeit polar) evaluation functions.for instance, the productivity-and-quality-adjusted life years (pqaly) evaluation function evaluates distributions by means of the weighted (through productivity and health levels) aggregate time span the distribution yields, so that health, productivity and lifespan of individuals enter the evaluation function multiplicatively. formally,where q : a → [0, 1] is a health state quality weight satisfying 0 ≤ q(a i ) ≤ q(a \* ) = 1 for eachas the next result states, this evaluation function is characterized when we dismiss health independence in the previous result (characterizing palys), and strengthen the other two independence axioms to consider the following ones.first, time invariance at common health and productivity, which states that for two individuals at common health and productivity, it does not matter to the social planner who receives the extra life years.tichp: for each d ∈ d, each pair i, j ∈ n with a i = a j = a and p i = p j = p, and each c > 0,second, productivity invariance at common health and time, which says that for two individuals at common health and time, it does not matter who gains in productivity.picht: for each d ∈ d, each pair i, j ∈ n with a i = a j = a and t i = t j = t, and each c > 0theorem 5 the following statements are equivalent:1. is represented by a pqaly evaluation function (5)."

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      "header": "satisfies COMMON, TICHP, PICHT, and TIUP.",

      "content": "a social planner may view both health effects and productivity effects as important outcomes of interventions and may therefore choose an evaluation function like the pqaly,where health status and productivity of individuals enter the evaluation function multiplicatively. this implies according to theorem 5 that one of the values applied by the social planner in this situation is that increases in lifetime among unproductive individuals following an intervention (axiom tiup) will not increase the desirability of that intervention. the social planner subscribes to two further values regarding invariance between different effect components where the first states that if an intervention leads to extra life years, it does not matter to the social planner which particular individual (among individuals with the same level of health and productivity) receives these extra life years (axiom tichp). the second value specifies that if an intervention leads to improved productivity, it does not matter which particular individual (among individuals with the same level of health and lifespan) is able to perform better in the workplace (axiom picht).our next result states that dismissing the tiup axiom in the previous statement we obtain the following alternative intriguing compromise (dubbed qaly-pqaly ) which evaluates distributions by means of a convex combination of the qalys and pqalys the distribution yields. formally,where q, r : a → [0, 1] are health state quality weight functions satisfying 0 ≤ q(a i ) ≤ q(a \* ) = 1 and 0 ≤ r(a i ) ≤ r(a \* ) = 1 for each a i ∈ a, and δ ∈ [0, 1].the qaly-pqaly evaluation function () divides the evaluation exercise into two separate tasks; namely the valuation of the pure health effects among individuals following an intervention, plus the valuation of productivity-and-quality adjusted lifespans of individuals.the parameter δ measures the relative importance that the social planner puts on pure health effects and productivity-and-quality adjusted life years resulting from an intervention.the following statements are equivalent:1. is represented by a qaly-pqaly evaluation function (6).similar to the previous evaluation function, a social planner choosing the qaly-pqaly evaluation function (6) considers both health effects and productivity effects as important outcomes of interventions. in contrast to the previous theorem, theorem 6 implies a rejection of axiom tiup according to which improvements in lifetime among unproductive individuals following an intervention do not increase the desirability of that intervention. apart from that, the social planner subscribes to the same two axioms regarding invariance between different effect components as above (tichp and picht).the previous family of evaluation functions (6) includes a natural sub-family of evaluation functions (qaly-paly ) that evaluate distributions by means of the convex combinations of the qalys and palys that the distribution yields. formally,where q : a → [0, 1] is a health state quality weight function satisfying 0 ≤ q(a i ) ≤ q(a \* ) = 1, for each a i ∈ a, and σ ∈ [0, 1].health effects and productivity effects enter the qaly-paly evaluation functionadditively so that these two effects are measured and valued independently of each other. the parameter σ indicates the relative importance that the social planner places on health and productivity effects of individuals respectively.this family of evaluation functions () is characterized when strengthening the productivity invariance at common health and time axiom to productivity invariance at common time, which says that for two individuals with common lifespan (and irrespective of their health status), it does not matter which of the two individuals improve their productivity.pict: for each d ∈ d, each pair i, j ∈ n with t i = t j = t, and each c > 0 such thatthe following statements are equivalent:1. is represented by a qaly-paly evaluation function. we also conclude this section applying the evaluation functions characterized in this section to the distributions from example 1. more precisely, we summarize the computations in the next table. we infer from there that a distribution is preferred to the other one for a certain range of the parameters defining the families of evaluation functions we are considering in this section. for instance, if we assume q(a) = r(a) = 0.5, then e δ (d ∆ ) < e δ (d λ ) for all members of the family. on the other hand, if we assume q(a) = r(a) = 0, thenall members of the family. finally, if we assume q(a) = r(a) = 0.4, thenif and only if δ < 1 3 . as for the family (), e σ (d ∆ ) < e σ (d λ ) if and only if σ < we have presented some central compromises to evaluate both health and productivity aspects of distributions in the previous section. we can even be more flexible to accommodate other (more general) compromises. as a matter of fact, those compromises considered above can be seen as members of a general family of evaluation functions that evaluate distributions by the weighted aggregation of lifetimes the distribution yields, where the weight is a function of health and productivity. formally,where but the family of evaluation functions (8) can also accommodate other evaluation functions that have not been introduced above. for instance, suppose that w is a semimultiplicative function in which productivity enters via a power function, whereas health enters via qalys, i.e., w(a i , p i ) = q(a i )p γ i , for each (a i , p i ) ∈ a × [0, 1], where γ ∈ (0, 1).where q : a → [0, 1] is a health state quality weight function satisfying 0 ≤ q(a i ) ≤ q(a \* ) = 1, for each a i ∈ a, and γ ∈ (0, 1).note that the previous evaluation function is formalizing a concern for the dispersion of productivity levels (as it is a concave function of those levels).the above is somewhat reminiscent of the focal welfare function within the literature on life-cycle preferences over consumption and health status. therein, multiplicative separability from consumption and health is typically assumed.in our case, we have productivity instead of consumption, but multiplicative separability can also be naturally obtained from the general family of evaluation functions.it turns out that the general family of evaluation functions () is characterized when combining the common set of axioms and time invariance at common health and productivity.the following statements are equivalent:1. is represented by an evaluation function (8).theorem 8 implies that if the social planner endorses the view that if an intervention leads to extra life years, it does not matter which particular individual (among individuals with the same level of health and productivity) receives these extra life years (axiom tichp), then the evaluation will be via a weighted aggregation of the lifetimes the intervention yields. and the weight for each individual lifetime will be obtained via a general function of the health and productivity levels they face.a weaker axiom than time invariance at common health and productivity, is time invariance at full health and productivity, which states that extra years can be interchangeable among individuals with full health and maximum productivity.tifhp: for each d ∈ d, each pair i, j ∈ n with a i = a j = a \* and p i = p j = 1, and each c > 0,if we replace time invariance at common health and productivity by time invariance at full health and productivity we characterize a more general family of evaluation functions, which extend to this context the notion of healthy years equivalent (e.g.,.more precisely, the healthy productive years equivalent (hpye ) evaluation function evaluates distributions by the unweighted aggregation of hpyes the distribution yields. formally,where f : a × [0, 1] × r + → r + is continuous with respect to its second and third variables andwhere, for each (a i , p i , tthe evaluation function () is obtained via an intuitive process. each individual triple d i = (a i , p i , t i ) is first associated with another triple (a \* , 1, f (a i , p i , t i )) in which the individual enjoys full health and maximal productivity, but a lower lifetime. this converts the multidimensional evaluation problem into a unidimensional one in which the social planner only needs to focus on lifetimes (which are simply aggregated afterwards). the precise lifetime amount, f (a i , p i , t i ), is actually a function of the original triple and it is obtained to guarantee that the social planner is indifferent between the original distribution and the new one. this is a well-defined function, due to the common axioms.note that this family (9) includes the previous one. to see that, note that for eachas the next result states, the general family of evaluation functions () is characterized when combining the common set of axioms and time invariance at full health and productivity.the following statements are equivalent:1. is represented by a hpye evaluation function (9).theorem 9 implies that if the social planner endorses the view that if an intervention leads to extra life years for individuals with full health and maximal productivity, it does not matter which particular individual receives these extra life years (axiom tifhp), then the evaluation will be via the unweighted aggregation of the hpyes the intervention yields (which are well defined due to common).finally, we can define the so-called generalized hpye evaluation function by the unweighted aggregation of the image of hpyes the distribution yields to a certain function. formally,where g : r + → r is a strictly increasing and continuous function, and f :is continuous with respect to its second and third variables and for each dwhere, for each (a i , p i , tour last result states that the generalized hpye evaluation function is precisely characterized by the set of common axioms.the following statements are equivalent:1. is represented by a generalized hpye evaluation function.theorem 10 implies that if the social planner dismisses the tifhp axiom, while still endorsing common, then the evaluation will be via a general (but strictly increasing and continuous) function of the hpyes the intervention yields (which are well defined due to common). thus, the evaluation will not necessarily be via a simple unweighted aggregation of hpyes, which was the consequence of the tifhp axiom, as formalized by the evaluation function."

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      "header": "Discussion",

      "content": "the results presented above in the form of evaluation functions and their required axioms may be utilised in empirical applications, for example as part of an economic evaluation of a health care or working environment intervention. the data collection of the economic evaluation will typically involve capturing information on all individuals in the intervention and control group regarding their costs, health status and productivity level during the follow-up period of the study.as illustrated throughout the text with the two distributions from example 1, the choice of evaluation function matters to a large extent when it comes to rank different distributions. instead of making that choice directly based on their functional forms, we rather believe the choice should be guided by the axioms they satisfy. hence the interest of our axiomatic approach.if the analyst (working on behalf of a social planner) is of the view that health effects and productivity effects are both important outcomes when assessing the benefit of the working environment intervention, evaluation functions ()-() may be used for calculating the combined effects on health and productivity in the intervention and control group. the analyst may choose a specific evaluation function based on an examination of the individual sets of axioms in terms of their expected acceptability to the society where the working environment intervention will be introduced. for example, the time independence for unproductive individuals (tiup) axiom may be considered unacceptable, as it conveys that gains in lifetime among individuals outside the labour market have no value. rejection of the tiup axiom would exclude the pqaly evaluation function. assume further that the analyst deems the axioms time invariance at common health and productivity (tichp) and productivity invariance at if the qaly-paly evaluation function is chosen, the next step is to estimate the corresponding parameters, including the one addressing the relative importance of improvements in health and productivity (σ), the quality weights of health states (q(a i )), productivity levels (p i ) and durations (t i ). the latter two parameters will typically be available directly from the data collection for the economic evaluation. quality weights of health states may be elicited from representative agents using a person trade-off method. 15 for example, each respondent would be asked which of the following interventions are most desirable for society:intervention a: 1000 individuals obtaining 1 year in full health and having zero productivity.intervention b: x individuals obtaining 1 year in health state a and having zero productivity.in particular, each respondent would be asked to identify the number of individuals x in intervention b to be indifferent between both interventions. the quality weight can then be derived as q(a) = 1000x . the parameter σ may be elicited using a different version of the person trade-off technique.to wit, respondents would now be asked to state which of the following interventions are most desirable for society: intervention c: one individual obtaining 1 year in full health and having zero productivity.intervention d: one individual obtaining y years in health state a and having maximum productivity.each respondent would then be asked to identify the duration y in intervention d to be indifferent between the two interventions. once y is identified, it follows from evaluation functionthat σ = σq(a)y + (1σ)y, which implies σ = y 1-q(a)y+y , from which the parameter σ can be estimated. when all parameters have been estimated, the total effects in the intervention and control group can be calculated using the paly-qaly evaluation function.the need for using a more flexible evaluation function (for example the qaly-pqaly). if people largely agree with this axiom (i.e., a majority is largely indifferent between adding productivity to one type or another, or roughly participants are split into those that favor persons of one type and those that favor persons of the other type) it provides support for using the qaly-paly. 15 the reader is referred to,, or, for details about the person trade-off technique and discussion. we also acknowledge here that the descriptive validity of this technique is highly questionable (e.g.,."

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      "header": "Concluding remarks",

      "content": "some of our models, particularly the more general functional forms () and (), embrace a wide spectrum of potential ethical and social concerns. but the more structured evaluation functions ()-() involve a time-linear component. thus, for each evaluation function of the form ()-(), if a person doubles her time (for a fixed productivity level and health state), her contribution to social welfare doubles. this standard feature is widely acknowledged in qaly and paly studies; indeed it reflects the basic idea of proportionally \"adjusting\" the years obtained based on available information about the years lived. in the context of qaly studies, more general functional forms have been proposed. in particular, an approach where the individual qaly component is transformed by a power function before being aggregated across individuals was proposed byand williams (1997), among others, and axiomatically characterized byand hougaard et al. () in their model focusing on population distributions of life years and health states.in a health setting, power qaly functional forms are typically associated to a formalization of the so-called \"fair innings\", a popular argument within the public health literature (e.g.,.they can also be seen as prioritarian evaluation functions (also known as prioritarian social welfare functionals), which rank well-being vectors according to the sum of a strictly increasing (dubbed equivalent health-adjusted lifespan) that is sensitive to inequality in both age-specific health and health-adjusted lifespan. it is a life years metric that nests health-adjusted life expectancy.in the present framework considering health states, productivity and life years, we could also impose a power transformation of the individual components in each of the structured evaluation functions (1)-(). this would entail determining one additional parameter for the model (or perform robustness analyses for a reasonable range of possible power transformations). we could also consider some specific prioritarian evaluation functions within the general evaluation functions ()-. the consequence would be to give more weight to the initial years from the point of view of a social planner. this would change the ethical and social implications of the evaluation function used. in particular, it would mean that some of the axioms would be violated, and thus we would need new (weaker) axioms to characterize such modified and more flexible functional form. an investigation into the axiomatic underpinnings of employing a power transformation (or other parametric concave transformations) in a framework incorporating individual health, productivity, and life years is left for future research. 17   as we mentioned in the introduction, there is a pressing need to protect the health and productivity of the economically active population. treatments for the elderly (retired people)have no effects on (labour market) productivity. this might render qalys more appropriate for the evaluation of these treatments. but using the same evaluation function for younger patients misses productivity effects. this is a possible motivation for age weights (another motivation is the fair innings argument mentioned above). our hybrid evaluation functions, such as pqalys, qalys-palys, qalys-pqalys or the more general functional form, offer an alternative way of dealing with productivity differences, selecting the appropriate parameters therein.we conclude mentioning that our framework allows for alternative plausible interpretations, as well as for further generalizations.regarding the former, we focused on chronic health states, for ease of exposition, but our analysis also allows to consider time-varying health. to wit, we made no assumptions regarding the domain of health states a (except for the existence of a maximal element). in particular, this allows for time trajectories rather than fixed levels of health (with the trajectory determined by t i ). that is, a i = a i (•), where a i (s) denotes the health status of individual i at time s ≤ t i .this would require a reinterpretation of some of the axioms we considered above. 18   likewise, instead of assuming that p i ∈ [0, 1] captures the productivity of individual i, we could assume that it captures the probability to succeed in life that individual i has. mariotti and veneziani (2018) refer to this as \"chances of success\" and characterize a multiplicative form to evaluate social profiles of \"chances of success\" (also known as \"boxes of life\"). 19 we could also derive their characterization results in our model upon endorsing first the axiom of health independence and a counterpart axiom of time independence (not considered in this paper). we, 17 a natural way to start would be by modifying the tichp axiom, so as to prefer to give the extra life years to the shorter-lived individual. 18 bossert and d'ambrosio (2013) is a nice example of an axiomatic analysis of time trajectories (streams) of wealth (rather than health). 19 see alsoandfor characterizations of alternative functional forms in the same model.nevertheless, acknowledge that their main axiom is one formalizing a non-interference principle that we do not consider in this paper. 20   as for further generalizations, we stress that the scope of our theory can be enlarged to account for more general evaluations. to wit, our theory deals with the evaluation of population distributions where individuals can be characterized by two instantaneous attributes (one qualitative and one quantitative) and a duration. these attributes can indeed be interpreted as health (qualitative) and productivity (quantitative), as we do in this paper. but there are other potential interpretations (such as happiness or well-being, to name a few). our results could therefore provide interesting lessons for those settings too.where 0 first, we prove that for each d ∈ d and each i ∈ n, there existsif t i = 0, then it follows from zero that t \* i = t i = 0. therefore, assume t i > 0. we prove that t \* i exists by contradiction. therefore, assume that t \* i does not exist. then, t = a ∪ b, whereby fhps, [(a \* , 1, t i ), d n \\{i} ] d, implying that either t \* i = t i (a contradiction), or t i ∈ b. assume the latter. thus, b is a non-empty set.by pld and zero, it follows that either t \* i = 0 (a contradiction), or 0 ∈ a. again, assume the latter. thus, a is a non-empty set.by cont, a and b are open sets relative to t . altogether, it follows that t is not a connected set, which is a contradiction. thus, t \* i exists, and due to lmfhp, it is uniquely determined. finally, by sep, we can determine each t \* i separately. therefore, let f i : a×[0, 1]×r + → r be such that f i (a i , p i , t i ) = t \* i for each i ∈ n. by anon, f i () = f j () = f () for each i, j ∈ n. by cont, f is continuous with respect to its second and third variable and, by the above, we know that 0 ≤ f (a i , p i , t i ) ≤ t i , so the range of f is a connected subset of r. also, by fhps, f (a i , p i , t i ) ≤ f (a i , 1, t i ), andwhich implies that social preferences only depend on the profile of hpyes, and, by cont, they do so continuously. as in the models ofwhere g : r + → r is strictly increasing.suppose first that is represented by a phef satisfying. by theorem 10, common holds. as for tifhp, let d ∈ d and i, j ∈ n be such that a i = a j = a \* and p i = p j = 1. then, for each c > 0,andthus,conversely, assume now that preferences satisfy all the axioms in common as well as tifhp. then, by theorem 10, for each pair d, d ′ ∈ d,where g : r + → r is strictly increasing. now, for each pair t i , t j ∈ r + , and for each c > 0, it follows by tifhp that g(f (a \* , 1, t i + c)) + g(f (a \* , 1, t j )) = g(f (a \* , 1, t i )) + g(f (a \* , 1, t j + c)).or, equivalently,in particular,for each x, y ≥ 0. as g is continuous and strictly increasing, it follows from theorem 1 in) that there exist α and β such that g(x) = αx + β, for each x > 0. by lmfhp, α > 0. consequently, is indeed represented by an evaluation function satisfying, as desired.suppose first that is represented by a phef satisfying. as this is a special case of, it follows from theorem 10 that common holds. as for tichp, let d ∈ d and i, j ∈ n be such that a i = a j = a and p i = p j = p. conversely, assume now that preferences satisfy all the axioms in the statement of theorem 8.then, by theorem 10, for each pair d, d ′ ∈ d,where = ϕ(a, p,= ϕ(a, p,in particular, ϕ(a, p, t → r be such that w(a, p) = ŵ(a,p) ŵ(a \* ,1) , for each (a, p) ∈ a × [0, 1]. thus, it follows that 1 = w(a \* , 1) ≥ w(a, p) ≥ 0, for each (a, p) ∈ a × [0, 1]. then, we may write: ϕ(a, p, t i ) = w(a, p)t i , where 0 ≤ w(a, p) ≤ w(a \* , p) ≤ w(a \* , 1) = 1, and 0 ≤ w(a, p) ≤ w(a, 1) ≤ w(a \* , 1) = 1 for each (a, p) ∈ a × [0, 1], as desired.suppose first that is represented by a phef satisfying. as this is a special case of, it follows from theorem 10 that common holds. it is straightforward to see that it also satisfies pi. as for tichfp, let d ∈ d and i, j ∈ n be such that a i = a j = a and p i = p j = 1.then, for each c > 0,conversely, assume now that preferences satisfy all the axioms in the statement of theoremwhere g : r + → r is strictly increasing. pi and tichfp together imply tichp. thus, preferences satisfy all the axioms in the statement of theorem 8. thus, for each d ∈ d,where 0 ≤ w(a, p) ≤ w(a \* , p) ≤ w(a \* , 1) = 1, and 0 ≤ w(a, p) ≤ w(a, 1) ≤ w(a \* , 1) = 1 for each (a, p) ∈ a × [0, 1]. now, by pi, w(a, p) = w(a, 1), for each a ∈ a. let q : a → r be such that q(a i ) = w(a i , 1), for each a i ∈ a. then, it follows that 1 = q(a \* ) ≥ q(a) ≥ 0, for each a ∈ a.and we may write:where 0 ≤ q(a) ≤ q(a \* ) = 1, for each a ∈ a, as desired.suppose first that is represented by a phef satisfying. as this is a special case of (10), it follows from theorem 10 that common holds. it is straightforward to see that it also satisfies hi. as for tifhcp, let d ∈ d and i, j ∈ n be such that a i = a j = a \* and p i = p j = p.then, for each c > 0,thus, as v(and each c > 0 such that p i + c, p j + c ∈ [0, 1]. in particular,suppose first that is represented by a phef satisfying. as this is a special case of (8), it follows from theorem 8 that common and tichp hold. it is straightforward to see that it also satisfies tiup. as for picht, let d ∈ d, and i, j ∈ n with a i = a j = a and t i = t j = t.then, for each c > 0 such that p i + c, p j + c ≤ 1, e[(a, p i + c, t), (a, p j , t), d n \\{i,j} ] = q(a)(p i + c)t + q(a)p j t + k∈n \\{i,j} q(a k )p k t k , and e[(a, p i , t), (a, p j + c, t), d n \\{i,j} ] = q(a)p i t + q(a)p j (t + c) + k∈n \\{i,j} q(a k )p k t k .thus, [(a, p i + c, t), (a, p j , t), d n \\{i,j} ] ∼ [(a, p i , t), (a, p j + c, t), d n \\{i,j} ].conversely, assume now that preferences satisfy all the axioms in the statement of theorem 5. then, they also satisfy the axioms of theorem 8. thus, for each pair d, d ′ ∈ d, and, therefore, is indeed represented by an evaluation function satisfying (5), as desired.suppose first that is represented by a phef satisfying. as this is a special case of (8), it follows from theorem 8 that common and tichp hold. as for picht, let d ∈ d, and i, j ∈ n with a i = a j = a and t i = t j = t. then, for each c > 0 such that p i + c, p j + c ≤ 1, e[(a, p i + c, t), (a, p j , t), d n \\{i,j} ] = δ(q(a)t + q(a)t) + (1δ)(q(a)(p i + c)t + q(a)p j t) + k∈n \\{i,j} δq(a k )t k + (1δ)r(a k )p k t k , and e[(a, p i , t), (a, p j + c, t), d n \\{i,j} ] = δ(q(a)t + q(a)t) + (1δ)(q(a)p i t + q(a)(p j + c)t) + k∈n \\{i,j} δq(a k )t k + (1δ)r(a k )p k t k . thus, [(a, p i + c, t), (a, p j , t), d n \\{i,j} ] ∼ [(a, p i , t), (a, p j + c, t), d n \\{i,j} ].conversely, assume now that preferences satisfy all the axioms in the statement of theorem for each a ∈ a, it follows that is represented by an evaluation function satisfying. or, equivalently, by an evaluation function satisfying, with δ = 0.case 3. α(a \* ) = 0 = β(a \* ).let q, r : a → r be such that r(a) = α(a) α(a \* ) and q(a) = β(a) β(a \* ) , for each a ∈ a. then, by fhps, 1 = q(a \* ) ≥ q(a) ≥ 0, and 1 = r(a \* ) ≥ r(a) ≥ 0. furthermore, 0 < α(a \* ), β(a \* ) < 1. now, if we let δ = β(a \* ) ∈ (0, 1), we have w(a, p) = δq(a) + (1δ)r(a)p, for each p ∈ [0, 1], and each a ∈ a. thus, for each pair d, d ′ ∈ d,where q, r : a → [0, 1] are such that 1 = q(a \* ) ≥ q(a) ≥ 0, and 1 = r(a \* ) ≥ r(a) ≥ 0 and δ ∈ (0, 1). consequently, is indeed represented by an evaluation function satisfying, with δ ∈ (0, 1) as desired.suppose first that is represented by a phef satisfying. as this is a special case of (), it follows from theorem 6 that common and tichp hold. as for pict, let d ∈ d, and i, j ∈ n with t i = t j = t. then, for each c > 0 such that p i + c, p j + c ≤ 1, e[(a i , p i +c, t), (a j , p j , t), d n \\{i,j} ] = σ(q(a i )t+q(a j )t)+(1-σ)((p i +c)t+p j t)+ conversely, assume now that preferences satisfy all the axioms in the statement of theorem 7. then, they also satisfy the axioms in theorem 6 (note that pict implies picht). thus, for each pair d, d ′ ∈ d,where q, r : a → [0, 1] are such that 1 = q(a \* ) ≥ q(a) ≥ 0, and 1 = r(a \* ) ≥ r(a) ≥ 0 andby pict, [(a i , p i + c, t), (a j , p j , t), d n \\{i,j} ] ∼ [(a i , p i , t), (a j , p j + c, t), d n \\{i,j} ],for each d ∈ d, and i, j ∈ n with t i = t j = t. now, as e[(a i , p i + c, t), (a j , p j , t), d n \\{i,j} ] = δ(q(a i )t + q(a j )t) + (1δ)(r(a i )(p i + c)t + r(a j )p j t) + k∈n \\{i,j} δq(a k )t k + (1σ)r(a k )p k t k , and e[(a i , p i , t), (a j , p j + c, t), d n \\{i,j} ] = δ(q(a i )t + q(a j )t) + (1δ)(r(a i )p i t + r(a j )(p j + c)t) + k∈n \\{i,j} δq(a k )t k + (1σ)r(a k )p k t k . thus, r(a i ) = r(a j ), for each pair a i , a j ∈ a. as, 1 = r(a \* ), it follows that r(a) = 1, for each a ∈ a. thus, letting σ = δ, we obtain that is indeed represented by an evaluation function satisfyingas desired."

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Figure 0‑1 – Segmentation full result