### **Anomaly Detection**

Lecture Notes for Chapter 9

Introduction to Data Mining, 2<sup>nd</sup> Edition by Tan, Steinbach, Karpatne, Kumar

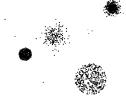
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# **Anomaly/Outlier Detection**

- What are anomalies/outliers?
  - The set of data points that are considerably different than the remainder of the data



- Natural implication is that anomalies are relatively rare
  - One in a thousand occurs often if you have lots of data
  - Context is important, e.g., freezing temps in July
- Can be important or a nuisance
  - 10 foot tall 2 year old
  - Unusually high blood pressure Edition

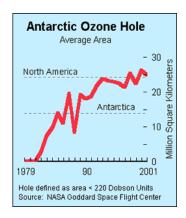
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# **Importance of Anomaly Detection**

#### Ozone Depletion History

- In 1985 three researchers (Farman, Gardinar and Shanklin) were puzzled by data gathered by the British Antarctic Survey showing that ozone levels for Antarctica had dropped 10% below normal levels
- Why did the Nimbus 7 satellite, which had instruments aboard for recording ozone levels, not record similarly low ozone concentrations?
- The ozone concentrations recorded by the satellite were so low they were being treated as outliers by a computer program and discarded!



#### Sources:

http://exploringdata.cqu.edu.au/ozone.html http://www.epa.gov/ozone/science/hole/size.html

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# **Causes of Anomalies**

- Data from different classes
  - Measuring the weights of oranges, but a few grapefruit are mixed in
- Natural variation
  - Unusually tall people
- Data errors
  - 200 pound 2 year old

### **Distinction Between Noise and Anomalies**

- Noise is erroneous, perhaps random, values or contaminating objects
  - Weight recorded incorrectly
  - Grapefruit mixed in with the oranges
- Noise doesn't necessarily produce unusual values or objects
- Noise is not interesting
- Anomalies may be interesting if they are not a result of noise
- Noise and anomalies are related but distinct concepts

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### **General Issues: Number of Attributes**

- Many anomalies are defined in terms of a single attribute
  - Height
  - Shape
  - Color
- Can be hard to find an anomaly using all attributes
  - Noisy or irrelevant attributes
  - Object is only anomalous with respect to some attributes
- However, an object may not be anomalous in any one attribute

### **General Issues: Anomaly Scoring**

- Many anomaly detection techniques provide only a binary categorization
  - An object is an anomaly or it isn't
  - This is especially true of classification-based approaches
- Other approaches assign a score to all points
  - This score measures the degree to which an object is an anomaly
  - This allows objects to be ranked
- In the end, you often need a binary decision
  - Should this credit card transaction be flagged?
  - Still useful to have a score
- How many anomalies are there?

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# **Other Issues for Anomaly Detection**

- Find all anomalies at once or one at a time
  - Swamping
  - Masking
- Evaluation
  - How do you measure performance?
  - Supervised vs. unsupervised situations
- Efficiency
- Context
  - Professional basketball team

### **Variants of Anomaly Detection Problems**

- Given a data set D, find all data points x ∈ D with anomaly scores greater than some threshold t
- Given a data set D, find all data points x ∈ D having the top-n largest anomaly scores
- Given a data set D, containing mostly normal (but unlabeled) data points, and a test point x, compute the anomaly score of x with respect to D

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# **Model-Based Anomaly Detection**

- Build a model for the data and see
  - Unsupervised
    - Anomalies are those points that don't fit well
    - Anomalies are those points that distort the model
    - Examples:
      - Statistical distribution
      - Clusters
      - Regression
      - Geometric
      - Graph
  - Supervised
    - Anomalies are regarded as a rare class
    - Need to have training data

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# **Additional Anomaly Detection Techniques**

- Proximity-based
  - Anomalies are points far away from other points
  - Can detect this graphically in some cases
- Density-based
  - Low density points are outliers
- Pattern matching
  - Create profiles or templates of atypical but important events or objects
  - Algorithms to detect these patterns are usually simple and efficient

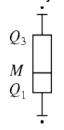
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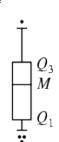
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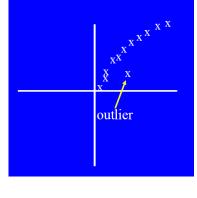
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# **Visual Approaches**

- Boxplots or scatter plots
- Limitations
  - Not automatic
  - Subjective







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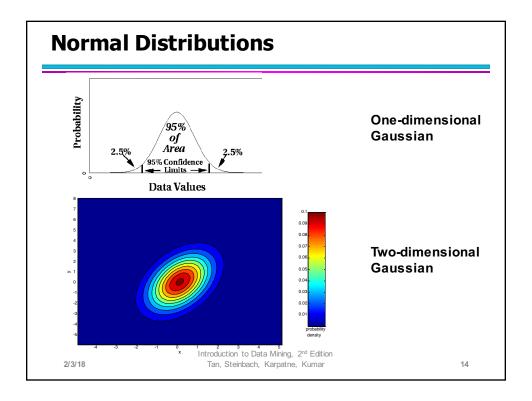
# **Statistical Approaches**

**Probabilistic definition of an outlier:** An outlier is an object that has a low probability with respect to a probability distribution model of the data.

- Usually assume a parametric model describing the distribution of the data (e.g., normal distribution)
- Apply a statistical test that depends on
  - Data distribution
  - Parameters of distribution (e.g., mean, variance)
  - Number of expected outliers (confidence limit)
- Issues
  - Identifying the distribution of a data set
    - Heavy tailed distribution
  - Number of attributes
  - Is the data a mixture of distributions?

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#### **Grubbs' Test**

- Detect outliers in univariate data
- Assume data comes from normal distribution
- Detects one outlier at a time, remove the outlier, and repeat
  - H<sub>0</sub>: There is no outlier in data
  - H<sub>A</sub>: There is at least one outlier
- Grubbs' test statistic:
- Reject H<sub>0</sub> if: Introduction to Data Mining, 2nd Edition

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# Statistical-based – Likelihood Approach

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- Assume the data set D contains samples from a mixture of two probability distributions:
  - M (majority distribution)
  - A (anomalous distribution)
- General Approach:
  - Initially, assume all the data points belong to M
  - Let L<sub>t</sub>(D) be the log likelihood of D at time t
  - For each point x<sub>t</sub> that belongs to M, move it to A
    - ◆ Let L<sub>t+1</sub> (D) be the new log likelihood.
    - Compute the difference,  $\Delta = L_t(D) L_{t+1}(D)$
    - If  $\Delta > c$  (some threshold), then  $x_t$  is declared as an anomaly and moved permanently from M to A

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### Statistical-based – Likelihood Approach

- Data distribution, D =  $(1 \lambda)$  M +  $\lambda$  A
- M is a probability distribution estimated from data
  - Can be based on any modeling method (naïve Bayes, maximum entropy, etc)
- A is initially assumed to be uniform distribution
- Likelihood at time t:

$$\begin{split} L_{t}(D) &= \prod_{i=1}^{N} P_{D}(x_{i}) = \left( (1-\lambda)^{|M_{t}|} \prod_{x_{i} \in M_{t}} P_{M_{t}}(x_{i}) \right) \left( \lambda^{|A_{t}|} \prod_{x_{i} \in A_{t}} P_{A_{t}}(x_{i}) \right) \\ LL_{t}(D) &= \left| M_{t} \middle| \log(1-\lambda) + \sum_{x_{i} \in M_{t}} \log P_{M_{t}}(x_{i}) + \middle| A_{t} \middle| \log \lambda + \sum_{x_{i} \in A_{t}} \log P_{A_{t}}(x_{i}) \right. \end{split}$$

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### Strengths/Weaknesses of Statistical Approaches

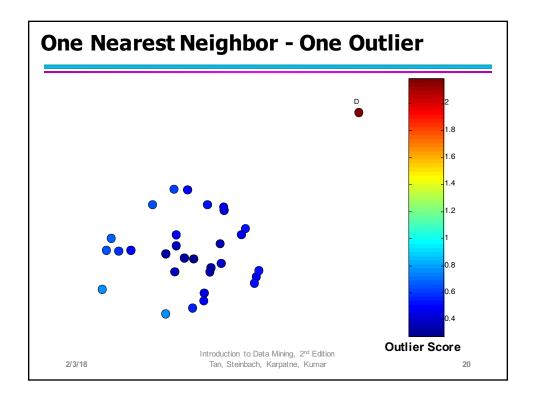
- Firm mathematical foundation
- Can be very efficient
- Good results if distribution is known
- In many cases, data distribution may not be known
- For high dimensional data, it may be difficult to estimate the true distribution
- Anomalies can distort the parameters of the distribution

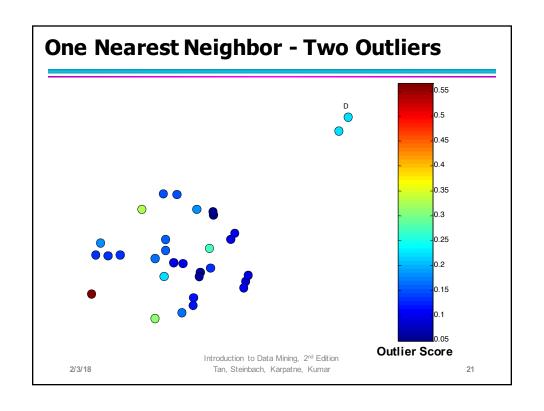
# **Distance-Based Approaches**

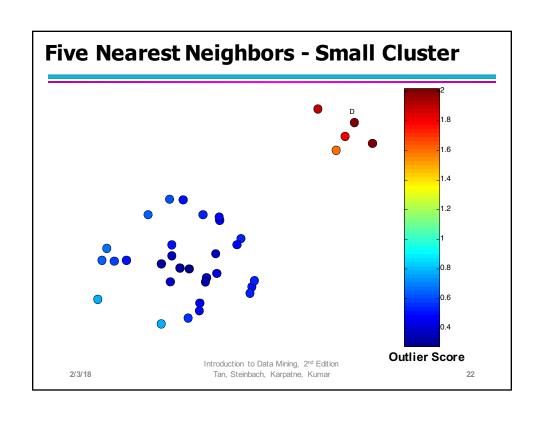
- Several different techniques
- An object is an outlier if a specified fraction of the objects is more than a specified distance away (Knorr, Ng 1998)
  - Some statistical definitions are special cases of this
- The outlier score of an object is the distance to its kth nearest neighbor

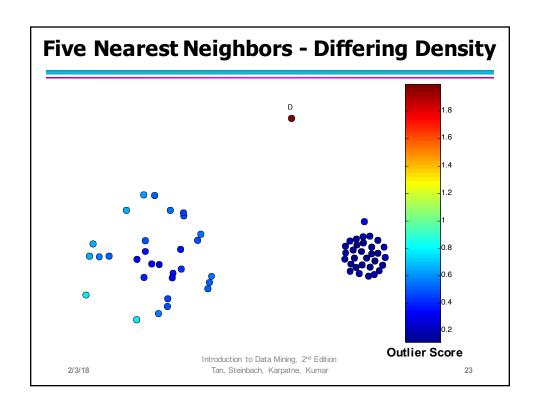
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### Strengths/Weaknesses of Distance-Based Approaches

- Simple
- Expensive O(n²)
- Sensitive to parameters
- Sensitive to variations in density
- Distance becomes less meaningful in highdimensional space

### **Density-Based Approaches**

- Density-based Outlier: The outlier score of an object is the inverse of the density around the object.
  - Can be defined in terms of the k nearest neighbors
  - One definition: Inverse of distance to kth neighbor
  - Another definition: Inverse of the average distance to k neighbors
  - DBSCAN definition
- If there are regions of different density, this approach can have problems

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### **Relative Density**

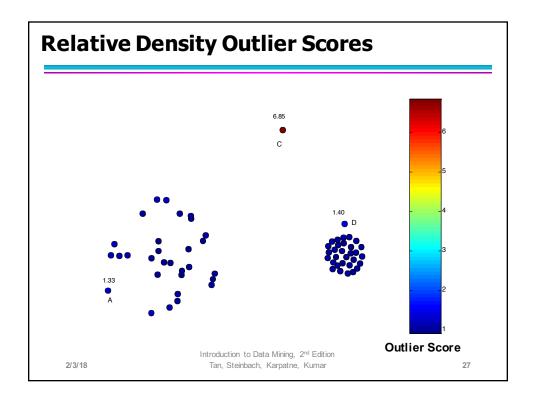
 Consider the density of a point relative to that of its k nearest neighbors

```
average\ relative\ density(\mathbf{x},k) = \frac{density(\mathbf{x},k)}{\sum_{\mathbf{y} \in N(\mathbf{x},k)} density(\mathbf{y},k)/|N(\mathbf{x},k)|}
```

#### Algorithm 10.2 Relative density outlier score algorithm.

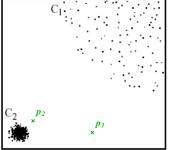
- 1:  $\{k \text{ is the number of nearest neighbors}\}$
- 2: for all objects x do
- Determine  $N(\mathbf{x}, k)$ , the k-nearest neighbors of  $\mathbf{x}$ .
- Determine  $density(\mathbf{x}, k)$ , the density of  $\mathbf{x}$ , using its nearest neighbors, i.e., the objects in  $N(\mathbf{x}, k)$ .
- 5: end for
- 6: for all objects x do
- Set the outlier  $score(\mathbf{x}, k) = average \ relative \ density(\mathbf{x}, k)$  from Equation 10.7.
- 8: end for

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# **Density-based: LOF approach**

- For each point, compute the density of its local neighborhood
- Compute local outlier factor (LOF) of a sample p as the average of the ratios of the density of sample p and the density of its nearest neighbors
- Outliers are points with largest LOF value



In the NN approach,  $p_2$  is not considered as outlier, while LOF approach find both  $p_1$  and  $p_2$  as outliers

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#### **Strengths/Weaknesses of Density-Based Approaches**

- Simple
- Expensive O(n²)
- Sensitive to parameters
- Density becomes less meaningful in highdimensional space

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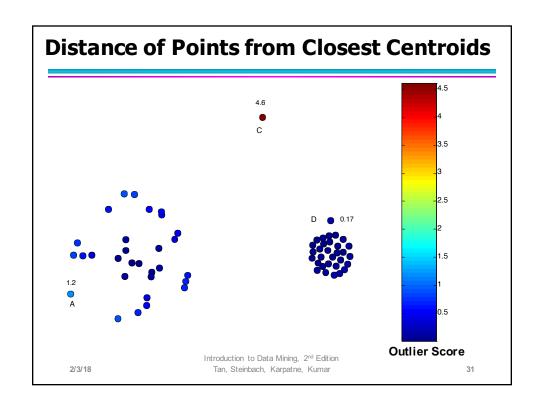
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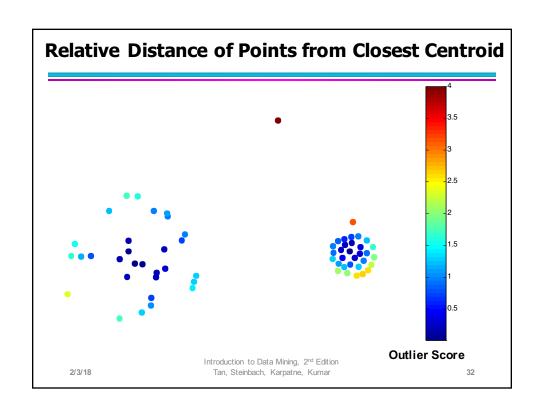
### **Clustering-Based Approaches**

- Clustering-based Outlier: An object is a cluster-based outlier if it does not strongly belong to any cluster
  - For prototype-based clusters, an object is an outlier if it is not close enough to a cluster center
  - For density-based clusters, an objec is an outlier if its density is too low
  - For graph-based clusters, an object is an outlier if it is not well connected
- Other issues include the impact of outliers on the clusters and the number of clusters

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### Strengths/Weaknesses of Distance-Based Approaches

- Simple
- Many clustering techniques can be used
- Can be difficult to decide on a clustering technique
- Can be difficult to decide on number of clusters
- Outliers can distort the clusters

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