



Outsourced Symmetric Private Information Retrieval

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ABSTRACT

In the setting of searchable symmetric encryption (SSE), a data owner \mathcal{D} outsources a database (or document/file collection) to a remote server \mathcal{E} in encrypted form such that \mathcal{D} can later search the collection at \mathcal{E} while hiding information about the database and queries from \mathcal{E} . Leakage to \mathcal{E} is to be confined to well-defined forms of data-access and query patterns while preventing disclosure of explicit data and query plaintext values. Recently, Cash et al. presented a protocol, OXT, which can run arbitrary boolean queries in the SSE setting and which is remarkably efficient even for very large databases.

In this paper we investigate a richer setting in which the data owner \mathcal{D} outsources its data to a server \mathcal{E} but \mathcal{D} is now interested to allow clients (third parties) to search the database such that clients learn the information \mathcal{D} authorizes them to learn but nothing else while \mathcal{E} still does not learn about the data or queried values as in the basic SSE setting. Furthermore, motivated by a wide range of applications, we extend this model and requirements to a setting where, similarly to private information retrieval, the client's queried values need to be hidden also from the data owner \mathcal{D} even though the latter still needs to authorize the query. Finally, we consider the scenario in which authorization can be enforced by the data owner \mathcal{D} without \mathcal{D} learning the policy, a setting that arises in court-issued search warrants.

We extend the OXT protocol of Cash et al. to support arbitrary boolean queries in all of the above models while withstanding adversarial non-colluding servers (\mathcal{D} and \mathcal{E}) and arbitrarily malicious clients, and while preserving the remarkable performance of the protocol.

1. INTRODUCTION

Consider a database DB composed of collection of documents or records and an application that needs to search DB based on the keywords contained in these records. For example, DB can be a medical relational database with records indexed by a set of attributes (e.g., name, zipcode, medical condition, etc.), an email repository indexed by English words and/or envelope information (date, sender, receivers, etc.), a collection of webpages indexed by text and metadata, etc. A search query consists of a boolean expression on keywords that returns all documents whose associated keywords satisfy that expression. In this paper we are concerned with applications where the database is outsourced to an external server \mathcal{E} and search is performed at \mathcal{E} *privately*. That is, \mathcal{E} stores an encrypted version of the original database DB (plus some metadata) and answers encrypted queries from clients such that the client obtains the documents matching his query without \mathcal{E} learning plaintext information about the data and queries.

The most basic setting of private data outsourcing as described above is where the owner of the data itself, \mathcal{D} , is the party performing the search at \mathcal{E} . In this setting, \mathcal{D} initially processes DB into an encrypted database EDB and sends it to \mathcal{E} . \mathcal{D} only keeps a set of cryptographic keys that allows her to later run encrypted searches on \mathcal{E} and decrypt the matching documents returned by \mathcal{E} . This setting is known as *searchable symmetric encryption (SSE)* and has been studied extensively [29, 15, 16, 10, 13, 11, 24]. While most of the research has focused on single-keyword searches (i.e., return all documents containing a given keyword), recently Cash et al. [9] provided the first SSE solution, the OXT protocol, that can support in a practical and private way arbitrary boolean queries on sets of keywords and in very large DBs. The leakage to \mathcal{E} , which is formally specified and proven in [9], is in the form of data-access and query patterns, never as direct exposure of plaintext data or searched values.

In this work we are concerned with richer outsourcing scenarios where multiple third parties (clients) access the data at \mathcal{E} but only through queries authorized by the data owner \mathcal{D} . For example, consider a hospital outsourcing an (encrypted) database to an external service \mathcal{E} such that clients (doctors, administrators, insurance companies, etc.) can search the database but only via queries authorized according to the hospital's policy and without these clients learning information on non-matching documents. As before, \mathcal{E} should learn as little as possible about data and queries.

In this multi-client scenario (to which we refer as *MC-SSE*), \mathcal{D} provides search tokens to clients based on their

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queries and according to a given authorization policy. Security considers multiple clients acting maliciously and possibly colluding with each other (trying to gain information beyond what they are authorized for) and a semi-trusted server \mathcal{E} which acts as “honest-but-curious” but does not collude with clients. Extending SSE solutions to the multi-client scenario is straightforward when (a) search tokens are fully determined by the query and (b) the SSE protocol does not return false positives (returning false positives, i.e. documents that do not match a query, is allowed in SSE since the recipient in that case is the owner of the data but not in the multi-client setting where clients are not allowed to learn data they were not authorized for). In such cases, \mathcal{D} would receive the client’s query, generate the corresponding SSE search tokens as if \mathcal{D} herself was searching the database, and provide the tokens to the client together with a signature that \mathcal{E} can check before processing the search. However, for enabling general boolean queries, the SSE OXT protocol of [9] requires a number of tokens that is not known a-priori (it depends on the searched data, not only on the query) and therefore the above immediate adaptation does not work.

Our first contribution is in extending the OXT protocol from [9] to the MC-SSE setting while preserving its full boolean-query capabilities and performance. In this extension, \mathcal{D} provides the client \mathcal{C} with a set of query-specific trapdoors which the client can then transform into search tokens as required by OXT. The set of trapdoors given to \mathcal{C} is fully determined by the query and independent of the searched data. An additional subtle technical challenge posed by OXT is how to allow \mathcal{E} to verify that the search tokens presented by \mathcal{C} are authorized by \mathcal{D} . The simple solution is for \mathcal{D} to sign the trapdoors, however in OXT these trapdoors need to be hidden from \mathcal{E} (otherwise \mathcal{E} can learn information about unauthorized searches) so a simple signature on them cannot be verified by \mathcal{E} . Our solution uses a *homomorphic signature* by \mathcal{D} on the trapdoors that \mathcal{C} can then transform homomorphically into signatures on the search tokens. We show that forging the tokens or their signatures is infeasible even by fully malicious clients.

The resulting MC-OXT protocol preserves the full functional properties of OXT, namely support for arbitrary boolean queries, the same level of privacy (i.e., same leakage profile) with respect to \mathcal{E} , and the same remarkable performance. Privacy with respect to clients is near-optimal (see Section 3.1 for why such leakage may be inevitable) with leakage confined only to information on the number of documents matching one of the query terms (typically, the least-frequent term).

Next, we extend the MC-OXT protocol to an even more challenging setting we call Outsourced Symmetric Private Information Retrieval (OSPIR), where on top of the MC-SSE requirements, one asks that *client queries be hidden from \mathcal{D}* - similarly to the Private Information Retrieval (PIR) primitive. This requirement arises in important outsourcing scenarios. In the medical database example mentioned above, the hospital authorizes doctors or other parties to search the medical database according to certain policy; however, in some cases the actual query values are to be kept secret from the hospital itself (due to privacy, liability and regulatory requirements). Only the minimal information for determining the compliance of a query to the policy should be disclosed to the hospital. For example, the policy may indicate that only conjunctions with a minimal number

of terms are allowed or that the query needs to include at least three of a set of attributes, etc. In such a case, there is no need for the hospital to learn the particular values being searched (such as a specific last name or medical condition). In other cases, as in outsourced patent or financial information search, the provider \mathcal{D} may want to enforce that a client \mathcal{C} pays for the type of query it is interested in but \mathcal{C} wants to keep his query hidden from both \mathcal{D} and \mathcal{E} . Applications to intelligence scenarios are discussed in [18] (see also [32]).

Thus, we relax the query privacy requirement with respect to \mathcal{D} to allow for minimal information needed for \mathcal{D} to determine policy compliance. Specifically, we consider the case where keywords are formed by pairs of attribute-values. For example, in a relational database, attributes are defined by the database columns (e.g., SSN, name, citizenship, etc.), while in an email repository attributes can refer to envelope information such as sender and receivers or to the message body (in which case the values are, say, English words). In this case, a policy defines the class of boolean expressions allowed for a given client and the attributes that may be used as inputs into these expressions. In order to enforce the policy, \mathcal{D} learns the boolean expression and attributes but nothing about the searched values. For policies defined via classes of attributes (e.g. allowing any attribute from the set of attributes {name, city, zipcode}) leakage to \mathcal{D} can be further reduced by revealing the class and not the specific attributes in the query.

Our most advanced result is extending the OXT protocol to the above OSPIR setting. The resultant protocol, OSPIR-OXT, adds some crucial new ingredients to OXT: It uses *oblivious PRFs* (OPRF) for hiding the query values from \mathcal{D} , uses attribute-specific keys for enforcing policy compliance, and uses homomorphic signatures (or the more general abstraction of *shared OPRFs*) for query verification by \mathcal{E} . A further extension of the protocol accommodates an external policy manager, e.g., a judge in a warrant-based search, who checks policy compliance and allows server \mathcal{D} to enforce the policy without learning the attributes being searched.

Performance-wise our extensions to OXT preserve the protocol’s performance in both pre-processing (creating EDB) and search phases. OSPIR-OXT adds to the computational cost by adding a few exponentiations but these are generally inexpensive relative to the I/O cost (especially thanks to common-base exponentiation optimizations). The protocols we provide for MC-SSE and OSPIR models support encrypted search over database containing tens of billions record-keyword pairs, for example a full snapshot of English Wikipedia or a 10-TByte, 100M-record US-census database (see Sections 4.3 and 4.4).

We achieve provable security against adaptive adversarial honest-but-curious server \mathcal{E} , against arbitrarily malicious (but non-colluding¹ with \mathcal{E}) server \mathcal{D} , and against arbitrarily malicious clients. Our security models extend the SSE model [13, 11, 9] to the more complex settings of MC-SSE and OSPIR. In all cases security is defined in the real-vs-ideal model and is parametrized by a specified leakage function $\mathcal{L}(\text{DB}, \mathbf{q})$. A protocol is said to be secure with leakage profile $\mathcal{L}(\text{DB}, \mathbf{q})$ against adversary \mathcal{A} if the actions of \mathcal{A} on adversarially-chosen input DB and queries set \mathbf{q} can be simulated with access to the leakage information $\mathcal{L}(\text{DB}, \mathbf{q})$ only

¹See Section 5.1.

(and not to DB or \mathbf{q}). This allows modeling and bounding partial leakage allowed by SSE protocols. It means that even an adversary that has full information about a database, or even chooses it, does not learn anything from the protocol execution other than what can be derived solely from the defined leakage profile.

Related work: Searchable symmetric encryption (SSE) has been extensively studied [29, 15, 16, 10, 13, 11, 24] (see [13, 11] for more on related work). Most SSE research focused on single-keyword search, and after several solutions with complexity linear in the database size, Curtmola et al. [13] present the first solution for single-keyword search whose complexity is linear in the number of matching documents. They also improve on previous security models, in particular by providing an adaptive security definition and a solution in this model.

Extending single-keyword SSE to search by conjunctions of keywords was considered in [16, 7, 2], but all these schemes had $O(|DB|)$ search complexity. The first SSE which can handle very large DBs and supports conjunctive queries is the OXT protocol discussed above, given by Cash et al. [9]. The MC-SSE and OSPIR schemes we present are based on this protocol and they preserve its performance and privacy characteristics.

Extension of the two-party client-server model of SSE to the multi-client setting was considered by Curtmola et al. [13], but their model disallowed per-query interaction between the data owner and the client, leading to a relatively inefficient implementation based on broadcast encryption. Multi-client SSE setting which allows such interaction was considered by Chase and Kamara [11] as SSE with “controlled disclosure”, and by Kamara and Lauter [23], as “virtual private storage”, but both considered only single-keyword queries and did not support query privacy from the data owner. De Cristofaro et al. [12] extended multi-client SSE to the OSPIR setting, which supports query privacy, but only for the case of single-keyword queries. In recent independent work, Pappas et al. [27] provide support for boolean queries in a setting similar to our OSPIR setting (but with honest-but-curious clients).

SSE schemes which support efficient updates of the encrypted database appeared in [30, 24] for single-keyword SSE. The OXT SSE scheme of [9] which supports arbitrary boolean queries, has been extended to the dynamic case in [8], and the same techniques apply to the MC-SSE and OSPIR schemes presented in this paper.

Recently Islam et al. [19] showed that frequency analysis revealed by access control patterns in SSE schemes can be used to predict single-keyword queries. Such attacks, although harder to stage, are possible for conjunctive queries as well, but the general masking and padding countermeasures suggested in [19] are applicable to the MC-OXT and OSPIR-OXT protocols.

In other directions, SSE was extended to the *public key* setting, allowing any party to encrypt into the database, first for single-keyword search [5, 31, 1, 3, 6, 28], and later for conjunctive queries as well [6], but all these PKSE schemes have $O(|DB|)$ search complexity. Universally composable SSE was introduced by [25], also with $O(|DB|)$ search complexity.

Multi-client SSE and OSPIR models are related to the work on multi-client ORAM, e.g. see the recent work of Huang and Goldberg [17], which aims for stronger privacy

protection of client’s queries from server \mathcal{E} , but multi-client ORAM supports DB lookups by (single) indexes instead of (boolean formulas on) keywords, and they can currently support much smaller DB sizes.

Paper organization. We first present our protocols for the case of conjunctive queries: in Section 2 we recall the basic OXT protocol [9], suitably reformulated for our generalizations, in Section 3 we address the multi-client SSE model, and in Section 4 we handle the OSPIR model. In Section 4.2 we explain how to extend support for general boolean queries. Our security models and claims are presented concisely in Section 5 — a complete treatment is deferred to the full version [20]. While the main implementation details and performance analysis is deferred to a companion paper [8], we provide some information on computational cost and performance measurements from our implementation in Section 4.3 and 4.4, respectively.

2. SSE AND THE OXT PROTOCOL

We first recall the SSE OXT protocol from [9] that forms the basis for our solution to searchable encryption in the more advanced MC and OSPIR models.

SSE protocols and formal setting [9]. Let λ be a security parameter. A database $DB = (\text{ind}_i, W_i)_{i=1}^d$ is a list of identifier and keyword-set pairs, where $\text{ind}_i \in \{0, 1\}^\lambda$ is a document identifier and $W_i \subseteq \{0, 1\}^*$ is a list of keywords in that document. We set W to $\bigcup_{i=1}^d W_i$. A *query* $\psi(\bar{w})$ is specified by a tuple of keywords $\bar{w} \in W^*$ and a boolean formula ψ on \bar{w} . We write $DB(\psi(\bar{w}))$ for the set of identifiers of documents that “satisfy” $\psi(\bar{w})$. Formally, this means that $\text{ind}_i \in DB(\psi(\bar{w}))$ iff the formula $\psi(\bar{w})$ evaluates to true when we replace each keyword w_j with true or false depending on if $w_j \in W_i$ or not (in particular $DB(w) = \{\text{ind}_i \text{ s.t. } w \in W_i\}$). Below we let d denote the number of records in DB, $m = |W|$, and $N = \sum_{w \in W} |DB(w)|$.

A *searchable symmetric encryption (SSE) scheme* Π consists of an algorithm EDBSetup and a protocol Search fitting the following syntax. EDBSetup takes as input a database DB and a list of document decryption keys RDK, and outputs a secret key K along with an encrypted database EDB. The search protocol proceeds between a *client* \mathcal{C} and *server* \mathcal{E} , where \mathcal{C} takes as input the secret key K and a query $\psi(\bar{w})$ and \mathcal{E} takes as input EDB. At the end of the protocol \mathcal{C} outputs a set of (ind, rdk) pairs while \mathcal{E} has no output. We say that an SSE scheme is *correct* if for all DB, RDK and all queries $\psi(\bar{w})$, for $(K, \text{EDB}) \leftarrow \text{EDBSetup}(DB, \text{RDK})$, after running Search with client input $(K, \phi(\bar{w}))$ and server input EDB, the client outputs $DB(\phi(\bar{w}))$ and $\text{RDK}[DB(\phi(\bar{w}))]$ where $\text{RDK}[S]$ denotes $\{\text{RDK}[\text{ind}] \mid \text{ind} \in S\}$. Correctness can be statistical (allowing a negligible probability of error) or computational (ensured only against computationally bounded attackers - see [9]).

Note (conjunctive vs. Boolean queries). Throughout the paper we present our protocols for the case of conjunctive queries where a query consists of n keywords $\bar{w} = (w_1, \dots, w_n)$ and it returns all documents containing all these keywords. The adaptation to the case of boolean queries is described in Section 4.2.

Note (the array RDK). Our SSE syntax, and the OXT description in Figure 1, includes as input to EDBSetup an array RDK that contains, for each document in DB, a key rdk used

to encrypt that document. When a client retrieves the index ind of a document matching its query, it also retrieves the *record-decrypting key* rdk needed to decrypt that record. This mechanism is not strictly needed in the SSE setting (where rdk could be derived from ind using a PRF with a secret key known to \mathcal{C}) and it is not part of the original OXT in [9], but it is needed in the more advanced models considered later. This extension does not change the functionality and security properties of OXT as analyzed in [9]).

Note (retrieval of matching encrypted records). Our formalism defines the output of the SSE protocol as the set of ind identifiers pointing to the encrypted records matching the query, together with the associated record decryption key. For the sake of generality, we do not model the processing and retrieval of encrypted records. This allows us to decouple the storage and processing of document payloads (which can be done in a variety of ways, with varying types of leakage) from the storage and processing of the metadata, which is the focus of our protocols.

SSE Security. The SSE setting considers security w.r.t. an adversarial server \mathcal{E} , hence security is parametrized via a leakage function capturing information learned by \mathcal{E} from the interaction with \mathcal{C} . See Section 5.

2.1 The OXT Protocol

The OXT protocol [9] is presented in Figure 1; see [9] for full design rationale and analysis. Here we provide a high level description as needed for the extensions to this protocol we introduce in the following sections.

The basis of OXT is the following simple search algorithm over *unencrypted* databases. The algorithm uses two types of data structures. First, for every keyword w there is an inverted index (a list) I_w pointing to the indices ind of all documents that contain w . Then, for every document ind there is a list L_{ind} of all keywords contained in document ind . To search for a conjunction $\bar{w} = (w_1, \dots, w_n)$, the client chooses the estimated least frequent keyword² in \bar{w} , say w_1 , and checks for each $\text{ind} \in I_{w_1}$ whether $w_i \in L_{\text{ind}}$, $i = 2, \dots, n$. If this holds for all $2 \leq i \leq n$ then ind is added to the result set. As a performance optimization, instead of maintaining a list L_{ind} for each ind , one can fix a hash function f and keep a data structure representing the set $X = \{f(w, \text{ind}) : w \in W, \text{ind} \in \text{DB}(w)\}$. Thus, the check $w \in L_{\text{ind}}$ can be replaced with the check $f(w, \text{ind}) \in X$. Protocol OXT adapts this algorithm to the encrypted setting as follows (we start with the description of a simplified version, corresponding to protocol BXT in [9], and then move to the more specific details of OXT).

For each keyword $w \in W$ an inverted index (corresponding to I_w above), referred to as $\text{TSet}(w)$, is built pointing to all the ind values of documents in $\text{DB}(w)$. Each $\text{TSet}(w)$ is identified by a string called $\text{stag}(w)$ and ind values in $\text{TSet}(w)$ are encrypted under a secret key K_e . Both $\text{stag}(w)$ and K_e are computed as a PRF applied to w with secret keys known to \mathcal{C} only. In addition, a data structure called XSet is built as an “encrypted equivalent” of the above set X as follows. First, for each $w \in W$, a value $\text{xtrap}(w) = F(K_X, w)$ is computed where K_X is a secret PRF key then for each $\text{ind} \in \text{DB}(w)$ a value $\text{xtag} = f(\text{xtrap}(w), \text{ind})$ is added to XSet where f is an unpredictable function of its inputs (e.g.,

f can be a PRF used with $\text{xtrap}(w)$ as the key and ind as input). The output EDB from the EDBSetup phase includes $\text{TSet} = \{\text{TSet}(w)\}_{w \in W}$ and the set XSet . In the *Search* protocol for a conjunction (w_1, \dots, w_n) , the client \mathcal{C} chooses the conjunction’s s-term (i.e., the estimated least frequent keyword in the conjunction, which we assume to be w_1), computes $\text{stag}(w_1)$ and K_e using \mathcal{C} ’s secret keys and computes $\text{xtrap}_i = F(K_X, w_i)$ for each $i = 2, \dots, n$. It then sends $(K_e, \text{stag}, \text{xtrap}_2, \dots, \text{xtrap}_n)$ to the server \mathcal{E} . \mathcal{E} uses stag to retrieve $\text{TSet}(w_1)$, uses K_e to decrypt the ind values in $\text{TSet}(w_1)$, and sends back to \mathcal{C} those ind for which $f(\text{xtrap}_i, \text{ind}) \in \text{XSet}$ for all $i = 2, \dots, n$.

The OXT protocol from Figure 1 follows the above logic but instantiates it in a way that minimizes leakage to \mathcal{E} . Rather than assuming a specific implementation of TSet , [9] abstracts this data structure through an API that we adopt here. Specifically, the abstract TSetSetup operation receives a collection \mathbf{T} of lists $\mathbf{t}(w)$ for each $w \in W$ and builds the TSet data structure out of these lists; it returns TSet and a key K_T . Then, $\text{TSetRetrieve}(\text{TSet}, \text{stag}(w))$ instantiates the retrieval of a $\text{TSet}(w)$ via its handle $\text{stag}(w)$ which is computed by a function $\text{TSetGetTag}(K_T, w)$ (typically a PRF). The elements in the $\mathbf{t}(w)$ lists are called *tuples* and their contents are defined by the OXT protocol. A TSet implementation provides two crucial security properties [9]: *privacy* in that the TSet datastructure does not reveal anything about the tuple lists in \mathbf{T} except their summary length $\sum_w |\mathbf{T}[w]|$; and *correctness* in that (except for negligible probability) $\text{TSetRetrieve}(\text{TSet}, \text{stag})$ returns $\mathbf{T}[w]$ for $\text{stag} = \text{TSetGetTag}(K_T, w)$, and it returns an empty set for all other stag values.

Next, we note that using the protocol described above leads to significant leakage in that the xtrap value allows \mathcal{E} to check whether $\text{xtag} = f(\text{xtrap}, \text{ind}) \in \text{XSet}$ for each value ind ever seen by \mathcal{E} , revealing correlation statistics between each s-term and each x-term ever queried by \mathcal{C} . This motivates the main mechanism in OXT, i.e. the instantiation of the function f via a two-party computation in which \mathcal{E} inputs an encrypted value ind , \mathcal{C} inputs xtrap and the ind -decryption key, and \mathcal{E} gets the value of $\text{xtag} = f(\text{xtrap}, \text{ind})$ without learning either the xtrap or ind values themselves. For this OXT uses a blinded DH computation over a group G (with generator g of prime order p). However, to avoid the need for interaction between \mathcal{E} and \mathcal{C} in the *Search* phase, the *blinding factors are pre-computed and stored as part of the tuples in the TSet lists*. Specifically, indexes ind are replaced in the computation of f with dedicated per-record values $\text{xind} \in Z_p^*$ (computed as $F_p(K_I, \text{ind})$ where F_p is a PRF with range Z_p^* , $\text{xtrap}(w)$ ’s are implemented as $g^{F_p(K_X, w)}$ (K_I and K_X are secret keys kept by \mathcal{C}), and xtag is re-defined as $(\text{xtrap}(w))^{\text{xind}}$. The blinding factor in the underlying two-party computation is pre-computed during EDBSetup and stored in the TSet . Namely, each tuple corresponding to a keyword w and document index ind contains a blinded value $y_c = \text{xind} \cdot z_c^{-1}$ for $\text{xind} = F_p(K_I, \text{ind})$ where z_c is an element in Z_p^* derived (via a PRF) from w and a tuple counter c (this counter, incremented for each tuple in the tuple list associated with w , ensures independence of each blinding value z_c).

During search, the server \mathcal{E} needs to compute the xtag values $g^{F_p(K_X, w_i) \cdot \text{xind}}$ for each xind in $\text{TSet}(w_1)$ and then test these for membership in XSet . To enable this the client sends, for the c -th tuple in \mathbf{t} , an n -long array $\text{xtoken}[c]$ de-

²The estimated least frequent keyword is called the conjunction’s s-term; the other terms in a conjunction are called x-terms.

EDBSetup(DB, RDK)

Key Generation. \mathcal{D} picks key K_S for PRF F_τ and keys K_T, K_X, K_I for PRF F_p . F_τ and F_p are PRF's which output strings in respectively $\{0, 1\}^\tau$ and Z_p^* , and τ is a security parameter.

- Initialize XSet to an empty set, and initialize \mathbf{T} to an empty array indexed by keywords from W .
- For each $w \in W$, build the tuple list \mathbf{t} and insert elements into set XSet as follows:
 - Initialize \mathbf{t} to be an empty list.
 - Set $\text{strap} \leftarrow F_\tau(K_S, w)$ and $(K_z, K_e) \leftarrow (F_\tau(\text{strap}, 1), F_\tau(\text{strap}, 2))$.
 - Initialize $c \leftarrow 0$; then for all ind in $\text{DB}(w)$ in random order:
 - * Set $\text{rdk} \leftarrow \text{RDK}(\text{ind})$, $\mathbf{e} \leftarrow \text{Enc}(K_e, (\text{ind}|\text{rdk}))$, $\text{xind} \leftarrow F_p(K_I, \text{ind})$.
 - * Set $c \leftarrow c + 1$, $z_c \leftarrow F_p(K_z, c)$, $y \leftarrow \text{xind} \cdot z_c^{-1}$. Append (\mathbf{e}, y) to \mathbf{t} .
 - * Set $\text{xtag} \leftarrow g^{F_p(K_X, w) \cdot \text{xind}}$ and add xtag to XSet.
 - $\mathbf{T}[w] \leftarrow \mathbf{t}$.
- Create $(\text{TSet}, K_T) \leftarrow \text{TSetSetup}(\mathbf{T})$, and output key $K = (K_S, K_X, K_T, K_I)$ and $\text{EDB} = (\text{TSet}, \text{XSet})$.

Search protocol

Client \mathcal{C} on input K defined as above and a conjunctive query $\bar{w} = (w_1, \dots, w_n)$:

- Sets $\text{stag} \leftarrow \text{TSetGetTag}(K_T, w_1)$; $\text{strap} \leftarrow F_\tau(K_S, w_1)$, $(K_z, K_e) \leftarrow (F_\tau(\text{strap}, 1), F_\tau(\text{strap}, 2))$.
- Sends to the server \mathcal{E} the message $(\text{stag}, \text{xtoken}[1], \text{xtoken}[2], \dots)$ where $\text{xtoken}[\cdot]$ are defined as:
 - For $c = 1, 2, \dots$, until \mathcal{E} sends **stop**:
 - * Set $z_c \leftarrow F_p(K_z, c)$ and set $\text{xtoken}[c, i] \leftarrow g^{F_p(K_X, w_i) \cdot z_c}$ for $i = 2, \dots, n$.
 - * Set $\text{xtoken}[c] \leftarrow (\text{xtoken}[c, 2], \dots, \text{xtoken}[c, n])$.

Server \mathcal{E} on input $\text{EDB} = (\text{TSet}, \text{XSet})$ responds as follows:

- Retrieve $\mathbf{t} \leftarrow \text{TSetRetrieve}(\text{TSet}, \text{stag})$ from TSet.
- For $c = 1, \dots, |\mathbf{t}|$ do:
 - Retrieve (\mathbf{e}, y) from the c -th tuple in \mathbf{t}
 - If $\forall i = 2, \dots, n : \text{xtoken}[c, i]^{y_c} \in \text{XSet}$ then send \mathbf{e} to client \mathcal{C} .
- When last tuple in \mathbf{t} is reached, sends **stop** to \mathcal{C} and halt.

For each received \mathbf{e} client \mathcal{C} computes $(\text{ind}|\text{rdk}) \leftarrow \text{Dec}(K_e, \mathbf{e})$ and outputs (ind, rdk) .

Figure 1: OXT: OBLIVIOUS CROSS-TAGS SSE SCHEME

defined by $\text{xtoken}[c, i] := g^{F_p(K_X, w_i) \cdot z_c}$, $i = 1, \dots, n$, where z_c is the precomputed blinding derived by \mathcal{C} from w (via a PRF) and the tuple counter c . \mathcal{E} then performs the T-set search to get the results for w_1 , and for each c it filters the c -th result by testing if $\text{xtoken}[c, i]^{y_c} \in \text{XSet}$ for all $i = 2, \dots, n$. This protocol is correct because $\text{xtoken}[c, i]^{y_c} = g^{F_p(K_X, w_i) \cdot z_c \cdot \text{xind} \cdot z_c^{-1}} = g^{F_p(K_X, w_i) \cdot \text{xind}}$, meaning that the server correctly recomputes the pseudorandom values in the XSet. Putting these ideas together results in the OXT protocol of Figure 1. Note that \mathcal{C} sends the xtoken arrays (each holding several values of the form $g^{F_p(K_X, w_i) \cdot z_c}$) until instructed to stop by \mathcal{E} . There is no other communication from server to client (alternatively, server can send the number of elements in $\text{TSet}(w)$ to the client who will respond with such number of xtoken arrays).

Note. The OXT protocol in Figure 1 derives keys K_e, K_z slightly differently than in the OXT description of [9]. The modified key derivation is closer to what we need for MC-OXT and OSPIR-OXT protocols presented in the following sections, without affecting the functionality or security of OXT.

3. MULTI-CLIENT SSE

We present an extension of the OXT protocol for the *multi-client SSE (MC-SSE)* setting described in the introduction and in more detail below. The extension preserves the functionality of OXT, supporting any boolean query, and superb performance, while securely serving multiple clients, all of which can behave maliciously.

Multi-Client SSE Setting. In MC-SSE there is the owner \mathcal{D} of the plaintext database DB, an external server \mathcal{E} that holds the encrypted database EDB, and clients that receive tokens from \mathcal{D} in order to perform search queries at \mathcal{E} . In other words, \mathcal{D} is outsourcing her search service to a third party but requires clients to first obtain search tokens from her. Her goal is to ensure service to clients via \mathcal{E} while leaking as little as possible information to \mathcal{E} about the plaintext data and queries, and preventing clients from running any other DB queries than those for which \mathcal{D} issued them a token. This is a natural outsourcing setting of increasing value in cloud-based platforms, and it was described by Chase and Kamara [11] as an *SSE with controlled disclosure*.

Formally, the MC-SSE setting changes the syntax of an SSE scheme by including an additional algorithm **GenToken**

which on input the secret key K , generated by the data owner \mathcal{D} in the **EDBSetup** procedure, and a boolean query $\psi(\bar{w})$, submitted by client \mathcal{C} , generates a search-enabling value **token**. Then, procedure **Search** is executed by server \mathcal{E} on input **EDB**, but instead of the client \mathcal{C} running on input K and query $\psi(\bar{w})$ (as in SSE), \mathcal{C} runs on input consisting only of the search token **token**. Correctness is defined similarly to the SSE case, namely, assuring (except for negligible error probability) that \mathcal{C} 's output sets $\text{DB}(\psi(\bar{w}))$ and $\text{RDK}[\text{DB}(\psi(\bar{w}))]$. Security is treated in Section 5.

3.1 The MC-OXT Protocol

We describe the changes to OXT from Figure 1 needed to support boolean queries in the MC-SSE setting. As before, the protocol is described for conjunctions with the adaptation to boolean queries described in Section 4.2.

EDBSetup(DB, RDK). This pre-processing phase is identical to the one in OXT except for the addition of a key K_M shared between \mathcal{D} and \mathcal{E} . The output from this phase is $K = (K_S, K_X, K_T, K_M)$ kept by \mathcal{D} and $\text{EDB} = (K_M, \text{TSet}, \text{XSet})$ stored at \mathcal{E} .

GenToken(K, \bar{w}). This is the new MC-specific phase in which \mathcal{D} , using key K , authorizes \mathcal{C} for a conjunction $\bar{w} = w_1, \dots, w_n$ and provides \mathcal{C} with the necessary tokens to enable the search at \mathcal{E} . We assume w_1 to be the s-term (and chosen by \mathcal{D} who has knowledge of term frequencies). Specifically, \mathcal{D} performs the following operations. She sets $\text{stag} \leftarrow \text{TSetGetTag}(K_T, w_1)$ and $\text{strap} \leftarrow F_\tau(K_S, w_1)$, same as \mathcal{C} does in OXT. Then, for $i = 2, \dots, n$, she picks $\rho_i \leftarrow Z_p^*$ and sets $\text{bxtrap}_i \leftarrow g^{F_p(K_X, w_i) \cdot \rho_i}$. Finally, she sets $\text{env} \leftarrow \text{AuthEnc}(K_M, (\text{stag}, \rho_2, \dots, \rho_n))$ and outputs $\text{token} = (\text{env}, \text{strap}, \text{bxtrap}_2, \dots, \text{bxtrap}_n)$ (which \mathcal{C} uses in the search phase).

To see how this enables search as in OXT, first note that with $\text{xtrap}_i = g^{F_p(K_X, w_i)}$, $i = 2, \dots, n$, the client can produce the values $g^{F_p(K_X, w_i) \cdot z_c}$ needed in the **Search** phase of OXT. Hence, \mathcal{D} could just provide the xtrap_i values to \mathcal{C} . However, \mathcal{D} needs to be able to sign (or MAC) these values so that \mathcal{E} can check that \mathcal{C} is authorized to this query and, e.g., did not truncate a conjunction or mix parts from different queries. Signing the plain xtrap values does not work since these values must not be seen by \mathcal{E} (it would allow \mathcal{E} to learn information from unauthorized searches). The solution is to provide \mathcal{C} with a *homomorphic signature* that \mathcal{C} can convert into individual signatures for all tokens sent to \mathcal{E} . This is accomplished as follows: \mathcal{D} picks one-time blinding factors ρ_2, \dots, ρ_n and provides \mathcal{C} with *blinded* (or MAC'ed) xtrap values $\text{bxtrap}_i = \text{xtrap}_i^{\rho_i}$ for $j = 2, \dots, n$, while providing the blinding factors (ρ_2, \dots, ρ_n) to \mathcal{E} in an encrypted and authenticated envelope env . To produce $g^{F_p(K_X, w_i) \cdot z_c}$ during **Search**, \mathcal{C} will compute $\text{bxtrap}_i^{z_c}$ and \mathcal{E} will raise this value to $1/\rho_i$. Security relies on the fact that if \mathcal{C} provides \mathcal{E} with values other than those given by \mathcal{D} , then when raised to $1/\rho_i$ by \mathcal{E} (where ρ_i is random and unknown to \mathcal{C}) the resulting values will not correspond to elements of XSet except with negligible probability.

Search Protocol. The **Search** protocol reflects the above changes: On $\text{token} = (\text{env}, \text{strap}, \text{bxtrap}_2, \dots, \text{bxtrap}_n)$, \mathcal{C} computes (K_z, K_e) from strap as in OXT. Then, it sends to \mathcal{E} the value env as well as the sequence $\text{bxtoken}[1], \text{bxtoken}[2], \dots$ which contains the same values as $\text{xtoken}[1], \text{xtoken}[2], \dots$ in OXT up to the blinding exponents ρ_i . Specifically, the values $\text{bxtoken}[c, i]$,

for $i = 2, \dots, n$, are computed by \mathcal{C} as $(\text{bxtrap}_i)^{z_c}$. On the receiving side, \mathcal{E} verifies the authenticity of env and decrypts it to find stag , which it uses to retrieve $\text{TSet}(w_1)$, and ρ_2, \dots, ρ_n . The only change from OXT is that the operation $\text{xtoken}[c, i]^y$ is replaced with $\text{bxtoken}[c, i]^{y/\rho_i}$.

Note (masking the size of $\text{TSet}(w_1)$). MC-OXT leaks to \mathcal{C} the size of $\text{TSet}(w_1) = \text{DB}(w_1)$ given by the number of bxtoken vectors requested by \mathcal{E} . Note that the exact size of this set can easily be masked by \mathcal{E} requesting more bxtoken values from \mathcal{C} than needed. We observe that some form of leakage on the frequency of the least frequent term in the conjunction appears to be inherent even for plaintext search algorithms. Indeed, it is likely (though there seem to be no proven lower bounds) that running time will be noticeably different for conjunctions with all terms being infrequent from the case that all terms are very frequent, except if short searches are artificially padded to full database size (or if conjunctions are pre-computed). Two considerations in masking the size of $\text{TSet}(w_1)$ are that (i) the masked size should be chosen as a step function of $|\text{TSet}(w_1)|$ (and not, say, a fixed linear function); (ii) During search, \mathcal{E} should return to \mathcal{C} all results matching a query only after \mathcal{E} received all the bxtoken vectors from \mathcal{C} ; indeed, sending the results as soon as they are found to match the query would leak information on $|\text{TSet}(w)|$ to \mathcal{C} (since no ind 's will be returned after \mathcal{C} sends $|\text{TSet}(w)|$ tokens). In the full version [20] we show a strategy applied by \mathcal{D} during **EDBSetup** to allow \mathcal{E} to send results as soon as they are found while avoiding the above leakage.

4. OUTSOURCED SYMMETRIC PIR

The OSPIR (for Outsourced Symmetric PIR) setting augments the MC-SSE setting with an additional requirement: The database owner \mathcal{D} should learn as little as possible about queries performed by clients while still being able to verify the compliance of these queries to her policy. Here we extend MC-OXT to this setting by augmenting the token generation component **GenToken** to support “blinding” by the client of query requests sent to \mathcal{D} , and adding a mechanism for \mathcal{D} to enforce policy-compliance of the query when only having access to their blinded versions. OSPIR-OXT supports *attribute-based policies* where \mathcal{D} learns information about query attributes but nothing about values (e.g., \mathcal{D} may learn that a query includes a last-name, a zipcode and two words from a text field but nothing about the actual queried keywords). The security model adds \mathcal{D} as a new adversarial entity trying to learn \mathcal{C} 's hidden query values. Refer to the introduction for more discussion about the OSPIR setting and attribute-based policies.

OSPIR SSE Syntax. An OSPIR-SSE scheme replaces the **GenToken** procedure which in MC-SSE is executed by the data owner \mathcal{D} on the cleartext client's query \bar{w} , with a two-party protocol between \mathcal{C} and \mathcal{D} that allows \mathcal{C} to compute a search-enabling token without \mathcal{D} learning \bar{w} . In addition, \mathcal{D} should be able to enforce an attribute-based query-authorization policy on these queries. For this, we assume that keyword set W is partitioned into m *attributes*, and let $I(w)$ denote the attribute of keyword w .³ An attribute-based policy is represented by a set of attribute-sequences

³ We assume that the string representing w has its attribute encoded into it, i.e. $w = (i, \text{val})$ for $i = I(w)$, so that Ryan as a first name is distinguished from Ryan as a last name.

\mathcal{P} s.t. a conjunctive query $\bar{w} = (w_1, \dots, w_n)$ is *allowed by policy* \mathcal{P} if and only if the sequence of attributes $\text{av}(\bar{w}) = (I(w_1), \dots, I(w_n))$ corresponding to this query is an element in set \mathcal{P} . Using this notation, the goal of the **GenToken** protocol is to let \mathcal{C} compute **token** corresponding to its query \bar{w} only if $\text{av}(\bar{w}) \in \mathcal{P}$. Reflecting these goals, an OSPIR-SSE scheme is a tuple $\Sigma = (\text{EDBSetup}, \text{GenToken}, \text{Search})$ where **EDBSetup** is an algorithm run by \mathcal{D} on inputs (DB, RDK) with outputs (EDB, K) , **GenToken** is a protocol run by \mathcal{C} on input \bar{w} and by \mathcal{D} on input (\mathcal{P}, K) , with \mathcal{C} outputting **token** or \perp and \mathcal{D} outputting **av**, and **Search** is a protocol run by \mathcal{C} on input **token** and by \mathcal{E} on input **EDB**, with \mathcal{C} outputting a set of **ind**'s matching his query and the corresponding set of **rdk**'s.

4.1 The OSPIR-OXT Protocol

The OSPIR-OXT protocol addresses the above OSPIR setting by enhancing MC-OXT with query-hiding techniques that allow \mathcal{D} to authorize queries without learning the queried values. Most changes with respect to MC-OXT are in the **GenToken** protocol. **EDBSetup** remains mostly unchanged except for the implementation of the PRFs, and **Search** is essentially unmodified.

We introduce the two main tools used in the design of **GenToken**. First, instead of the use of regular PRFs for **stag** and **xtag** computations in OXT and MC-OXT, the OSPIR-OXT protocol uses an “oblivious PRF” (OPRF) computation between \mathcal{C} and \mathcal{D} . A PRF $F(K, w)$ is called *oblivious* [26] if there is a two-party protocol in which \mathcal{C} inputs w , \mathcal{D} inputs K , \mathcal{C} learns the value of $F(K, w)$ and \mathcal{D} learns nothing. A simple example is the Hashed DH OPRF which we use in our implementation of the OSPIR-OXT protocol, defined as $F(K, x) = H(x)^K$ where H is a hash function onto $G \setminus \{1\}$ where G is a group of prime order p , and K is chosen at random in Z_p^* . In this case, the OPRF protocol consists of \mathcal{C} sending $a = H(x)^r$ for random r in Z_p^* , \mathcal{D} sending back $b = a^K$ and \mathcal{C} computing $H(x)^K$ as $b^{1/r}$. The second tool used in **GenToken** is needed to enforce an *attribute-based policy* and guarantee that only queries on authorized attributes can generate valid tokens for search at \mathcal{E} . To enforce such policies we have \mathcal{D} use a different key for each possible attribute; for example, when a **stag** (or **xtag**) is requested for attribute ‘zipcode’ the key that \mathcal{D} inputs into the OPRF computation is different than the key used for attribute ‘name’ or attribute ‘text’. The point is that if \mathcal{C} claims to be querying zipcode but actually enters the keyword “Michael” into the OPRF computation, the output for \mathcal{C} will be the tag $F(K_{\text{zip}}, \text{“Michael”})$, where K_{zip} is a zipcode-specific key, which will match no tag stored at \mathcal{E} .

To obtain OSPIR-OXT we combine the above two tools with an authorization mechanism similar to the one used in MC-OXT via a homomorphic signature (using the ρ_i exponents) for binding together the n tokens corresponding to an n -term conjunctive query in a way that \mathcal{E} can verify. We describe the changes to MC-OXT (defined via Figure 1 and the modifications in Section 3) required by OSPIR-OXT. We first replace the PRF F_p used in computing **xtrap** and **xtag** values with a PRF F_G which maps w directly onto the group G generated by g , i.e. we set **xtrap** as $F_G(K_X, w)$ instead of $g^{F_p(K_X, w)}$, hence **xtag** = **(xtrap)**^{xind} will now be computed as $F_G(K_X, w)^{\text{xind}}$ instead of $g^{F_p(K_X, w) \cdot \text{xind}}$. We similarly replace the PRF F_τ used in computing the **strap** value with the PRF F_G , i.e. we set **strap** as $F_G(K_S, w)$ instead of $F_\tau(K_S, w)$.

(Since we use **strap** as a key to F_τ in deriving (K_z, K_e) , we assume that a PRF F_τ key can be extracted from a random group element.)

We also make a specific assumption on the implementation of the function **TSetGetTag** used to derive **stag**(w) value, i.e., the handle pointing to the set **TSet**(w) which is computed as **TSetGetTag**(K_T, w). First, we assume that **TSetGetTag** is implemented using PRF F_G . Second, to enable enforcement of attribute-based policies we assume that the key K_T in **TSetGetTag** is formed by an array of F_G keys $K_T = (K_T[1], \dots, K_T[m])$, where $K_T[i]$ is the key to be used only for keywords with attribute $I(w) = i$. For notational convenience we define a PRF F_G^m s.t. $F_G^m(K_T, w) = F_G(K_T[I(w)], w)$, and we set **stag**(w) = **TSetGetTag**(K_T, w) to $F_G^m(K_T, w)$. Since we explicitly handle the keys used in the **TSetGetTag** implementation we also need to modify the **TSet** API: We will initialize **TSet** as **TSet** \leftarrow **TSetSetup'**(**T**), where **T** indexes the tuple lists **t**(w) not by the keywords w but by the corresponding **stag**(w) values. (This API change does not affect existing **TSet** implementations [9] because they internally use **stag**(w) = **TSetGetTag**(K_T, w) to store the **t**(w) list.) The PRF we use in the computation of **xtag**'s will be similarly attribute-partitioned. Namely, K_X is also an array of m independent F_G keys $K_X = (K_X[1], \dots, K_X[m])$, the **xtrap** value for keyword w is defined as $F_G^m(K_X, w)$, and the **xtag** corresponding to keyword w and index **xind** is set to $(F_G^m(K_X, w))^{\text{xind}}$.

In OSPIR-OXT, there are two two-party protocols involved in the computation of F_G . In the first case, the protocol implements an OPRF computation in which \mathcal{C} enters an input w , \mathcal{D} enters a key K_S , and the output is $F_G(K_S, w)$ for \mathcal{C} and \perp for \mathcal{D} . In the second case, F_G^m is computed via a protocol, that we call a *shared OPRF* (S-OPRF), in which \mathcal{C} inputs w and $i = I(w)$, and \mathcal{D} enters a key K and additional input $\rho \in Z_p^*$; the output learned by \mathcal{D} is i , and the output learned by \mathcal{C} is $(F_G^m(K, x))^\rho = (F_G(K[i], x))^\rho$. Note that the pair of outputs $((F_G^m(K, x))^\rho, \rho)$ can be seen as a secret sharing of $F_G^m(K, x)$, hence the name *shared-OPRF*. OSPIR-OXT uses the OPRF protocol to let \mathcal{C} learn the **strap** value corresponding to the w_1 s-term, i.e. **strap** = $F_G(K_S, w_1)$, without \mathcal{D} learning w_1 . The S-OPRF protocol is used to let \mathcal{C} compute a *blinded stag* **bstag** = $[F_G^m(K_T, w_1)]^{\rho_1}$ and the *blinded xtraps* **bxtrap** _{i} = $[F_G^m(K_I, w_i)]^{\rho_i}$, for $i = 2, \dots, n$. The functionality of the blinding ρ_i is the same as in the case of MC-OXT, namely, as a form of homomorphic signature binding and authorizing **stag** and **xtrap**'s that \mathcal{E} can verify. As in MC-OXT, \mathcal{E} will receive the corresponding (de)blinding factors ρ_1, \dots, ρ_n in the authenticated envelope **env**.

To simplify the description of OSPIR-OXT, we assume that both OPRF and S-OPRF protocols take a single round of interaction between \mathcal{C} and \mathcal{D} , as is indeed the case for several efficient OPRF's of interest [14, 21], including the Hashed Diffie-Hellman OPRF [22] used in our implementation below. We denote \mathcal{C} 's initial computation in the OPRF protocol as $(a, r) \leftarrow \text{OPRF}.\mathcal{C}_1(x)$ (a is the value sent to \mathcal{D} and r is randomness used by \mathcal{C}), \mathcal{D} 's response computation as $b \leftarrow \text{OPRF}.\mathcal{D}(K, a)$, and \mathcal{C} 's local computation of the final output as $\text{OPRF}.\mathcal{C}_2(b, r)$. We use the corresponding notation in the case of S-OPRF, except that S-OPRF. \mathcal{D} takes as an input a triple (K, i, a) where i is an attribute and outputs a pair (b, ρ) . See below for a simple implementation of these procedures for the case of the Hashed Diffie-Hellman OPRF.

GenToken protocol

- Client \mathcal{C} , on input $\bar{w} = (w_1, \dots, w_n)$ where w_1 is chosen as s-term:
 - Compute $(a_s, r_s) \leftarrow \text{OPRF}.\mathcal{C}_1(w_1)$, and $(a_i, r_i) \leftarrow \text{S-OPRF}.\mathcal{C}_1(w_i)$ for each $i = 1, \dots, n$.
 - Send (a_s, a_1, \dots, a_n) and $\text{av} = (I(w_1), \dots, I(w_n))$ to \mathcal{D} .
- Data owner \mathcal{D} , on input policy \mathbf{P} and master key $K = (K_S, K_X, K_T, K_I, K_P, K_M)$:
 - Abort if av is not in policy set \mathbf{P} . Otherwise set av as \mathcal{D} 's local output.
 - Compute $b_s \leftarrow \text{OPRF}.\mathcal{D}(K_S, a_s)$.
 - Compute $(b_1, \rho_1) \leftarrow \text{S-OPRF}.\mathcal{D}(K_T, I_1, a_1)$, and $(b_i, \rho_i) \leftarrow \text{S-OPRF}.\mathcal{D}(K_X, I_i, a_i)$ for $i = 2, \dots, n$.
 - Set $\text{env} \leftarrow \text{AuthEnc}(K_M, (\rho_1, \rho_2, \dots, \rho_n))$ and send $(\text{env}, b_s, b_1, \dots, b_n)$ to \mathcal{C} .
- \mathcal{C} outputs $\text{token} = (\text{env}, \text{strap}, \text{bstag}, \text{bstrap}_2, \dots, \text{bstrap}_n)$ where $\text{strap} \leftarrow \text{OPRF}.\mathcal{C}_2(b_s, r_s)$, $\text{bstag} \leftarrow \text{S-OPRF}.\mathcal{C}_2(b_1, r_1)$, and $\text{bstrap}_i \leftarrow \text{S-OPRF}.\mathcal{C}_2(b_i, r_i)$ for $i = 2, \dots, n$.

Figure 2: TOKEN GENERATION IN OSPIR-OXT

OSPIR-OXT Specification. With the above ingredients and notation we specify OSPIR-OXT on the basis of MC-OXT via the following changes.

Keys. Select key K_S for F_G ; K_T and K_X for F_G^m ; K_I for F_P ; and K_M for the authenticated encryption scheme.

EDBSetup. Follow the EDBSetup procedure of MC-OXT except for computing $\text{strap} \leftarrow F_G(K_S, w)$ and $\text{xtag} \leftarrow (F_G^m(K_X, w))^{\text{xind}}$, and for implementing the TSetGetTag procedure as $\text{TSetGetTag}(K_T, w) = F_G^m(K_T, w)$, which means that we compute $\text{stag}(w) \leftarrow F_G^m(K_T, w)$; index $\mathbf{t}(w)$ in \mathbf{T} by $\text{stag}(w)$ instead of by w itself; and generate TSet using the modified API procedure $\text{TSetSetup}'(\mathbf{T})$.

GenToken protocol. This is the main change with respect to OSPIR-OXT; it follows the above mechanisms and is presented in Figure 2.

Search protocol. Same as MC-OXT except that stag is not included under env but rather it is provided to \mathcal{E} by \mathcal{C} as bstag from which \mathcal{E} computes $\text{stag} \leftarrow (\text{bstag})^{1/\rho_1}$.

Instantiation via Hashed Diffie-Hellman OPRF. Our implementation and analysis of OSPIR-OXT assumes the use of Hashed DH OPRF mentioned above, namely, $F_G(K, x) = (H(x))^K$. The instantiations of OPRF and S-OPRF protocols in this case are as follows. $\text{OPRF}.\mathcal{C}_1(x)$ and $\text{S-OPRF}.\mathcal{C}_1(x)$ both pick random r in Z_p^* , set $a \leftarrow (H(x))^r$, and output (a, r) . Procedure $\text{OPRF}.\mathcal{D}(K, a)$, where $K \in Z_p^*$ is a key for PRF F_G , outputs $b \leftarrow a^K$. Procedure $\text{S-OPRF}.\mathcal{D}(K, i, a)$, where $i \in \{1, \dots, m\}$ and $K = (K[1], \dots, K[m]) \in (Z_p^*)^m$ is a key for PRF F_G^m , picks random ρ in Z_p^* , computes $b \leftarrow a^{K[i] \cdot \rho}$, and outputs (b, ρ) . Procedures $\text{OPRF}.\mathcal{C}_1(b, r)$ and $\text{S-OPRF}.\mathcal{C}_1(b, r)$ both output $b^{1/r}$. Note that if parties follow the protocol, \mathcal{C} 's final output is equal to $(H(x))^K = F_G(K, x)$ in the OPRF protocol, while in the S-OPRF protocol it is equal to $(H(x))^{K[i] \cdot \rho}$, which is equal to $(F_G^m(K, x))^\rho$ if $i = I(x)$. These OPRF and S-OPRF protocols emulate their corresponding ideal functionalities in ROM under so-called One-More Gap Diffie-Hellman assumption [22], see Section 5.

Figure 3 shows the OSPIR-OXT scheme instantiated with the above Hashed DH OPRF. It helps to visualize the entire protocol and it reflects our actual implementation. In Figure 3 we denote keys K_T and K_X of PRF F_G^m by vectors of

exponents in Z_p^* , respectively (k_1, \dots, k_m) and (e_1, \dots, e_m) , where m is the number of attributes. Also, because of the specific OPRF instantiation we equate a_s to a_1 in \mathcal{C} 's message of the GenToken protocol, instead of computing these two blinded versions of keyword w_1 separately, as in Figure 2.

4.2 Supporting Boolean Queries

For simplicity we presented our protocols for the case of conjunctions. The protocols can be readily adapted to search boolean queries in “searchable normal form (SNF)”, i.e., of the form “ $w_1 \wedge \phi(w_2, \dots, w_m)$ ” (intended to return any document that matches keyword w_1 and in addition satisfies the formula ϕ on the remaining keywords). In this case, OXT and its derivatives change only in the way \mathcal{E} determines which tuples match a query (i.e., which values \mathbf{e} it sends back to \mathcal{C}). Specifically, in OXT the c -th tuple matches if and only if $\text{xtoken}[c, i]^{y/\rho_i} \in \text{XSet}$ for all $2 \leq i \leq n$. Instead, for boolean queries as above, \mathcal{E} will have a set of boolean variables v_2, \dots, v_n and will set v_i to the truth value of the predicate $\text{xtoken}[c, i]^{y/\rho_i} \in \text{XSet}$. A tuple is matching if and only if the result of evaluating ϕ on these values returns true. The complexity of boolean search is same as for conjunctions, i.e., proportional to $|\text{DB}(w_1)|$, and leakage to \mathcal{E} is the same as for a conjunctive query on the same set of keywords except that \mathcal{E} also learns the expression ϕ being evaluated. See [9] for details and support of other forms of boolean queries.

In the OSPIR-SSE setting, supporting boolean queries requires policies that are defined in terms of such queries. Specifically, a policy will determine a set of allowed pairs (ψ, I) where ψ is a symbolic boolean expression and I a sequence of attributes, one per each variable in ψ . Thus, leakage to \mathcal{D} will include I (as in the case of conjunctions) plus the symbolic expression being evaluated.

4.3 Computational Cost

Here we provide an operations count for OSPIR-OXT when instantiated with the DH-based OPRF noting its (mild) overhead over the original OXT protocol from [9]. The computational cost of OSPIR-OXT is easy to quantify by inspecting Figure 3 in Page .

The cost of pre-processing (**EDBSetup**) is dominated by operations related to the group G , mainly exponentiations: For every $w \in W$:

1. One hashing operation, $H(w)$, of keyword w into an element of the group G .
2. Two exponentiations: $\text{strap}(w) = (H(w))^{K_S}$ and $\text{stag}(w) = (H(w))^{k_i}$.
3. For every ind in $\text{DB}(w)$: One exponentiation $H(w)^{e_i \cdot \text{ind}}$ for computing an **XSet** element.

The first two items are specific to **OSPIR-OXT** while the third is from the original **OXT** protocol, except that here the base for exponentiation is changed from the generator g in **OXT** to the value $H(w)$. Hence the overhead introduced by **OSPIR-OXT** is given by the first two items and the variable base. Importantly, the overhead for the first two items is only linear in $|W|$, typically much smaller than the number of exponentiations in **OXT** (item 3), namely one per pair (w, ind) for $\text{ind} \in \text{DB}(w)$. As for the latter exponentiations, while the bases are variable, each $H(w)$ is typically used with a very large number of exponentiations (as the number of documents containing w) hence allowing for significant same-base optimizations. The hashing of w into the group G (item 1) is modeled as a random oracle, hence it rules out algebraic implementations such as $g^{h(w)}$. For the elliptic curves groups we use, H is realized by sampling a field element e and a bit b from a PRNG seeded with w until (e, b) is the compressed representation of a valid group element. Depending on the particular nature of a curve, the generic square root algorithms required in solving the Weierstrass equation, though, can be extremely inefficient: Our original implementation for the chosen NIST 224p curve using OpenSSL's standard algorithms was more than an order of magnitude slower than a normal exponentiation and considerably more when common-base optimization is used. By implementing our own algorithm inspired by [4] and optimizing it for this particular field, we could reduce the cost down to the order of an exponentiation. Once all these optimizations are in place, the performance of **OSPIR-OXT** is remarkable as shown in Section 4.4 and, in much more details, in a companion paper [8].

The dominating cost of **GenToken** is just $2n + 1$ exponentiations for the client and $n + 1$ for \mathcal{D} .

Finally, the cost of query processing between \mathcal{C} and \mathcal{E} (**Search**) on a n -term SNF expression is as follows:

1. \mathcal{C} computes $n - 1$ exponentiations for each tuple in $\text{TSet}(w_1)$
2. \mathcal{E} performs up to $n - 1$ exponentiations for each element in $\text{TSet}(w_1)$.

Note that \mathcal{C} can apply same-base optimization to the exponentiations since each term in the SNF expression has its own fixed base. On the other hand, \mathcal{E} cannot use same-base optimizations. However, note that as soon as one of the values $\text{xtoken}[c, i]^{y/\rho_i}$ for a conjunction is found not to be in **XSet**, the other terms for this conjunction do not have to be evaluated (hence avoiding the need for these exponentiations). Similarly, for general Boolean expressions, early termination can be exploited to reduce costly computation. This highlights an important optimization for query processing (especially for queries with large $\text{TSet}(w_1)$ sets): Besides

choosing the s -term as a term with high-entropy to keep $\text{TSet}(w_1)$ small, also choose the evaluation order of x -terms of an SNF expression such that it maximizes the probability of early termination and, hence, reduces the number of (expected) exponentiations executed by \mathcal{E} , e.g., for conjunctions order the x -terms in descending order of entropy (equivalently, ascending order of frequency).

Note (frequency ordering). In the **OSPIR** setting the client may not know the frequency of terms in the database and \mathcal{D} will not know the query values to choose such terms optimally. Thus, the exact mechanism for determining the above ordering will depend on the specific setting. In our implementation we decide on ordering based on typical entropy of attributes; e.g., assuming last names have more entropy than names, and names more entropy than addresses, etc. (note that an attribute-based ordering is more privacy-preserving for the client than a value-based one).

4.4 Implementation and performance

The practicality of the proposed schemes was validated by experiments on DBs which included e.g. English-language Wikipedia (13,284,801 records / 2,732,311,945 indexed tuples), and a synthetic US census database (100 million records / 22,525,274,592 index tuples, resulting in **EDB** with 1.7 TB **TSet** and 0.4 TB **XSet**). To illustrate search efficiency, in the census DB case we executed complex queries like

```
SELECT ID WHERE FNAME='CHARLIE' AND
SEX='FEMALE' AND NOT (STATE='NY' OR
STATE='MA' OR STATE='PA' OR STATE='NJ')
```

in about 4 seconds on an IBM Blade dual Intel 4-core Xeon processor and storage provided by a (low-end) 6.2TB RAID-5 storage system. Preprocessing of such large DBs (**TSet** and **XSet** creation) has been feasible by, among other things, optimization of common-base exponentiations, achieving aggregated (parallel) rate of about 500,000 exp./s/sec. for the NIST 224p elliptic curve.

See [8] for details on implementation and performance as well as for the extension of **OXT** and **OSPIR-OXT** to support dynamic databases (where documents can be added, deleted and modified).

5. SECURITY

We analyze security of the **OSPIR-SSE** scheme. We focus on the **OSPIR** case as it is the more comprehensive setting and it contains **MC-SSE** as a special case. The **SSE-OXT** protocol is analyzed in the **SSE** setting in [9].

5.1 Security and Correctness Definitions

SSE security definitions where the only adversarial entity is server \mathcal{E} are provided in prior work. Here we follow the definitions from [9] - which in turn follow [11, 13] - and extend them to the **MC** setting by considering multiple malicious clients and to the **OSPIR** setting by adding also the data owner \mathcal{D} as an adversarial entity. All security definitions follow the ideal/real model framework of secure computation and are parametrized by a *leakage function* \mathcal{L} bounding the information leaked to an adversarial party in addition to the intended output for that party. Specifically, we ask that whatever an adversary can do by running the real protocol on data and queries *chosen by the adversary*, a simulator can do solely on the basis of the leakage function.

Correctness. We say that an OSPIR-SSE scheme $\Sigma = (\text{EDBSetup}, \text{GenToken}, \text{Search})$ is *computationally correct* if for every efficient algorithm A , there is a negligible probability that the following experiment outputs 0. On inputs (DB, RDK) and $\bar{w}^{(1)}, \dots, \bar{w}^{(m)}$ provided by A , execute $(K, \text{EDB}) \leftarrow \text{EDBSetup}(\text{DB}, \text{RDK})$; and for $i = 1, 2, \dots$, execute protocol GenToken on C 's input $\bar{w}^{(i)}$ and \mathcal{D} 's inputs (P, K) , denote C 's output as $\text{token}^{(i)}$, execute protocol Search between C on input $\text{token}^{(i)}$ and \mathcal{E} on input EDB and denote C 's outputs as a pair $(\text{indSet}^{(i)}, \text{rdkSet}^{(i)})$. Output 1 if for each i we have that $\text{indSet}^{(i)} = \text{DB}(\bar{w}^{(i)})$ and $\text{rdkSet}^{(i)} = \text{RDK}[\text{DB}(\bar{w}^{(i)})]$. Otherwise output 0.

Security against adversarial server \mathcal{E} . Security against adversarial (honest-but-curious) \mathcal{E} has been the focus of prior SSE work. Adapting the definition of \mathcal{L} -semantic security against adaptive attacks (by the server \mathcal{E}) from [9] to our setting is straightforward and is omitted here.

Security against adversarial clients. The definition captures the information leaked to a malicious client in addition to the intended output $\text{DB}(\bar{w})$ and the corresponding record-decrypting keys $\text{RDK}[\text{DB}(\bar{w})]$. The definition compares the real execution to an emulation of an interaction with algorithm $\text{I-SSE}_{\mathcal{L}}$, which models an ideal functionality of the OSPIR-SSE scheme instantiated with the leakage function \mathcal{L} . The interactive algorithm $\text{I-SSE}_{\mathcal{L}}$, running on local input $(\text{DB}, \text{RDK}, P)$, answers queries $\bar{w} \in W^*$ by checking if $\text{av}(\bar{w}) \in P$. If the check verifies, then it replies to this \bar{w} with a triple $(\text{DB}(\bar{w}), \text{RDK}[\text{DB}(\bar{w})], \mathcal{L}(\text{DB}, \bar{w}))$, and if $\text{av}(\bar{w}) \notin P$ then it sends back a rejection symbol \perp .

DEFINITION 1. Let $\Pi = (\text{EDBSetup}, \text{GenToken}, \text{Search})$ be an OSPIR-SSE scheme. Given algorithms \mathcal{L} , A , and $S = (S_0, S_1, S_2)$ we define experiments (algorithms) $\text{Real}_A^\Pi(\lambda)$ and $\text{Ideal}_{A,S}^\Pi(\lambda)$ as follows:

$\text{Real}_A^\Pi(\lambda)$: $A(1^\lambda)$ chooses $(\text{DB}, \text{RDK}, P)$, and the experiment runs $(K, \text{EDB}) \leftarrow \text{EDBSetup}(\text{DB}, \text{RDK})$. Adversary A can then adaptively invoke instances of the protocol GenToken and Search , interacting with party \mathcal{D} running on input K and P in the first case and with party \mathcal{E} running on input EDB in the second case. Note that A can behave arbitrarily in all these protocol instances. Let q be the number of GenToken instances and let av_i be \mathcal{D} 's local output in the i -th instance. If at any point A halts and outputs a bit b , the game outputs $(b, \text{av}_1, \dots, \text{av}_q)$.

$\text{Ideal}_{A,S}^\Pi(\lambda)$: $A(1^\lambda)$ chooses $(\text{DB}, \text{RDK}, P)$ as above, while the experiment initializes $S = (S_0, S_1, S_2)$ by running $\text{st} \leftarrow S_0(1^\lambda)$. Subsequently, each time A invokes an instance of protocol GenToken , it interacts with the experiment running $S_1(\text{st}, P)$, whereas if A invokes an instance of protocol Search , it interacts with the experiment running $S_2(\text{st})$. Both S_1 and S_2 algorithms are allowed to update the global simulator's state st while interacting with A . Both can issue queries \bar{w} to $\text{I-SSE}_{\mathcal{L}}(\text{DB}, \text{RDK}, P)$. Let q be the number of these queries and let $\text{av}_i = I(\bar{w}_i)$, where \bar{w}_i is the i -th query. As above, if at any point A halts and output a bit b , the game outputs $(b, \text{av}_1, \dots, \text{av}_q)$.

We call Π \mathcal{L} -semantically-secure against malicious clients if for any efficient algorithm A there is an efficient algorithm S s.t. the statistical difference between tuples $(b, \text{av}_1, \dots, \text{av}_q)$ output by experiments Real_A^Π and $\text{Ideal}_{A,S}^\Pi$ is a negligible function of the security parameter λ .

Security against adversarial data owner. Security against a data-owner \mathcal{D} models privacy of the client's queries \bar{w} against malicious \mathcal{D} , given an adaptive choice of the client's queries. Similarly to the case of security against either the client C or the EDB-storing server \mathcal{E} , this security definition also allows for leakage of some information $\mathcal{L}(\bar{w})$ regarding the query \bar{w} to \mathcal{D} .

DEFINITION 2. Let $\Pi = (\text{EDBSetup}, \text{GenToken}, \text{Search})$ be an OSPIR-SSE scheme. Given algorithms \mathcal{L} , A , and S we define experiments (algorithms) $\text{Real}_A^\Pi(\lambda)$ and $\text{Ideal}_{A,S}^\Pi(\lambda)$ as follows:

$\text{Real}_A^\Pi(\lambda)$: Adversary $A(1^\lambda)$ can adaptively invoke any number of GenToken instances by specifying a query \bar{w} and interacting with party C running the GenToken protocol on input \bar{w} . At any point A can halt and output a bit, which the game uses as its own output.

$\text{Ideal}_{A,S}^\Pi(\lambda)$: Adversary $A(1^\lambda)$ can adaptively invoke any number of GenToken instances as above, but for any query \bar{w} which A specifies, it interacts with S running on input $\mathcal{L}(\bar{w})$. As above if A halts and output a bit, the game uses this bit as its own output.

We call Π \mathcal{L} -semantically-secure against malicious data owner if for any efficient alg. A there is an efficient alg. S s.t. $\Pr[\text{Real}_A^\Pi(\lambda)=1] - \Pr[\text{Ideal}_{A,S}^\Pi(\lambda)=1] \leq \text{neg}(\lambda)$.

Note (non-collusion between \mathcal{D} and \mathcal{E}). We stress that even though the data owner \mathcal{D} can be arbitrarily malicious, we assume that \mathcal{D} and \mathcal{E} do not collude. Indeed, client's security in the OSPIR-OXT scheme we propose is not maintained against such collusion. Moreover, providing query-privacy from \mathcal{D} under collusion with \mathcal{E} would have the (impractical) cost of a single-server symmetric PIR protocol. The hospital example mentioned in the introduction, is a case where such non-collusion requirement makes sense. Indeed, it is the hospital interest not to learn the queries: It helps avoiding liability and complying with regulations as well as withstanding potential insider attacks. Similarly, for a service providing private access to a database (e.g. to a patent repository) preserving client privacy is part of its very business model. See also [18].

5.2 Security of OSPIR-OXT

Correctness of OSPIR-OXT. We first argue that protocol OSPIR-OXT is correct.

THEOREM 3. The OSPIR-SSE scheme OSPIR-OXT instantiated with the Hashed Diffie-Hellman OPRF is computationally correct assuming that the DDH assumption holds, that the T-set implementation is computationally correct, that F_p is a secure PRF, and assuming the Random Oracle Model for hash function H .

Since T-set implementation is computationally correct, any correctness errors can only come from collisions in PRF functions, including function F_{K_X, K_I} effectively used in computing xtag values, defined as $F_{K_X, K_I}(w, \text{ind}) = (F_G^m(K_X, w))^{F_p(K_I, \text{ind})}$. But assuming the PRF property of F_p , and the PRF property of F_G^m , which holds under DDH in ROM, function F_{K_X, K_I} is a PRF too, and so collision probability is negligible, resulting in negligible error probability over the execution of the OSPIR-OXT correctness experiment.

Security of OSPIR-OXT. Using the security notions explained above we describe the security properties of the OSPIR-SSE scheme OSPIR-OXT instantiated with the Hashed Diffie-Hellman OPRF, as shown in Figure 3. We first state the OM-GDH security assumption required for the security of the OPRF and S-OPRF sub-protocols of this OSPIR-OXT instantiation.

One-More Gap Diffie-Hellman (OM-GDH). Let $G = G_\lambda$ be a prime order cyclic group of order $p = p(\lambda)$ generated by g . We say that the *One-More Gap Diffie-Hellman (OM-GDH) assumption* holds in G if $\text{Adv}_{G,A}^{\text{ddh}}(\lambda)$ is negligible for all efficient adversaries A , where $\text{Adv}_{G,A}^{\text{ddh}}(\lambda)$ is defined as the probability that A wins the following game: (1) The game chooses random t in Z_p^* and two random elements h_1, h_2 in G ; (2) A , on input h_1, h_2 , specifies a single query a to the Diffie-Hellman oracle, which on input a returns $b \leftarrow a^t$; (3) A can make any number of queries to a *Decisional Diffie-Hellman* oracle $\text{DDH}_t(\cdot, \cdot)$, which on input (h, v) returns 1 if $v = h^t$ and 0 otherwise; (4) Finally A outputs two values v_1, v_2 , and we say that A wins the game if $v_1 = (h_1)^t$ and $v_2 = (h_2)^t$.

Security against adversarial server \mathcal{E} . The OSPIR-SSE scheme OSPIR-OXT is \mathcal{L}_{OXT} -semantically-secure against adaptive server \mathcal{E} under the same assumptions and for the same leakage function \mathcal{L}_{OXT} as the underlying SSE scheme OXT of [9]. This is because the specific PRF's used by OSPIR-OXT in EDB construction are instantiations of general PRF's considered in OXT, and because \mathcal{E} 's view of the Search protocol in the OSPIR-OXT scheme can be generated from \mathcal{E} 's view of Search in the OXT scheme. Specifically, each ρ_i in env is random in Z_p^* , and btag and each $\text{btoken}[c, i]$ value in Figure 3 can be computed by exponentiating values stag and $\text{xtoken}[c, i]$ in Figure 1 to, respectively, ρ_1 and ρ_i .

Security against adversarial client \mathcal{C} . Let $\text{Mask}(|\text{DB}(w_1)|)$ denote an upper bound on $|\text{DB}(w_1)|$ used by \mathcal{E} to mask the size of $\text{TSet}(w_1)$ when responding to \mathcal{C} 's queries as described at the end of Section 3.

THEOREM 4. *Let \mathcal{L} be a defined as $\mathcal{L}(\text{DB}, \bar{w}) = \text{Mask}(|\text{DB}(w_1)|)$ for $\bar{w} = (w_1, \dots, w_n)$. OSPIR-SSE scheme OSPIR-OXT instantiated with the Hashed Diffie-Hellman OPRF is \mathcal{L} -semantically-secure against malicious clients assuming that the One-More Gap Diffie-Hellman assumption holds in G , that F_p is a secure PRF, that the T-set implementation is (computationally) correct, that $(\text{AuthEnc}, \text{AuthDec})$ is an IND-CPA and Strongly-UF-CMA authenticated encryption scheme, and assuming the Random Oracle Model for hash function H .*

PROOF. See full version [20]. \square

Security against adversarial data owner \mathcal{D} . In our OSPIR-SSE scheme a malicious \mathcal{D} learns nothing about clients' query $\bar{w} = (w_1, \dots, w_n)$ except for the vector of attributes $\text{av}(\bar{w}) = (I(w_1), \dots, I(w_n))$.

THEOREM 5. *Let \mathcal{L} be a leakage function defined as $\mathcal{L}(\bar{w}) = \text{av}(\bar{w})$. OSPIR-SSE scheme OSPIR-OXT instantiated with the Hashed Diffie-Hellman OPRF is \mathcal{L} -semantically-secure against malicious data owner.*

PROOF. See full version [20]. \square

Note that the \mathcal{D} 's view of the GenToken protocol in the OSPIR-OXT scheme consists of the attribute vector $\text{av}(\bar{w})$

and the values a_s, a_1, \dots, a_n . In the Hashed DH OPRF instantiation of this scheme in Figure 3, these values are formed as $a_j \leftarrow H(w_j)^{r_j}$ for random r_j 's in Z_p^* (additionally, a_s is set to a_1). Since G is of prime order, every element in $G \setminus \{1\}$ is a generator, and thus each a_j is uniform in G . Thus \mathcal{D} 's view of the GenToken protocol can be trivially simulated from $\mathcal{L}(\bar{w}) = \text{av}(\bar{w})$.

5.3 Extensions: Reducing Leakage to \mathcal{D}

In the full version [20] we show how to adapt OSPIR-OXT to a setting where a third party, called a *policy manager*, authorizes queries while \mathcal{D} can enforce them without learning the policy, the boolean expression or the queried attributes; only the number of such attributes is learned by \mathcal{D} . This setting is precisely what is needed to implement searches authorized by a warrant while keeping the searched information hidden from all parties except the authorized searcher.

In addition, OSPIR-OXT can be extended (even without introducing a policy manager) so that the leakage about queried attributes to \mathcal{D} is further limited to the minimum needed to make policy decisions (e.g., \mathcal{D} may not need to know the exact attributes in a query but only the attribute classes they belong to).

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Group operations. G is a cyclic group of prime order p generated by an element g . H is a hash function with range in $G \setminus \{1\}$.

EDBSetup(DB, RDK)

Key Generation. \mathcal{D} picks key K_S and two vectors of elements $K_T = (k_1, \dots, k_m)$ and $K_X = (e_1, \dots, e_m)$ at random in Z_p^* (m = number of attributes); key K_I for PRF F_p ; and key K_M for a symmetric authenticated encryption AuthEnc . F_p and F_τ are PRF's which outputs strings in respectively Z_p^* and $\{0, 1\}^\tau$, and τ is a security parameter.

- Initialize **XSet** to an empty set, and initialize **T** to an empty array indexed by group elements in G .
- For each $w = (i, val) \in W$, build the tuple list **t** and add elements to set **XSet** as follows:
 - Initialize **t** to an empty list.
 - Set **strap** $\leftarrow (H(w))^{K_S}$, **stag** $\leftarrow (H(w))^{k_i} [= F_G^m(K_T, w)]$, $(K_z, K_e) \leftarrow (F_\tau(\text{strap}, 1), F_\tau(\text{strap}, 2))$.
 - Initialize $c \leftarrow 0$; then for all **ind** in **DB**(w) in random order:
 - * Set **rdk** $\leftarrow \text{RDK}(\text{ind})$, **e** $\leftarrow \text{Enc}(K_e, (\text{ind}|\text{rdk}))$, **xind** $\leftarrow F_p(K_I, \text{ind})$.
 - * Set $c \leftarrow c + 1$, $z_c \leftarrow F_p(K_z, c)$, $y \leftarrow \text{xind} \cdot z_c^{-1}$. Append (\mathbf{e}, y) to **t**.
 - * Set **xtag** $\leftarrow H(w)^{e_i \cdot \text{xind}} [= (F_G^m(K_X, w))^{\text{xind}}]$ and add **xtag** to **XSet**.
 - **T**[**stag**] $\leftarrow \mathbf{t}$.
- Create **TSet** $\leftarrow \text{TSetSetup}'(\mathbf{T})$, and output key $K = (K_S, K_X, K_T, K_I, K_M)$ and **EDB** = (**TSet**, **XSet**, K_M).

GenToken protocol

Client \mathcal{C} on input a conjunctive query $\bar{w} = (w_1, \dots, w_n)$, where w_1 is chosen as s-term, proceeds as follows:

- Pick $r_1, \dots, r_n \xleftarrow{\$} Z_p^*$ and set $a_j \leftarrow (H(w_j))^{r_j}$ for $j = 1, \dots, n$.
- Send to \mathcal{D} the blinded queries a_1, \dots, a_n and the attribute sequence $\mathbf{av} = (I(w_1), \dots, I(w_n))$.

Data owner \mathcal{D} on input policy P and key K proceeds as follows:

- Abort if $\mathbf{av} \notin P$. Otherwise set \mathbf{av} as a local output. Pick $\rho_1, \dots, \rho_n \xleftarrow{\$} Z_p^*$.
- Set **strap'** $\leftarrow (a_1)^s$, **bstag'** $\leftarrow (a_1)^{k_{i_1} \cdot \rho_1} [= (a_1)^{K_T[i_1] \cdot \rho_1}]$, and **bstrap'** $_j \leftarrow (a_j)^{e_{i_j} \cdot \rho_j} [= (a_j)^{K_X[i_j] \cdot \rho_j}]$ for $j = 2, \dots, n$.
- Reply to \mathcal{C} with (**strap'**, **bstag'**, **bstrap'** $_2, \dots, \text{bstrap}'_n$) and $\mathbf{env} = \text{AuthEnc}_{K_M}(\rho_1, \dots, \rho_n)$.

\mathcal{C} sets:

- **strap** $\leftarrow (\text{strap}')^{r_1^{-1}}$; **bstag** $\leftarrow (\text{bstag}')^{r_1^{-1}}$; **bstrap** $_j \leftarrow (\text{bstrap}'_j)^{r_j^{-1}}$ ($\forall j=2, \dots, n$);
- **token** $\leftarrow (\mathbf{env}, \text{strap}, \text{bstag}, \text{bstrap}_2, \dots, \text{bstrap}_n)$.

Search protocol

Client \mathcal{C} on input **token** proceeds as follows:

- Set $(K_z, K_e) \leftarrow F_\tau(\text{strap}, 1), F_\tau(\text{strap}, 2)$, and send to \mathcal{E} the message $(\mathbf{env}, \text{bstag}, \text{bxtoken}[1], \text{bxtoken}[2], \dots)$ defined as follows:
 - For $c = 1, 2, \dots$, until \mathcal{E} sends **stop**:
 - * Set $z_c \leftarrow F_p(K_z, c)$ and set **bxtoken**[c, i] $\leftarrow (\text{bstrap}_i)^{z_c}$ for $i = 2, \dots, n$.
 - * Set **bxtoken**[c] $\leftarrow (\text{bxtoken}[c, 2], \dots, \text{bxtoken}[c, n])$.

Server \mathcal{E} on input **EDB** = (**TSet**, **XSet**, K_M) responds as follows:

- Upon receiving $\mathbf{env}, \text{bstag}$ from \mathcal{C} , decrypt/verify \mathbf{env} ; if verification fails return “no results” and **stop**.
- Set **stag** $\leftarrow (\text{bstag})^{1/\rho_1}$ and retrieve **t** $\leftarrow \text{TSetRetrieve}(\text{TSet}, \text{stag})$ from **TSet**.
- For $c = 1, \dots, |\mathbf{t}|$ do:
 - Receive **bxtoken**[c] from \mathcal{C} and retrieve value (\mathbf{e}, y) from the c -th tuple in **t**.
 - Check if **bxtoken**[c, i] $^{y/\rho_i} \in \mathbf{XSet}$ for all $i = 2, \dots, n$. If so, send **e** to \mathcal{C} (else nothing is returned for this tuple).
 - When last tuple in **t** is reached, send **stop** to \mathcal{C} and halt.

For each received **e** client \mathcal{C} computes $(\text{ind}|\text{rdk}) \leftarrow \text{Dec}(K_e, \mathbf{e})$ and outputs (ind, rdk) .

Figure 3: OSPIR-OXT INSTANTIATED FOR CONJUNCTIONS WITH THE HASHED DIFFIE-HELLMAN OPRF