### Recurrent Neural Networks

CS114B Lab 11

Kenneth Lai

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▶ Discriminative approaches:

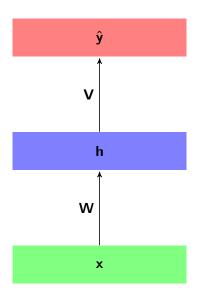
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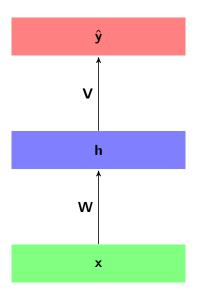
- Discriminative approaches:
  - At each time step, use local features to compute local scores, and use the Viterbi algorithm to make predictions for the whole sentence
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    - Neural networks

#### Feedforward Neural Networks

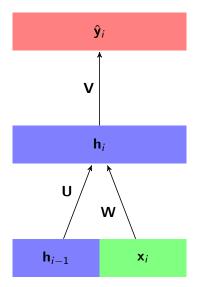


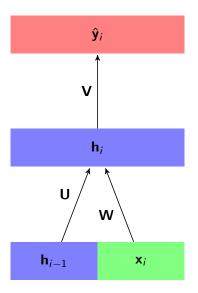
- Output layer
- ► Hidden layer(s)
- ► Input layer
- $h = g(\mathbf{x} \cdot \mathbf{W})$
- $\quad \quad \mathbf{\hat{y}} = g(\mathbf{h} \cdot \mathbf{V})$

#### Feedforward Neural Networks

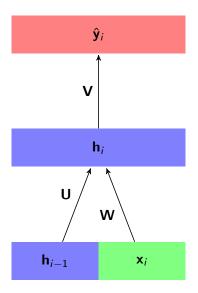


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- ► Hidden layer(s)
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- ▶  $\mathbf{h} = g(\mathbf{x} \cdot \mathbf{W})$
- $\hat{\mathbf{y}} = g(\mathbf{h} \cdot \mathbf{V})$ 
  - We will assume that the dummy feature 1 is part of x and h, and that the bias term is part of W and V, etc.

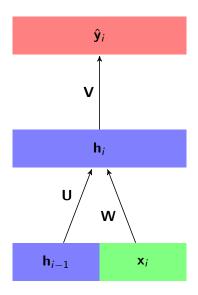




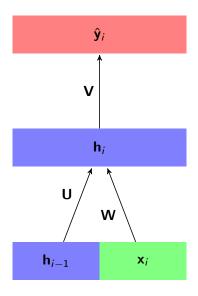
► At each time *i*, the input to the neural network consists of:



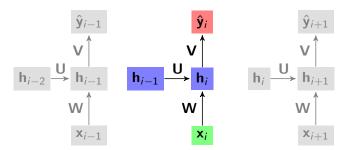
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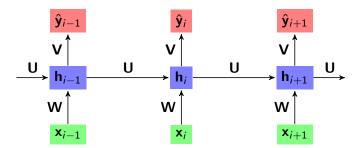


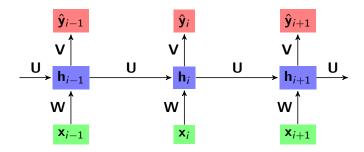
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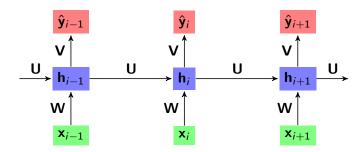
- ► At each time *i*, the input to the neural network consists of:
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- $h_i = g(\mathbf{x}_i \cdot \mathbf{W} + \mathbf{h}_{i-1} \cdot \mathbf{U})$



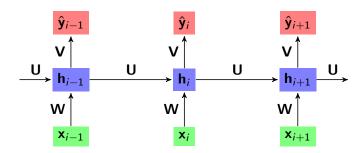




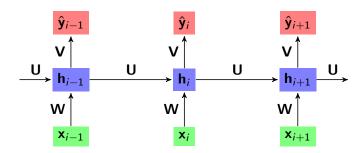
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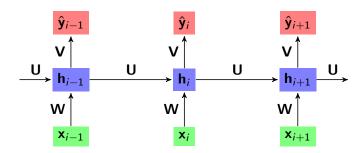


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- ▶ What context information is embedded in  $\mathbf{h}_{i-1}$ ?
  - ▶ Previous word  $\mathbf{x}_{i-1}$
  - Previous context **h**<sub>i-2</sub>

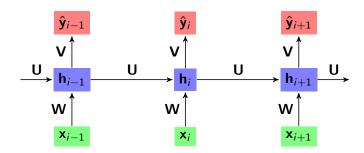


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  - Previous context **h**<sub>i-2</sub>
    - ▶ Previous previous word  $\mathbf{x}_{i-2}$
    - ▶ Previous previous context  $\mathbf{h}_{i-3}$

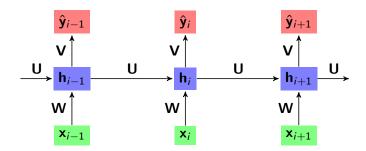




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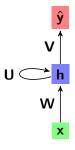
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  - What about previous parts of speech (as in HMMs, CRFs, structured perceptrons)?



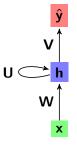
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    - To learn more, take StatNLP in the fall!



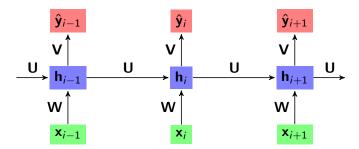
### Recurrent Neural Networks

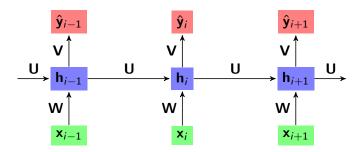


#### Recurrent Neural Networks

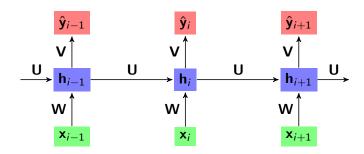


► Neural networks in which the output of a layer in one time step is input to a layer in the next time step

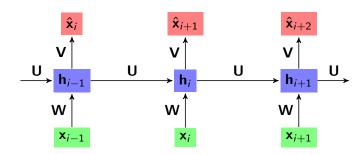




 Sequence labeling: predict current tag given current word, history

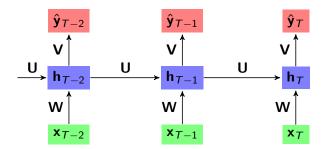


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- ► Language modeling: predict next word given current word, history

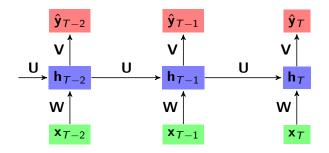


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#### RNNs for Text Classification

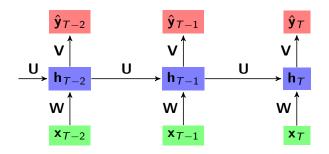


#### RNNs for Text Classification



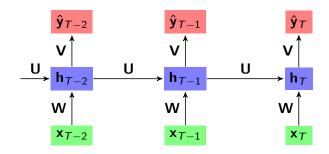
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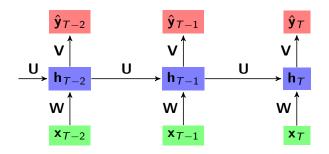
- ▶ What context information is embedded in h<sub>T</sub>?
  - Current word x<sub>T</sub>
  - ► Context  $\mathbf{h}_{T-1}$

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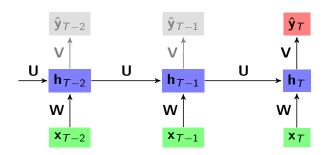
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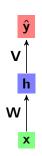
- ▶ What context information is embedded in h<sub>T</sub>?
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- ▶ Use  $\mathbf{h}_{\mathcal{T}}$  to predict class  $\hat{\mathbf{y}}_{\mathcal{T}}$  of entire document

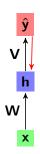
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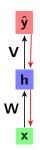
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- ▶ Use  $\mathbf{h}_T$  to predict class  $\hat{\mathbf{y}}_T$  of entire document
  - Ignore other outputs

- ► For each matrix of weights **W**, starting from the output and working backwards:
  - ▶ Compute gradient  $(\nabla L)^{[\mathbf{W}]}$
- ► For each matrix of weights **W**:
  - ▶ Move in direction of negative gradient

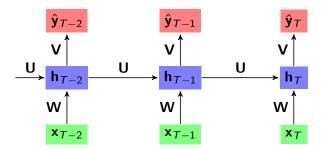


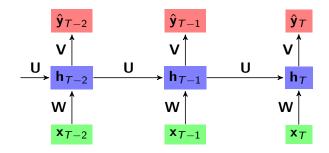


• Compute gradient  $(\nabla L)^{[\mathbf{V}]}$ 

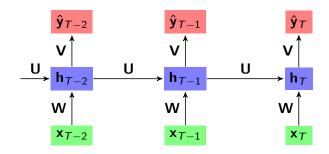


- Compute gradient  $(\nabla L)^{[V]}$
- ▶ Use  $(\nabla L)^{[\mathbf{V}]}$  to compute gradient  $(\nabla L)^{[\mathbf{W}]}$

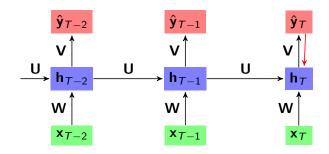




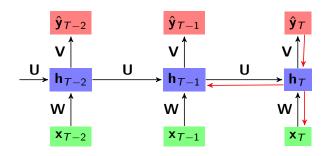
Start at the end of the text and work backwards



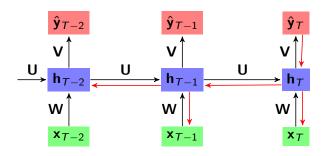
- Start at the end of the text and work backwards
  - Let  $(\nabla L)_{i,j}^{[\mathbf{W}]}$  denote the part of the gradient for weight matrix  $\mathbf{W}$  at time i that comes from the output at time j



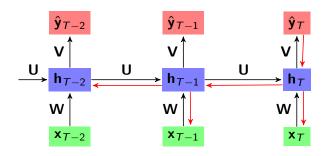
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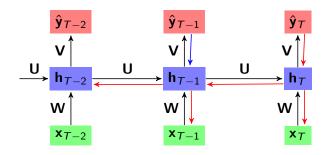


- Start at the end of the text and work backwards
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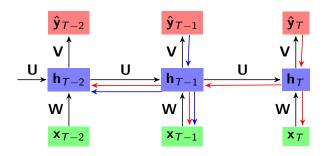


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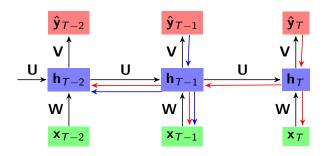
  - etc.



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  - etc.

▶ The overall gradient for a weight matrix  $\mathbf{W}$  is the sum of the gradients at each time i from each output  $\hat{\mathbf{y}}_{j}$ 

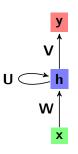
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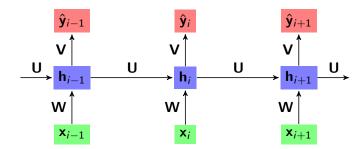
$$(\nabla L)^{[\mathbf{W}]} = \sum_{j=1}^{T} \sum_{i=1}^{j} (\nabla L)_{i,j}^{[\mathbf{W}]}$$

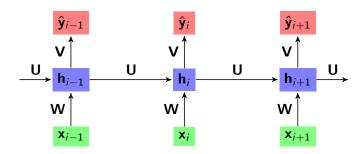
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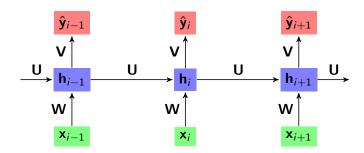
▶ Then move in direction of negative gradient







▶ Output  $\hat{\mathbf{y}}_i$  depends on hidden state  $\mathbf{h}_i$  (i.e. current word  $\mathbf{x}_i$  and history/(past) context  $\mathbf{h}_{i-1}$ )



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- What about future context?

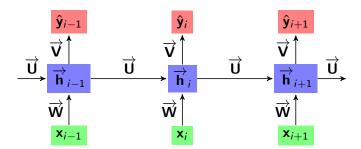
#### Bidirectional RNNs

► Idea: Train two RNNs: passing the input into one forward and one backward

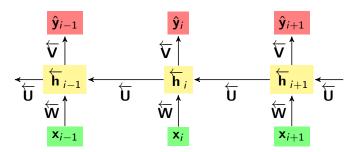
#### Bidirectional RNNs

- Idea: Train two RNNs: passing the input into one forward and one backward
- ▶ Output  $\hat{\mathbf{y}}_i$  depends on forward hidden state  $\overrightarrow{\mathbf{h}}_i$  and backward hidden state  $\overleftarrow{\mathbf{h}}_i$

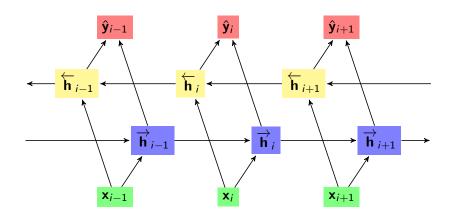
### Forward RNN

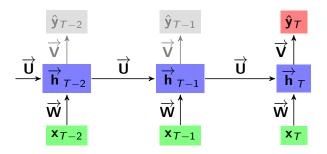


#### **Backward RNN**

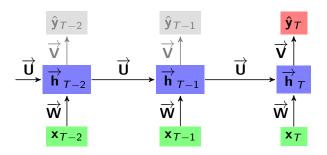


#### **Bidirectional RNN**

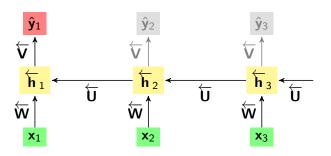




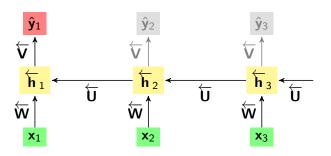
ightharpoonup  $\overrightarrow{\mathbf{h}}_{\mathcal{T}}$  encodes the whole text



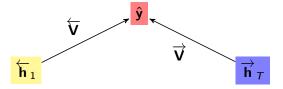
- $\overrightarrow{\mathbf{h}}_T$  encodes the whole text
  - Use  $\overrightarrow{\mathbf{h}}_T$  to predict class  $\hat{\mathbf{y}}_T$  of entire document

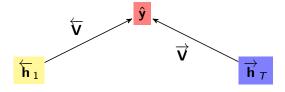


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- $\rightarrow$   $\mathbf{h}_1$  also encodes the whole text
  - Use  $\overleftarrow{\mathbf{h}}_1$  to predict class  $\widehat{\mathbf{y}}_1$  of entire document





• Use  $\overrightarrow{\mathbf{h}}_T$  and  $\overleftarrow{\mathbf{h}}_1$  to predict class  $\hat{\mathbf{y}}$  of entire document

## Context and Long-Distance Dependencies

▶  $\mathbf{h}_{i-1}$  encodes the (past, in a forward RNN) context  $\mathbf{x}_1, ..., \mathbf{x}_{i-1}$ 

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- Context is local

► Example: subject-verb agreement

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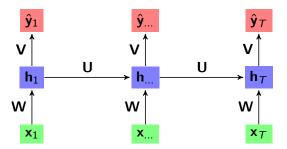
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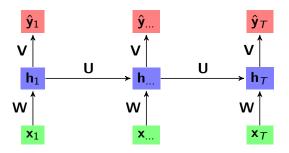
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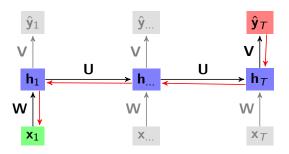
- Example: subject-verb agreement
- ► The flights the airline was cancelling were full.
  - ► The context for "was" is mostly "airline"
  - ► The context for "were" is mostly "cancelling", "was", "airline"

- Example: subject-verb agreement
- ► The flights the airline was cancelling were full.
  - ► The context for "was" is mostly "airline"
  - ► The context for "were" is mostly "cancelling", "was", "airline"
    - Very little "flights"





• What is  $(\nabla L)_{1,T}^{[\mathbf{W}]}$ ?



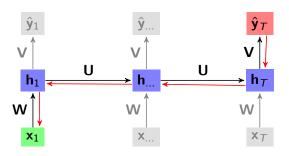
• What is  $(\nabla L)_{1,T}^{[\mathbf{W}]}$ ?

- ► For all layers i:
  - $(\nabla L)^{[i]} = (\mathbf{a}^{[i-1]})^T \cdot \delta^{[i]}$

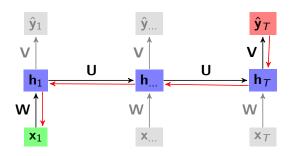
- ► For all layers *i*:
  - $(\nabla L)^{[i]} = (\mathbf{a}^{[i-1]})^T \cdot \delta^{[i]}$ 
    - For simplicity, we will assume that the minibatch size m=1

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    - For simplicity, we will assume that the minibatch size m=1
- ► For an output layer £:

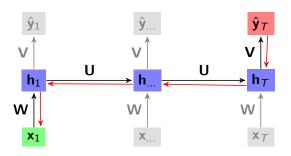
For a hidden layer i:



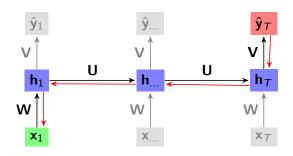
$$(\nabla L)_{1,T}^{[\mathbf{W}]} = \mathbf{x}^T \cdot \delta^{[\mathbf{h}_1]}$$



$$\begin{split} (\nabla L)_{1,\mathcal{T}}^{[\mathbf{W}]} &= \mathbf{x}^{\mathcal{T}} \cdot \delta^{[\mathbf{h}_1]} \\ &= \mathbf{x}^{\mathcal{T}} \cdot ((\delta^{[\mathbf{h}_2]} \cdot \mathbf{U}^{\mathcal{T}}) \odot g'(\mathbf{z}^{[\mathbf{h}_1]})) \end{split}$$



$$\begin{split} (\nabla L)_{1,T}^{[\mathbf{W}]} &= \mathbf{x}^{T} \cdot \delta^{[\mathbf{h}_{1}]} \\ &= \mathbf{x}^{T} \cdot ((\delta^{[\mathbf{h}_{2}]} \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{1}]})) \\ &= \mathbf{x}^{T} \cdot ((((\delta^{[\mathbf{h}_{3}]} \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{2}]})) \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{1}]})) \end{split}$$

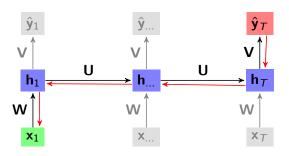


$$(\nabla L)_{1,T}^{[\mathbf{W}]} = \mathbf{x}^{T} \cdot \delta^{[\mathbf{h}_{1}]}$$

$$= \mathbf{x}^{T} \cdot ((\delta^{[\mathbf{h}_{2}]} \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{1}]}))$$

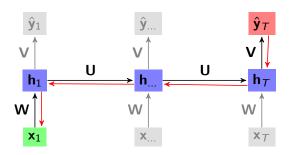
$$= \mathbf{x}^{T} \cdot ((((\delta^{[\mathbf{h}_{3}]} \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{2}]})) \cdot \mathbf{U}^{T}) \odot g'(\mathbf{z}^{[\mathbf{h}_{1}]}))$$

$$= \dots$$



$$\begin{split} (\nabla L)_{1,T}^{[\mathbf{W}]} &= \mathbf{x}^T \cdot \delta^{[\mathbf{h}_1]} \\ &= \mathbf{x}^T \cdot ((\delta^{[\mathbf{h}_2]} \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_1]})) \\ &= \mathbf{x}^T \cdot ((((\delta^{[\mathbf{h}_3]} \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_2]})) \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_1]})) \\ &= \dots \end{split}$$

▶ If weights/derivatives are small, vanishing gradient

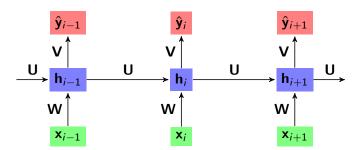


$$\begin{split} (\nabla L)_{1,T}^{[\mathbf{W}]} &= \mathbf{x}^T \cdot \delta^{[\mathbf{h}_1]} \\ &= \mathbf{x}^T \cdot ((\delta^{[\mathbf{h}_2]} \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_1]})) \\ &= \mathbf{x}^T \cdot ((((\delta^{[\mathbf{h}_3]} \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_2]})) \cdot \mathbf{U}^T) \odot g'(\mathbf{z}^{[\mathbf{h}_1]})) \\ &= \dots \end{split}$$

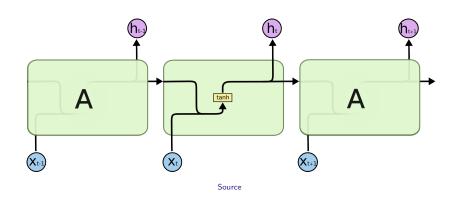
- If weights/derivatives are small, vanishing gradient
- If weights/derivatives are large, exploding gradient

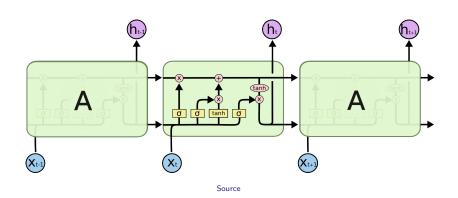


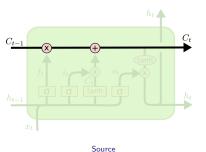
## Simple RNN

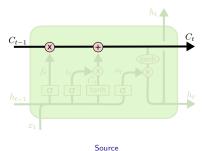


# Simple RNN

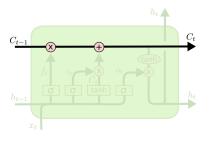






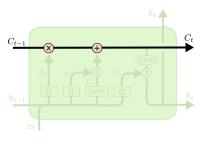


Separate memory (cell) state

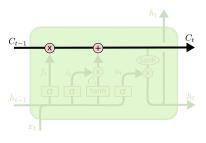


Source

- ► Separate memory (cell) state
  - Reading from and writing to memory controlled by gates

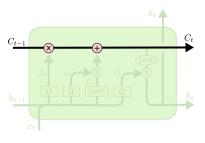


- Source
- Separate memory (cell) state
  - Reading from and writing to memory controlled by gates
    - ▶ Each gate contains one or two neural network layers



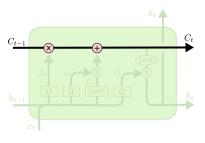
Source

- Separate memory (cell) state
  - Reading from and writing to memory controlled by gates
    - ► Each gate contains one or two neural network layers
  - ► State persists across time



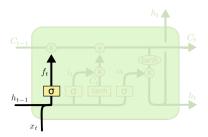
Source

- ► Separate memory (cell) state
  - Reading from and writing to memory controlled by gates
    - Each gate contains one or two neural network layers
  - State persists across time
    - May remember information from long ago

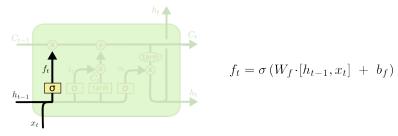


Source

- Separate memory (cell) state
  - Reading from and writing to memory controlled by gates
    - ► Each gate contains one or two neural network layers
  - State persists across time
    - May remember information from long ago
    - Gradients for memory don't decay with time

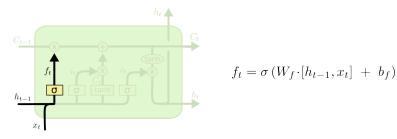


$$f_t = \sigma \left( W_f \cdot [h_{t-1}, x_t] + b_f \right)$$

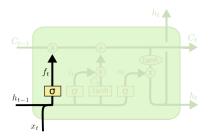


Source

► Neural network layer with logistic activation function



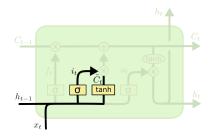
- Neural network layer with logistic activation function
- Element-wise multiplication of forget gate output with memory state



$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$

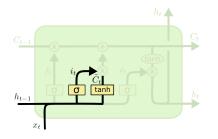
- Neural network layer with logistic activation function
- Element-wise multiplication of forget gate output with memory state
  - Mask: What parts of memory to forget/remember?

## Input Gate



$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  

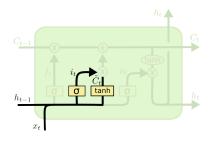
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$



$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

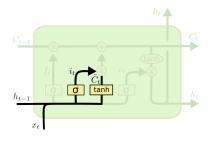
Source

Two parts



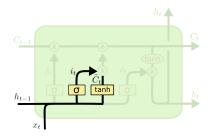
$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

- Two parts
  - 1. Candidate choice



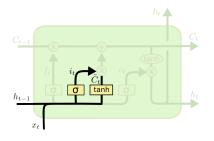
$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

- ► Two parts
  - 1. Candidate choice
    - ▶ Logistic activation function



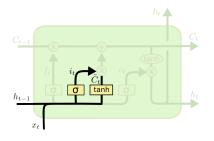
$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

- ► Two parts
  - 1. Candidate choice
    - ► Logistic activation function
    - What parts of memory to update?



$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

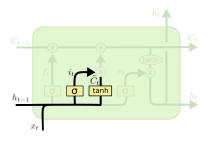
- Two parts
  - 1. Candidate choice
    - ▶ Logistic activation function
    - What parts of memory to update?
  - 2. Candidate values



$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  

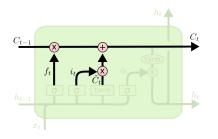
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

- Two parts
  - 1. Candidate choice
    - ► Logistic activation function
    - What parts of memory to update?
  - 2. Candidate values
    - Tanh activation function

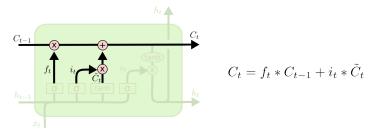


$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

- Two parts
  - 1. Candidate choice
    - ▶ Logistic activation function
    - What parts of memory to update?
  - 2. Candidate values
    - ► Tanh activation function
    - ▶ How much to update them by?

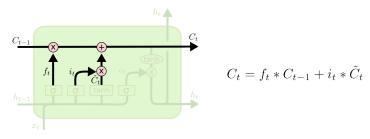


$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

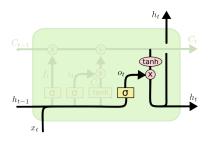


Source

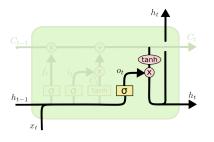
► Element-wise multiplication of two outputs



- Source
- ► Element-wise multiplication of two outputs
- ► Then element-wise addition with memory state



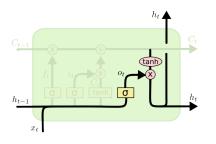
$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh(C_t)$$



$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

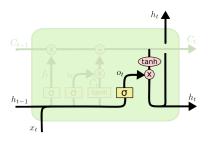
Source

► Logistic activation function



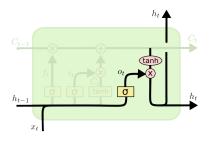
$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

- Logistic activation function
  - ▶ What parts of memory to output?



$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

- Logistic activation function
  - What parts of memory to output?
- ▶ Element-wise multiplication with tanh of memory state



$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

- ► Logistic activation function
  - ▶ What parts of memory to output?
- ▶ Element-wise multiplication with tanh of memory state
  - ► This is the "hidden layer output" that gets passed on to the output layer/next time step