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# 700. Search in a BST <sup>□</sup> (/problems/search-in-a-binary-search-tree/)

Sept. 13, 2019 | 2.5K views

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Given the root node of a binary search tree (BST) and a value. You need to find the node in the BST that the node's value equals the given value. Return the subtree rooted with that node. If such node doesn't exist, you should return NULL.

For example,

```
Given the tree:

4

/\
2 7

/\
1 3

And the value to search: 2
```

You should return this subtree:

```
2
/\
1 3
```

In the example above, if we want to search the value 5, since there is no node with value 5, we should return NULL.

Note that an empty tree is represented by NULL, therefore you would see the expected output (serialized tree format) as [], not null.



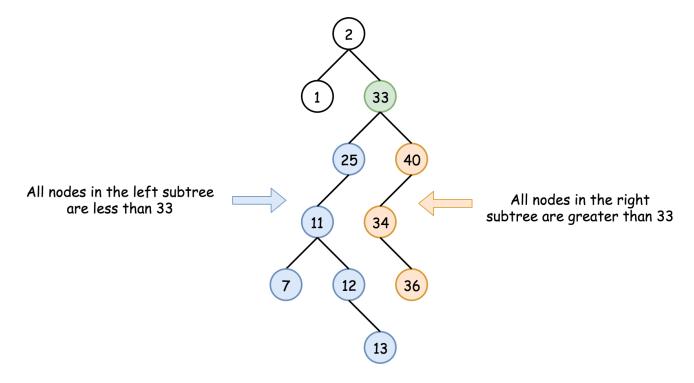
## Solution

## Binary Search Tree.

Binary Search Tree is a binary tree where the key in each node

- is greater than any key stored in the left sub-tree,
- and less than any key stored in the right sub-tree.

Here is an example:



Such data structure provides the following operations in a logarithmic time:

- · Search.
- Insert (https://leetcode.com/articles/insert-into-a-bst/).
- Delete (https://leetcode.com/articles/delete-node-in-a-bst/).

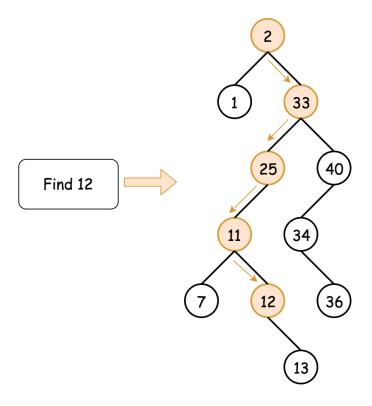
## Approach 1: Recursion

#### 



The recursion implementation is very straightforward:

- If the tree is empty root == null or the value to find is here val == root.val return root.
- If val < root.val go to search into the left subtree searchBST(root.left, val).
- If val > root.val go to search into the right subtree searchBST(root.right, val).
- Return root.



#### Implementation

```
Сору
Java
       Python
   class Solution:
1
2
        def searchBST(self, root: TreeNode, val: int) -> TreeNode:
3
            if root is None or val == root.val:
4
                return root
5
6
            return self.searchBST(root.left, val) if val < root.val \</pre>
7
                else self.searchBST(root.right, val)
```

#### **Complexity Analysis**

ullet Time complexity :  $\mathcal{O}(H)$ , where H is a tree height. That results in  $\mathcal{O}(\log N)$  in the average case, and  $\mathcal{O}(N)$  in the worst case.

Let's compute time complexity with the help of master theorem (https://en.wikipedia.org

/wiki/Master\_theorem\_(analysis\_of\_algorithms))  $T(N) = aT\left(\frac{N}{b}\right) + \Theta(N^d)$ . The equation represents dividing the problem up into a subproblems of size  $\frac{N}{b}$  in  $\Theta(N^d)$  time. Here at step there is only one subproblem a=1, its size is a half of the initial problem b=2, and all this happens in a constant time d=0, as for the binary search. That means that  $\log_b a=d$  and hence we're dealing with case 2 (https://en.wikipedia.org /wiki/Master\_theorem\_(analysis\_of\_algorithms)#Case\_2\_example) that results in  $\mathcal{O}(n^{\log_b a}\log^{d+1}N) = \mathcal{O}(\log N)$  time complexity.

• Space complexity :  $\mathcal{O}(H)$  to keep the recursion stack, i.e.  $\mathcal{O}(\log N)$  in the average case, and  $\mathcal{O}(N)$  in the worst case.

### Approach 2: Iteration

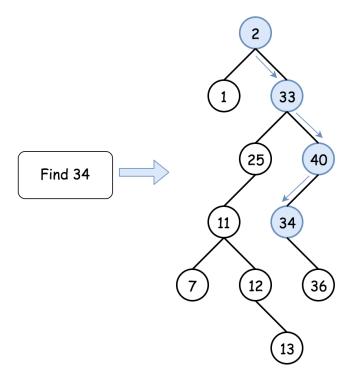
To reduce the space complexity, one could convert recursive approach into the iterative one:

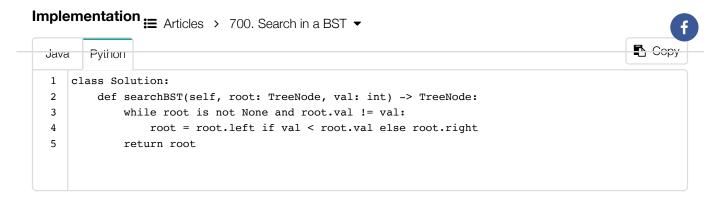
 While the tree is not empty root != null and the value to find is not here val != root.val:

o If val < root.val - go to search into the left subtree root = root.left.

o If val > root.val - go to search into the right subtree root = root.right.

• Return root.





#### **Complexity Analysis**

• Time complexity :  $\mathcal{O}(H)$ , where H is a tree height. That results in  $\mathcal{O}(\log N)$  in the average case, and  $\mathcal{O}(N)$  in the worst case.

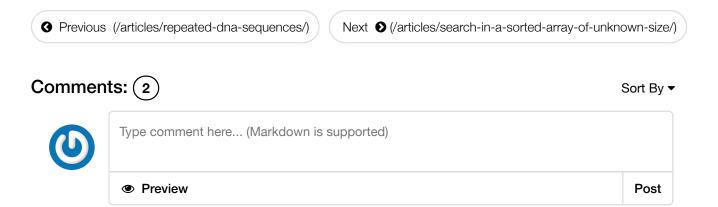
Let's compute time complexity with the help of master theorem (https://en.wikipedia.org /wiki/Master\_theorem\_(analysis\_of\_algorithms))  $T(N)=aT\left(\frac{N}{b}\right)+\Theta(N^d)$ . The equation represents dividing the problem up into a subproblems of size  $\frac{N}{b}$  in  $\Theta(N^d)$  time. Here at step there is only one subproblem a=1, its size is a half of the initial problem b=2, and all this happens in a constant time d=0, as for the binary search. That means that  $\log_b a=d$  and hence we're dealing with case 2 (https://en.wikipedia.org

/wiki/Master\_theorem\_(analysis\_of\_algorithms)#Case\_2\_example) that results in  $\mathcal{O}(n^{\log_b a} \log^{d+1} N) = \mathcal{O}(\log N)$  time complexity.

ullet Space complexity :  $\mathcal{O}(1)$  since it's a constant space solution.

Analysis written by @liaison (https://leetcode.com/liaison/) and @andvary (https://leetcode.com/andvary/)

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ajaay (ajaay) ★ 4 ② September 13, 2019 1:58 PM 

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If the compiler supports tail-recursion optimization, I think the recursive solution would also



(/ajaay

use O(1) memory. GCC supports this if the -O2 or -O3 flags are used.

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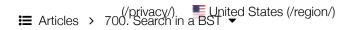
**SHOW 1 REPLY** 



qiuqiushasha (qiuqiushasha) ★9 ② September 14, 2019 8:24 AM @tailrec in Scala is my favoriate

(/qiuqiushasha)

1 ∧ ∨ ☐ Share ¬ Reply





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