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231. Power of two (/problems/power-of-two/)

Aug. 17, 2019 | 2.1K views

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Given an integer, write a function to determine if it is a power of two.

Example 1:

Input: 1
Output: true
Explanation: $2^0 = 1$

Example 2:

Input: 16
Output: true
Explanation: $2^4 = 16$

Example 3:

Input: 218
Output: false

Solution

Overview

We're not going to discuss here an obvious $\mathcal{O}(\log N)$ time solution

Java

Python

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```

1 class Solution(object):
2     def isPowerOfTwo(self, n):
3         if n == 0:
4             return False
5         while n % 2 == 0:
6             n /= 2
7         return n == 1

```

Instead, the problem will be solved in $\mathcal{O}(1)$ time with the help of bitwise operators. The idea is to discuss such bitwise tricks as

- How to get / isolate the rightmost 1-bit : $x \& (-x)$.
- How to turn off (= set to 0) the rightmost 1-bit : $x \& (x - 1)$.

These tricks are often used as something obvious in more complex bit-manipulation solutions, like for N Queens problem (<https://leetcode.com/articles/n-queens-ii/>), and it's important to recognize them to understand what is going on.

Intuition

The idea behind both solutions will be the same: a power of two in binary representation is one 1-bit, followed by some zeros:

$$1 = (00000001)_2$$

$$2 = (00000010)_2$$

$$4 = (00000100)_2$$

$$8 = (00001000)_2$$

A number which is not a power of two, has more than one 1-bit in its binary representation:

$$3 = (00000011)_2$$

$$5 = (00000101)_2$$

$$6 = (00000110)_2$$

$$7 = (00000111)_2$$

The only exception is 0, which should be treated separately.

Approach 1: Bitwise Operators : Get the Rightmost 1-bit



Get/Isolate the Rightmost 1-bit

Let's first discuss why $x \& (-x)$ is a way to keep the rightmost 1-bit and to set all the other bits to 0.

Basically, that works because of two's complement (https://en.wikipedia.org/wiki/Two%27s_complement). In two's complement notation $-x$ is the same as $\neg x + 1$. In other words, to compute $-x$ one has to revert all bits in x and then to add 1 to the result.

Adding 1 to $\neg x$ in binary representation means to carry that 1-bit till the rightmost 0-bit in $\neg x$ and to set all the lower bits to zero. Note, that the rightmost 0-bit in $\neg x$ corresponds to the rightmost 1-bit in x .

In summary, $-x$ is the same as $\neg x + 1$. This operation reverts all bits of x except the rightmost 1-bit.

Two's complement :
 $-x = \neg x + 1$

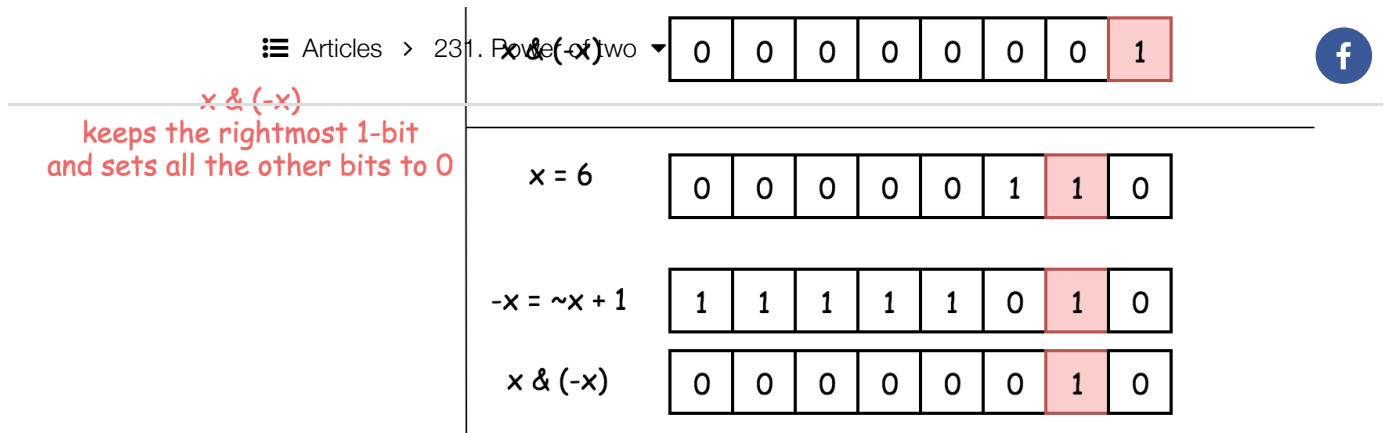
All bits are inverted
except the rightmost 1-bit

$x = 7$	0	0	0	0	0	1	1	1
$\neg x$	1	1	1	1	1	0	0	0
$\neg x + 1$	1	1	1	1	1	0	0	1

$x = 6$	0	0	0	0	0	1	1	0
$\neg x$	1	1	1	1	1	0	0	1
$\neg x + 1$	1	1	1	1	1	0	1	0

Hence, x and $-x$ have just one bit in common - the rightmost 1-bit. That means that $x \& (-x)$ would keep that rightmost 1-bit and set all the other bits to 0.

$x = 7$	0	0	0	0	0	1	1	1
$-x = \neg x + 1$	1	1	1	1	1	0	0	1

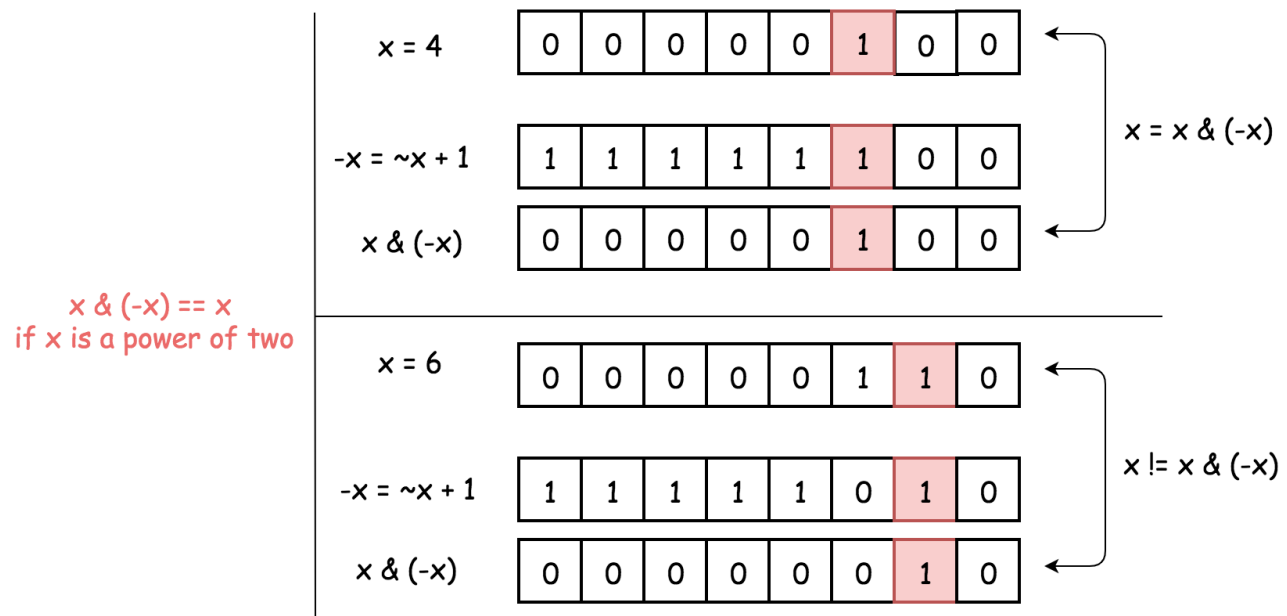


Detect Power of Two

So let's do $x \& (-x)$ to keep the rightmost 1-bit and to set all the others bits to zero. As discussed above, for the power of two it would result in x itself, since a power of two contains just one 1-bit.

Other numbers have more than 1-bit in their binary representation and hence for them $x \& (-x)$ would not be equal to x itself.

Hence a number is a power of two if $x \& (-x) == x$.



Implementation

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```

1 class Solution(object):
2     def isPowerOfTwo(self, n):
3         if n == 0:
4             return False
5         return n & (-n) == n

```

Complexity Analysis

- Time complexity : $\mathcal{O}(1)$.
- Space complexity : $\mathcal{O}(1)$.

Approach 2: Bitwise operators : Turn off the Rightmost 1-bit

Turn off the Rightmost 1-bit

Let's first discuss why $x \& (x - 1)$ is a way to set the rightmost 1-bit to zero.

To subtract 1 means to change the rightmost 1-bit to 0 and to set all the lower bits to 1.

Now AND operator: the rightmost 1-bit will be turned off because $1 \& 0 = 0$, and all the lower bits as well.

Turn off
the rightmost 1-bit :
 $x \& (x - 1)$

</

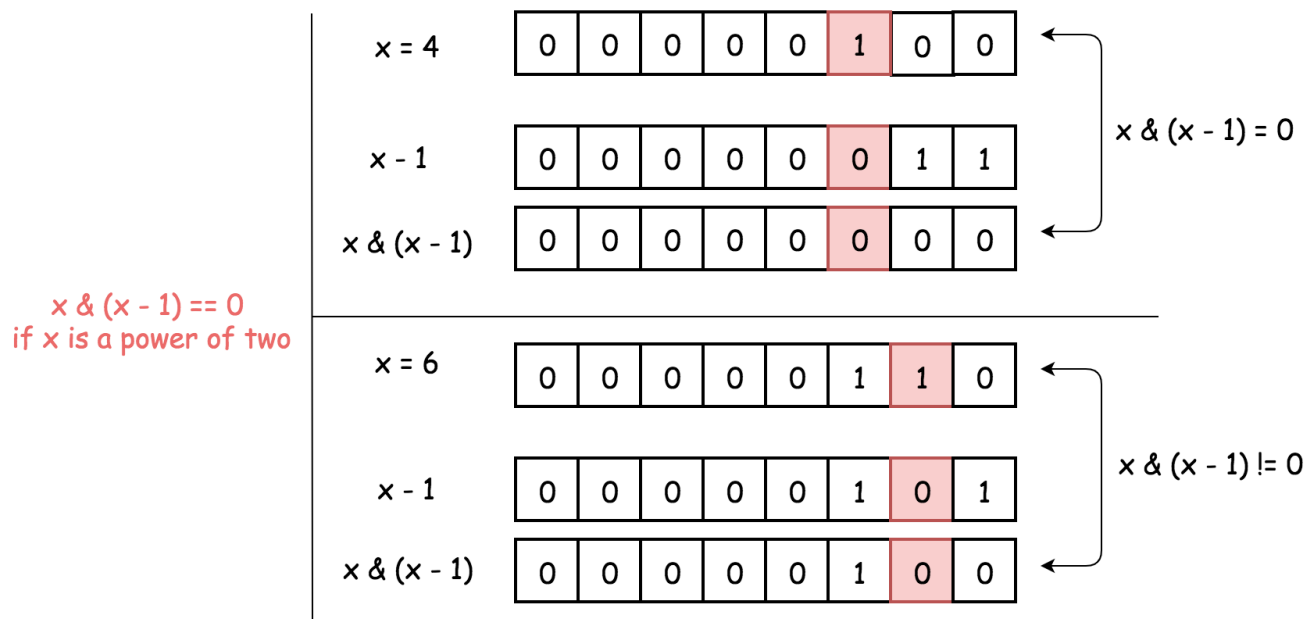
Detect Power of Two

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The solution is straightforward:

1. Power of two has just one 1-bit.
2. $x \& (x - 1)$ sets this 1-bit to zero, and hence one has to verify if the result is zero $x \& (x - 1) == 0$.



Implementation

Java

Python



```

1 class Solution(object):
2     def isPowerOfTwo(self, n):
3         if n == 0:
4             return False
5         return n & (n - 1) == 0

```

Complexity Analysis

- Time complexity : $\mathcal{O}(1)$.
- Space complexity : $\mathcal{O}(1)$.

Analysis written by @liaison (<https://leetcode.com/liaison/>) and @andvary (<https://leetcode.com/andvary/>)

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Ixyuan0420 (Ixyuan0420) ★ 5 ⌚ August 18, 2019 12:39 AM

Great post. Thanks ;)

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(/yendoan007)

yendoan007 (yendoan007) ★ 2 ⌚ August 17, 2019 6:23 PM

Great solution and explanation.

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(/maroochydore)

maroochydore (maroochydore) ★ 1 ⌚ September 10, 2019 5:43 AM

I took granted that number is always integer type. but computer already deals with number as binary format. Handling number with bitwise gives me huge inspiration always.

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(/nits2010)

nits2010 (nits2010) ★ 339 ⌚ August 20, 2019 6:16 AM

sir x = 8 binary is 1000
there are 3 zero at the end, not 2 zero.

and x = 8 - 1 = 7 has binary 111
not 011

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(/bitsraja)

bitsraja (bitsraja) ★ 1 ⌚ August 19, 2019 8:51 AM

why did you convert the int value to long ?

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