33. Search in Rotated Sorted Array [☑] (/problems /search-in-rotated-sorted-array/)

Jan. 10, 2019 | 43.2K views

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Suppose an array sorted in ascending order is rotated at some pivot unknown to you beforehand.

```
(i.e., [0,1,2,4,5,6,7] might become [4,5,6,7,0,1,2]).
```

You are given a target value to search. If found in the array return its index, otherwise return -1.

You may assume no duplicate exists in the array.

Your algorithm's runtime complexity must be in the order of $O(\log n)$.

Example 1:

```
Input: nums = [4,5,6,7,0,1,2], target = 0
Output: 4
```

Example 2:

```
Input: nums = [4,5,6,7,0,1,2], target = 3
Output: -1
```

Solution

Approach 1: Binary search

The problem is to implement a search in $\mathcal{O}(\log(N))$ time that gives an idea to use a binary search.

The algorithm is quite straightforward:

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- Find a rotation index rotation_index, i.e. index of the smallest element in the array. Binary search works just perfect here.
- rotation_index splits array in two parts. Compare nums[0] and target to identify in which part one has to look for target.
- Perform a binary search in the chosen part of the array.

Target = 5

4 5 6 7 8 1 2 3

(1) Find rotation index = index of the smallest element

4 5 6 7 8 1 2 3

1. Pick the element in the middle as a pivot. 7 > 8 = False,

- Pick the element in the middle as a pivot. 7 > 8 = False, hence 8 is not the smallest element.
- 2. 7 > 4, continue the search on the right side.
- 3. Pick the element in the middle as a pivot. 1 > 2 = False, hence 2 is not the smallest element.
- 4. 1 > 8, continue the search on the left side.
- 5. Pick the element in the middle as a pivot. 8 > 1 = True, hence 1 is the smallest element and rotation_index = 5.

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- Perform a binary search in the chosen part of the array.

Target = 5

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2 Where to look for a target?

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1. Target > nums[0] (5 > 4). Search on the left of the rotation index.



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- rotation_index splits array in two parts. Compare nums [0] and target to identify in which part one has to look for target.
- Perform a binary search in the chosen part of the array.

Target = 5

3 Binary search

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1. Pick the element in the middle as a pivot. 6 > 5, hence continue the search on the left side.

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2. Pick the element in the middle as a pivot. 4 < 5 = True, hence continue to search on the right side.

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3. 5 is the target. Return its index = 1

H P H

3/:

```
Python
Java
1
   class Solution:
2
       def search(self, nums, target):
3
4
           :type nums: List[int]
           :type target: int
6
           :rtype: int
7
8
           def find_rotate_index(left, right):
9
               if nums[left] < nums[right]:</pre>
                   return 0
10
11
12
               while left <= right:
13
                   pivot = (left + right) // 2
                   if nums[pivot] > nums[pivot + 1]:
14
15
                       return pivot + 1
16
                   else:
17
                       if nums[pivot] < nums[left]:</pre>
18
                           right = pivot - 1
19
                       else:
20
                           left = pivot + 1
21
22
           def search(left, right):
23
24
               Binary search
25
26
               while left <= right:
                   nivot - /10ft + right / / 2
```

Complexity Analysis

- Time complexity : $\mathcal{O}(\log(N))$.
- Space complexity : $\mathcal{O}(1)$.

Approach 2: One pass

Instead of two passes, all this could be done in one pass. Kudos for this solution go to @haoyangfan (https://leetcode.com/haoyangfan/).

Algorithm

- Initiate start to be equal to 0, and end to be equal to n 1.
- Perform standard binary search. While start <= end:
 - Take an index in the middle mid as a pivot.
 - o If nums [mid] == target, the job is done, return mid.
 - Now there could be two situations:
 - Pivot element is larger than the first element in the array, i.e. the part of array from the first element to the pivot one is non-rotated.

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- If the target is in that non-retated part as well: go left: end = mid 1 and sorted Array 1.
- Otherwise: go right: start = mid + 1.
- Pivot element is smaller than the first element of the array, i.e. the rotation index is somewhere between 0 and mid. That means that the part of array from the pivot element to the last one is non-rotated.
 - If target is in that non-rotated part as well: go right: end = mid + 1.
 - Otherwise: go left: start = mid 1.
- We're here because the target is not found. Return -1.

Implementation

```
Copy
       Python
Java
 1
    class Solution:
 2
        def search(self, nums: List[int], target: int) -> int:
            start, end = 0, len(nums) - 1
 3
 4
            while start <= end:
 5
                mid = start + (end - start) // 2
 6
                if nums[mid] == target:
 7
                    return mid
 8
                elif nums[mid] >= nums[start]:
 9
                     if target >= nums[start] and target < nums[mid]:</pre>
10
                         end = mid - 1
11
                     else:
12
                         start = mid + 1
13
14
                     if target <= nums[end] and target > nums[mid]:
                         start = mid + 1
15
16
                     else:
17
                         end = mid - 1
            return -1
```

Complexity Analysis

- Time complexity : $\mathcal{O}(\log(N))$.
- Space complexity : $\mathcal{O}(1)$.

Analysis written by @liaison (https://leetcode.com/liaison/) and @andvary (https://leetcode.com/andvary/)

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haoyangfan (haoyangfan) ★ 384 ② January 24, 2019 6:42 PM

16-line C solution beats 100% that uses most basic form of binary search

(/haoyangfan)

```
int search(int* nums, int numsSize, int target) {
    int start = 0, end = numsSize - 1;
    while (start <= end) {</pre>
```

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reyou (reyou) ★ 31 ② April 26, 2019 6:32 PM

Formula: If a sorted array is shifted, if you take the middle, always one side will be sorted. Take the recursion according to that rule.

- 1- take the middle and compare with target, if matches return.
- 2- if middle is bigger than left side, it means left is sorted

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Sithis (sithis) ★ 4455 ② January 11, 2019 4:04 AM

One pass solution.

(/sithis)

```
public int search(int[] a, int key) {
    int lo = 0;
    int hi = a.length - 1;
```

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Python 3 modified binary search (readable)(fast)(short)

(/lim142857)

```
# Initilize two pointers
begin = 0
end = len(nums) - 1
                        Read More
```

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softwareshortcut (softwareshortcut) ★ 87 ② April 18, 2019 7:34 AM

Creating helper methods is key otherwise you'd easily get lost dealing with indices. Great exercise, thanks for sharing. I see shorter solutions in the comments, but they might be tricky to come up with during an interview.

2 A V C Share Reply



(/elstestnewway)

elstestnewway (elstestnewway) ★ 2 ② January 13, 2019 8:04 AM

Language C 0 ms

int search(int *nums, int numsSize, int target) {

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nish_d (nish_d) ★ 12 ② January 10, 2019 6:29 AM

find_rotate_index and search are doing almost the same thing. Is there a way to combine them both? We might have come across target in find_rotate_index already, and just need to end the program there.

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yiqi_yan (yiqi_yan) ★ 22 ② January 16, 2019 11:57 AM

The Java code has a bug: find_rotate_index doesn't deal with the case where the array is completely rotated.

e.g.: input [5,4,3,1]

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O(n + log(n))? The worst case is when the pivot is at index n - 1.

So if I understand this correctly when n = 1 000 000 in worst case scenario (pivot is at index n - 1))

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softwareshortcut (softwareshortcut) ★ 87 ② July 8, 2019 10:40 AM Recursive version in Java.

(/softwareshortcut)

```
class Solution {
   public int search(int[] nums, int target) {
     int size = nums.length;
```

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