

Neural Network

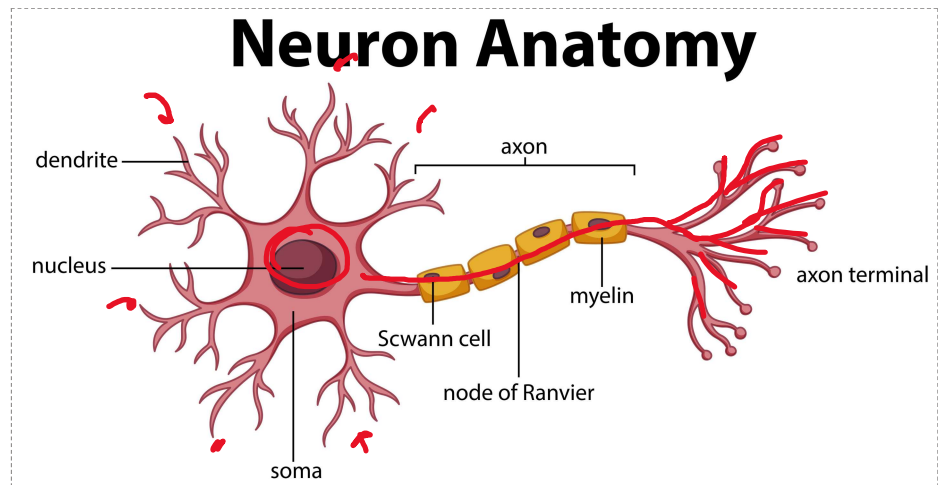
19 June 2025 13:13

Motive - Replicate human brain



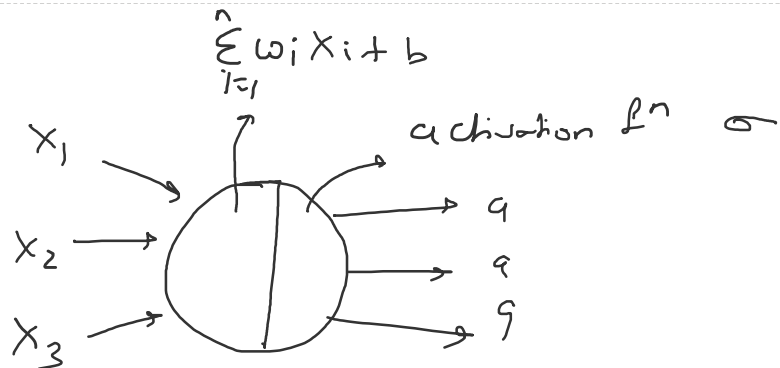
GPU

human brain \rightarrow neuron

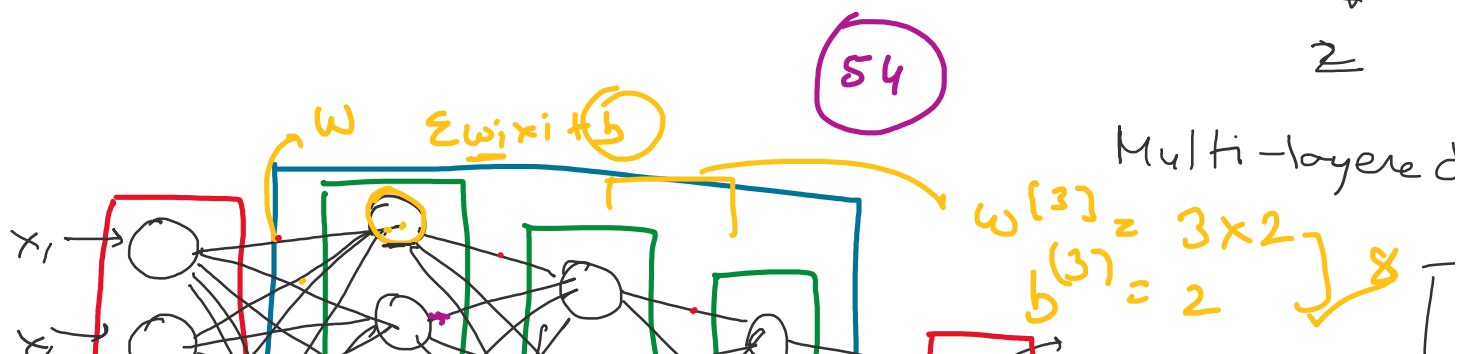


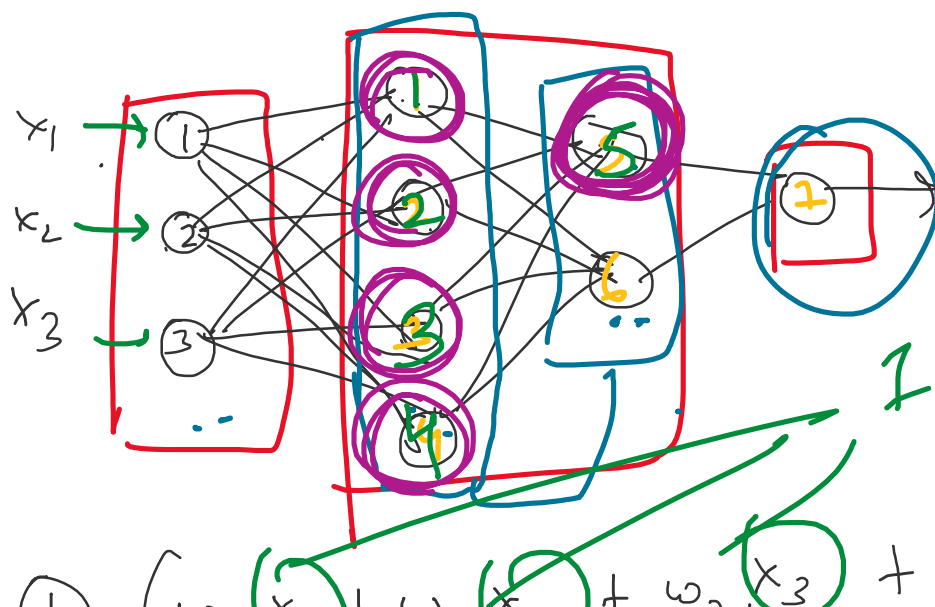
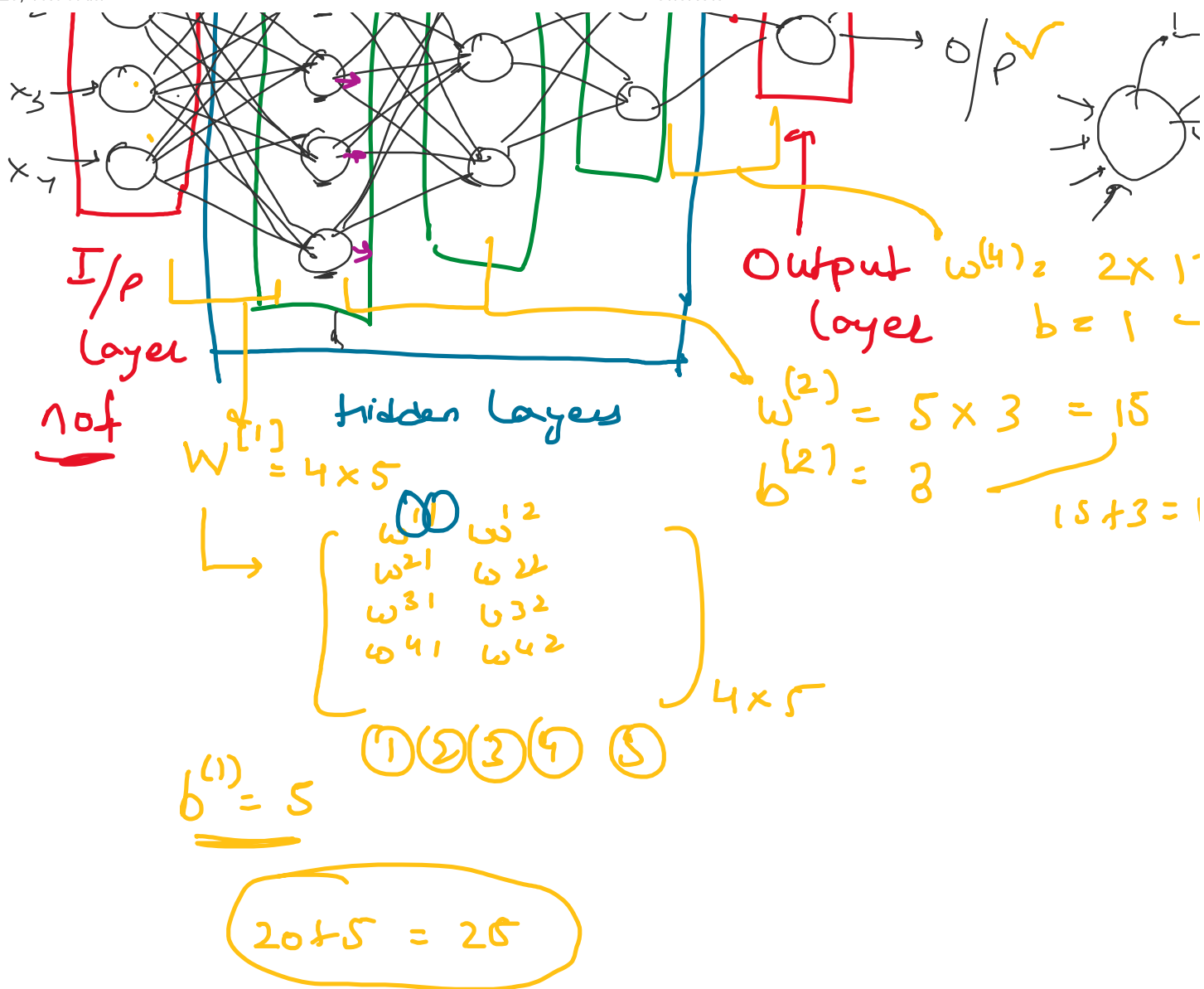
Artificial Neuron

Perceptron



$$a = \sigma \left(\sum_{i=1}^n w_i x_i + b \right)$$





$$\begin{aligned}
 (1) &= \sigma(w_{11}x_1 + w_{21}x_2 + b_1) \\
 (2) &= \sigma(w_{12}x_1 + w_{22}x_2 + w_{32}x_3 + b_2) \\
 (3) &= \sigma(w_{13}x_1 + w_{23}x_2 + w_{33}x_3 + b_3) \\
 (4) &= \sigma(w_{14}x_1 + w_{24}x_2 + w_{34}x_3 + b_4) \\
 (5) &= \sigma(w_{15}(1) + w_{25}(2) + w_{35}(3) + w_{45}(4) + b_5) \\
 (6) &= \sigma(w_{16}(1) + w_{26}(2) + w_{36}(3) + w_{46}(4) + b_6) \\
 (7) &= \sigma(w_{57}(5) + w_{67}(6) + b_7) \Rightarrow
 \end{aligned}$$

O/P

Activation Functions

$$(1) \text{ Sigmoid} = \frac{1}{1+e^{-z}} \quad \sigma(z) \in \{$$

$$(2) \text{ Tanh} = \frac{e^z - e^{-z}}{e^z + e^{-z}} \quad \tanh(z)$$

$$e^z + e^{-z}$$

③ $\text{Relu} = \max(0, z)$ $\text{Relu}(z) \in$

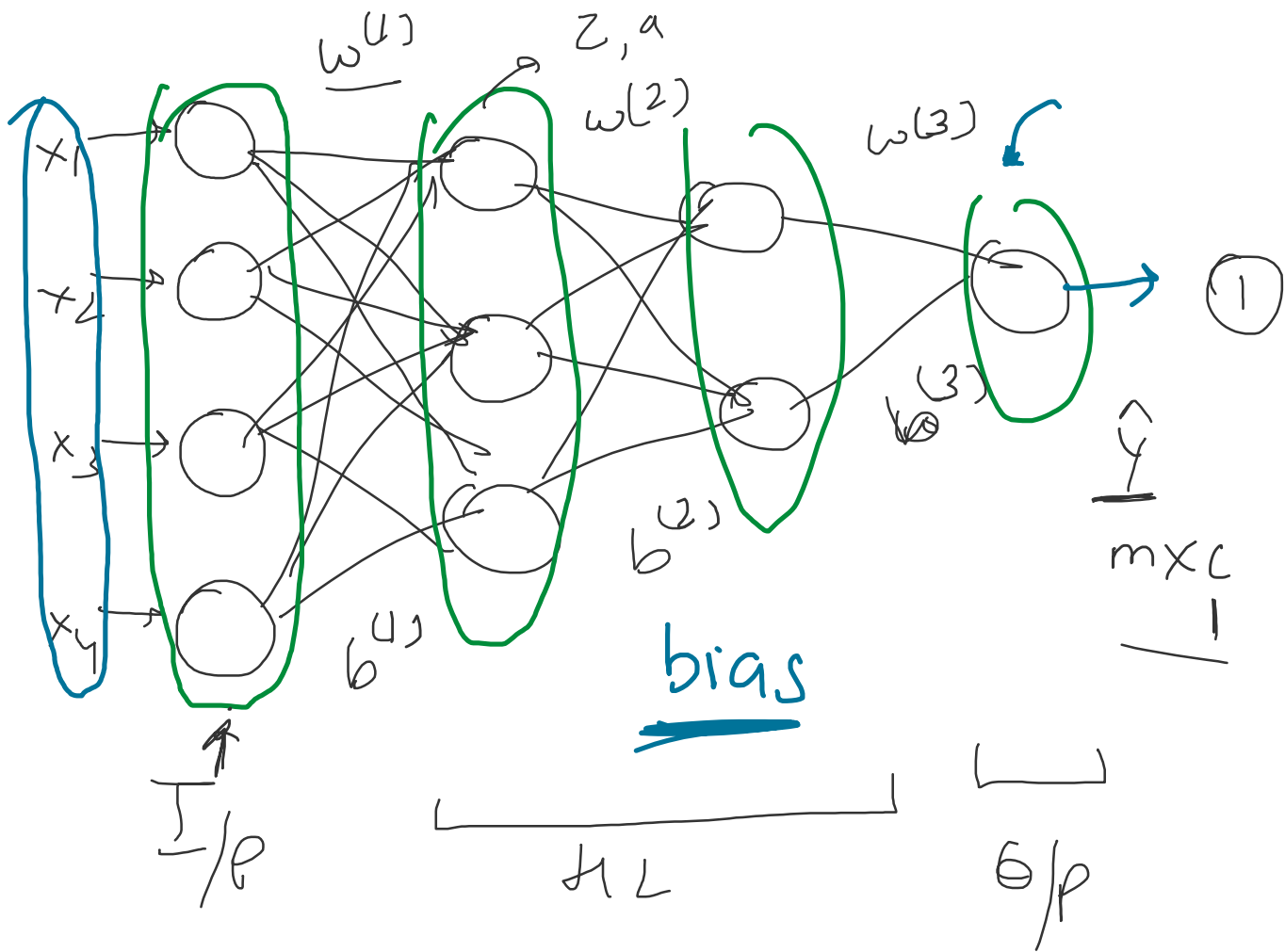
④ $\text{Leaky Relu} = \max(0.01z, z) \in -\infty,$

⑤ $\text{Softmax} : \left[\frac{e^{z_i}}{\sum_{j=1}^n e^{z_j}} \right] \rightarrow$

Output layer (multiclass classification)

Forward Propagation

Backward Propagation



$$J = \sum_{i=1}^m \left[y_i \log(a^{(3)}) + (1 - y_i) \log(1 - a^{(3)}) \right]$$

Gradient Descent

$$\omega^{(1)}, \omega^{(2)}, \omega^{(3)} \quad b^{(4)},$$

$$\frac{\partial J}{\partial \omega^{(4)}}, \frac{\partial J}{\partial \omega^{(2)}}, \frac{\partial J}{\partial \omega^{(3)}} \rightarrow \frac{\partial J}{\partial b^{(4)}}$$

$$\frac{\partial J}{\partial \omega^{(3)}} = \left[\frac{\partial J}{\partial a^{(3)}} \times \frac{\partial a^{(3)}}{\partial z^{(3)}} \right] \times \frac{\partial z}{\partial \omega}$$

$$\frac{\partial J}{\partial \omega^{(2)}} = \left[\frac{\partial J}{\partial a^{(3)}} \times \frac{\partial a^{(3)}}{\partial z^{(3)}} \right] \times \dots$$

$$\frac{\partial J}{\partial \omega^{(1)}} = \left[\frac{\partial J}{\partial a^{(3)}} \times \frac{\partial a^{(3)}}{\partial z^{(3)}} \times \frac{\partial z^{(3)}}{\partial a^{(2)}} \right]$$

