## Questions: Amortized Analysis

1. Consider inserting the keys 10, 22, 31, 4, 15, 28, 17, 88, 59 into a hash table of length m = 11 using open addressing with the auxiliary hash function h'(k) = k.

Illustrate the result of inserting these keys using linear probing, using quadratic probing with  $c_1 = 1$  and  $c_2 = 3$ , and using double hashing with  $h_1(k) = k$ , and  $h_2(k) = 1 + (k \mod(m-1))$ .

- 2. Suppose we perform a sequence of n operations on a data structure in which the ith operation costs i if i is an exact power of 2, and 1 otherwise. Use aggregate analysis to determine the amortized cost per operation.
  - 3. Redo the question.2 using a potential method of analysis.