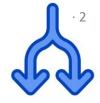


# **Practical Concurrent and Parallel Programming V**

#### **Performance Measurements**

Jørgen Staunstrup

## Agenda



- Performance measurements: motivation and introduction
- Pitfalls (and avoiding them)
- Calculating means and variance (efficiently)
- Measurements of thread overhead
- Algorithms for parallel computing

## Agenda



- Performance measurements: motivation and introduction
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From Week01

Inherent: User interfaces and other kinds of input/output

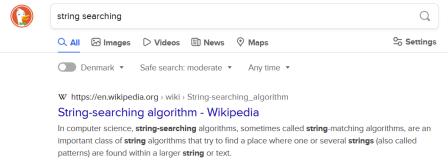
**Exploitation:** Hardware capable of simultaneously executing multiple streams of statements

**Hidden:** Enabling several programs to share some resources in a manner where each can act as if they had sole ownership

#### Motivation 1: Time consuming computations



#### Searching in a (large) text



https://www.geeksforgeeks.org/applications-of-string-matching-algorithms/

#### Computing prime numbers

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, ...
```

Cornerstone of all computer security

https://science.howstuffworks.com/math-concepts/prime-numbers.htm

#### Motivation 2: Analyzing code



# Thread creation is expensive?

The Java tutorials say that creating a Thread is expensive. But why exactly is it expensive? What exactly is happening when a Java Thread is created that makes its creation expensive? I'm taking the statement as true, but I'm just interested in mechanics of Thread creation in JVM.

Thread lifecycle overhead. Thread creation and teardown are not free. The actual overhead

But how expensive?

- ~ 600 ns to create (on this laptop)
- ~ 20 times more time than creating a simple object

40000 ns to start a thread !!! (on this laptop)

Today: How to get such numbers!

## (Performance) Measurements



Key in many sciences (experiments, observations, predictions, ...)

A bit of statistics

A bit of numerical analysis

A bit of computer architecture (cores, caches, number representation, )

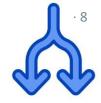
Code for measuring execution time

Based on Microbenchmarks in Java and C# by Peter Sestoft (see benchmarkingNotes.pdf in material for this week)

All numbers in these slides were measured in August 2021 on a:

Intel Core i5-1035G4 CPU @ 1.10GHz, 4 Core(s), 8 Logical Processor(s)

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## Example: measuring a (simple) function

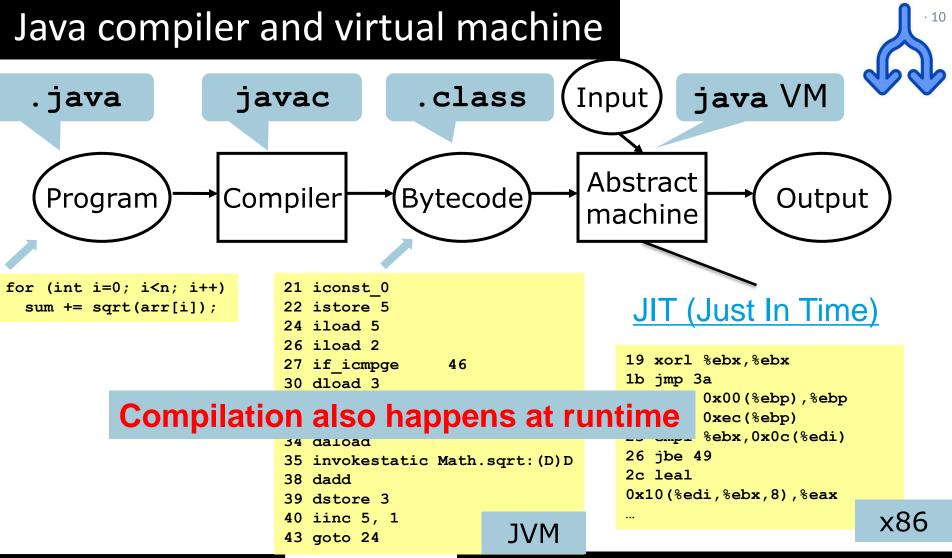


```
cd code-exercises/week05exercises
gradle -PmainClass=exercises05.measurement
```

Try to do this, what result do you get?

```
start= System.nanoTime();
multiply(126465);
end= System.nanoTime();
System.out.println(end-start+" ns");
```

#### What is going on?





Peter Sestoft (sestoft@itu.dk)

Accompanying code: Benchmark.java

IT University of Copenhagen, Denmark

On PCPP GitHub (week05)

Version 0.8.0 of 2015-09-16

**Abstract:** Sometimes one wants to measure the speed of software, for instance, to measure whether a

```
class Benchmark {
  public static void main(String[] args) { new Benchmark(); }

public Benchmark() {
    // SystemInfo(); A
    // Mark0();
    // Mark1();
    ...
    Mark6("multiply", i -> multiply(i));
    ...
    // SortingBenchmarks();
    ...
```



#### A simple Timer class for Java

Works on all platforms (Linux, MacOS, Windows)

```
public class Timer {
  private long start, spent = 0;
  public Timer() { play(); }
  public double check()

  { return (System.nanoTime()-start+spent)/le9; }
  public void pause() { spent += System.nanoTime()-start; }
  public void play() { start = System.nanoTime(); }
}
```

In what time unit do we get the results?

# Example: measuring a simple function



```
private static double multiply(int i) {
  double x = 1.1 * (double) (i & 0xFF);
  return x * x * x * x * x * x * x * x * x * x
    * x * x * x * x * x * x * x * x * x * ;
public static double Mark2() {
   Timer t = new Timer();
   int count = 100 000 000;
   double dummy = 0.0;
                                         In what time unit do we get the results?
   for (int i=0; i<count; i++)</pre>
     dummy += multiply(i);
   double time = (t.check() / count) * 1e9 ;
   System.out.printf("%6.1f ns%n", time);
   return dummy;
```

# Automating multiple runs (Mark3)



#### Results will usually vary

```
public static double Mark3() {
  int n = 10;
  int count = 100 000 000;
  double dummy = 0.0;
  for (int j=0; j < n; j++) {
    Timer t = new Timer();
    for (int i=0; i < count; i++)
    dummy += multiply(i);
    double time = t.check() * 1e9 / count;
    System.out.printf("%6.1f ns%n", time);
  return dummy;
```

```
24.6 ns
24.6 ns
24.6 ns
24.4 ns
24.3 ns
24.5 ns
24.4 ns
24.7 ns
24.6 ns
```

# What is the running time?



What should you report as the result, when the observations are:

30.7 ns 30.3 ns 30.1 ns 30.7 ns 30.5 ns 30.4 ns 30.9 ns 30.3 ns 30.5 ns 30.8 ns ?

30.7 ns 100.2 ns 30.1 ns 30.7 ns 20.2 ns 30.4 ns 2.0 ns 30.3 ns 30.5 ns 5.4 ns ??

Mean: 30.4 ns

What if they are:

Mean: 31.0 ns??

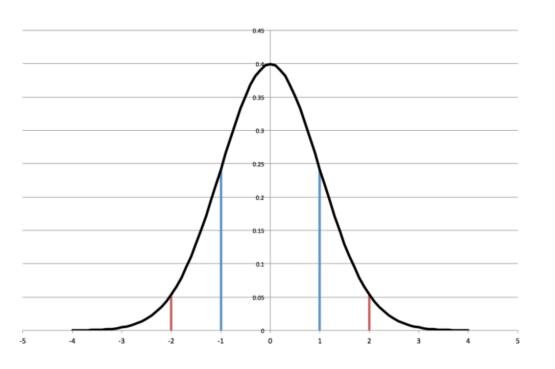
## Agenda



- Performance measurements: motivation and introduction
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- Measurements of thread overhead
- Algorithms for parallel computing

#### Normal distribution





Measuring physical properties

Your exam grades

Course evaluations

Fabrication faults

Running time of Java code

...

```
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```

```
public static double Mark5() {
  int n = 10, count = 1, totalCount = 0;
  double dummy = 0.0, runningTime = 0.0, st = 0.0, sst = 0.0;
  do {
    count *= 2;
    st = sst = 0.0;
    for (int j=0; j < n; j++) {
      Timer t = new Timer();
      for (int i=0; i<count; i++) dummy += multiply(i);
      runningTime = t.check();
      double time = runningTime * 1e9 / count;
      st += time;
      sst += time * time;
      totalCount += count;
    double mean = st/n, sdev = Math.sqrt((sst - mean*mean*n)/(n-1));
    System.out.printf("%6.1f ns +/- %8.2f %10d%n", mean, sdev, count);
  } while (runningTime < 0.25 && count < Integer.MAX VALUE/2);
  return dummy / totalCount;
```



```
public static double Mark5() {
  int n = 10, count = 1, totalCount = 0;
  double dummy = 0.0, runningTime = 0.0, st = 0.0, sst = 0.0;
  do {
    count *= 2;
    st = sst = 0.0;
    for (int j=0; j < n; j++) {
      Timer t = new Timer();
      for (int i=0; i<count; i++) dummy += multiply(i);
      runningTime = t.check();
      double time = runningTime * 1e9 / count;
      st += time;
      sst += time * time;
      totalCount += count;
    double mean = st/n, sdev = Math.sqrt((sst - mean*mean*n)/(n-1));
    System.out.printf("%6.1f ns +/- %8.2f %10d%n", mean, sdev, count);
  } while (runningTime < 0.25 && count < Integer.MAX VALUE/2);
  return dummy / totalCount;
```

#### Mark5

Can we give the function to be measured as a parameter?



```
public static double Mark5() {
  int n = 10, count = 1, totalCount = 0;
  double dummy = 0.0, runningTime = 0.0, st = 0.0, sst = 0.0;
  do {
    count *= 2;
    st = sst = 0.0;
    for (int j=0; j < n; j++) {
      Timer t = new Timer();
      for (int i=0; i<count; i++) dummy += multiply(i);
      runningTime = t.check();
      double time = runningTime * 1e9 / count;
      st += time;
      sst += time * time;
      totalCount += count;
    double mean = st/n, sdev = Math.sqrt((sst - mean*mean*n)/(n-1));
    System.out.printf("%6.1f ns +/- %8.2f %10d%n", mean, sdev, count);
  } while (runningTime < 0.25 && count < Integer.MAX VALUE/2);
  return dummy / totalCount;
```

## Parameterizing function to be measured



```
private static double multiply(int i) {
   . . .
}
```

```
Java: multiply(i) is a number
```

```
Java: i -> multiply(i) is a function
```

https://docs.oracle.com/javase/tutorial/java/javaOO/lambdaexpressions.html

```
Mark6( . . , i -> multiply(i));
```

## Mark6 - introduce a functional argument

lambda



```
public static double Mark6(String msq, IntToDoubleFunction f) {
  int n = 10, count = 1, totalCount = 0;
  double dummy = 0.0, runningTime = 0.0, st = 0.0, sst = 0.0;
 do {
                                                                       The function f is
   count *= 2;
   st = sst = 0.0;
                                                                       benchmarked
    for (int j=0; j < n; j++) {
      Timer t = new Timer();
     for (int i=0; i<count; i++) dummy += f.applyAsDouble(i);</pre>
     runningTime = t.check();
     double time = runningTime * 1e9 / count;
      st += time; sst += time * time; totalCount += count;
    double mean = st/n, sdev = Math.sqrt((sst - mean*mean*n)/(n-1));
    System.out.printf("%-25s %15.1f ns %10.2f %10d%n", msg, mean, sdev, count);
  } while (runningTime < 0.25 && count < Integer.MAX VALUE/2);
  return dummy / totalCount;
public interface IntToDoubleFunction { double applyAsDouble(int i); }
Mark6("multiply", i -> multiply(i));
```

## Example use of Mark6



```
Mark6("multiply", i -> multiply(i));
```

multiply	595.0 ns	1407.81	2
multiply	147.5 ns	90.10	4
multiply	212.5 ns	152.53	8
multiply	170.6 ns	59.44	16
multiply	201.9 ns	157.69	32
multiply	60.8 ns	34.55	64
multiply	65.1 ns	59.83	128
multiply	54.3 ns	14.85	256
multiply	24.6 ns	0.75	524288
multiply	24.6 ns	0.88	1048576
multiply	24.9 ns	2.71	2097152
multiply	24.3 ns	0.85	4194304
multiply	24.2 ns	0.72	8388608
multiply	25.0 ns	1.38	16777216

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## Mark7 - printing only final values



```
public static double Mark7(String msg, IntToDoubleFunction f) {
    ...
    do {
        ...
    } while (runningTime < 0.25 && count < Integer.MAX_VALUE/2);
    double mean = st/n, sdev = Math.sqrt((sst - mean*mean*n)/(n-1));
    System.out.printf("%-25s %15.1f %10.2f %10d%n", msg, mean, sdev, count);
    return dummy / totalCount;
}</pre>
```

## Timing prime calculation



```
private static boolean isPrimeS(int n) {
  int k = 2;
  while (k < n \&\& n \& k != 0) k++;
  return n \ge 2 \&\& k \ge n;
private static boolean isPrime(int n) {
  int k = 2;
  while (k * k <= n && n % k != 0) k++;</pre>
  return n \ge 2 \&\& k * k > n;
```

Does it matter which one we use?

## Agenda



- Performance measurements: motivation and introduction
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#### Thread creation



```
Mark7("Thread create",
    i -> {
        Thread t = new Thread(() -> {
            for (int j=0; j<1000; j++)
                ai.getAndIncrement();
        });
    return t.hashCode(); // to confuse compiler to not optimize
});</pre>
```

Takes 700 ns

Slow or fast?

What are we really measuring?

A thread is an object, so let us start finding the cost of creating a simple object.

```
class Point {
  public final int x, y;
  public Point(int x, int y) { this.x = x; this.y = y; }
}

Mark7("hashCode()", i -> myPoint.hashCode());

Mark7("Point creation",
    i -> {
     Point p = new Point(i, i);
     return p.hashCode();
    });
```

hashCode() 3 ns Point creation 50 ns

So object creation is: ~ 47 ns

Thread creation ~ 650ns

#### Thread create + start



What are we really measuring?

#### Thread create + start



For loop not included, why?

#### Thread create + start



#### Takes ~ 47000 ns

- So, a lot of work goes into starting a thread
- Even after creating it
- Note: does not include executing the loop

#### Never create threads for small computations !!!

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# Algorithms for parallel computing



#### Quicksort: <a href="https://www.chrislaux.com/quicksort.html">https://www.chrislaux.com/quicksort.html</a>

```
private static void qsort(int[] arr, int a, int b) {
   if (a < b) {
      int i = a, j = b;
      int x = arr[(i+j) / 2];
      do {
        while (arr[i] < x) i++;
        while (arr[j] > x) j--;
        if (i <= j) { swap(arr, i, j); i++; j--; }
      } while (i <= j);
      qsort(arr, a, j); qsort(arr, i, b);
   }
}</pre>
see SearchAndSort.java in week 05 material
```

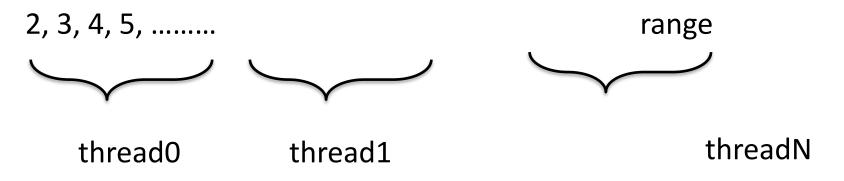
,

#### Prime counting: <a href="https://www.dcode.fr/prime-number-pi-count">https://www.dcode.fr/prime-number-pi-count</a>

```
long count = 0;
final int from = 0, to = range;
for (int i=from; i<to; i++) if (isPrime(i)) count++;</pre>
```

#### Multithreaded version of CountPrimes





Code for exercises week05: TestCountPrimesThreads.java

```
private static long countParallelN(int range, int threadCount
  final int perThread= range / threadCount;
  final LongCounter lc= new PrimeCounter();
  Thread[] threads= new Thread[threadCount];
  for (int t=0; t<threadCount; t++) {</pre>
    final int from= perThread * t,
          to= (t+1==threadCount) ? range : perThread * (t+1);
           threads[t] = new Thread(()
           -> {for (int i=from; i<to; i++)
                                 if (isPrime(i)) lc.increment();
                        });
    for (int t=0; t<threadCount; t++) threads[t].start();</pre>
    try { for (int t=0; t<threadCount; t++) threads[t].join();</pre>
        } catch (InterruptedException exn) { }
    return lc.get();
```

## **TestCountPrimesThreads**

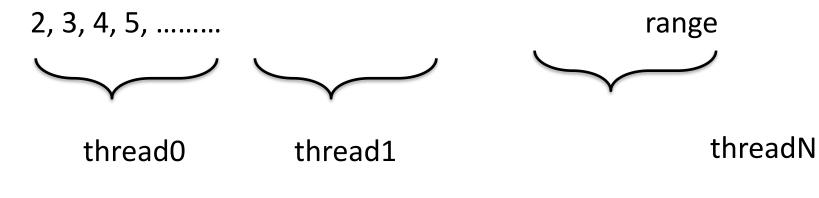


countSequentia	al	5922958.0 ns	289879.33
countParallel	1	7107236.6 ns	448417.55
countParallel	2	6069944.7 ns	802224.61
countParallel	3	3621185.5 ns	152693.03
countParallel	4	3124067.0 ns	640480.51
countParallel	5	3699514.7 ns	364428.77
countParallel	6	4114074.2 ns	642562.19
countParallel	7	2049595.7 ns	26888.15
countParallel	8	1801465.6 ns	12532.85
countParallel	9	1793099.1 ns	11017.57
countParallel	10	1798921.4 ns	11541.43
countParallel	11	1807408.3 ns	9763.61

## Good or bad?



countParallel	1	7107236.6 ns	448417.55
countParallel	2	6069944.7 ns	802224.61
countParallel	3	3621185.5 ns	152693.03
countParallel	4	3124067.0 ns	640480.51
•••			



Is this good or bad, and why?

# Breaking the task into smaller pieces/tasks





When a thread is done with one task, it gets a new task until all tasks are done

Thread(runnable1).start();

Thread(runnable2).start();

new Thread(runnable3).start();

ExecutorService pool;

pool.execute(runnable1);

pool.execute(runnable2); pool.execute(runnable2);

https://howtodoinjava.com/java/multi-threading/java-fixed-size-thread-pool-executor-example/

Threads are expensive!

Reuse of threads



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### Prime counter task (skeleton)

```
47
```

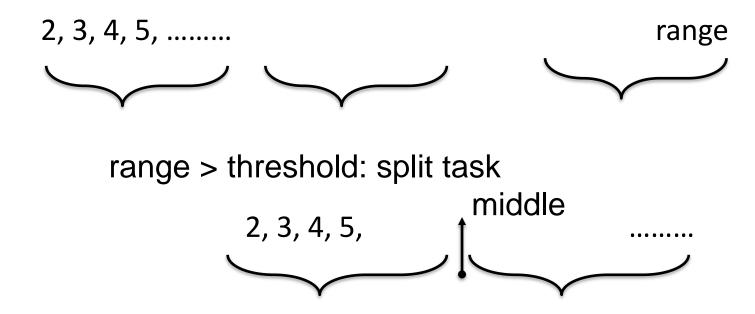
```
public class countPrimesTask implements Runnable {
 private final int low;
  private final int high;
  private final ExecutorService pool;
  @Override public void run() {
    int mid= low+(high-low)/2;
    pool.submit( new countPrimesTask(low, mid, pool) );
    pool.submit( new countPrimesTask(mid+1, high, pool) );
               Shortcomings:
                1. How to stop?
               2. Will create too many "small" tasks
```

3. Returning result (# primes)

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# Reducing the number of tasks





range <= threshold: count the number of primes sequentially

# Splitting tasks



More next week

```
@Override
  public void run() {
  if ((high-low) < threshold) {</pre>
      for (int i=low; i<=high; i++) if (isPrime(i)) lc.increment();</pre>
  } else {
      int mid= low+(high-low)/2;
      pool.submit(new countPrimesTask(lc, low, mid, pool, threshold) );
      pool.submit(new countPrimesTask(lc, mid+1, high, pool, threshold) );
```

1. How to stop?

Shortcomings:

- 2. Will create too many "small" tasks
- 3. Returning result (# primes)

```
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```

```
public class countPrimesExecutor {
  private final PrimeCounter lc; // Global shared variable
                                   // requires atomicity
   public class countPrimesTask implements Runnable {
     public void run() {
          for (int i=low; i<=high; i++)</pre>
            if (isPrime(i)) lc.increment();
```

Could 1c become a bottleneck?

### Counting the primes

```
-53
```

```
public class countPrimesExecutor {
  private final LongCounter lc; // Global shared variable !!!
                                  // requires atomicity
   public class countPrimesTask implements Runnable {
     public void run() {
          for (int i=low; i<=high; i++)</pre>
            if (isPrime(i)) lc.increment();
```

Exercise 5.2?

#### Thread vs Executor



Counting primes in the range 2..1\_000\_000

Sequential 1.2 Sec

Threads (4) 0.5 Sec

Executor 0.4 Sec

More on executors next week

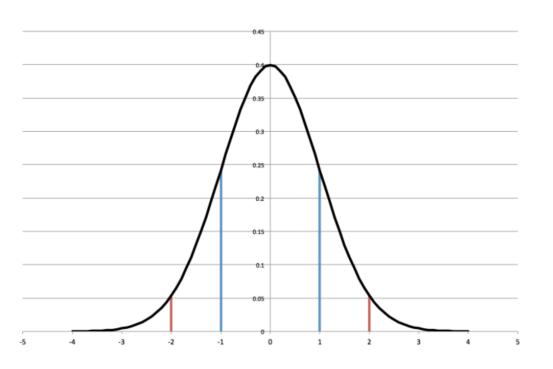
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#### Normal distribution





Measuring physical properties

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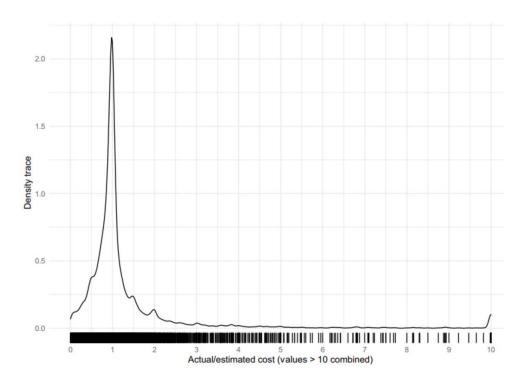
Fabrication faults

Running time of Java code

...

### But there are exceptions





Source: Bent Flyvbjerg, Alexander Budzier, Jong Seok Lee, Mark Keil, Daniel Lunn & Dirk W. Bester (2022) The Empirical Reality of IT Project Cost Overruns: Discovering A Power-Law Distribution, Journal of Management Information Systems, 39:3, 607-639, DOI: 10.1080/07421222.2022.2096544

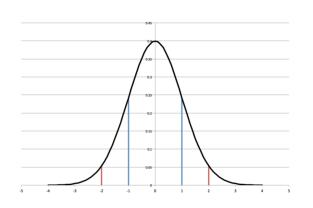
# Standard deviation/variance



$$\mu = \frac{1}{n} \sum_{j=1}^{n} t_j$$

Mean

Benchmark note p6



# Standard deviation/variance

$$\mu = \frac{1}{n} \sum_{j=1}^{n} t_j$$

$$\sigma = \sqrt{\frac{1}{n-1} \sum_{j=1}^{n} (t_j - \mu)^2}$$

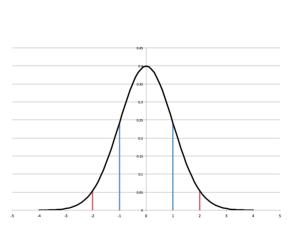
Mean

Standard deviation

Benchmark note p6

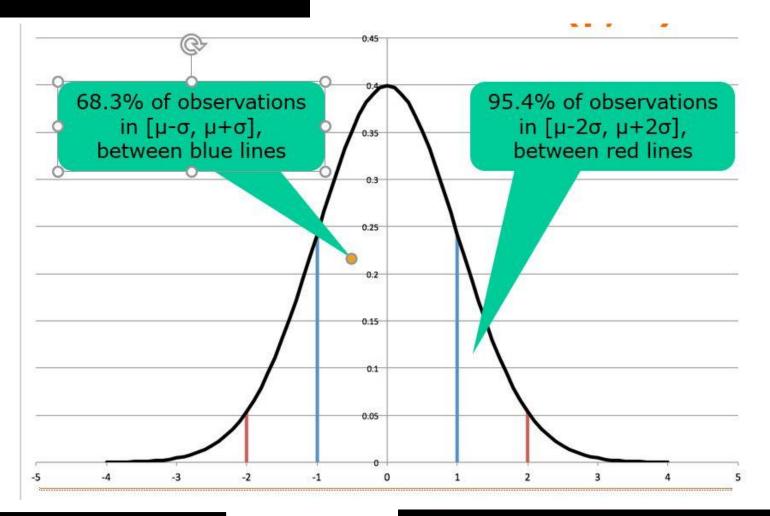
Mean: 32.5 ns Standard deviation: 6.2

30.7 ns 30.3 ns 30.1 ns 30.7 ns 50.2 ns 30.4 ns 30.9 ns 30.3 ns 30.5 ns 30.8 ns ??



#### Normal distribution





#### Outliers



What should you report as the result, when the observations are:

30.7 ns 30.3 ns 30.1 ns 30.7 ns 50.2 ns 30.4 ns 30.9 ns 30.3 ns 30.5 ns 30.8 ns ??

Mean: 32.5 ns Standard deviation: 6.2

50.2 is an outlier

because there is a probability of less than 4.6 % that 50.2 is a correct observation



$$\mu = \frac{1}{n} \sum_{j=1}^{n} t_j$$

$$\sigma = \sqrt{\frac{1}{n-1} \sum_{j=1}^{n} (t_j - \mu)^2}$$

Requires two passes through the data

```
\sigma^2 = \frac{1}{n(n-1)} \left( n \sum_{j=1}^n t_j^2 - \left( \frac{1}{n} \sum_{j=1}^n t_j \right)^2 \right)
```

Can be done in one pass (on-line alg.)

# The two formulas give the same result



$$\mu = \frac{1}{n} \sum_{j=1}^{n} t_{j}$$

$$\sigma = \sqrt{\frac{1}{n-1} \sum_{j=1}^{n} (t_{j} - \mu)^{2}}$$

$$\sigma = \sqrt{\frac{1}{n-1} \sum_{j=1}^{n} (t_{j}^{2} + \mu^{2} - 2t_{j}\mu)}$$

$$\sigma^{2} = \frac{1}{n-1} \sum_{j=1}^{n} (t_{j}^{2} + \mu^{2} - 2t_{j}\mu)$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} + \sum_{j=1}^{n} (\mu^{2} - 2t_{j}\mu)$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} + \sum_{j=1}^{n} (\mu^{2} - 2t_{j}\mu)$$

ormula in Benchmark note

See exercises05.pdf

$$\sigma^{2} = \frac{1}{n-1} \sum_{j=1}^{n} (t_{j}^{2} + \mu^{2} - 2t_{j}\mu)$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} + \sum_{j=1}^{n} (\mu^{2} - 2t_{j}\mu))$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} + n\mu^{2} - 2\mu \sum_{j=1}^{n} t_{j})$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} + n\mu^{2} - 2\mu n\mu)$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} - n\mu^{2})$$

$$\sigma^{2} = \frac{1}{n-1} (\sum_{j=1}^{n} t_{j}^{2} - n\mu^{2})$$

$$\sigma^{2} = \frac{1}{n(n-1)} (n \sum_{j=1}^{n} t_{j}^{2} - \mu^{2})$$

$$\sigma^{2} = \frac{1}{n(n-1)} (n \sum_{j=1}^{n} t_{j}^{2} - (\frac{1}{n} \sum_{j=1}^{n} t_{j})^{2})$$

Formula used in code (one pass algorithm)

also https://en.wikipedia.org/wiki/Algorithms for calculating variance

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### Warning



$$\sigma^{2} = \frac{1}{n(n-1)} \left( n \sum_{i=1}^{n} x_{i}^{2} - \left( \sum_{i=1}^{n} x_{i} \right)^{2} \right)$$

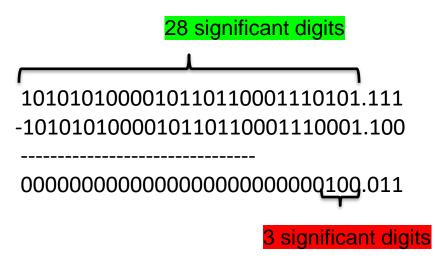
Beware: sst - mean \* mean \* n

can be a very small number

# Digit loss



Beware of cancellation when subtracting numbers that are close to each other:



https://blog.demofox.org/2017/11/21/floating-point-precision