STATS 506 HW 1

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Github URL:

https://github.com/ZHAOShengchun67734538/STAT-506-HW-1

Question 1

(a)

	Туре	Alcohol	Malic.acid	Ash	Alcalinity.of.ash	Magnesium	Total.phenols
1	1	14.23	1.71	2.43	15.6	127	2.80
2	1	13.20	1.78	2.14	11.2	100	2.65
3	1	13.16	2.36	2.67	18.6	101	2.80
4	1	14.37	1.95	2.50	16.8	113	3.85
5	1	13.24	2.59	2.87	21.0	118	2.80
6	1	14.20	1.76	2.45	15.2	112	3.27
Flavanoids Nonflavanoid.phenols Proanthocyanins Color.intensity Hue							
1		3.06		0.	28 2.29)	5.64 1.04
2		2.76		0.	26 1.28	}	4.38 1.05

```
3
        3.24
                               0.30
                                                 2.81
                                                                   5.68 1.03
4
        3.49
                               0.24
                                                 2.18
                                                                   7.80 0.86
        2.69
                               0.39
                                                 1.82
                                                                   4.32 1.04
5
6
        3.39
                               0.34
                                                 1.97
                                                                   6.75 1.05
  OD280.or.OD315 Proline
1
             3.92
                      1065
2
             3.40
                      1050
3
             3.17
                     1185
4
             3.45
                      1480
             2.93
                      735
5
6
             2.85
                      1450
```

nrow(wine.data);ncol(wine.data)

- [1] 178
- [1] 14
- (b)

table(wine.data\$Type)

1 2 3 59 71 48

From the result, we can find that class 1 has 59 instances, class 2 has 71 instances, and class 3 has 48 instances. The output result is the same as the outcome reported in the "wine.names" file.

(c)

(1)

cor(wine.data\$Alcohol, wine.data\$Color.intensity)

[1] 0.5463642

(2)

```
wine.class1 = wine.data[which(wine.data[,1] == 1),]
wine.class2 = wine.data[which(wine.data[,1] == 2),]
wine.class3 = wine.data[which(wine.data[,1] == 3),]
cor1 = cor(wine.class1$Alcohol, wine.class1$Color.intensity)
cor2 = cor(wine.class2$Alcohol, wine.class2$Color.intensity)
cor3 = cor(wine.class3$Alcohol, wine.class3$Color.intensity)
cor1;cor2;cor3
```

- [1] 0.4082913
- [1] 0.2697891
- [1] 0.3503777

From the result, we can find that in three class, the alcohol and color intensity have positive correlation, and the class 1 has the highest correlation and class 2 has the lowest correlation.

(3)

```
wine.data[which(wine.data[,11] == max(wine.data[,11])),2]
```

[1] 14.34

The 11-th column is the Color Intensity. From the result, we can find the alcohol content of wine with the highest color intensity is 14.34.

(4)

```
rownumber = nrow(wine.data[which(wine.data[,10]>wine.data[,4]),])
(rownumber/nrow(wine.data))*100
```

[1] 8.426966

The 10-th column is Proanthocyanins and the 4-th column is Ash. From the result, we can find it has 8.426966% of wines had a higher content of Proanthocyanins compare to Ash.

(d)

```
overall = apply(wine.data[,2:14],2,mean)
  c1 = apply(wine.data[which(wine.data[,1] == 1),2:14],2,mean)
  c2 = apply(wine.data[which(wine.data[,1] == 2),2:14],2,mean)
  c3 = apply(wine.data[which(wine.data[,1] == 3),2:14],2,mean)
  rbind(overall, c1, c2, c3)
                                 Ash Alcalinity.of.ash Magnesium Total.phenols
         Alcohol Malic.acid
                                               19.49494 99.74157
overall 13.00062
                   2.336348 2.366517
                                                                       2.295112
c1
        13.74475
                   2.010678 2.455593
                                               17.03729 106.33898
                                                                       2.840169
c2
        12.27873
                   1.932676 2.244789
                                               20.23803 94.54930
                                                                       2.258873
сЗ
        13.15375
                   3.333750 2.437083
                                               21.41667 99.31250
                                                                       1.678750
        Flavanoids Nonflavanoid.phenols Proanthocyanins Color.intensity
overall 2.0292697
                              0.3618539
                                                1.590899
                                                                5.058090
         2.9823729
                              0.2900000
                                                1.899322
                                                                5.528305
c1
c2
         2.0808451
                              0.3636620
                                                1.630282
                                                                3.086620
сЗ
         0.7814583
                              0.4475000
                                                1.153542
                                                                7.396250
              Hue OD280.or.OD315
                                   Proline
overall 0.9574494
                        2.611685 746.8933
c1
                        3.157797 1115.7119
        1.0620339
c2
        1.0562817
                        2.785352 519.5070
сЗ
        0.6827083
                        1.683542 629.8958
(e)
  # The 7-th column is phenols
  class1 = wine.data[which(wine.data[,1] == 1),7]
  class2 = wine.data[which(wine.data[,1] == 2),7]
  class3 = wine.data[which(wine.data[,1] == 3),7]
  n1 = length(class1)
  n2 = length(class2)
  n3 = length(class3)
  mean1 = mean(class1)
  mean2 = mean(class2)
  mean3 = mean(class3)
  var1 = var(class1)
  var2 = var(class2)
  var3 = var(class3)
  # In the t-test, we use two sample t-test
  # Assumen they have equal variance, set alpha = 0.05
```

```
# For class 1 and class 2
pooled.var12 = (((n1 - 1)*var1) + ((n2 - 1)*var2))/(n1 + n2 - 2)
t.stat12 = (mean1 - mean2)/sqrt(pooled.var12*(1/n1 + 1/n2))
pvalue12 = 2*pt(-abs(t.stat12), (n1+n2-2))

# For class 2 and class 3
pooled.var23 = (((n2 - 1)*var2) + ((n3 - 1)*var3))/(n2 + n3 - 2)
t.stat23 = (mean2 - mean3)/sqrt(pooled.var23*(1/n2 + 1/n3))
pvalue23 = 2*pt(-abs(t.stat23), (n2+n3-2))

# For class 1 and class 3
pooled.var13 = (((n1 - 1)*var1) + ((n3 - 1)*var3))/(n1 + n3 - 2)
t.stat13 = (mean1 - mean3)/sqrt(pooled.var13*(1/n1 + 1/n3))
pvalue13 = 2*pt(-abs(t.stat13), (n1+n3-2))

# We also need to adjust the p-value for comparison
pvalues = c(pvalue12, pvalue23, pvalue13)
pvalues
```

[1] 6.865291e-11 2.203376e-09 2.437614e-32

```
adjust.pvalues = p.adjust(pvalues, method = "holm")
adjust.pvalues
```

[1] 1.373058e-10 2.203376e-09 7.312843e-32

Class 1 & Class 2: After Holm correction, the adjusted p-value is 1.373058e-10, which is lower than 0.05, there is a statistically significant.

Class 2 & Class 3: After Holm correction, the adjusted p-value is 2.203376e-09, which is lower than 0.05, there is a statistically significant.

Class 1 & Class 3: After Holm correction, the adjusted p-value is 7.312843e-32, which is lower than 0.05, there is a statistically significant.

Summary: The two-sample t-tests show that there are statistically significant differences in phenol levels between any of the class pairs.

Question 2

(a)

```
# After download the data to my own computer,
  # import the data from my own computer
  data = read.csv("C:/Users/z1883/Desktop/AskAManager.csv", header = TRUE)
  head(data)
             Timestamp How.old.are.you. What.industry.do.you.work.in.
1 1 4/27/2021 11:02:10
                                  25-34 Education (Higher Education)
2 2 4/27/2021 11:02:22
                                  25-34
                                                     Computing or Tech
3 3 4/27/2021 11:02:38
                                  25-34 Accounting, Banking & Finance
4 4 4/27/2021 11:02:41
                                  25-34
                                                            Nonprofits
5 5 4/27/2021 11:02:42
                                  25-34 Accounting, Banking & Finance
6 6 4/27/2021 11:02:46
                                  25-34 Education (Higher Education)
                                 Job.title
        Research and Instruction Librarian
2 Change & Internal Communications Manager
3
                      Marketing Specialist
4
                           Program Manager
5
                        Accounting Manager
            Scholarly Publishing Librarian
  If.your.job.title.needs.additional.context..please.clarify.here.
1
2
3
4
5
6
  What.is.your.annual.salary...You.ll.indicate.the.currency.in.a.later.question..If.you.are.
1
2
3
4
5
  How.much.additional.monetary.compensation.do.you.get..if.any..for.example..bonuses.or.over
1
2
3
4
5
6
  Please.indicate.the.currency If..Other...please.indicate.the.currency.here..
1
                           USD
```

```
2
                            GBP
3
                            USD
4
                            USD
5
                            USD
6
                            USD
  If.your.income.needs.additional.context..please.provide.it.here.
2
3
4
5
6
  What.country.do.you.work.in.
                 United States
1
2
                United Kingdom
3
                             US
4
                            USA
5
                             US
6
                            USA
  If.you.re.in.the.U.S...what.state.do.you.work.in. What.city.do.you.work.in.
                                       Massachusetts
1
                                                                          Boston
2
                                                                       Cambridge
3
                                            Tennessee
                                                                     Chattanooga
4
                                            Wisconsin
                                                                       Milwaukee
5
                                      South Carolina
                                                                      Greenville
6
                                        New Hampshire
                                                                         Hanover
  How.many.years.of.professional.work.experience.do.you.have.overall.
1
                                                               5-7 years
2
                                                            8 - 10 years
3
                                                             2 - 4 years
4
                                                            8 - 10 years
5
                                                            8 - 10 years
6
                                                            8 - 10 years
 How.many.years.of.professional.work.experience.do.you.have.in.your.field.
                                                                     5-7 years
1
2
                                                                     5-7 years
3
                                                                   2 - 4 years
                                                                     5-7 years
4
5
                                                                     5-7 years
                                                                   2 - 4 years
  What.is.your.highest.level.of.education.completed. What.is.your.gender.
                                      Master's degree
                                                                       Woman
1
2
                                        College degree
                                                                  Non-binary
```

```
3
                                       College degree
                                                                      Woman
4
                                                                      Woman
                                       College degree
5
                                       College degree
                                                                      Woman
6
                                      Master's degree
                                                                        Man
  What.is.your.race...Choose.all.that.apply..
1
                                         White
2
                                         White
3
                                         White
4
                                         White
5
                                         White
6
                                         White
(b)
  colnames(data) = c("No.", "Timestamp", "Age", "Industry", "Job Title",
                      "Job Title Supplement", "Salary", "Monetary Compensation",
                      "Currency of Salary", "Other Currency",
                      "Additional Context of Income",
                      "Working Country", "Working State(if in the US)",
                      "Working City", "Overall Working Years",
                      "Working Years in your field",
                      "Highest education level", "Gender", "Race(indicate all)")
  head(data)
  No.
               Timestamp
                                                      Industry
                            Age
1
   1 4/27/2021 11:02:10 25-34 Education (Higher Education)
   2 4/27/2021 11:02:22 25-34
                                            Computing or Tech
   3 4/27/2021 11:02:38 25-34 Accounting, Banking & Finance
   4 4/27/2021 11:02:41 25-34
                                                    Nonprofits
    5 4/27/2021 11:02:42 25-34 Accounting, Banking & Finance
    6 4/27/2021 11:02:46 25-34 Education (Higher Education)
                                  Job Title Job Title Supplement Salary
1
        Research and Instruction Librarian
                                                                   55000
2 Change & Internal Communications Manager
                                                                   54600
3
                      Marketing Specialist
                                                                   34000
4
                            Program Manager
                                                                   62000
5
                         Accounting Manager
                                                                   60000
            Scholarly Publishing Librarian
                                                                   62000
  Monetary Compensation Currency of Salary Other Currency
1
                                        USD
2
                   4000
                                        GBP
3
                     NA
                                        USD
```

```
4
                    3000
                                        USD
5
                    7000
                                        USD
                                        USD
6
                     NA
  Additional Context of Income Working Country Working State(if in the US)
                                  United States
1
                                                               Massachusetts
2
                                 United Kingdom
3
                                                                    Tennessee
4
                                             USA
                                                                    Wisconsin
5
                                              US
                                                              South Carolina
                                             USA
6
                                                               New Hampshire
  Working City Overall Working Years Working Years in your field
        Boston
1
                            5-7 years
                                                         5-7 years
2
     Cambridge
                         8 - 10 years
                                                         5-7 years
3
                          2 - 4 years
   Chattanooga
                                                       2 - 4 years
4
     Milwaukee
                         8 - 10 years
                                                         5-7 years
5
    Greenville
                         8 - 10 years
                                                         5-7 years
       Hanover
                         8 - 10 years
                                                       2 - 4 years
                               Gender Race(indicate all)
  Highest education level
          Master's degree
                                Woman
                                                    White
1
2
           College degree Non-binary
                                                    White
3
           College degree
                                Woman
                                                    White
4
           College degree
                                Woman
                                                    White
5
           College degree
                                Woman
                                                    White
6
          Master's degree
                                                    White
                                  Man
(c)
  us.data = data[which(data[,9] == "USD"),]
  head(us.data)
  No.
               Timestamp
                                                      Industry
                            Age
1
    1 4/27/2021 11:02:10 25-34
                                Education (Higher Education)
   3 4/27/2021 11:02:38 25-34 Accounting, Banking & Finance
   4 4/27/2021 11:02:41 25-34
   5 4/27/2021 11:02:42 25-34 Accounting, Banking & Finance
    6 4/27/2021 11:02:46 25-34 Education (Higher Education)
    7 4/27/2021 11:02:51 25-34
                                                    Publishing
                            Job Title Job Title Supplement Salary
1 Research and Instruction Librarian
                                                             55000
3
                Marketing Specialist
                                                             34000
4
                     Program Manager
                                                             62000
5
                  Accounting Manager
                                                             60000
```

```
6
      Scholarly Publishing Librarian
                                                              62000
7
                Publishing Assistant
                                                              33000
  Monetary Compensation Currency of Salary Other Currency
                       0
                                         USD
1
3
                     NA
                                         USD
4
                    3000
                                         USD
5
                    7000
                                         USD
6
                      NA
                                         USD
7
                    2000
                                         USD
  Additional Context of Income Working Country Working State(if in the US)
                                  United States
                                                                Massachusetts
1
3
                                              US
                                                                    Tennessee
                                             USA
4
                                                                    Wisconsin
5
                                              US
                                                               South Carolina
6
                                             USA
                                                                New Hampshire
7
                                             USA
                                                               South Carolina
  Working City Overall Working Years Working Years in your field
        Boston
                            5-7 years
                                                          5-7 years
1
3
   Chattanooga
                          2 - 4 years
                                                       2 - 4 years
4
     Milwaukee
                         8 - 10 years
                                                          5-7 years
    Greenville
5
                         8 - 10 years
                                                          5-7 years
       Hanover
                         8 - 10 years
                                                       2 - 4 years
6
      Columbia
                          2 - 4 years
                                                       2 - 4 years
  Highest education level Gender Race(indicate all)
1
          Master's degree
                            Woman
                                                White
3
           College degree
                            Woman
                                                White
4
           College degree
                                                White
                            Woman
5
           College degree
                            Woman
                                                White
          Master's degree
                                                White
6
                              Man
7
           College degree
                            Woman
                                                White
  # the number of rows before restrict
  nrow(data)
[1] 28062
  # the number of rows after restrict
  nrow(us.data)
```

[1] 23374

We can see from the result, after restrict, there is 23374 data, clearly, it worked.

(d)

There are three types of mistakes that we need to delete.

- 1, The age is under 18, which is contradictory with our assumption.
- 2, The overall-working-years is smaller than working-years-in-your-field. because it is nonsense, we need to delete the working-years-in-your-field is larger than overall-working-years.
- 3, Since in "Age" and "Overall Working Years" column is a range, if the max age minus 18 is less than the min working-overall-years, which means they must start to work under 18, which is contradictory with our assumption, so, we also should delete these rows.

```
# solve the mistake 1
  unique(us.data$Age)
                                                        "65 or over"
[1] "25-34"
                 "45-54"
                              "35-44"
                                           "18-24"
[6] "55-64"
                 "under 18"
  us.data1 = us.data[-which(us.data[,3] == "under 18"),]
  unique(us.data1$Age)
[1] "25-34"
                 "45-54"
                             "35-44"
                                                        "65 or over"
                                           "18-24"
[6] "55-64"
  # solve the mistake 2
  # First we need to check how many categories thery have
  unique(us.data1$`Overall Working Years`)
                      "2 - 4 years"
                                          "8 - 10 years"
[1] "5-7 years"
                                                             "21 - 30 years"
                      "41 years or more" "31 - 40 years"
                                                             "1 year or less"
[5] "11 - 20 years"
  unique(us.data1$`Working Years in your field`)
[1] "5-7 years"
                      "2 - 4 years"
                                          "21 - 30 years"
                                                             "11 - 20 years"
                      "1 year or less"
[5] "8 - 10 years"
                                          "31 - 40 years"
                                                             "41 years or more"
```

From the result, we can find "overall working years" and "Working Years in your field" have the same categories, which are: 1 year or less, 2-4 years, 5-7 years, 8-10 years, 11-20 years, 21-30 years, 31-40 years, 41 years or more. So, we could use integer number 1, 2, 3,..., 8 to represent each category respectively, since it is easy to compare.

```
# do transformation to "overall working years"
  n1 = nrow(us.data1)
  overall.label = c(1:n1)*0
  for(i in 1:n1)
    if(us.data1[i,15] == "1 year or less"){overall.label[i] = 1}
    if(us.data1[i,15] == "2 - 4 years"){overall.label[i] = 2}
    if(us.data1[i,15] == "5-7 years"){overall.label[i] = 3}
    if(us.data1[i,15] == "8 - 10 years"){overall.label[i] = 4}
    if(us.data1[i,15] == "11 - 20 years"){overall.label[i] = 5}
    if(us.data1[i,15] == "21 - 30 years"){overall.label[i] = 6}
    if(us.data1[i, 15] == "31 - 40 years"){overall.label[i] = 7}
    if(us.data1[i,15] == "41 years or more"){overall.label[i] = 8}
  # do the same transformation to "Working Years in your field"
  field.label = c(1:n1)*0
  for(i in 1:n1)
    if(us.data1[i,16] == "1 year or less"){field.label[i] = 1}
    if(us.data1[i,16] == "2 - 4 years"){field.label[i] = 2}
    if(us.data1[i,16] == "5-7 years"){field.label[i] = 3}
    if(us.data1[i,16] == "8 - 10 years"){field.label[i] = 4}
    if(us.data1[i,16] == "11 - 20 years"){field.label[i] = 5}
    if(us.data1[i,16] == "21 - 30 years"){field.label[i] = 6}
    if(us.data1[i,16] == "31 - 40 years"){field.label[i] = 7}
    if(us.data1[i,16] == "41 years or more"){field.label[i] = 8}
  us.data1 = cbind(us.data1, overall.label, field.label)
  us.data2 = us.data1[-which(us.data1[,20] < us.data1[,21]),1:19]
  nrow(us.data2)
[1] 23145
  # solve the mistake 3
  unique(us.data2$Age)
```

```
[1] "25-34" "45-54" "35-44" "18-24" "65 or over"
[6] "55-64"

unique(us.data2$`Overall Working Years`)

[1] "5-7 years" "2 - 4 years" "8 - 10 years" "21 - 30 years"
[5] "11 - 20 years" "41 years or more" "31 - 40 years" "1 year or less"
```

Transformation to the Age column:

From the above result, we find the age column has 6 categories, so we only take the max value of each category and minus 18, for example, if the Age = "45-54", we only take 54 and do the calculation 54-18 = 36, then assign 36 to the new column "max.age". And for category "65 or over", we take the max value as 84 (because in general case, there are very little people working over 84) and do 84-18 = 66, then assign 66 to the new column "max.age".

Transformation to the Overall working years column:

From the above result, we find this column has 8 categories, so, we only take the min value of each category. For example, if "Overall working years" = "1 year or less", then assign 0 to the new column "min.overall", if "Overall working years" = "41 years or more", then assign 41 to the new column "min.overall".

```
n2 = nrow(us.data2)
\max.age = c(1:n2)*0
for(i in 1:n2)
  if(us.data2[i,3] == "18-24"){max.age[i] = 6}
  if(us.data2[i,3] == "25-34"){max.age[i] = 16}
  if(us.data2[i,3] == "35-44"){max.age[i] = 26}
  if(us.data2[i,3] == "45-54"){max.age[i] = 36}
  if(us.data2[i,3] == "55-64"){max.age[i] = 46}
  if(us.data2[i,3] == "65 \text{ or over"})\{max.age[i] = 66\}
}
min.overall = c(1:n2)*0
for(i in 1:n2)
  if(us.data2[i,15] == "1 year or less"){min.overall[i] = 0}
  if(us.data2[i,15] == "2 - 4 years"){min.overall[i] = 2}
  if(us.data2[i,15] == "5-7 years"){min.overall[i] = 5}
  if(us.data2[i,15] == "8 - 10 years"){min.overall[i] = 8}
  if(us.data2[i,15] == "11 - 20 years"){min.overall[i] = 11}
```

```
if(us.data2[i,15] == "21 - 30 years"){min.overall[i] = 21}
if(us.data2[i,15] == "31 - 40 years"){min.overall[i] = 31}
if(us.data2[i,15] == "41 years or more"){min.overall[i] = 41}
}
us.data2 = cbind(us.data2, max.age, min.overall)
us.data3 = us.data2[-which(us.data2[,20]<us.data2[,21]),1:19]
nrow(us.data3)</pre>
```

[1] 23116

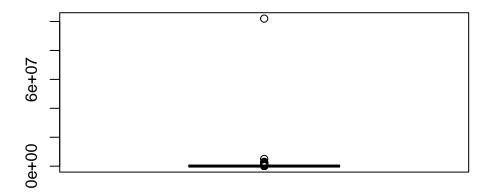
From, we have eliminate all the rows for which their age, years of experience in their field, and years of experience total are impossible, the final total number of observation is 23116.

(e)

```
# First, let find whether they have NA value
sum(is.na(us.data3[,7]))
```

[1] 0

```
# From the result, we can find there is no NA value,
# So, we just need to eliminate the outliers of the salary
# In this section, we choose to use IQR Method to delete the outliers.
boxplot(us.data3[,7])
```



```
Q1 = quantile(us.data3[,7],0.25)

Q3 = quantile(us.data3[,7],0.75)

IQR = Q3 - Q1

IQR

75%

55644

low = Q1-1.5*IQR

up = Q3+1.5*IQR

low;up

25%

-27110

75%

195466
```

```
# since low is negative, but salary cannot be negative
# So, we just need to consider the data which is larger than Q3+1.5*IQR
us.data4 = us.data3[-which(us.data3[,7]>up),]
head(us.data4)
```

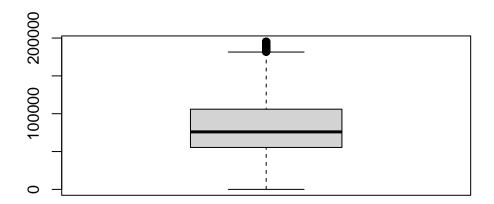
```
No.
               Timestamp
                                                      Industry
                            Age
1
    1 4/27/2021 11:02:10 25-34 Education (Higher Education)
   3 4/27/2021 11:02:38 25-34 Accounting, Banking & Finance
3
   4 4/27/2021 11:02:41 25-34
4
                                                    Nonprofits
   5 4/27/2021 11:02:42 25-34 Accounting, Banking & Finance
   6 4/27/2021 11:02:46 25-34 Education (Higher Education)
    7 4/27/2021 11:02:51 25-34
                                                    Publishing
                            Job Title Job Title Supplement Salary
1 Research and Instruction Librarian
                                                             55000
3
                Marketing Specialist
                                                             34000
4
                     Program Manager
                                                             62000
5
                                                             60000
                  Accounting Manager
6
      Scholarly Publishing Librarian
                                                             62000
                Publishing Assistant
                                                             33000
  Monetary Compensation Currency of Salary Other Currency
1
                                        USD
3
                     NA
                                        USD
4
                    3000
                                        USD
5
                    7000
                                        USD
6
                                        USD
                     NA
7
                    2000
                                        USD
  Additional Context of Income Working Country Working State(if in the US)
                                  United States
1
                                                               Massachusetts
3
                                             US
                                                                    Tennessee
4
                                            USA
                                                                    Wisconsin
5
                                             US
                                                              South Carolina
6
                                            USA
                                                               New Hampshire
7
                                            USA
                                                              South Carolina
  Working City Overall Working Years Working Years in your field
1
        Boston
                            5-7 years
                                                         5-7 years
3
  Chattanooga
                          2 - 4 years
                                                       2 - 4 years
4
     Milwaukee
                         8 - 10 years
                                                         5-7 years
5
    Greenville
                         8 - 10 years
                                                         5-7 years
6
       Hanover
                         8 - 10 years
                                                       2 - 4 years
7
      Columbia
                          2 - 4 years
                                                       2 - 4 years
  Highest education level Gender Race(indicate all)
1
          Master's degree Woman
                                                White
```

```
College degree
3
                                                White
                            Woman
4
           College degree
                            Woman
                                                White
           College degree
5
                                                White
                            Woman
6
          Master's degree
                              Man
                                                White
           College degree
7
                                                White
                            Woman
```

nrow(us.data4)

[1] 22207

boxplot(us.data4[,7])



- # from the new plot, we can find the new data is much better than before.
- # and the new data set has 22207 observations

Question 3

(a)

```
#' check palindromic
#' @param positive integer
#' @return a list which contain
#' whether it is a palindromic
#' and give us the reverse of the input
#' @examples if you input not a positive integer
#' it will stop run and give you a warning, if you input
#' 728827, it will return $isPalindromic TRUE, reversed 728827
isPalindromic = function(value)
  # we must assure that the input is a postive integer.
  if(!is.numeric(value))
    warning("Input must be a positive integer.")
    stop("This input is not a numeric, please try again.")
  if(abs(value) != value)
    warning("Input must be a positive integer.")
    stop("This input is not a positive number, please try again.")
  if(value != as.integer(value))
    warning("Input must be a positive integer.")
    stop("This input is not an integer, please try again.")
  # it is more easy to do operation on character rather than integer.
  value = as.integer(value)
  input = as.character(value)
  # this is to split the whole string into one character
  # and it will be easy to reverse, after reverse,
  # let the reversed single characters be pasted without blank.
  rev.input = paste(rev(unlist(strsplit(input, NULL))), collapse="")
  rev.value = as.integer(rev.input)
  # check whether it is a palindromic
  result <- (rev.value == value)
  list.data = list(result, rev.value)
  names(list.data) = c("isPalindromic", "reversed")
  return(list.data)
}
```

```
# you can verified the below three comments from the R code I uploaded in
  # Githhub, we cannot render this quarto file if we execute the below
  # three comments.
  #isPalindromic("dasdas")
  #isPalindromic(-12.88)
  #isPalindromic(3456.897)
  isPalindromic(7556)
$isPalindromic
[1] FALSE
$reversed
[1] 6557
  isPalindromic(6789)
$isPalindromic
[1] FALSE
$reversed
[1] 9876
  isPalindromic(8228)
$isPalindromic
[1] TRUE
$reversed
[1] 8228
(b)
```

For palindromic, there exist 3 special cases.

- 1, Integer 0-8: for this case, we consider these number are palindromic, the next palindromic is number + 1, for example, if input is 8, then, output will be 9.
- $2, 9, 99, 999, \dots$, for this kind of number, the next palindromic is number +2, for example, if you input is 99999, then, the output is 100001.
- 3 10, 100,1000, ..., for this kind of number, the next palindromic is number + 1, for example, if you input is 100000, then, the output is 100001.

```
#' Find next palindromic
#' @param positive integer
#' @return the next palindromic which is
#' strictly larger than the input.
#' @examples if you input not a positive integer
#' it will stop run and give you a warning
#' if you input 7668, the output is 7777.
nextPalindrome = function(value)
  next.palindromic = 0
  if(!is.numeric(value))
    warning("Input must be a positive integer.")
    stop("This input is not a numeric, please try again.")
  }
  if(abs(value) != value)
    warning("Input must be a positive integer.")
    stop("This input is not a positive number, please try again.")
  if(value != as.integer(value))
    warning("Input must be a positive integer.")
    stop("This input is not an integer, please try again.")
  }
  ###################################
  # Special Case
  value = as.integer(value)
  if(value \leq 8 \& value \geq 0)
    next.palindromic = value + 1
    return(next.palindromic)
  if(log10(value) == as.integer(log10(value)))
    next.palindromic = value + 1
    return(next.palindromic)
  }
```

```
if(log10(value+1) == as.integer(log10(value+1)))
 next.palindromic = value + 2
 return(next.palindromic)
######################################
# Genral Case
# First, we need to find how many digits does this number have.
# it's more easy to do operations after converting the number to a string.
input = as.character(value)
n = nchar(input)
if(n\%\%2 == 0)
  # For the number has even digits:
  # Splitting the number into two halves.
  # Mirroring the left half.
  # If the mirrored left half number is larger than the right half number,
  # just paste the original left half with the mirrored left half,
  # and then it will be the next palindromic.
  # If the mirrored left half number is less or equal than
  # the right half number,
  # then, constantly increase the original left half number by 1,
  # then mirrored this new left half number,
  # then paste the new left half number with its mirrored one to form a
  # palindromic, then use this palindromic to compare with the input,
  # until this palindromic is larger than the input value
  # we can stop increasing the left half number
  # and output the palindromic.
  # This will be the next palindromic.
  leftinput = substr(input, 1, n/2)
  rightinput = substr(input, ((n/2)+1), n)
  rev.leftinput = paste(rev(unlist(strsplit(leftinput, NULL))),
                        collapse="")
  rev.leftvalue = as.integer(rev.leftinput)
  leftvalue = as.integer(leftinput)
  rightvalue = as.integer(rightinput)
  if(rev.leftvalue > rightvalue)
```

```
char = paste(leftinput,rev.leftinput,sep = "")
    next.palindromic = as.integer(char)
    return(next.palindromic)
  if(rev.leftvalue <= rightvalue)</pre>
    sign = TRUE
    while(sign)
      leftvalue = leftvalue + 1
      leftinput = as.character(leftvalue)
      rev.leftinput = paste(rev(unlist(strsplit(leftinput, NULL)))),
                            collapse="")
      char = paste(leftinput,rev.leftinput,sep = "")
      palindromic = as.integer(char)
      if(palindromic > value)
        next.palindromic = palindromic
        sign = FALSE
        return(next.palindromic)
    }
  }
}else
  # For the number has odd digits
  # the odd digits number has the middle digit
  # splitting the number into left half number (without the middle digit),
  # left-middle half number (means left half + middle digit)
  # and the right half number.
  # if the left half number is larger than the right half numer,
  # just paste the original left half number, middle digits,
  # and with the mirrored left half number,
  # and then it will be the next palindromic.
  # if the left half number is less or equal the right half number,
  # constantly increase the left-middle half number by 1,
  # mirror this left-middle half number without mirroring the middle
  # digits (which means after increaseing, we only mirror the left half,
  # but donot mirror the middle digit), then paste the increased
```

```
# left-middle half number with the mirrored left half number together,
# this will be a palindromic, then, compare this palindromic with
# the input value,
# until this palindromic is larger than the input value
# we can stop increasing the left-middle half number,
# and output the palindromic.
# This will be the next palindromic.
leftinput = substr(input, 1, (n-1)/2)
left.middle.input = substr(input,1,(n+1)/2)
rightinput = substr(input,(((n+1)/2)+1),n)
rev.leftinput = paste(rev(unlist(strsplit(leftinput, NULL)))),
                      collapse="")
rev.leftvalue = as.integer(rev.leftinput)
leftvalue = as.integer(leftinput)
left.middle.value = as.integer(left.middle.input)
rightvalue = as.integer(rightinput)
if(rev.leftvalue > rightvalue)
  char = paste(left.middle.input,rev.leftinput,sep = "")
 next.palindromic = as.integer(char)
 return(next.palindromic)
}
if(rev.leftvalue <= rightvalue)</pre>
  sign = TRUE
 while(sign)
    left.middle.value = left.middle.value + 1
    left.middle.input = as.character(left.middle.value)
    num = nchar(left.middle.input)
    leftinput = substr(left.middle.input, 1, (num-1))
    rev.leftinput = paste(rev(unlist(strsplit(leftinput, NULL))),
                          collapse="")
    char = paste(left.middle.input,rev.leftinput,sep = "")
    palindromic = as.integer(char)
    if(palindromic > value)
      next.palindromic = palindromic
      sign = FALSE
      return(next.palindromic)
```

```
}
      }
    }
  # Test Case:
  nextPalindrome(728827)
[1] 729927
  nextPalindrome(39951)
[1] 39993
  nextPalindrome(7152)
[1] 7227
  nextPalindrome(765431537)
[1] 765434567
  nextPalindrome(999)
[1] 1001
  nextPalindrome(10000)
[1] 10001
  nextPalindrome(1800)
[1] 1881
(c)
```

```
nextPalindrome(391)

[1] 393

nextPalindrome(9928)

[1] 9999

nextPalindrome(19272719)

[1] 19277291

nextPalindrome(109)

[1] 111

nextPalindrome(2)
```