Name:

CSE341 Autumn 2017, Midterm Examination October 30, 2017

Please do not turn the page until 2:30.

Rules:

- The exam is closed-book, closed-note, etc. except for one side of one 8.5x11in piece of paper.
- Please stop promptly at 3:20.
- There are 100 points, distributed unevenly among 6 questions (all with multiple parts):
- The exam is printed double-sided.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit. But clearly indicate what is your final answer.
- The questions are not necessarily in order of difficulty. Skip around. Make sure you get to all the questions.
- If you have questions, ask.
- Relax. You are here to learn.

Name:

1. (20 points) This problem uses this datatype binding, where an exp is a simple arithmetic expression like we studied in class except instead of negations and multiplications, we have doubling and (integer) division.

- (a) Write a function eval_exp of type exp -> int that returns the "answer" for "executing" the arithmetic expression. Some notes on division:
 - Use integer division, which in ML is done with the infix operator div. For example, in ML, 6 div 4 is 1.
 - Division by zero will raise an exception, which is fine.
- (b) Give an example of a value of type exp where:
 - Calling eval_exp with your expression causes a division-by-zero exception, but ...
 - ... no use of the Divide constructor has Constant O as its second argument.
- (c) Write a function no_literal_zero_divide of type exp -> bool that returns true if and only if no use of the Divide constructor has Constant 0 as its second argument. Notes:
 - So, no_literal_zero_divide applied to your answer to the previous question would evaluate to true.
 - You should *not* use eval_exp this question has nothing to do with evaluating expressions.

Name:____

2. (20 points) This problem uses this somewhat silly function:

- (a) What is the type of f?
- (b) What does f([3],[10]) evaluate to?
- (c) What does f([3,4],[10,11]) evaluate to?
- (d) What does f([3,4,5],[10,11,12]) evaluate to?
- (e) What does f([3,4,5,6],[10,11,12,13]) evaluate to?
- (f) Describe in at most 1 English sentence all the inputs to f such that the result of f is NONE.
- (g) Yes or no: Is f tail-recurisve?

For each of the remaining questions, give one of these answers (just the letter is enough):

- A. The result no longer type-checks.
- B. The result type-checks but gives different answers for some inputs.
- C. The result type-checks and gives the same answer for all inputs.

Also, ignore the syntax detail that the first branch has no | character and the others do — assume that is fixed appropriately.

- (h) What happens if we move branch 2 of f to be the first pattern in the case expression?
- (i) What happens if we move branch 3 of f to be the first pattern in the case expression?
- (j) What happens if we move branch 4 of f to be the first pattern in the case expression?
- (k) What happens if we move branch 5 of f to be the first pattern in the case expression?

Name:

3. (12 points) In this problem, we ask you to give *good* error messages for why a short ML program does *not* type-check. A *specific* phrase or short sentence is plenty.

For example, for the program,

```
fun f1 (x,y) = if x then y + 1 else x
```

a fine answer would be, "the then-branch-expression and the else-branch-expression do not have the same type."

Give good error messages for each of the following:

```
(a) fun f2 g xs =
      case xs of
          [] => []
        | x::xs' => (g x) :: f2 xs'
(b) fun f3 xs =
      case xs of
          [] => NONE
        | x::[] => SOME 1
        | x::xs' => SOME (1 + (f3 xs'))
(c) datatype t = A of int | B of (int * t) list
   fun f4 x =
      let
          fun aux ys =
            case ys of
                 [] => []
               | (i,j)::ys => (i+1,j)::(aux ys)
      in
          {\tt case}\ {\tt x}\ {\tt of}
              A i => x
            | B ys \Rightarrow B (aux x)
      end
(d) exception Foo
   fun f5 x = if x > 3 then x else raise Foo
   fun f6 y = (f5 (y+1)) handle _ => false
```

4. (21 points)

- (a) Without using any helper functions (except ::) write a function zipWith of type ('a * 'b -> 'c) -> 'a list -> 'b list -> 'c list as follows:
 - It takes three arguments in curried form.
 - The length of the result is the length of the shorter of the second or third argument.
 - The i^{th} element of the output is the first argument applied to the i^{th} elements of the second and third arguments.
- (b) Use a val binding and a partial application of zipWith to define a function first_bigger of type int list -> int list -> bool list where, for example, first_bigger [1,7,9] [0,10,9,4,2] = [true, false, false]
- (c) Here are two ML library functions:
 - List.map : ('a -> 'b) -> 'a list -> 'b list map as discussed in class, with curried arguments
 - ListPair.zip : 'a list * 'b list -> ('a * 'b) list equivalent to zipWith (fn pr => pr) except takes its arguments as a pair

Reimplement zipWith in one line using these two library functions and a fun binding.

- (d) How many times does zipWith (fn = > true) [1,2,3] [7,8,9] call the :: function (so do not count uses of the :: pattern) if zipWith is your answer to part (a)?
- (e) How many times does zipWith (fn _ => true) [1,2,3] [7,8,9] call the :: function (so do not count uses of the :: pattern) if zipWith is your answer to part (c)?

5. (8 points) Here is a definition of flat_map as shown in section (recall @ is list append):

```
fun flat_map f xs =
  case xs of
    [] => []
    | x::xs' => (f x) @ flat_map f xs'
```

- (a) Reimplement a curried map of type ('a -> 'b) -> 'a list -> 'b list in one line using a fun binding and flat_map.
- (b) Reimplement a curried filter of type ('a -> bool) -> 'a list -> 'a list in one line using a fun binding and flat_map.

Name:

- 6. (19 points) This problem considers an ML module RBNum1 for numbers in the range 0–999 that also have a "color" of blue or red. The structure definition is on a separate page you will *not* turn in.
 - (a) Complete this signature definition so that clients of RBNum1 can use all the function bindings in RBNum1 but are not able to make "bad" values like Red ~7 or Blue 2000.

```
signature RBNUM =
sig
   val max_value : int
   exception OutOfRange
```

end

(b) Complete this structure definition so that it also has signature RBNUM and is equivalent to RBNum1 from any client's perspective. You need to add four bindings — put them in the left column of the table below.

```
structure RBNum2 :> RBNUM =
struct
type t = int
exception OutOfRange
val max_value = 999
fun red_num i = if i > max_value orelse i < 0 then raise OutOfRange else i
fun blue_num i = if i > max_value orelse i < 0 then raise OutOfRange else i+1000
(* ... part (b) ... *)
end</pre>
```

- (c) For each of the bindings you added in part (b), what are their types *inside* the RBNum2 module? Put your answers in the middle column of the table.
- (d) For each of the bindings you added in part (b), is it possible for the client to implement an equivalent function outside the module? Put your yes/no answers in the right column of the table.

part (b)	part (c)	part (d)

Name:

Here is an extra page in case you need it. If you use it for a question, please write "see also extra sheet" or similar on the page with the question.

```
Here is RBNum1 on a separate page. Do not turn in this page, so do not write answers on it.

structure RBNum1 :> RBNUM =
struct

val max_value = 999

exception OutOfRange

datatype t = Red of int | Blue of int

fun red_num i = if i > max_value orelse i < 0 then raise OutOfRange else Red i

fun blue_num i = if i > max_value orelse i < 0 then raise OutOfRange else Blue i

fun is_blue x = case x of Red _ => false | Blue _ => true

fun is_red x = case x of Red _ => true | Blue _ => false

fun is_max_blue x = case x of Red _ => false | Blue i => i = 999

fun to_int x = case x of Red i => i | Blue i => i
```

end