N.T.			
Name:			

CSE 341, Spring 2011, Midterm Examination 27 April 2011

Please do not turn the page until everyone is ready.

Rules:

- The exam is closed-book, closed-note, except for one side of one 8.5×11 in. piece of paper.
- Please stop promptly at 1:20.
- You can rip apart the pages, but please staple them back together before you leave.
- There are **60** points total, distributed **unevenly** among **5** questions (most with multiple parts).
- When writing code, style matters, but don't worry about indentation.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit.
- The questions are not necessarily in order of difficulty. **Skip around.**
- If you have questions, ask.
- Relax. You are here to learn.

1. This problem uses this datatype definition for a binary tree:

- (a) (5 points) Write a function sum that returns the sum of the values stored in the Leaf nodes of a Tree. Your function only needs to work correctly on trees whose Leaf nodes contain integer values.
- (b) (8 points) Write a function height that returns the height of a Tree. For the purposes of this question, the height of a tree consisting of only a Leaf node is 0; the height of any other tree is 1 greater than the height of its tallest subtree.

For full credit, your solution may not use any additional functions (either defined by you or in the standard SML library), and may not compute the height(s) of any subtrees more than once. (Hint: let may be your friend.)

(c) (2 points) What are the types of functions sum and height from parts (a) and (b)?

```
(a) fun sum tree =
       case tree of
            Leaf n \Rightarrow n
          | Node(_,1,r) => (sum 1) + (sum r)
(b) fun height tree =
       case tree of
            Leaf _ => 0
          | Node(_,1,r) =>
            let
                val lheight = 1 + height l
                val rheight = 1 + height r
            in
                if lheight > rheight then lheight else rheight
            end
(c) sum : (int, 'a) Tree -> int
   height : ('a, 'b) Tree -> int
```

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2. (8 points) Write a tail-recursive function fib n that returns a list of the first n Fibonocci numbers for n > 0. For example,

```
fib 8 = [0,1,1,2,3,5,8,13]
fib 1 = [0]
```

(Recall that the Fibonocci numbers are the series beginning with 0 and 1, and each successive number is the sum of the previous two.)

For full credit the number of tail-recursive calls made by your function should be linear in n. However, you do not need to worry about the costs of accumulating the answers in a list (i.e, don't worry about the costs of the list append operations).

```
fun fib n =
  let
    fun fibaux(acc,n,curr,next) =
        if n = 0
        then acc
        else fibaux(acc@[curr],n-1,next,curr+next)
  in
        fibaux([],n,0,1)
  end
```

- 3. For each of the following programs, give the value that ans is bound to after evaluation.
 - (a) **(3** points)

```
val x = 1
val y = 2
val f = fn y => x + y
val x = 5
val y = 10
val ans = f x + y
```

(b) (**3** points)

```
\begin{array}{l} val \ x = 1 \\ val \ y = 2 \\ val \ z = 3 \\ fun \ f \ x = let \ val \ x = 10 \ in \ fn \ y \Rightarrow x+y+z \ end \\ val \ y = 2 \\ val \ ans = f \ y \ 7 \end{array}
```

(c) (3 points)

```
val q = fn x => List.map tl x
val ans = q [[1,2,3],[4,5]]
```

- (a) 16
- (b) 20
- (c) [[2,3],[5]]

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- 4. One of your colleagues has been insisting that a language without a "real" for-loop must be useless. You have decided to settle the argument by showing that an equivalent loop can be written in SML.
 - (a) (9 points) Write a function named for with parameters loopvarinit test incr body and accinit that has the same effect as the following loop in one of those lesser languages:

```
acc = accinit;
for ( loopvar = loopvarinit; test(loopvar); loopvar = incr(loopvar) ) {
  acc = body(loopvar, acc);
}
yield acc; /* i.e., the final value of acc is the "value" of the loop */
```

In the above description, loopvar and acc are additional values that are not parameters of for. You will want to have similar values in your solution. Your solution must be properly tail-recursive and may not use any other functions defined outside of function for.

fun for loopvarinit test incr body accinit =

(b) (5 points) Complete the following function so that it uses function for to compute the sum of the numbers 1 through n. You should supply appropriate values (integers and anonymous functions) for the parameters of for.

fun	sum	(n:	int)	=				
	for				 	 	 	

```
(a) fun for loopvarinit test incr body accinit =
    let
        fun loop(loopvar, acc) =
            if test loopvar
            then loop(incr loopvar, body(loopvar,acc))
            else acc
    in
            loop(loopvarinit, accinit)
        end
(b) for 1 (fn x => x <= n) (fn n => n+1) (fn (x,y) => x+y) 0;
```

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5. Suppose we are implementing a dictionary (collection) of words. Version 1.0 of the software uses this SML structure definition:

```
structure D :> DICT =
struct
  datatype dictionary = None | Cons of string * dictionary

fun member(s,dict) =
   case dict of
     None => false
     | Cons(str,rest) => s=str orelse member(s,rest)

fun add(s,dict) = if member(s,dict) then dict else Cons(s,dict) end
```

Now suppose that in version 2.0 of the software we want to replace that structure with this new one, where the dictionary datatype in version 1.0 is replaced with a regular SML string list.

```
structure D :> DICT =
struct
  type dictionary = string list
    ... (* see part a *)
end
```

(a) (8 points) Write the necessary function bindings to complete version 2.0 of the structure so that it has the same functionality as the version 1.0 structure.

Hint: Be sure that your new version of the structure includes sufficient operations so that client code can construct new dictionaries and process them.

Write your answer on the next page.

(b) (6 points) Complete this signature so that *both* version 1.0 and version 2.0 of the structure will type-check without errors. Use one abstract type definition and any necessary val bindings.

```
signature DICT =
sig
...
end
```

Write your answer on the next page.

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Answers for question 5 can be written here.

```
(a) structure D :> DICT =
   struct
   type dictionary = string list
   val None = [];
   fun member(s,dict) =
       case dict of
           [] => false
         | x::xs => x=s orelse member(s,xs)
   fun add(s,dict) = if member(s,dict) then dict else s::dict
   end
(b) signature DICT =
   sig
     type dictionary
     val None : dictionary
     val add : string * dictionary -> dictionary
     val member : string * dictionary -> bool
   end
```