

4.(a) the conclusion is correct, because we can proof P

In correct way with given propositions

1. $(P \vee R) \rightarrow (Q \wedge R)$ given

2. $\neg S \rightarrow (R \wedge Q)$ given

3. $S \rightarrow (P \wedge Q)$ given

4. $\neg(R \wedge Q) \rightarrow S$ Contrapositive: 2

5.1 $\neg(R \wedge Q)$ Assumption

5.2 S MP: 4, 5.1

5.3 $(P \wedge Q)$ MP: 3, 5.2

5 $\neg(R \wedge Q) \rightarrow (P \wedge Q)$ Double Proof Rule

6. $(R \wedge Q) \vee (P \wedge Q)$ Law of implication: 5

7. $(R \vee P) \wedge Q$ distributive: 6

8. Q Elim A: 7

(b) step 4: inference rules only can be applied to

whole formulas, in this step it eliminate "R" in "R ∧ Q" but it's only a part of whole formula

step 5: same as step 4

(others are correct according to the rules they use, but because 4. and 5 is incorrect, every step that related to them are incorrect and whole proof is also incorrect)

step 12: wrong rule name

should be identity