

(a) Domain of discourse: all people

Predicate domination: $P(x, y) ::= "y \text{ is } x\text{'s parent}"$

$$\neg \forall x \exists y \exists z (P(x, y) \wedge P(x, z))$$

$$\equiv \exists x \forall y \forall z \neg (P(x, y) \wedge P(x, z)) \quad \text{de Morgan's Law}$$

$$\equiv \exists x \forall y \forall z (\neg P(x, y) \vee \neg P(x, z)) \quad \text{de Morgan's Law}$$

(b) Domain of discourse: all CSE courses

Predicate $L(x) ::= "x \text{ is 300-level course}"$

domination: $P(x, y) ::= "y \text{ is prerequisite course of } x"$

$$\neg ((\forall x \exists y (L(x) \rightarrow P(x, y))) \wedge (\exists x \exists y \exists z (L(x) \wedge P(x, y) \wedge P(x, z))))$$

$$\equiv \neg \forall x \exists y (L(x) \rightarrow P(x, y)) \vee \neg \exists x \exists y \exists z (L(x) \wedge P(x, y) \wedge P(x, z)) \quad \left. \begin{array}{l} \text{de} \\ \text{Morgan's} \\ \text{Law} \end{array} \right\}$$

$$\equiv \exists x \forall y (\neg (L(x) \rightarrow P(x, y))) \vee \forall x \forall y \forall z (\neg (L(x) \wedge P(x, y) \wedge P(x, z)))$$

$$\equiv \exists x \forall y (\neg (L(x) \rightarrow P(x, y))) \vee \forall x \forall y \forall z (\neg L(x) \vee \neg P(x, y) \vee \neg P(x, z)) \quad \left. \begin{array}{l} \text{Law of} \\ \text{implication} \end{array} \right\}$$

$$\equiv \exists x \forall y (\neg (\neg L(x) \vee P(x, y))) \vee \forall x \forall y \forall z (\neg L(x) \vee \neg P(x, y) \vee \neg P(x, z))$$

$$\equiv \exists x \forall y (L(x) \wedge \neg P(x, y)) \vee \forall x \forall y \forall z (\neg L(x) \vee \neg P(x, y) \vee \neg P(x, z))$$

de Morgan's