

$$(c) \neg \forall x \exists y (P(x, y) \rightarrow \neg P(y, x))$$

$$\equiv \exists x \forall y (\neg (P(x, y) \rightarrow \neg P(y, x))) \text{ de Morgan's Law}$$

$$\equiv \exists x \forall y (\neg (\neg P(x, y) \vee \neg P(y, x))) \text{ Law of implication}$$

$$\equiv \exists x \forall y (P(x, y) \wedge P(y, x)) \text{ de Morgan's Law}$$

There exists an activity x , which is more fun than any activities, and all activities are more fun than x .

$$(d) \neg \forall x \forall y ((P(x, y) \oplus Q(y)) \rightarrow \neg \exists z Q(z))$$

$$\equiv \neg \forall x \forall y (\neg (P(x, y) \oplus Q(y)) \vee \neg \exists z Q(z)) \text{ Law of implication}$$

$$\equiv \exists x \exists y \neg (\neg (P(x, y) \oplus Q(y)) \vee \neg \exists z Q(z)) \text{ de Morgan's}$$

$$\equiv \exists x \exists y ((P(x, y) \oplus Q(y)) \wedge \exists z Q(z)) \text{ Law}$$

There exist a course x and a course y , x is a pre-requisite for course y that I'm not taking, or x is not a pre-requisite for y that I'm currently taking, meanwhile there exists a course z that I'm taking.