$$V(\mathcal{K}_a^{\ell}) \cup \{\eta_1\} = \sigma_{ij}(V(\mathcal{P}_a^{\ell})),$$