

$$\alpha_{\mathbb{S}^3} = \frac{1}{2}r_1^2d\theta_1 + \frac{1}{2}r_2^2d\theta_2, \quad r_1^2 + r_2^2 = 1.$$