

$$\sum_{j=1}^\infty \langle T\tilde{e}_j, T\tilde{e}_j \rangle_{\mathfrak{H}_0} < \infty,$$