$$\tilde{\mathcal{S}}_{jk}(A) := \sum_{\ell \in I_k} a_{i_j,\ell} 3mu, 18mu j, k = 1, ..., m.$$