

$$|\vartheta(t)| \leq 2|t|\log|t|, \quad |t| > 4, \quad |\Re t| \geq 1.$$