$$\sigma_{\xi+1}(\sigma_{\lambda-1}^{-1}(\kappa_a^\ell)) = \kappa_a^\ell,$$