

$$\frac{\|\mathbf{a}^{(\mathbf{i})}\|}{\sigma_{\max}(A_k^{(i)})} \leq r \leq \frac{\|\mathbf{a}^{(\mathbf{i})}\|}{\sigma_{\min}(A_k^{(i)})}.$$