$$r \leq \frac{||\mathbf{a}^{(i)}||}{\sigma_{\min}(A^{(i)})}.$$