

$$S_1 := \sum_{n=1}^N \frac{1}{n^s} + (\varepsilon/6), \qquad S_2 := \sum_{k=0}^K \frac{C_k(q)}{a^k} + RS_K + (A_1\varepsilon/3).$$