$$\sigma_{\lambda-1}^{-1}(\kappa_a^{\ell}) = \sigma_{\lambda-1}^{-1}(\mu) \in N_{X_L}(\sigma_{\lambda-1}^{-1}(\mu)) \setminus V(\mathcal{C}_a^{\ell}).$$