

$$-\int_0^1 \frac{d}{dx} e^T P \frac{d}{dx} e = -\int_0^1 \frac{d}{dx} \hat{e}^T P \frac{d}{dx} \hat{e}$$