

$$(V(\mathcal{S}_a^{\ell-1}) \setminus \{\kappa_a^{\ell-1}\}) \cup (V(\mathcal{S}_b^{\ell-1}) \setminus \{\kappa_b^{\ell-1}\}).$$