$$d(v_i, v_j) \leq d(v_i, \sigma') + d(\sigma', v_j) \leq 4n^3(1 + f(n)) + 4n^3(1 + f(n)) \leq 8n^3(1 + 2f(n))$$