$\sigma_{\lambda-2}(\sigma_{\lambda-1}^{-1}(\kappa_a^{\ell})) \notin V(\mathcal{S}_a^{\ell}) \setminus {\{\kappa_a^{\ell}\}}$