

$$(\theta, p_\theta, z, s, t) \mapsto (\vartheta, r, p_\theta, p_r, w) = (\theta, e^s, e^s p_\theta, z, t + e^s z).$$