

$$(\theta, p_\theta, z, s) \mapsto (x_1, x_2, y_1, y_2) = (e^s \cos \theta, e^s \sin \theta, z \cos \theta - p_\theta \sin \theta, z \sin \theta + p_\theta \cos \theta).$$