$$e^{\Omega(n)} = \mathcal{D}(n) \leq e^{(1-o(1))n\log n}.$$