$$-\Omega_s \succ 0 \iff \mathcal{D}2kP_s - 2\alpha I_N - gL - 2\frac{k^2}{\pi^2}P_s \succ 0$$