$\mathcal{X}_{F_k}^* = \mathcal{X}_{f_k}^* \times \mathcal{X}_{f_k}^* \dots \times \mathcal{X}_{f_k}^*^n.$