

$$\sigma_{\lambda-1}(v_a^\ell)=\mu',\; \sigma_\lambda(\sigma_{\lambda-1}^{-1}(\mu'))=\kappa_a^\ell.$$