

$$R_{\theta_0}|_{J^1S^1}(\theta, p_\theta, z) = (\theta + \theta_0, p_\theta, z); \eta|_{J^1S^1}(\theta, p_\theta, z) = (\theta, -p_\theta, -z).$$