$$\sigma_{\lambda-1}(v_a^\ell) = \mu', \ \sigma_\lambda(\sigma_{\lambda-1}^{-1}(\mu')) = \kappa_a^\ell.$$