$\sigma_{i+1}^{-1}(V(\mathcal{K}^{\ell})) \subset V(\mathcal{P}_a^{\ell}) \cup V(\mathcal{P}_b^{\ell}).$