$$\sigma_{\lambda-2}^{-1}(\mu) \neq \sigma_{\lambda-1}^{-1}(\mu) \text{ or } \sigma_{\lambda-2}^{-1}(\kappa_a^{\ell}) \neq \sigma_{\lambda-1}^{-1}(\kappa_a^{\ell});$$