$|\sigma_i^{-1}(\{\mu_1, \mu_2\}) \setminus (V(\mathcal{P}_a^{\ell}) \cup V(\mathcal{P}_b^{\ell}))| \le 1.$