$$e^T(0)P\tilde{K}\int_0^1 e = -\int_0^1 (\dot{e}^T + e)P\tilde{K}e$$