

$$\sigma_{\lambda-1}^{-1}(\kappa_a^\ell) = \sigma_{\lambda-1}^{-1}(\mu) \in N_{X_L}(\sigma_{\lambda-1}^{-1}(\mu)) \setminus V(\mathcal{C}_a^\ell).$$