$$s_\lambda \cdot s_{(\alpha)} = \sum_{\nu/\lambda \in \mathrm{Horz}(\alpha)} s_\nu \qquad s_\lambda \cdot s_{(1^r)} = \sum_{\nu/\lambda \in \mathrm{Vert}(r)} s_\nu$$