

$$\{\kappa_a^{\ell+1}\} = \sigma_k^{-1}(V(\mathcal{K}^\ell)) \setminus (V(\mathcal{P}_a^\ell) \cup V(\mathcal{P}_b^\ell)) \text{ for } k > \xi.$$