$$\frac{\mu_f}{2}d(x_k^{(i)}, \mathcal{X}_{f_k}^*)^2 \leq f_k(x) - f_k^* \leq \frac{L_f}{2}d(x_k^{(i)}, \mathcal{X}_{f_k}^*)^2,$$