

$$|\sigma_{\lambda-2}(V(\mathcal{C}_b^\ell) \setminus (V(\mathcal{S}_b^\ell) \setminus \{\kappa_b^\ell\}))| \geq 3,$$