

$$|\sigma^{-1}(V(\mathcal{K}^\ell) \setminus (V(\mathcal{P}_a^\ell) \cup V(\mathcal{P}_b^\ell)))| = 1,$$