$$\sum_{j=1}^{\infty} \langle T\tilde{e}_j, T\tilde{e}_j \rangle_{\mathcal{H}_0} < \infty,$$