

$$c\phi_{pN+k}(pn+r)\equiv 0\pmod{p}$$