

$$\sigma_{\lambda-1}^{-1}(\kappa_a^\ell)\in\{v_a^{\ell-2,\ell-1},v_b^{\ell-2,\ell-1},v_a^{\ell,\ell+1},v_b^{\ell,\ell+1}\}$$