$$\sigma_{\lambda-1}\big(\sigma_\lambda^{-1}(\kappa_a^\ell)\big) \in \{\kappa_a^{\ell-1}, \kappa_b^{\ell-1}\},$$