$\Phi_k(q) \equiv \frac{(q;q)_{\infty}}{(q^{k+1};q^{k+1})_{\infty}} \pmod{2}.$