

$$\{\mu, \sigma_i(v_a^\ell)\} \subset \sigma_{i+1}^{-1}(V(\mathcal{K}^\ell)) \setminus (V(\mathcal{P}_a^\ell) \cup V(\mathcal{P}_b^\ell)).$$