

$$\sigma_\zeta^{-1}(\kappa_b^2) \in V(\mathcal{C}_a^2) \setminus N_{X_L}[\mathrm{bd}(\mathcal{C}_a^2)];$$