

$$2^d > 10(J+3) \quad \text{and} \quad 2^d \geq 2^{4J+4}/\varepsilon_6 > 147.3 \cdot 2^{4J-4}/\varepsilon_6$$