

$$\sigma_{\lambda-1}(\mathcal{P}_b^1) \setminus \{\kappa_b^1\} \subset (V(\mathcal{S}_b^1) \setminus \{\kappa_b^1\}) \cup V(\mathcal{K}^1) = N_{Y_L}(\kappa_b^1),$$