

$$\sigma_{\lambda-1}(\sigma_{\lambda}^{-1}(\kappa_a^{\ell})) \in \{\kappa_{\lambda}^{\ell-1}, \kappa_{\beta}^{\ell-1}\},$$