

$$\sigma_\zeta(\sigma_{\xi+1}^{-1}(\kappa_a^2)) \neq \kappa_a^2,$$