

$$\sigma_{\lambda'}'(V(\mathcal{P}_a^{L+2}) \setminus \{v_a^{L+1}\}) = \sigma_s(V(\mathcal{P}_a^{L+1})) = V(K_a^{L+1}).$$