

$$(\theta, p_\theta, z, s) \mapsto (x_1, x_2, y_1, y_2) = (e^s \cos\theta, e^s \sin\theta, z \cos\theta - p_\theta \sin\theta, z \sin\theta + p_\theta \cos\theta).$$