

$$\sigma_j(\sigma_{\lambda-1}^{-1}(\kappa_a^\ell)) \in V^{(\ell+1)} \text{ for } \xi+1 \leq j \leq \lambda-1$$