

$$d(\sigma', \tau') \leq 4(n+1)^3 + |E(Y')| \leq 4(n+1)^3 + \binom{n+1}{2} = 4n^3(1 + f(n)),$$