

$$|\sigma_i^{-1}((\mu_1, \mu_2)) \setminus (V(\mathcal{P}_a^\ell) \cup V(\mathcal{P}_b^\ell))| \leq 1,$$