

$$\sigma_j(\sigma_{\lambda-1}^{-1}(\kappa_a^\ell)) \in V(\mathcal{K}^{\ell+1}) \text{ for } \xi+1 \leq j \leq \lambda-1$$