$\sigma_{\xi+1}(\sigma_{\lambda-1}^{-1}(\kappa_a^{\ell})) = \kappa_a^{\ell},$