

$$\sigma_{\xi-2}^{-1}(\{\kappa_a^\ell, \mu\}) \subset V(\mathcal{C}_b^\ell) \text{ and } \sigma_{\xi-2}(\sigma_{\xi-1}^{-1}(\kappa_a^\ell)) \in V(\mathcal{C}_b^\ell).$$