$\sigma_{i+1}^{-1}(\sigma_i(v_a^{\ell})) \in /1muV(\mathcal{P}_a^{\ell}),$