

$$\sigma_\xi^{-1}(\kappa_a^\ell) \in \textcolor{blue}{1muV}(\mathcal{P}_a^\ell) \setminus \{v_a^\ell\},$$