

$$R_{\theta_0}|_{J^1S^1}(\theta,p_\theta,z) = (\theta+\theta_0,p_\theta,z); \eta|_{J^1S^1}(\theta,p_\theta,z) = (\theta,-p_\theta,-z).$$