

$$\sigma_{\lambda-2}^{-1}(\kappa_a^\ell) \in N_{X_L}(\sigma_{\lambda-1}^{-1}(\kappa_a^\ell)) \cap V(X^{\ell-1}),$$