$Z_u = \mathbb{E}^{\mu_0^u} \left[\exp(-\Phi_u(u)) \right], \quad Z_\sigma = \mathbb{E}^{\mu_0^\sigma} \left[\exp(-\Phi_\sigma(\sigma)) \right].$