$$\sigma_{\lambda-1}^{-1}(\kappa_a^{\ell}) \in \{v_a^{\ell-2,\ell-1}, v_b^{e-2,\ell-1}, v_b^{\ell,\ell+1}\}$$