$$D_k(\sigma) = \{(s, x) \mid \mathrm{rank}(\sigma(s, x)) \le k\}.$$