$$\sigma_{i_{j+1}-1}^{-1}(\mu) \notin V(\mathcal{P}_a^\ell) \cup V(\mathcal{P}_b^\ell).$$