$$S_{k\ell}[a] := \begin{pmatrix} a_1 & a_2 & \dots & a_{\ell} \dots \\ \dots & \dots & \dots a_1 & a_2 \\ \dots & a_{\ell} & & \end{pmatrix}.$$