$\{\sigma_{i+1}(v_a^{\ell}), \sigma_{i+1}(v_b^{\ell})\} \cap V(\mathcal{K}^{\ell}) = \emptyset.$