$$\sigma_{\lambda-1}(v_a^{\ell}) = \mu', \ \sigma_{\lambda}(\sigma_{\lambda-1}^{-1}(\mu')) = \kappa_a^{\ell}.$$