

$$\hat{f}_k^* \leq \phi^* + \frac{\min(L_f, L_\phi)}{2} d(\mathcal{X}_{\mathcal{F}_k}^f, \mathcal{X}_\phi^*)^2.$$