$$L_{g,r,d} = \int_{(r+1,d+1)} \sigma_{1^r}^g \cdot \left[\sum_{\alpha_0+...+\alpha_r=(r+1)(d-r)-rg} \left(\prod_{i=0}^{r} \sigma_{\alpha_i} \right) \right].$$