$$1_N^T \mathcal{D} 1_N = 2ks - 2\alpha N - 2\frac{k^2}{\pi^2}s > 0$$