

$$\sum_{j=1}^\infty \langle T\tilde e_j, T\tilde e_j \rangle_{\mathfrak{H}_0} < \infty,$$