$$\sigma_{\lambda-1}^{-1}(\kappa_a^\ell) \in \{v_a^{\ell-2,\ell-1}, v_b^{\ell-2,\ell-1}, v_a^{\ell,\ell+1}, v_b^{\ell,\ell+1}\}$$