$\sigma_{\xi}^{-1}(\kappa_a^{\ell}) \in V(\mathcal{P}_a^{\ell}) \setminus \{v_a^{\ell}\} \text{ for } \xi + 1 \le j \le \lambda - 1.$