$S_1 := \sum_{n=1}^N \frac{1}{n^s} + \mathfrak{O}^*(\varepsilon/6), \qquad S_2 := \sum_{k=0}^K \frac{C_k(q)}{a^k} + RS_K + \mathfrak{O}^*(A_1\varepsilon/3).$