$\sigma_i^{-1}(\{\kappa_a^\ell,\kappa_b^\ell\}) \subset \sigma_i^{-1}(V({}^{\ell-1})) \setminus (V(\mathcal{P}_a^{\ell-1}) \cup V(\mathcal{P}_b^{\ell-1})),$