

$$\phi_{p^{\ell-1}}(pn+r)\equiv 0\pmod{p}.$$