$$\sigma_i^{-1}(\mu) = \sigma_{i+1}^{-1}(\mu) \notin V(\mathcal{P}_a^{\ell}) \cup V(\mathcal{P}_b^{\ell}),$$