

$$\sigma_{\lambda-1}(\sigma_{\lambda}^{-1}(\kappa_a^{\ell})) \in \{\kappa_a^{\ell+1}, \kappa_b^{\ell+1}\},$$