

$$L_{g,r,d}=\int_{(r+1,d+1)}\sigma_{1^r}^g\cdot\left[\sum_{\alpha_0+\ldots+\alpha_r=(r+1)(d-r)-rg}\left(\prod_{i=0}^r\sigma_{\alpha_i}\right)\right]$$