

Perceptron Summary

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1 Context

Perceptron performs well when the dataset is linearly separable. In this experiment, I use a dataset which is non-linearly separable to test perceptron.

2 Equation Derivation

Perceptron use a hyperplane to separate dataset into two class. Several samples will be misclassified until the proper hyperplane has been found (only if the dataset is linearly separable). At each epoch, use these misclassified samples to adjust hyperplane i.e. minimize the loss function).

Loss function: (M is a set of misclassified samples)

$$L(w, b) = - \sum_{x_i \in M} y^{(i)} (w^T x_i + b)$$

Use batch gradient descent to minimize loss function:

$$\begin{aligned} \frac{\partial L}{\partial w} &= - \sum_{x_i \in M} y^{(i)} x_i \\ \frac{\partial L}{\partial b} &= - \sum_{x_i \in M} y^{(i)} \end{aligned}$$

Update parameters:

$$\begin{aligned} w &:= w + \eta y^{(i)} x_i \\ b &:= b + \eta y^{(i)} \end{aligned}$$

3 Experiment

3.1 Introduction

Here is a dataset about breast cancer ¹. Use perceptron to classify this dataset. Select model from 10 of them based on the result of 4-fold cross val-

¹[https://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+\(Diagnostic\)](https://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+(Diagnostic))

idation. As this dataset is nonlinear separable, stop the training process when misclassified samples are less than 10% of training set.

3.2 Result

The error percentage is as low as around 0.9%, and precision can be 95% while recall is 63%.

4 Summary

Perceptron is easy to implement and has good performance on binary classification task.