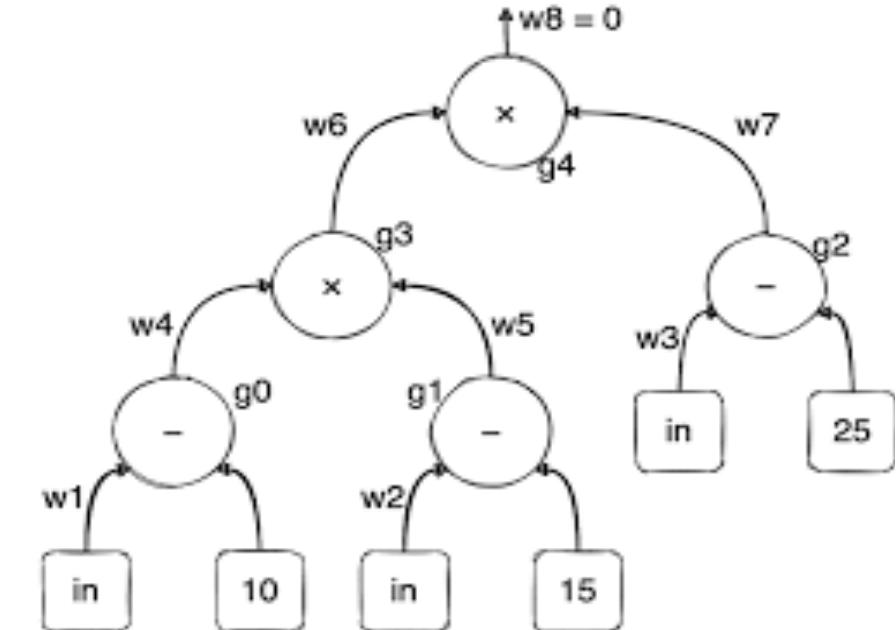
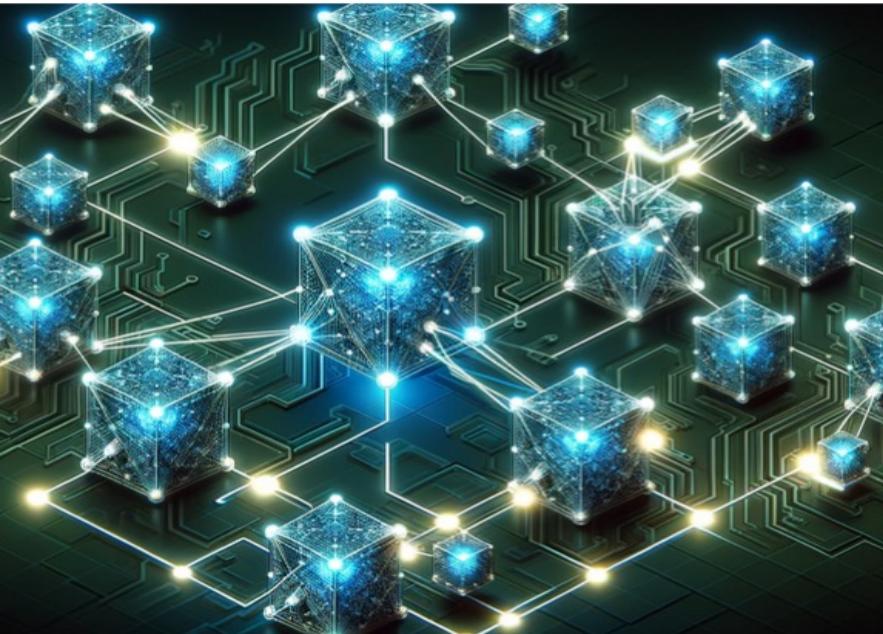


Compute Offchain, Verify Onchain: How to Build zk-DApps with Circom and ZoKrates



Alvaro Alonso, Johannes Sedlmeir, Jonathan Heiss

Tutorial at ICBC 2024

Who are we?

Alvaro Alonso



Dr. Johannes Sedlmeir

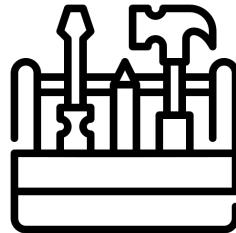
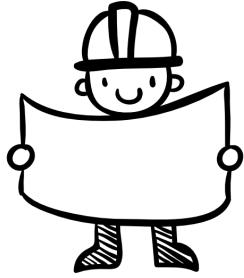


Dr. Jonathan Heiss



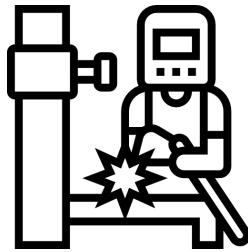
Agenda

Motivation & Concept



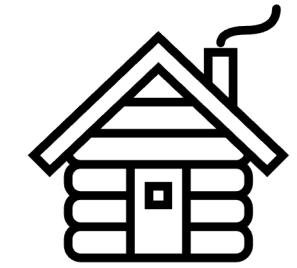
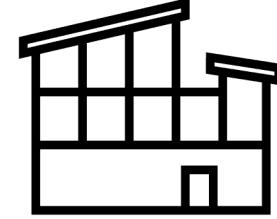
Why are zk-SNARKs relevant
for blockchains?

Hands-on



How to build and deploy dApps
with zk-DSLs?

Applications



What can be built with zk-
SNARKs?

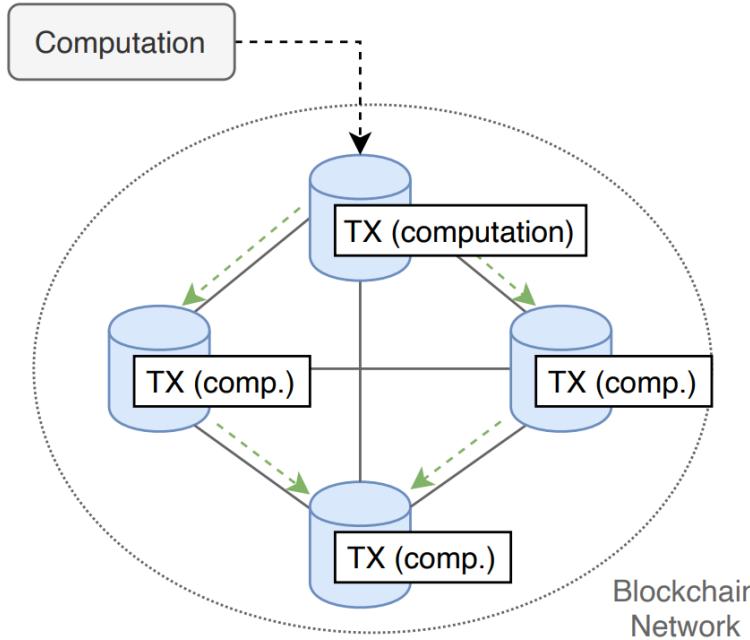
Blockchain-based decentralized applications often involve the processing of large amounts of or sensitive data

#	Pattern	Example use cases	References	Types of sensitive information
1	Payment	Bitcoin, central bank digital currencies	Nakamoto (2008), Dashkevich et al. (2020)	Individuals' and businesses' revenues, expenses, balances, turnover and business partners
2	Tamper-proof documentation	Notarization, Cardossier	EC (2021), Zavolokina et al. (2020)	Content and validity status of documents, information that could be sold on a market
3	Cross-organizational workflow management	Tradelens, MediLedger	Jensen et al. (2019), Mattke et al. (2019)	Frequency and type of processes, relationships between organizations involved
4	Ubiquitous services	Oracles (Chainlink), DeFi (Uniswap)	Al-Breiki et al. (2020), Wang et al. (2019), Werner et al. (2021)	Risk exposure associated with financial investments
5	Digital identities	Namecoin, German asylum case	Kalodner et al. (2015), Amend et al. (2021)	Individuals' names, addresses, health information, permissions and achievements
6	Tokenization	Ticketing (GUTs), investments and fractional ownership	Regner et al. (2019), Sunyaev et al. (2021), Whitaker and Kräussl (2020)	Individuals' and organizations' investment decisions and voting behaviour
7	Machine economy	Micropayments, economically autonomous robots	Jöhnk et al. (2021), Schweizer et al. (2020)	All of the above; machines are typically associated with organizations or individuals

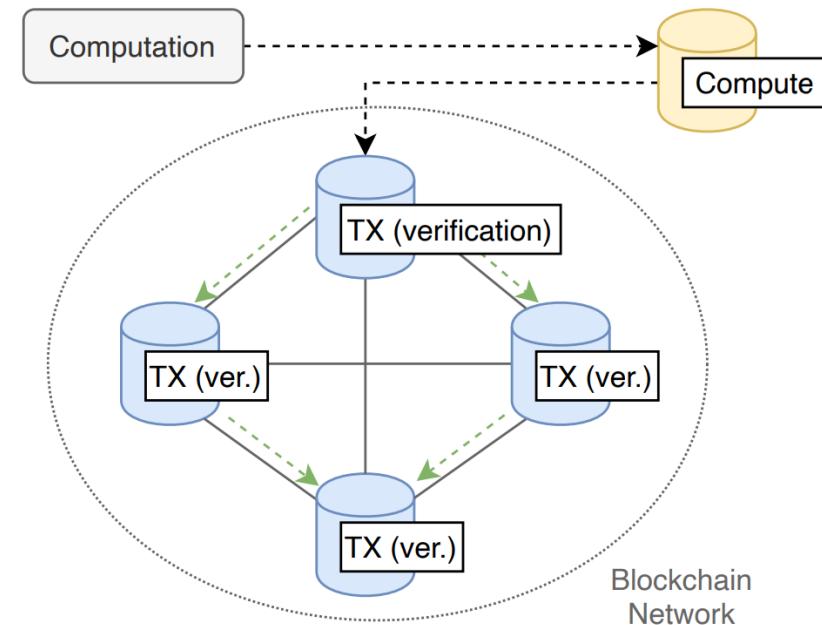
Sedlmeir, J., Lautenschlager, J., Fridgen, G., & Urbach, N. (2022). The transparency challenge of blockchain in organizations. *Electronic Markets*, 32(3), 1779-1794.

Motivation

Default on Blockchains:
Replicated Computation



Verifiable Off-chain Computation (VOC):
Replicated Verification

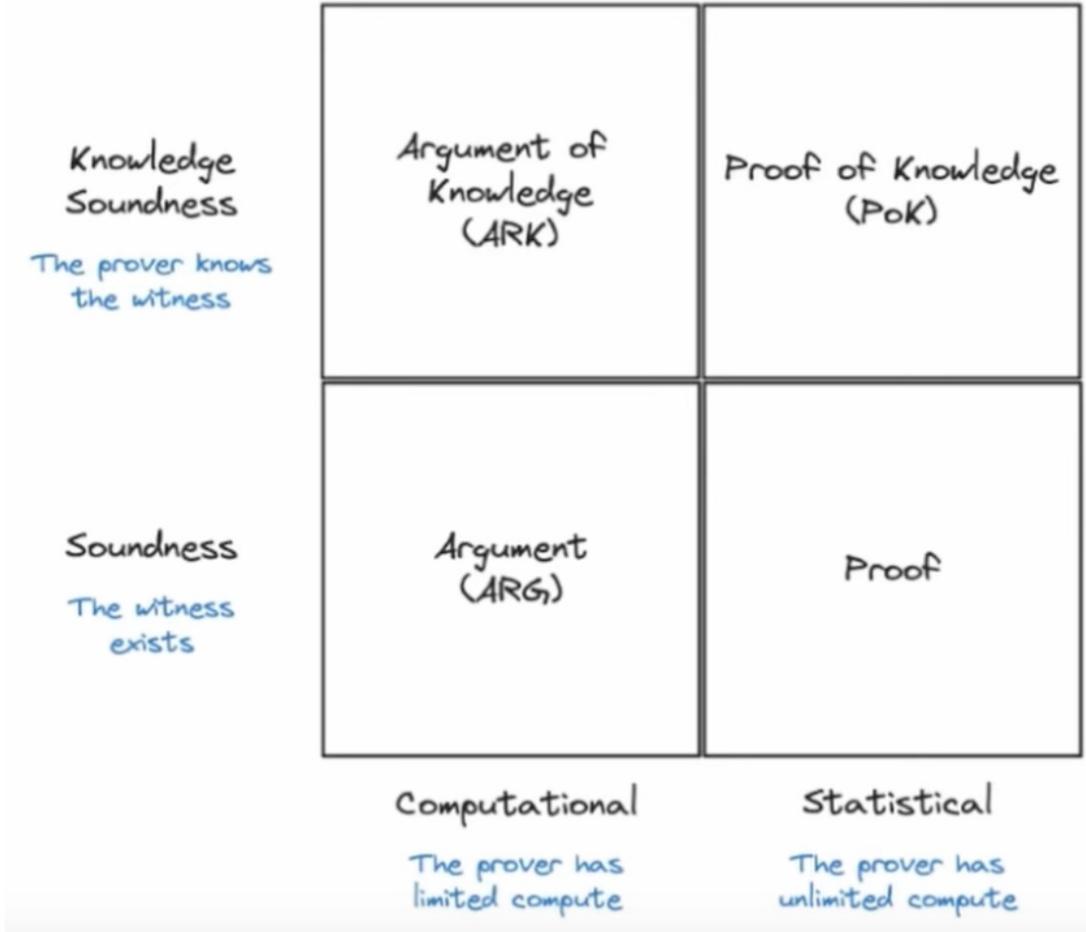


→ *Limitations: Privacy, Scalability*

Why are SNARKs important?

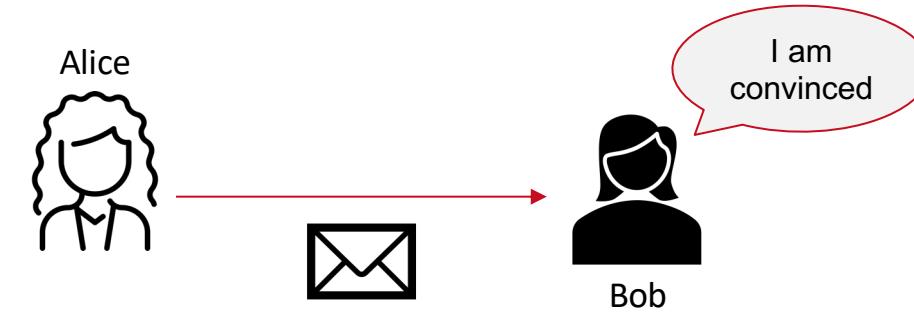
1. Arguments of Knowledge (ARK) → convince another party not only of the accuracy of a statement but also that the prover knows why it is true

This is important in situations where conflict of interests arise and where replay is a potential issue.



Why are SNARKs important?

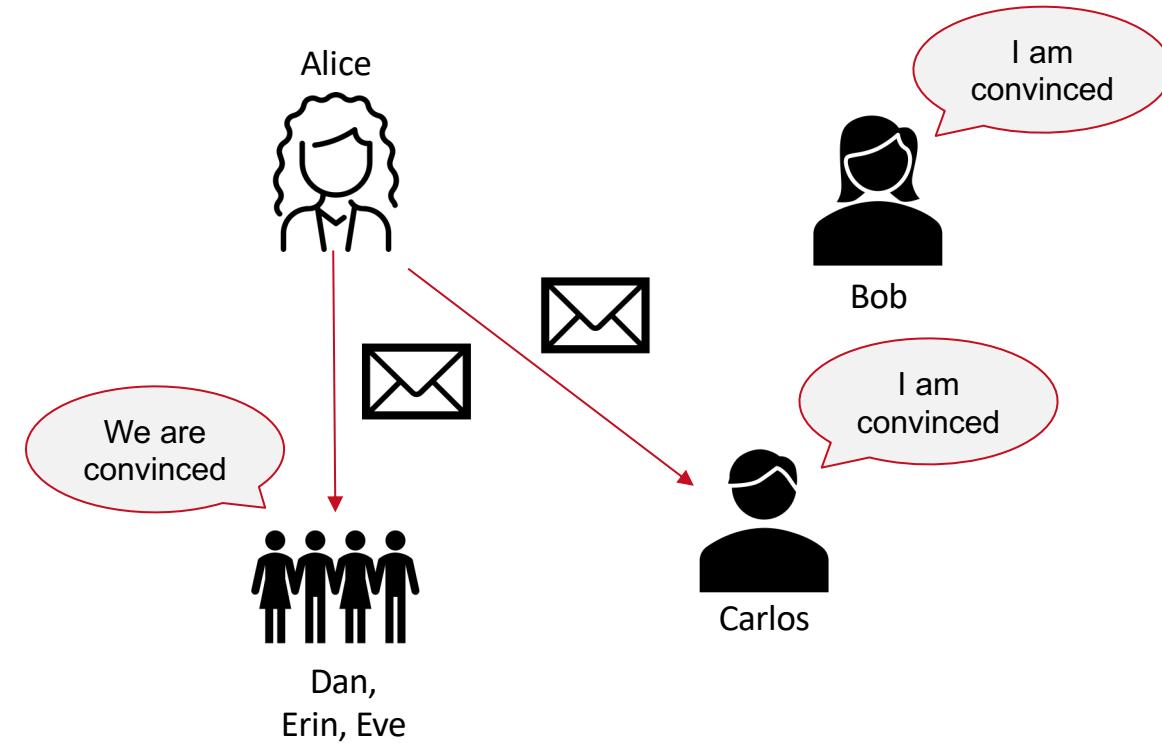
1. Arguments of Knowledge (ARK)
2. Non-Interactive



Note: In some scenarios, it may be desirable to have an interactive process because then only the designated verifier is convinced (and cannot sell verifiable data). For the blockchain case, however, non-interactivity is critical to simultaneously convince all nodes (deterministically).

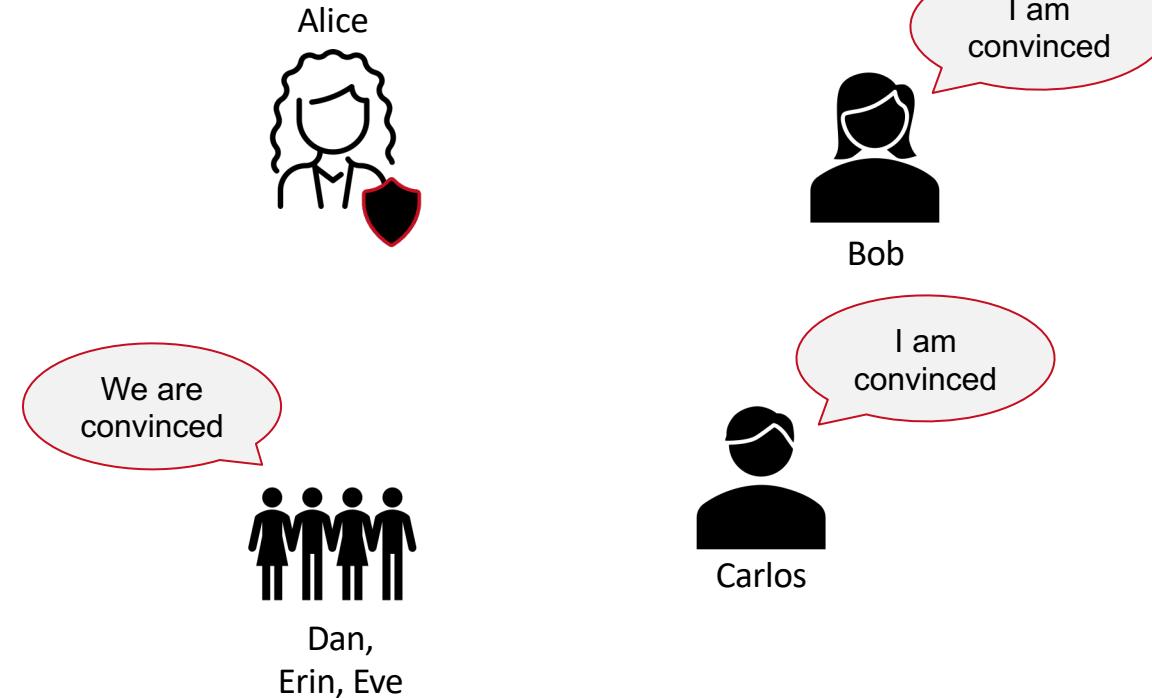
Why are SNARKs important?

1. Arguments of Knowledge (ARK)
2. Non-Interactive
3. Succinct – its verification is much shorter than the verification of an actual proof



Why are zk-SNARKs important?

1. Arguments of Knowledge (ARK)
2. Non-Interactive
3. Succinct
4. Zero Knowledge – the verifier(s) will learn nothing other than the validity of the statement



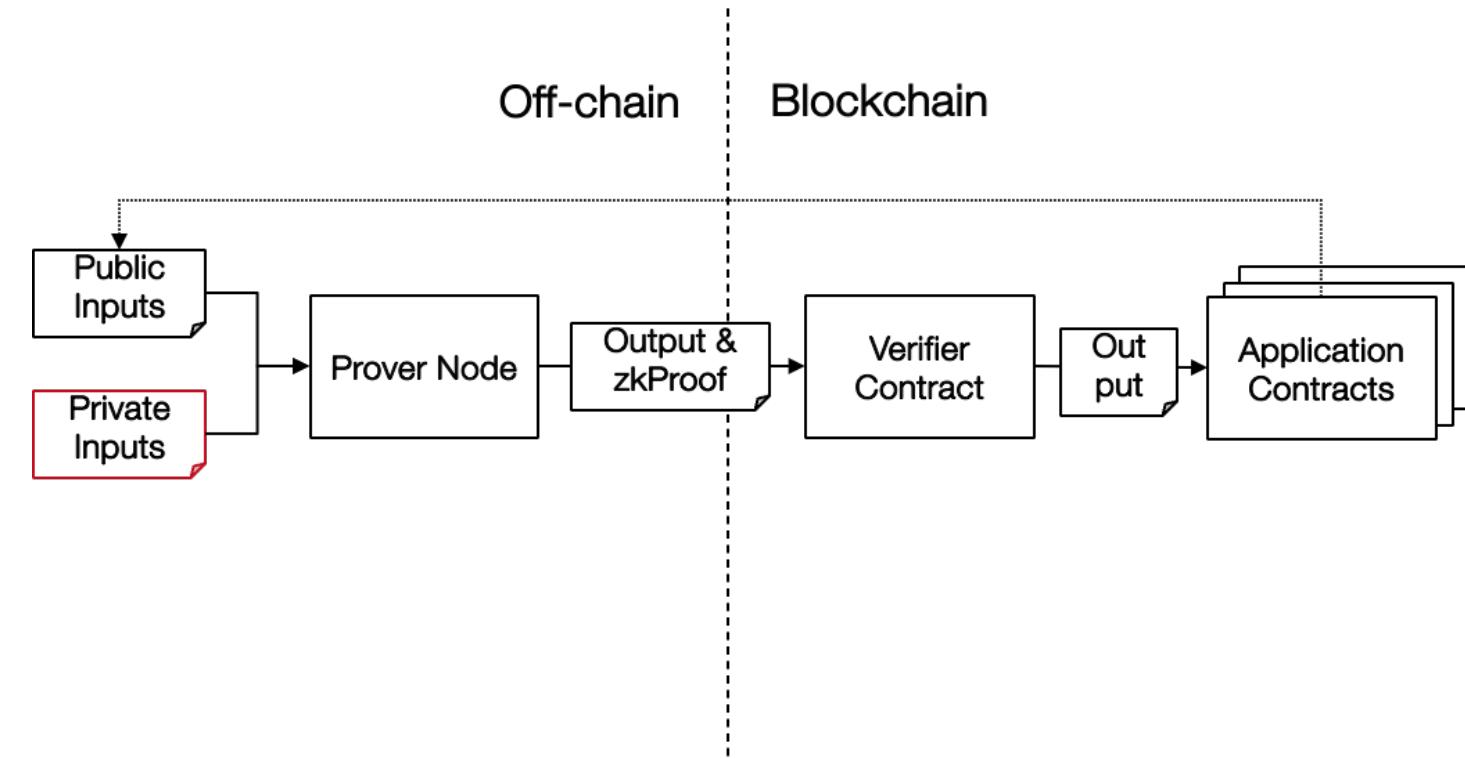
Zk-DApps

Build decentralized applications (dApp) where parts of the logic are executed off-chain.

Computational correctness can be verified on-chain through ZKPs like zkSNARKs.

→ Privacy, Scalability

Examples: zk-Rollups, zk-Exchanges, zk-(Decentralized) Federated Learning, ...



Why a Domain Specific Language (DSL) toolkit?

- Current programming languages do not satisfy this paradigm
- Zk-SNARK "circuits" are very large
- Requires expert knowledge
- Requires of low-level optimizations to run efficiently
- The process stages are well-defined

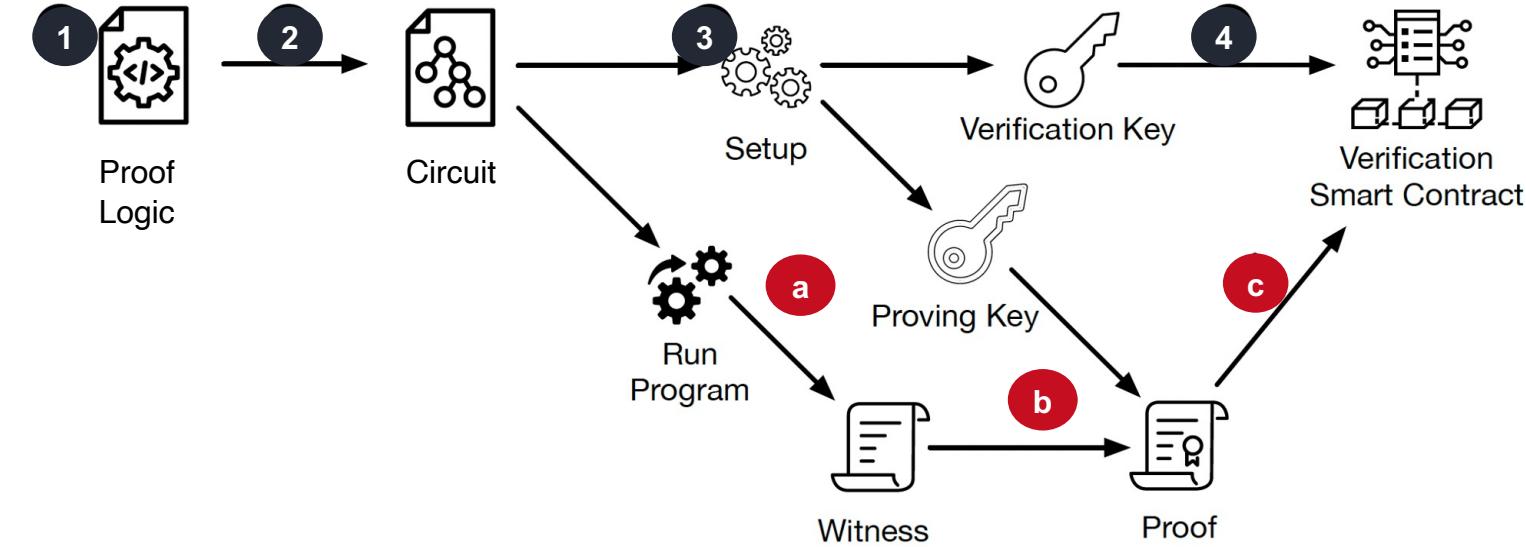
zk-SNARKs Development Workflow

One time operations

1. Define Program Logic
2. Compile into Algebraic Circuit
3. Execute Setup (get Key Pair)
4. Export Verifier Contract

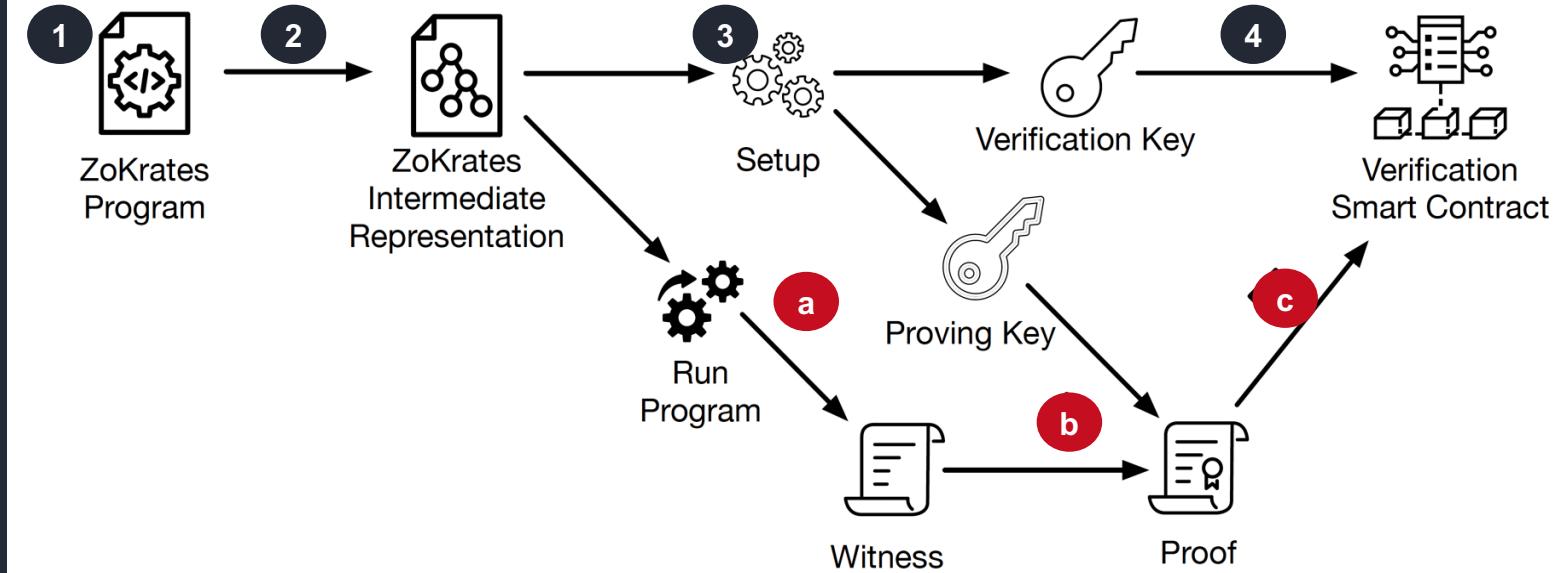
Recurring Operations

- a Compute Witness
- b Generate Proof
- c Verify Proof On-chain



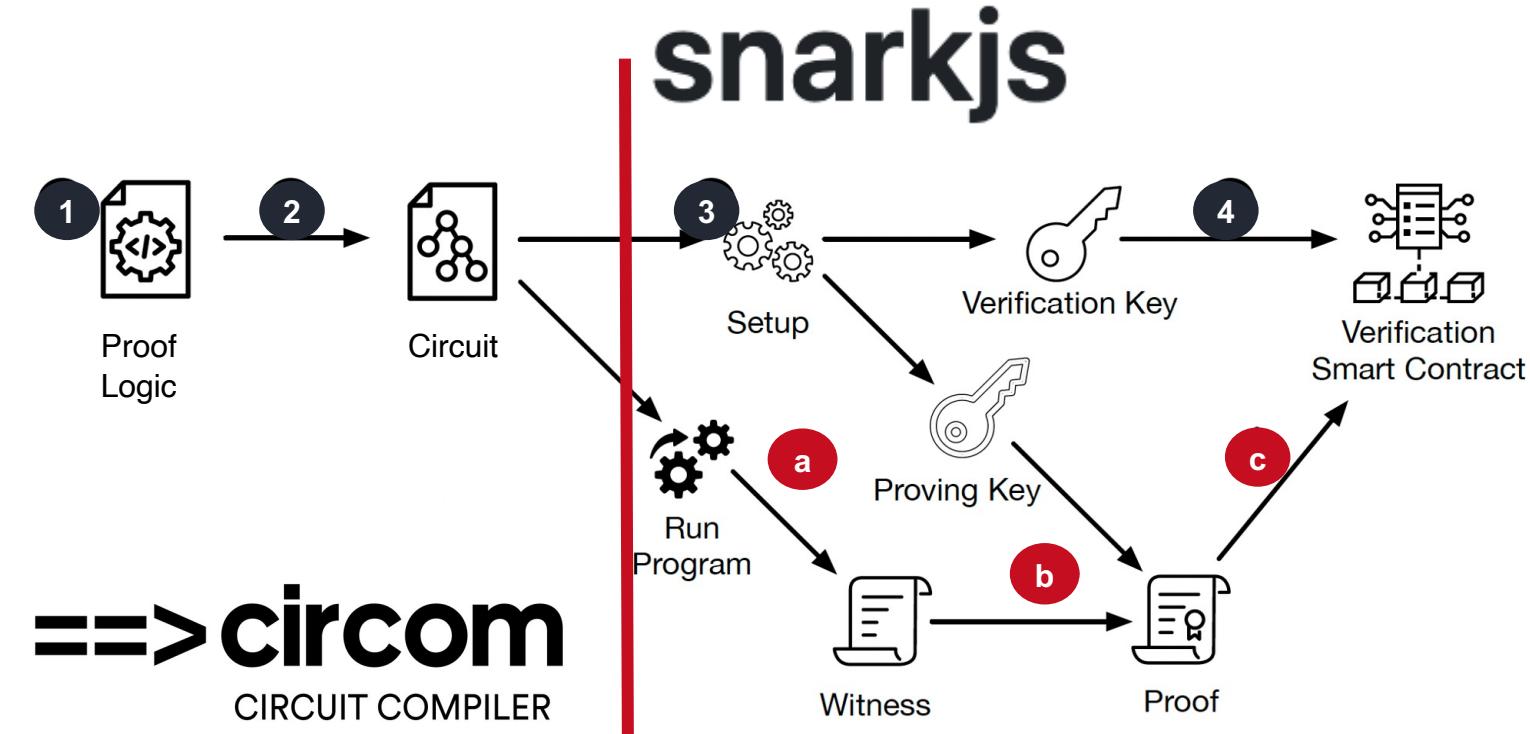
ZoKrates

- One-stop solution for Verifiable Offchain Computations (VOC)
 - Supports all steps 1-c
- Python-/Rust-like syntax
- Opinionated Compiler



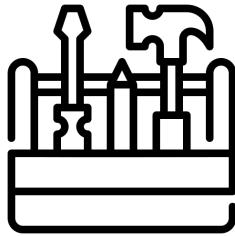
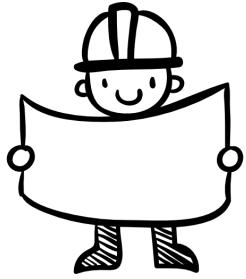
Circom / SnarkJS

- Modular tool for CIRcuit COMpilation
- HDL



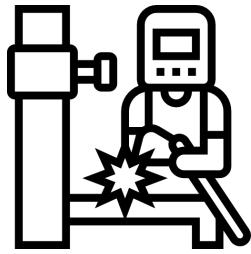
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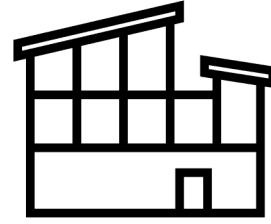
What are Zero-Knowledge Proofs (ZKPs) and why are they relevant for blockchains?

Hands-on



How to use zk-DSLs?

Applications

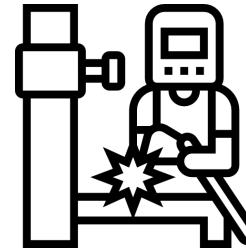


What can be built with ZKPs?

Learning Objectives

- Understand constraint systems
- Start an interactive environment
- Write our first program in ZoKrates & Circom
- Generate & verify proofs

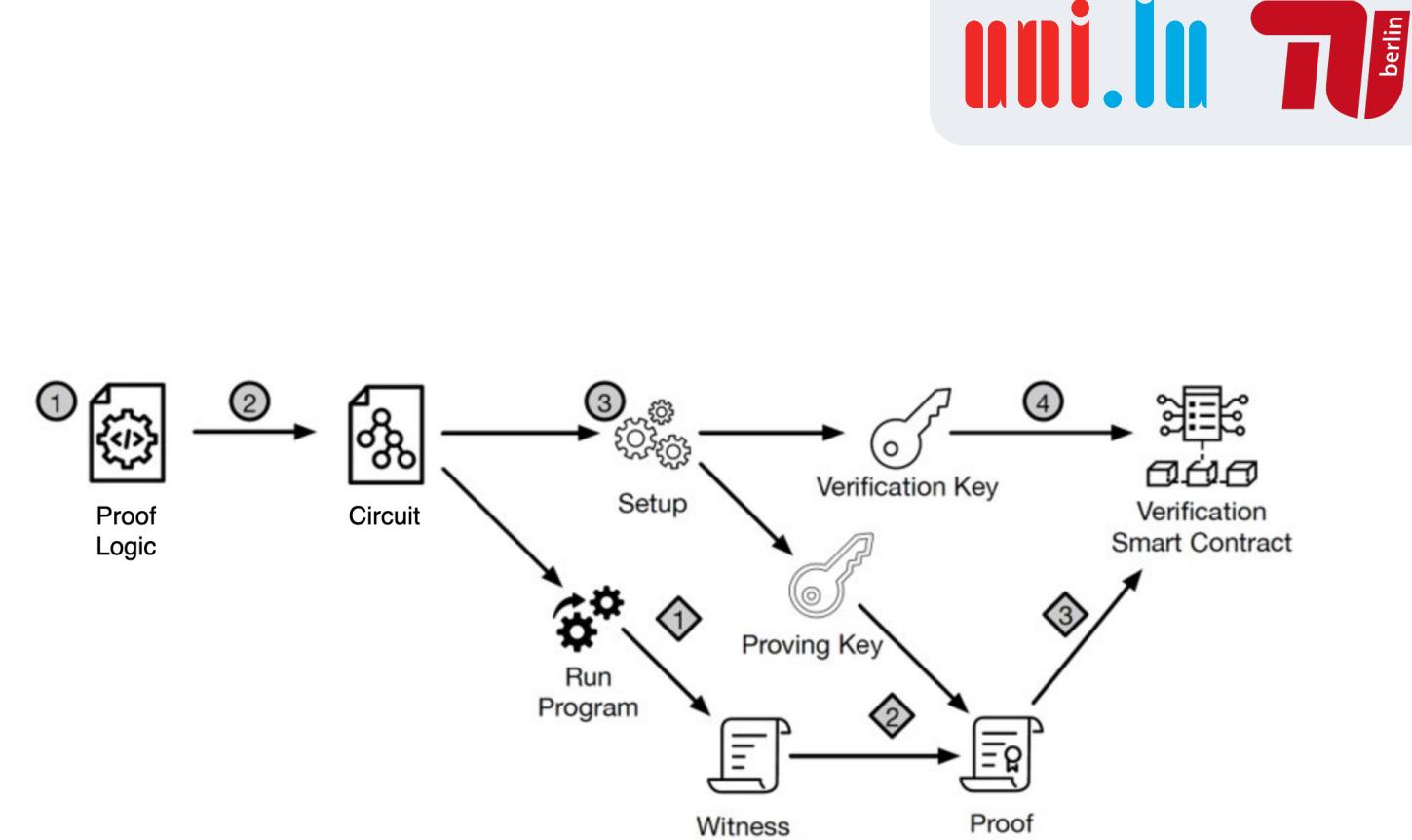
Hands-on



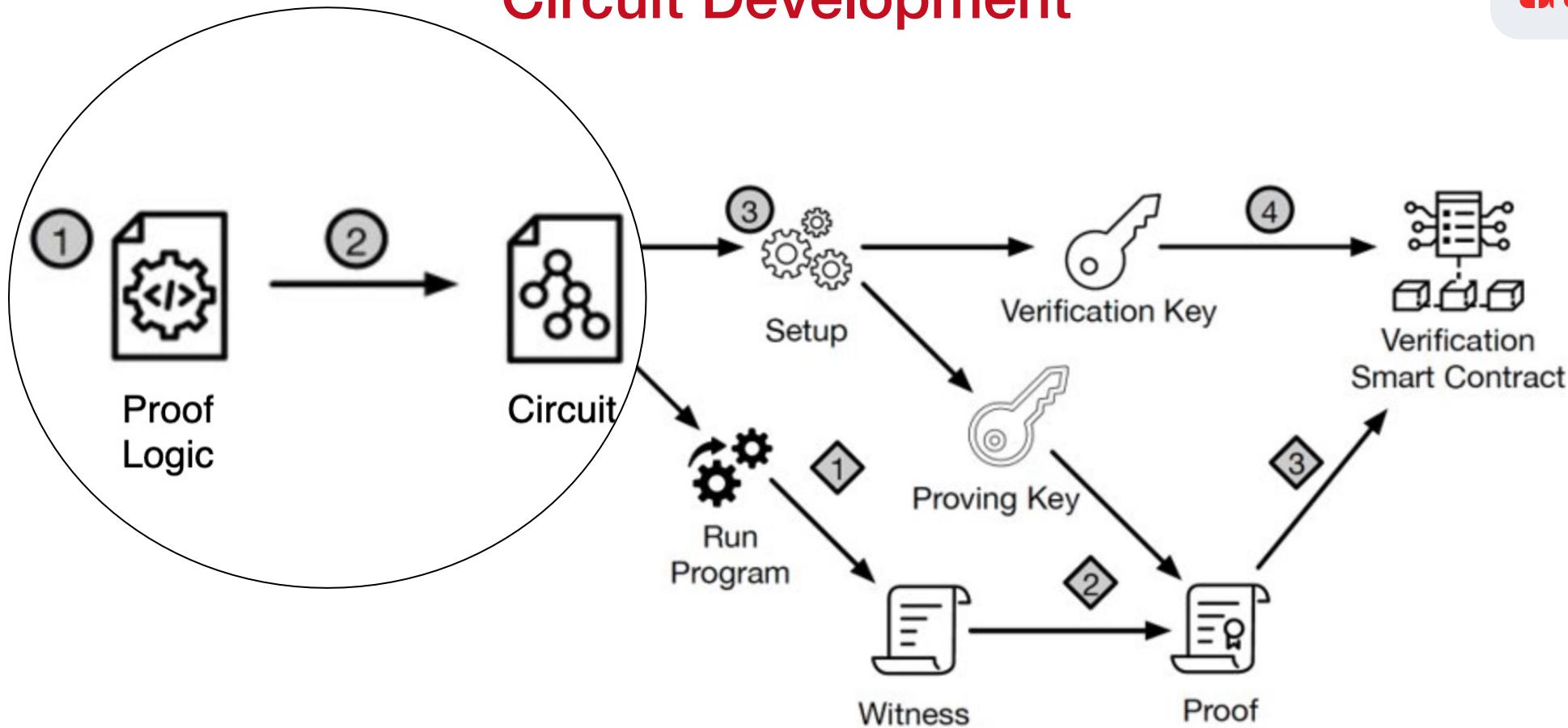
How to use zk-DSLs?

Learning Objectives

- Understand constraint systems (1&2)
- Write our first program in ZoKrates & Circom (1&2)
- Proof & Verify the proofs created



Circuit Development



How do you formally verify a program ?

Arithmetization is the process of turning a generic statement or question into a set of equation to be verified or solved[1]

In zk-SNARKs, we need arithmetization to for several reasons:

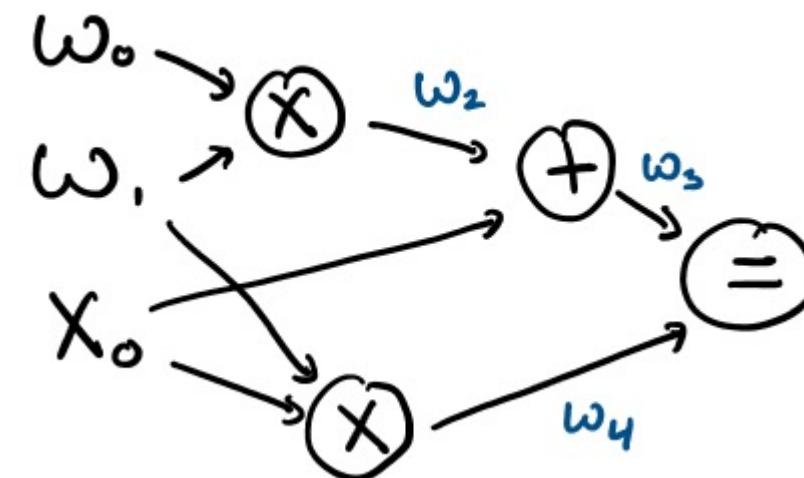
1. Guarantee the correctness of the computation
2. We need the set of equations to follow the same structure
3. Succinctness - The verification of the computation can be done efficiently
4. It allows for Zero-Knowledge

To satisfy all the above points we use algebraic constrain systems. An specially for this tutorial we will use the **Rank 1 Constrain System (R1CS)**.

R1CS: a common Arithmetic Circuit format

- Circuit form: Directed Cyclic Graph (DAG) of "wires" and "gates"
 - o Gates: nodes
 - o Wires: edges

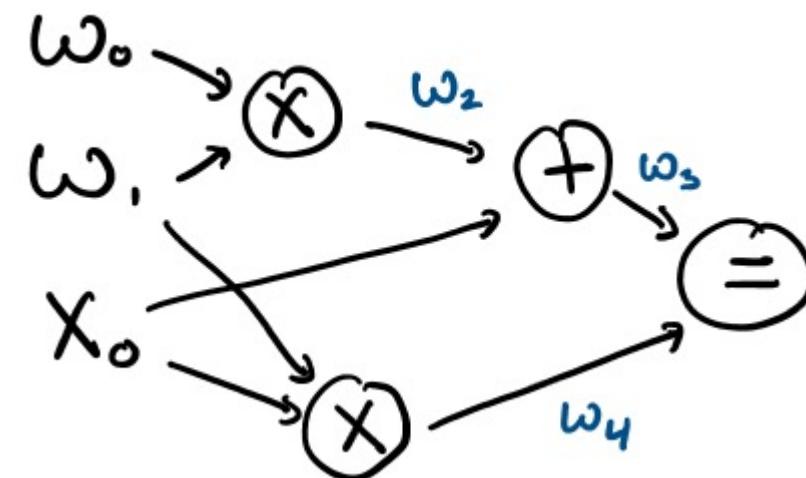
The number of gates determine the memory requirements and proving time



R1CS: a common Arithmetic Circuit format

- Circuit form: Directed Cyclic Graph (DAG) of "wires" and "gates"
 - o Gates: nodes
 - o Wires: edges
- Matrix form: n equations of form: $\alpha \times \beta = \gamma$
 - o where α, β, γ are affine (linear) combinations of variables

The number of gates determine the memory requirements and proving time



- $w_0 \times w_1 = w_2$
- $w_3 = w_2 + x_0$
- $w_1 \times x_0 = w_4$
- $w_3 = w_4$

- Wires -> Signals
- Gates -> Gates

```
// Primitive Types
signal aSignal = 42;
signal arraySignal[254];

// Composite Types

// functions
Component myComponent(){
    signal input in1;
    signal input in2;
    ...
    signal output out;
}

// for loops
signal arraySignal[254];

// Imports from Standard Library
include "circomlib/poseidon.circom";
include "https://github.com/0xPARC/circom-
secp256k1/blob/master/circuits/bigint.circom"

let dc = 0;
for (dc=0; cd<256; dc++) {
    arraySignal[dc] <== 2;
}

// conditional expressions
signal input condition1;
signal input condition2;
component conditionCheck = IsEqual();
IsEqual.in[0] <== condition1;
IsEqual.in[1] <== condition2;

signal output out
out <== conditionCheck.out * 42 + (1 -
conditionCheck.out) * 7;
```

ZoKrates Language

```
// Imports from Standard Library
from "ecc/babyjubjubParams" import
BabyJubJubParams
import "hashes/sha256/512bit" as sha256;

// Primitive Types
field a = 42;
bool b;
u32 = 255;

// Composite Types
field[256] c = [0; 256]

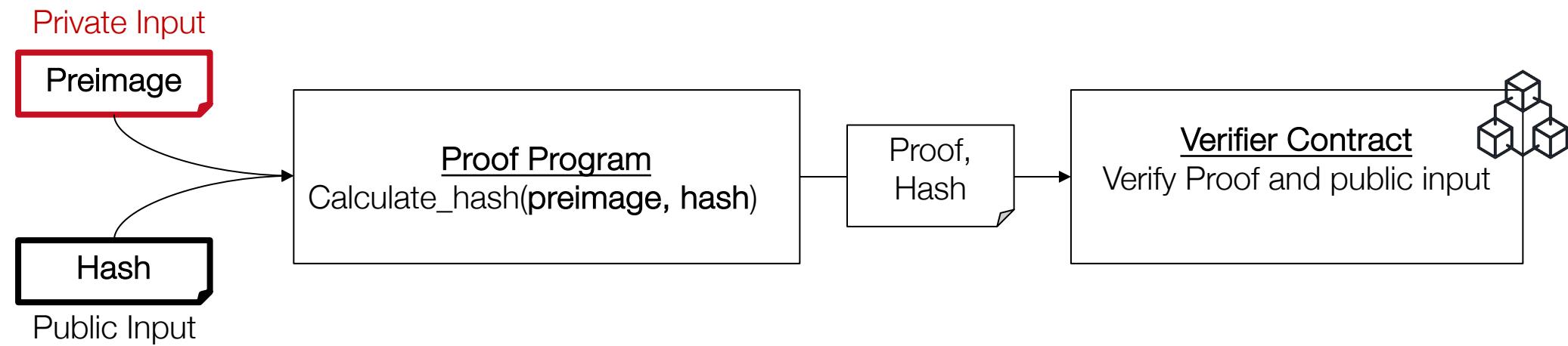
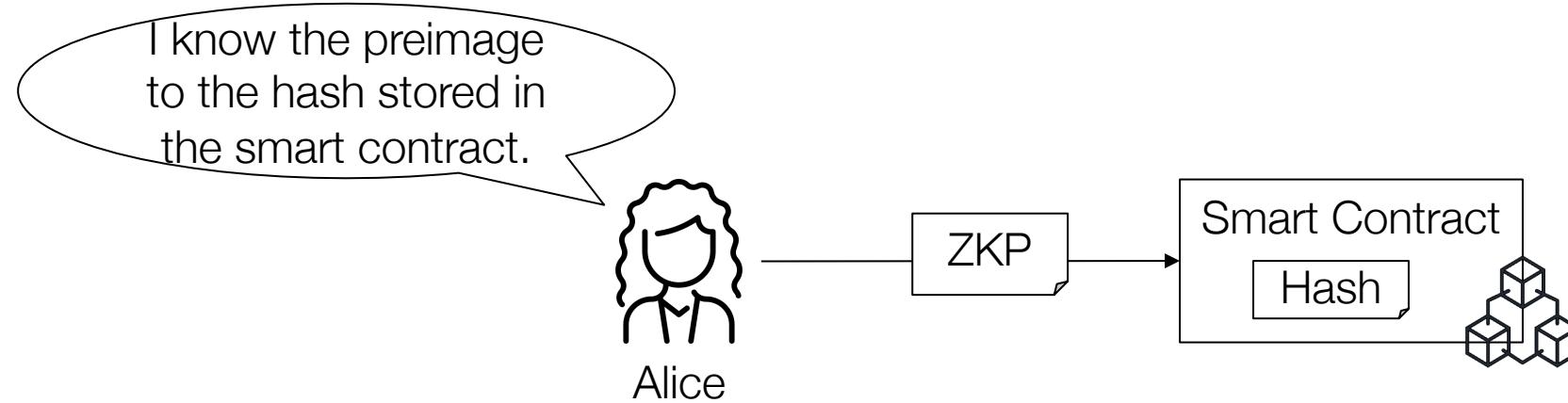
// functions
def incr(private field a, field b) -> field {
    return a + b;
}

// conditions & assertions
assert(2 + 2 == 4);

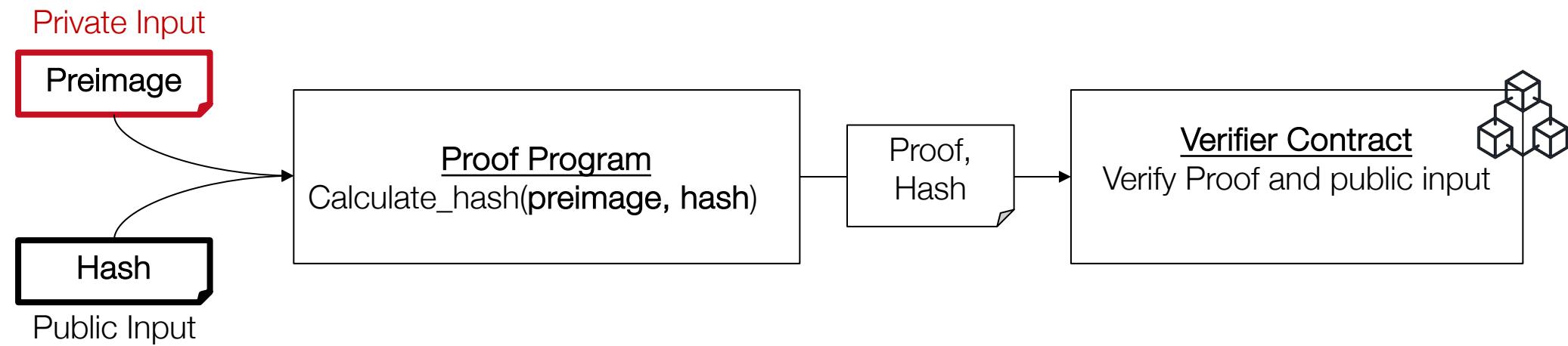
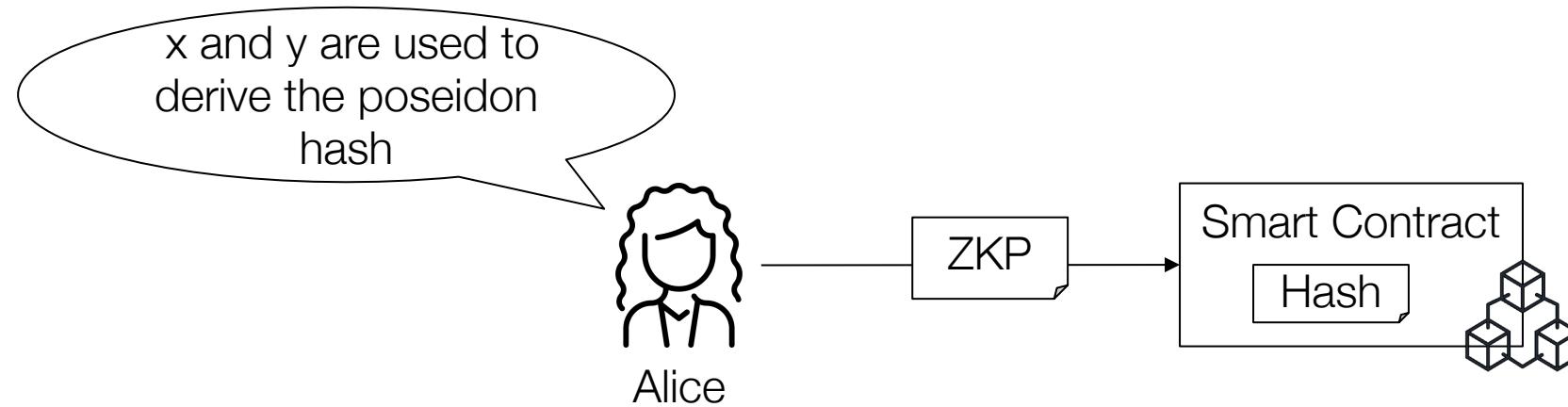
// for loops
for const u32 i in 0..4 {
    res = res + i;
}

// conditional expressions
if x == 1 {
    cheap(x)
} else {
    expensive(x) // both branches executed
}
```

Proving Knowledge of a Hash's Preimage

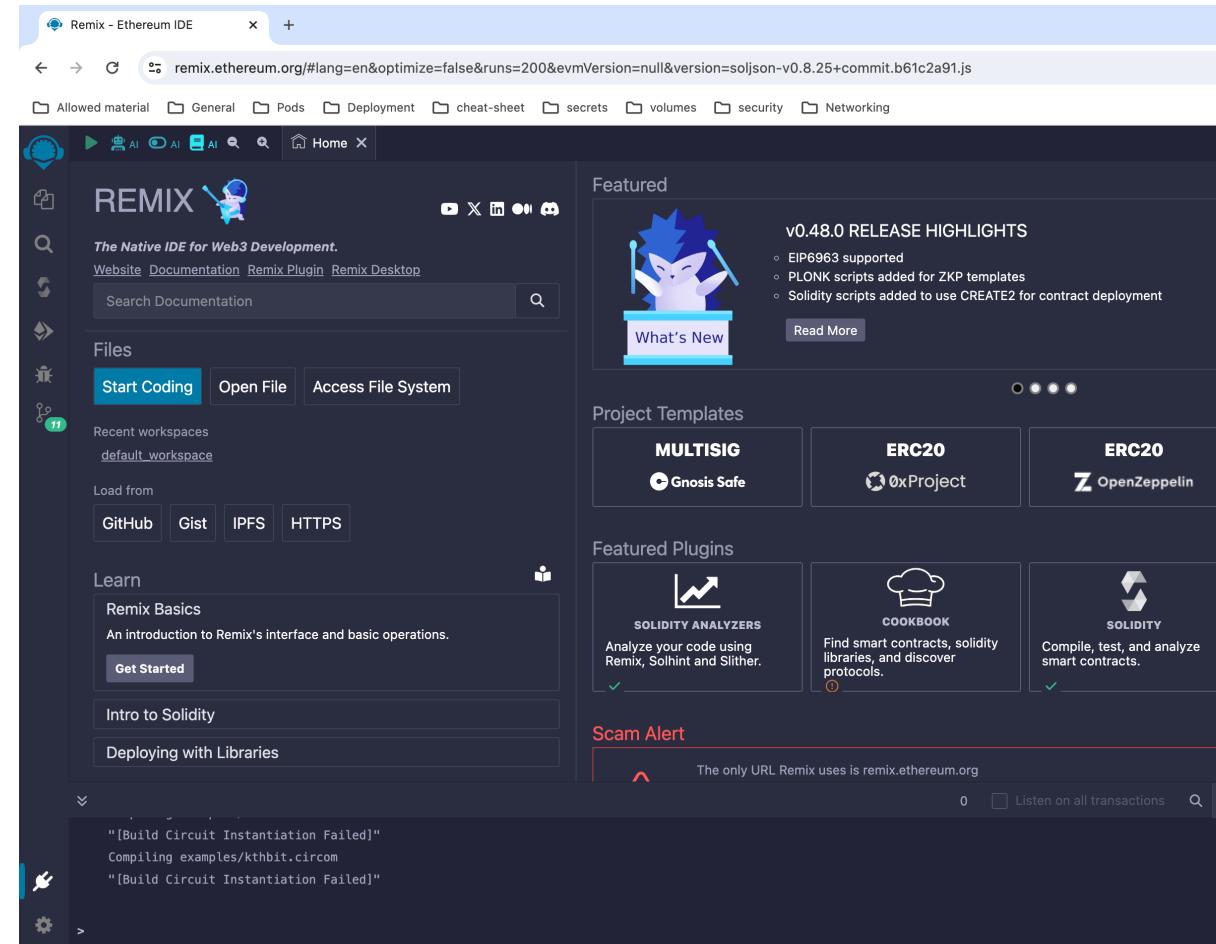


Ex.: Proving Knowledge of a Poseidon Hash



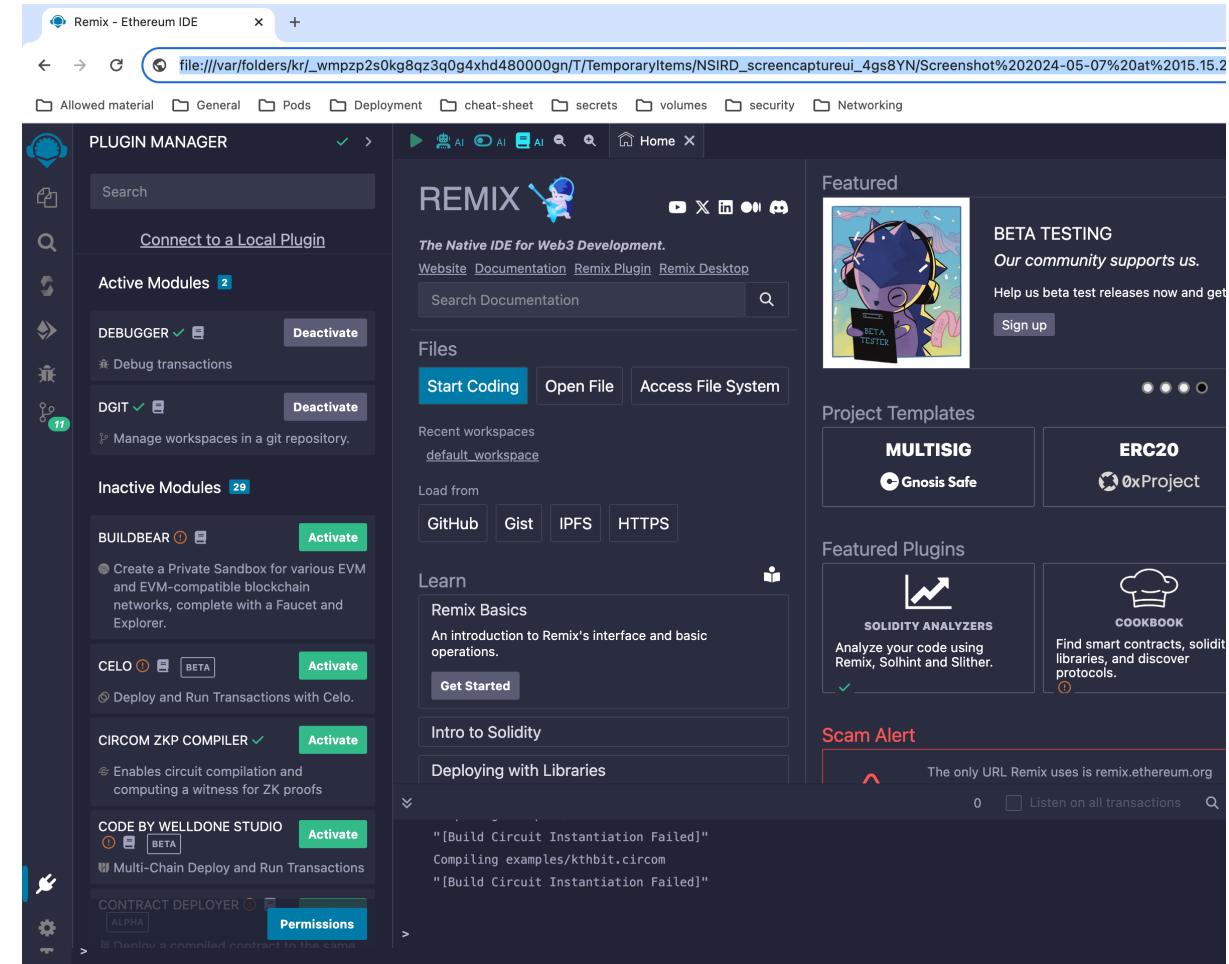
Setup

1. Go to remix.ethereum.org



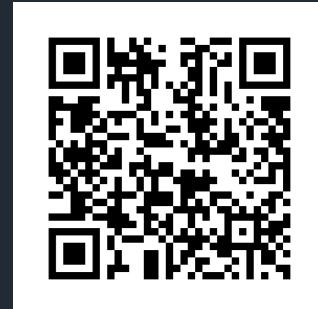
Setup

1. Go to remix.ethereum.org
2. Install the ZoKrates and Circos plug-in



Setup

1. Go to remix.ethereum.org
2. Install the ZoKrates and Circos plug-in
3. Import following repo to remix: https://github.com/ZK-Plus/ICBC24_Tutorial_Compute-Offchain-Verify-Onchain



The screenshot shows the Remix Ethereum IDE interface. The left sidebar is titled 'FILE EXPLORER' and contains options like 'Create', 'Clone' (which is highlighted), 'Rename', 'Download', 'Delete', 'Publish to Gist', 'Delete All', 'Backup', 'Restore', 'Solidity Test Workflow', 'Mocha Chai Test Workflow', 'Slither Workflow', 'Add Etherscan scripts', 'Add contract deployer scripts', 'Add Sindri ZK scripts', and 'Add Create2 Solidity factory'. The main workspace area displays the Remix logo and navigation links for 'Website', 'Documentation', 'Remix Plugin', 'Remix Desktop', and a search bar for 'Search Documentation'. Below this are sections for 'Files', 'Recent workspaces', and 'Load from' (GitHub, Gist, IPFS, HTTPS). A 'Learn' section provides links to 'Remix Basics', 'Intro to Solidity', and 'Deploying with Libraries'. On the right, there's a 'Featured' section with a video player icon and a 'WATCH TO LEARN' button, a 'Project Templates' section with 'MULTISIG' and 'ERC20' options, a 'Featured Plugins' section with 'SOLIDITY ANALYZERS' and 'COOKBOOK' icons, and a 'Scam Alert' section with a warning message about circuit instantiation failed.

Setup

1. Go to remix.ethereum.org
2. Install the ZoKrates and Circos plug-in
3. Import following repo to remix: https://github.com/ZK-Plus/ICBC24_Tutorial_Compute-Offchain-Verify-Onchain
4. Program templates are in the exercise folder

The screenshot shows the Remix Ethereum IDE interface. The FILE EXPLORER sidebar displays a project structure for 'ICBC24_Tutorial_Compute-Offchain-Verify-Onchain'. The 'exercise' folder is selected, containing subfolders 'circom' and 'zokrates', and files like 'package-lock.json', 'package.json', 'poseidon.js', 'README.md', '.gitignore', 'LICENSE', and another 'README.md'. The main code editor window shows a Circom script named 'poseidon.circom'. The script includes pragmas for 'circom 2.1.8' and 'circomlib/circuits/poseidon.circom'. It defines a template 'verifyHash' with three signal inputs: 'hash', 'a', and 'b'. A note '//TODO: verify a poseidon hash here' is present. A component 'main' is defined with a public method 'hash' that calls the 'verifyHash' template. The bottom status bar indicates 'Cloning' the repository multiple times.

```
pragma circom 2.1.8;
include "circomlib/circuits/poseidon.circom";

template verifyHash () {
    signal input hash;
    signal input a;
    signal input b;

    //TODO: verify a poseidon hash here
}

component main { public [ hash ] } = verifyHash();
```

Resources

- Standard library (stdlib):
 - o Circom: <https://github.com/iden3/circomlib>
 - o ZoKrates: <https://github.com/Zokrates/ZoKrates> > zokrates_stdlib
- Documentation:
 - o Circom: <https://docs.circom.io/circom-language/signals/>
 - o ZoKrates: <https://zokrates.github.io/>
- Getting Help:
 - o Circom's Telegram group: <https://t.me/iden3io>
 - o ZoKrates Gitter group: https://app.gitter.im/#/room/#ZoKrates_Lobby:gitter.im
- Test example:
 - o Preimage: 1, 2
 - o Hash: 7853200120776062878684798364095072458815029376092732009249414926327
459813530

Circom

Computing a Poseidon hash

```
pragma circom 2.1.6;

include "circomlib/poseidon.circom";

template verifyHash () {
    signal input hash;
    signal input a;
    signal input b;

    component hasher = Poseidon(2);
    hasher.inputs[0] <== a;
    hasher.inputs[1] <== b;

    hasher.out === hash;
    log("hash", hasher.out);
}

component main { public [ hash ] } = verifyHash();
```

ZoKrates

```
import "hashes/poseidon/poseidon" as poseidon;

def main(field hash, private field[2] preimage) {

    field digest = poseidon(preimage);
    assert(digest == hash);
}
```

Non-deterministic advice

Some operations are complex to do in a circuit but their correctness can easily be checked.

In this case, it makes sense to supply the result of this computation to the circuit as external information that needs to be validated.

```
1  pragma circom 2.1.8;
2
3
4  template squareRoot () {
5      signal input a;
6      signal input b;
7
8      a * a === b;
9  }
10
11
12 component main { public [ b ] } = squareRoot();
13
```

Number of iterations must be known at compile time.

```

15
16 ✓ def merkleTreeProof<DEPTH>(u32[8] root, MerkleTreeProofStruct<DEPTH> proof) -> bool {
17     // Start from the leaf
18     u32[8] mut digest = proof.leaf;
19
20     // Loop up the tree
21     for u32 i in 0..DEPTH {
22         (u32[8], u32[8]) s = select(proof.directionSelector[i], digest, proof.path[i]);
23         digest = hash(s.0, s.1);
24     }
25
26     return digest == root;
27 }
28
29 const u32 TREE_DEPTH = 2;
30
31 ✓ def main(u32[8] tree_root, MerkleTreeProofStruct<TREE_DEPTH> merkle_proof) {
32     assert(merkleTreeProof(tree_root, merkle_proof));
33 }      You, 13 minutes ago • merkle proof example

```

α	β	γ
x_1	y_1	z_1
x_2	y_2	z_2
...
x_n	y_n	z_n

Branching

1. Both branches are always executed.

```
def main(field x) -> field {
    return if x == 1 {
        cheap(x)
    } else {
        expensive(x) // both branches executed
    };
}
```

Branching

1. Both branches are always executed.
2. An unsatisfied constraint inside any branch will make the whole execution fail, even if this branch is not logically executed.

```
def main(field x) -> field {
    return if x == 0 {
        0
    } else {
        1 / x // executed even for x := 0, which leads to the execution failing
    };
}
```

Branching

1. Both branches are always executed.
2. An unsatisfied constraint inside any branch will make the whole execution fail, even if this branch is not logically executed.
3. No break / continue. If we need to break a loop and return a specific value, we can

```
pragma circom 2.1.8;

include "circomlib/comparators.circom";

template ReturnIfCondition () {
    signal input inputs[5];
    signal input index;

    component checkers[5];

    signal runningReturnSum[6];
    runningReturnSum[0] <= 0;

    signal output value;

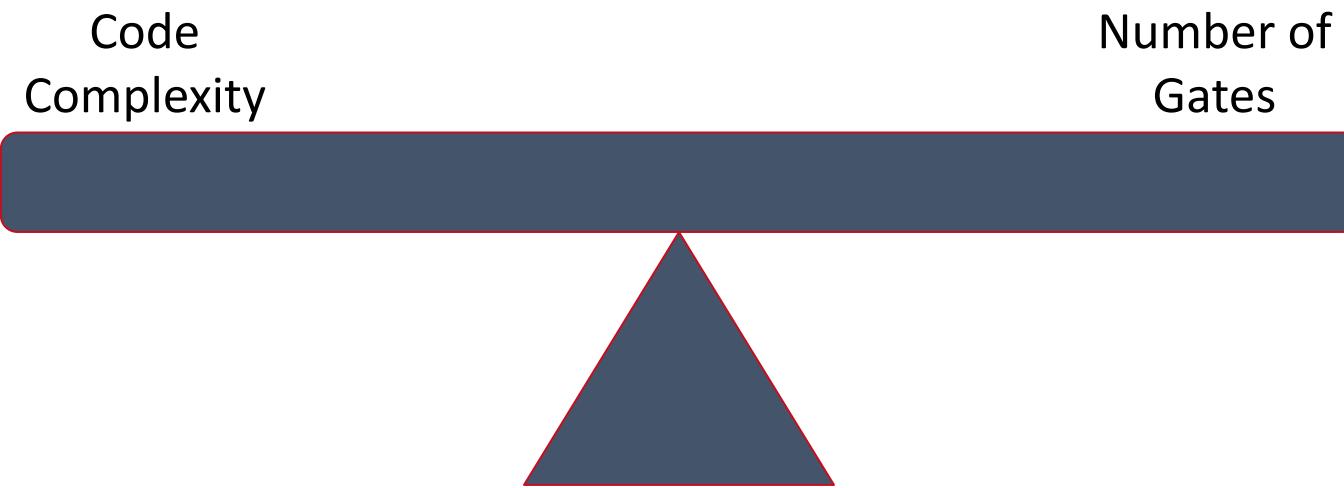
    for (var i=0; i<5; i++){
        checkers[i] = IsEqual();
        checkers[i].in[0] <= i;
        checkers[i].in[1] <= index;

        runningReturnSum[i+1] <= runningReturnSum[i] + checkers[i].out * inputs[i];
        log("Running return sum at index: ", runningReturnSum[i+1]);
    }

    value <= runningReturnSum[5];
}

component main = ReturnIfCondition();

/* INPUT = {
    "inputs": ["1", "2", "3", "4", "5"],
    "index": "2"
} */
```



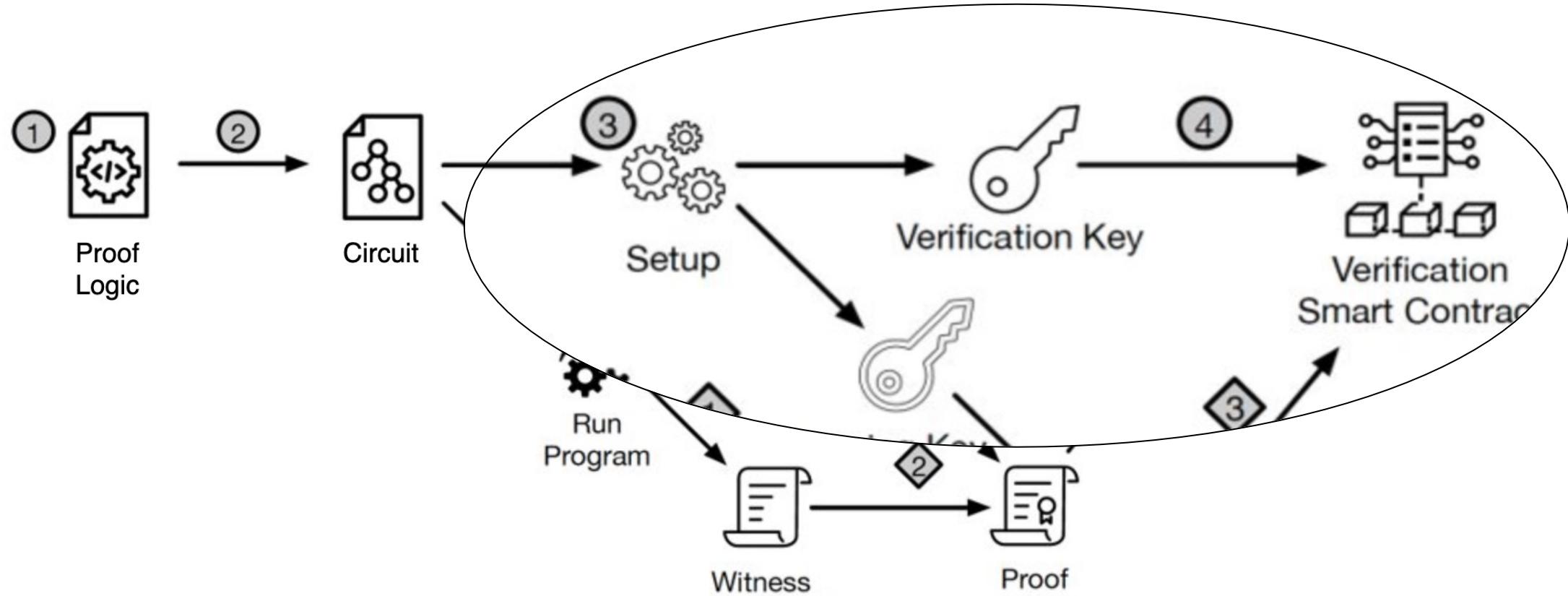
Support of Cryptographic Primitives

Support of Cryptographic Primitives

- Standard library
- 3rd party library

	Circum	ZoKrates
Hashes		
SHA256	✓	✓
SHA3	✓	✓
Poseidon	✓	✓
Pedersen	✓	✓
MimC	✓	✓
Poseidon2	✓	✗
Keccak	✓	✗
Signatures	✓	
EdDSA	✓	✓
ECDSA	✓	✗
Encryption Algorithms		
ElGamal	✓	✗
RSA	✓	✗
AES	✓	✗

Setup & Deployment



Setup

The trusted setup is done in two steps:

1. "Phase 1", does not depend on the program and is called Powers of Tau.
2. "phase 2" is circuit-specific, so it should be done separately for each different program.

Check [Circos](#)'s and [ZoKrates](#)' documentation for information on the process.

snarkjs

```
# export proving key  
$ snarkjs groth16 setup circuit.r1cs pot12_final.ptau  
proving_key.zkey  
  
# export verification key  
$ snarkjs zkey export verificationkey proving_key.zkey  
verification_key.json
```

ZoKrates

```
# export keys from final parameters (proving and  
verification key)  
$ zokrates mpc export -i final.params
```

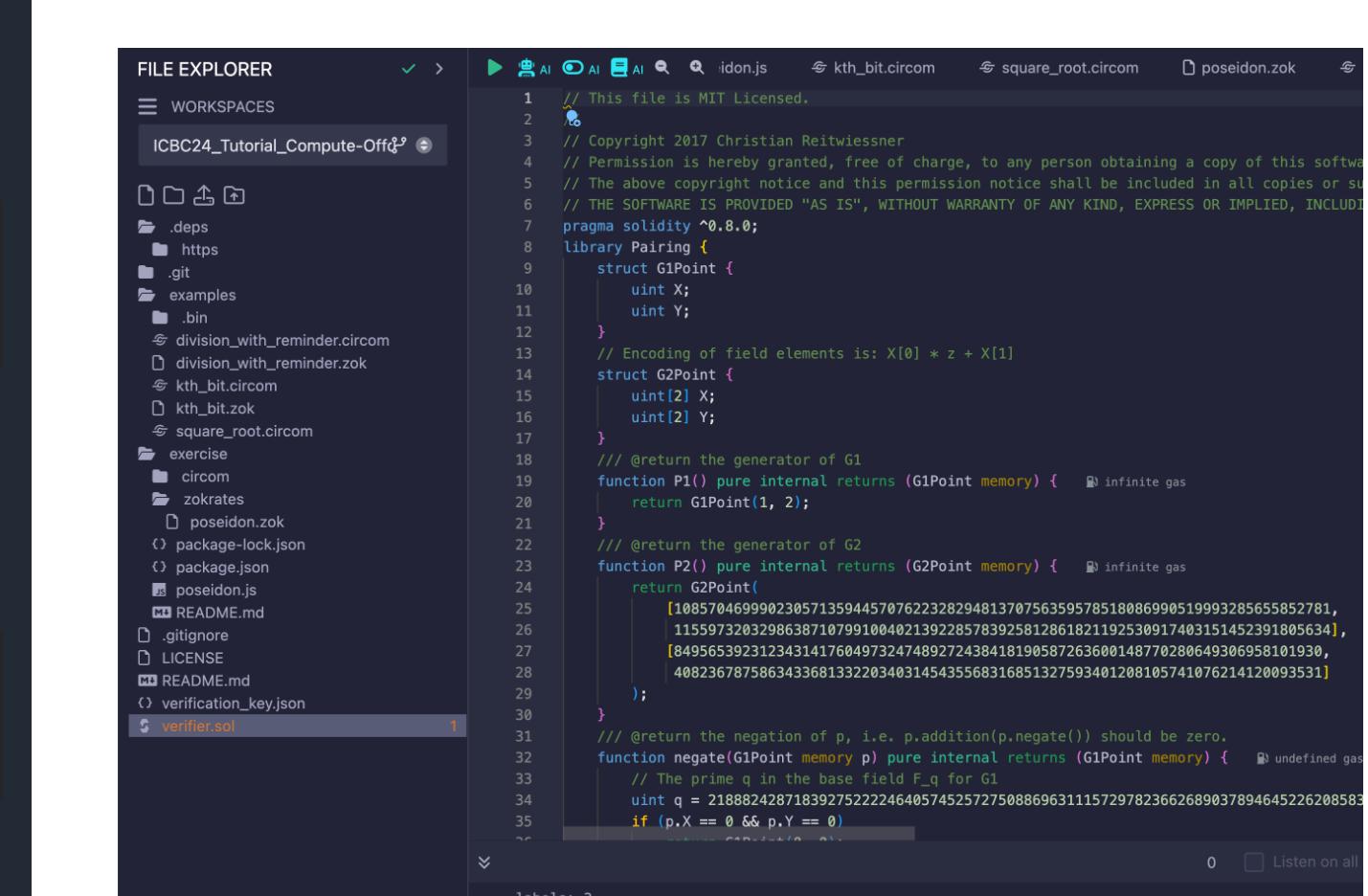
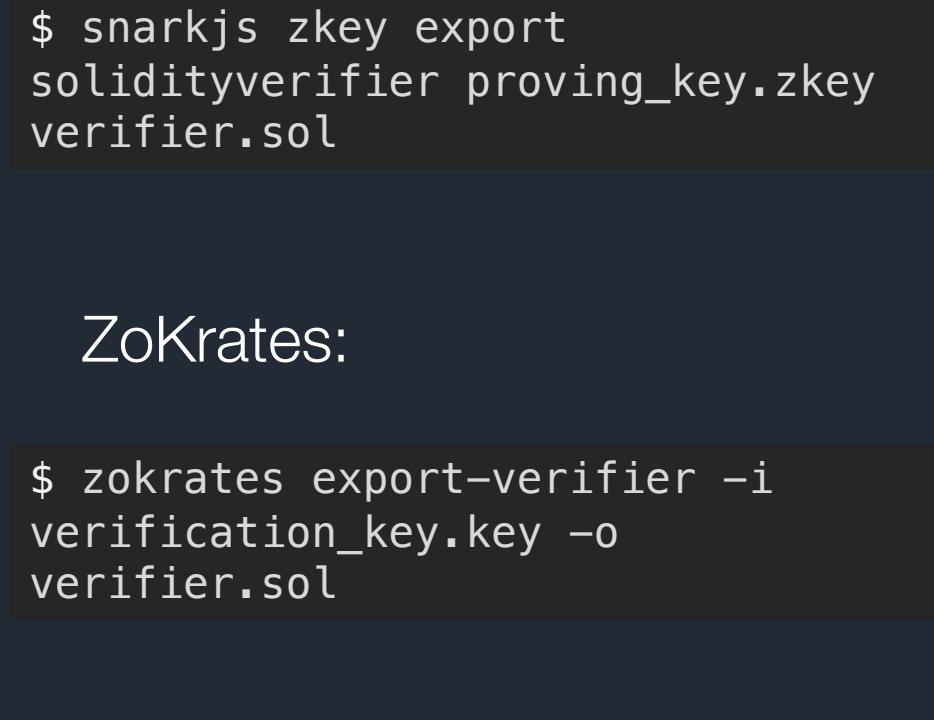
Export verifier contract

Snarkjs:

```
$ snarkjs zkey export
solidityverifier proving_key.zkey
verifier.sol
```

ZoKrates:

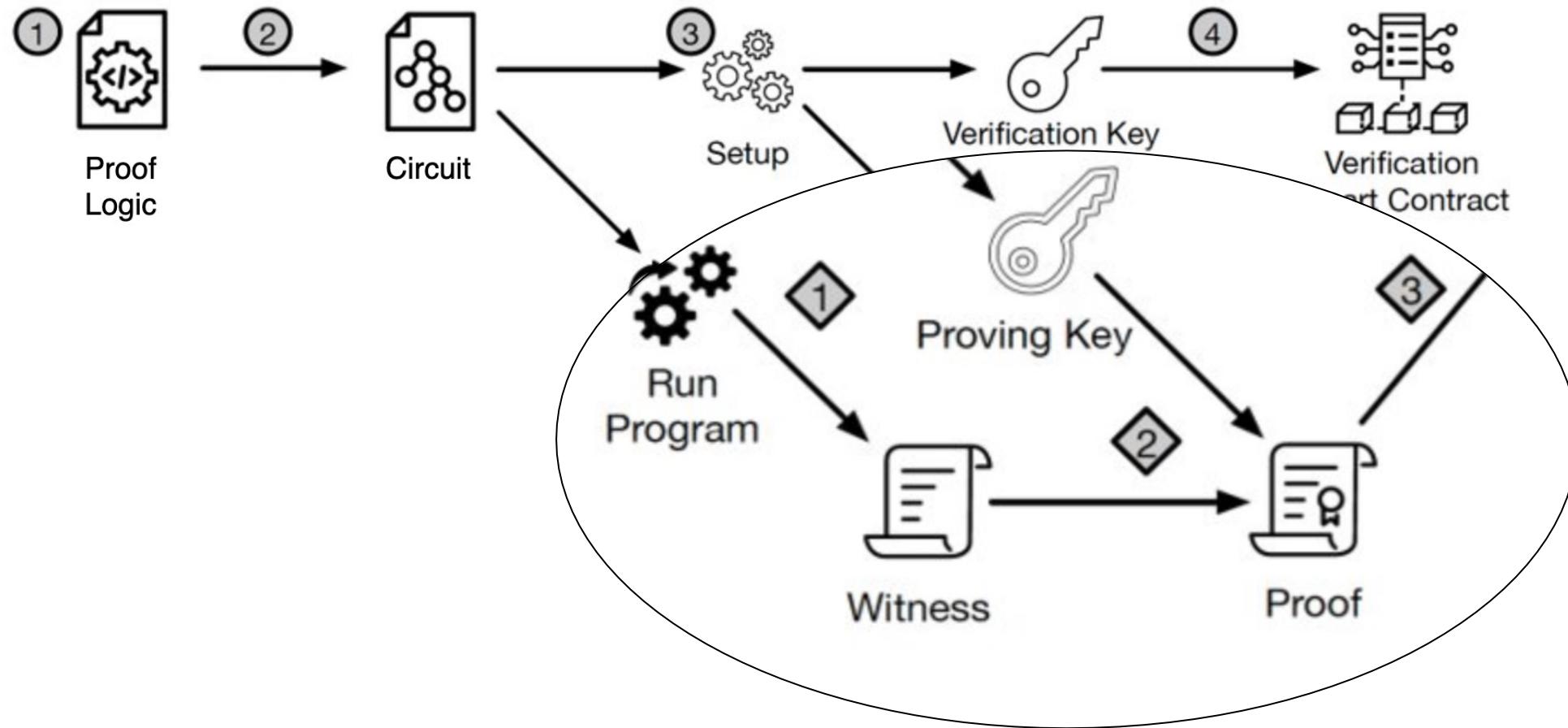
```
$ zokrates export-verifier -i
verification_key.key -o
verifier.sol
```



The screenshot shows a terminal window with two tabs open. The left tab displays the command to export a verifier contract using Snarkjs. The right tab displays the command to export a verifier contract using ZoKrates. Both tabs show the output of the command, which is a file named 'verifier.sol'.

```
// This file is MIT Licensed.
// Copyright 2017 Christian Reitwiessner
// Permission is hereby granted, free of charge, to any person obtaining a copy of this software
// The above copyright notice and this permission notice shall be included in all copies or
// THE SOFTWARE IS PROVIDED "AS IS", WITHOUT WARRANTY OF ANY KIND, EXPRESS OR IMPLIED, INCLUDING
// pragma solidity ^0.8.0;
library Pairing {
    struct G1Point {
        uint X;
        uint Y;
    }
    // Encoding of field elements is: X[0] * z + X[1]
    struct G2Point {
        uint[2] X;
        uint[2] Y;
    }
    /// @return the generator of G1
    function P1() pure internal returns (G1Point memory) { infinite gas
        return G1Point(1, 2);
    }
    /// @return the generator of G2
    function P2() pure internal returns (G2Point memory) { infinite gas
        return G2Point(
            [1085704699023057135944570762232829481370756359578518086990519993285655852781,
            11559732032986387107991004021392285783925812861821192530917403151452391805634],
            [8495653923123431417604973247489272438418190587263600148770280649306958101930,
            4082367875863433681332203403145435568316851327593401208105741076214120093531]
        );
    }
    /// @return the negation of p, i.e. p.addition(p.negate()) should be zero.
    function negate(G1Point memory p) pure internal returns (G1Point memory) { undefined gas
        // The prime q in the base field F_q for G1
        uint q = 2188824287183927522246405745257275088696311157297823662689037894645226208583
        if (p.X == 0 && p.Y == 0)
            return G1Point(0, 0);
    }
}
labels: 3
```

Proving



Generate the input arguments

Through popular cryptography libraries:

- Circomlib (js)
- ZnaKes (python)
- Hashlib (python)
- ...

```
3  const circomlibjs = require("circomlibjs");
4
5  (async function () {
6    const preimage = [1, 2]
7    const poseidon = await circomlibjs.buildPoseidon();
8    const hash = poseidon.F.toString(poseidon(preimage));
9    console.log(`poseidon hash of preimage(${preimage}) is: ${hash}`);
10   })()
11
12
```

Proving

1. Automatically in JS

```
2 const snarkjs = require("snarkjs");
3 const fs = require("fs");
4
5 async function run() {
6     const { proof, publicSignals } = await snarkjs.groth16.fullProve(
7         {a: 10, b: 21},
8         "circuit.wasm",
9         "proving.zkey"
10    );
11 }
12 |
```

```
2 import { initialize } from "zokrates-js";
3
4 initialize().then(zokratesProvider) => {
5
6     // witness computation
7     const { witness, output } = zokratesProvider.computeWitness(circuit, ["2"]);
8
9     // generate proof
10    const proof = zokratesProvider.generateProof(
11        circuit.program,
12        witness,
13        keypair.pk
14    );
15 }
16 |
```

Proving

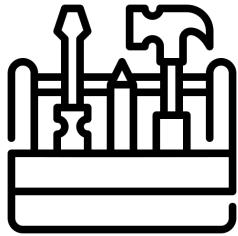
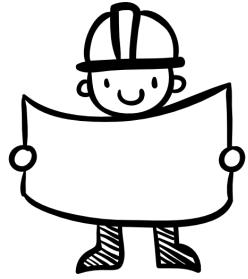
1. Automatically in JS
2. Manually with the cli

```
$ node generate_witness.js multiplier2.wasm input.json  
witness.wtns  
$ snarkjs groth16 prove proving_key.zkey witness.wtns  
proof.json public.json
```

```
$ zokrates compute-witness -i circuit -a 1 2 ...  
$ zokrates generate-proof -i circuit -p proving_key -w  
witness
```

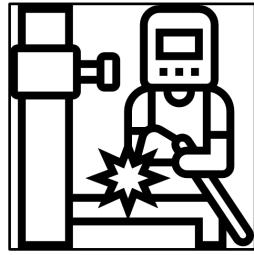
Agenda

Motivation & Concept



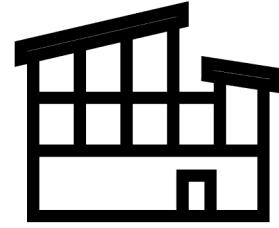
What are Zero-Knowledge Proofs (ZKPs) and why are they relevant for blockchains?

Hands-on



How to use zk-DSLs?

Applications



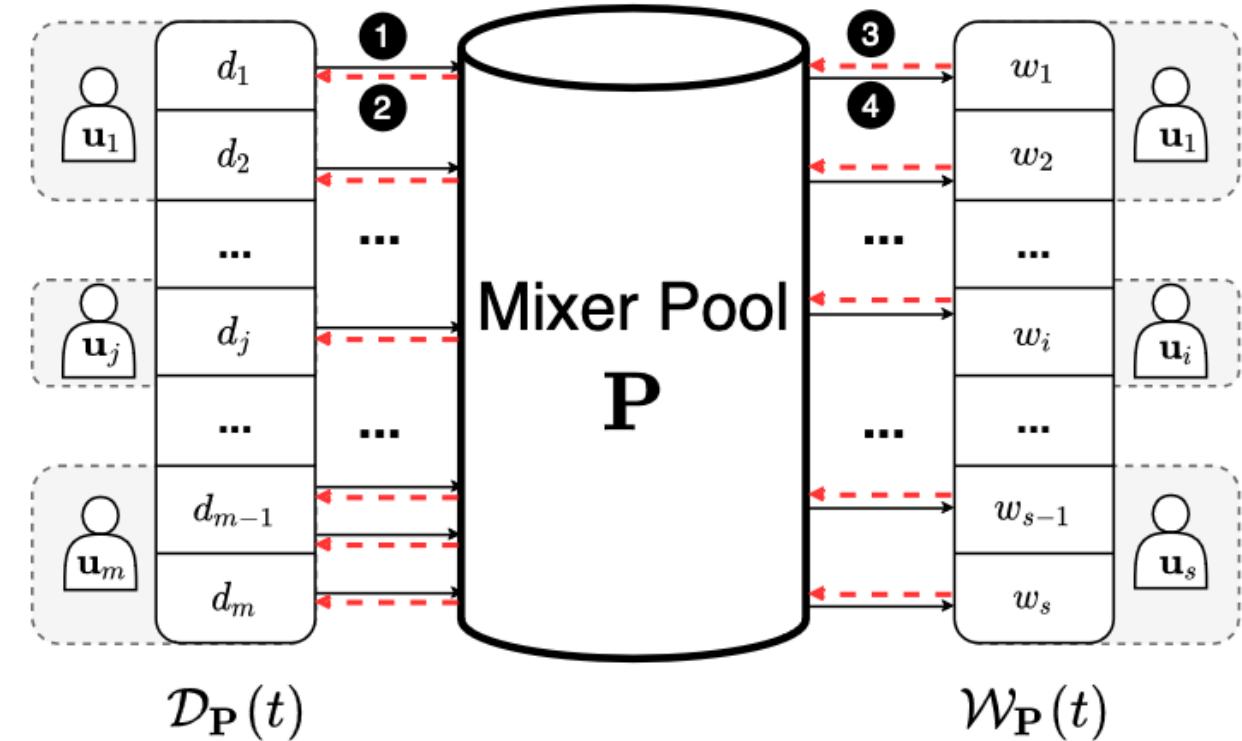
What can be built with ZKPs?

Application 1: Transaction Mixers

Mixers (Tornado Cash)

Achieve higher account privacy by pooling together funds from multiple users.

1. Deposit tokens in mixer pool
2. Receive deposit key
3. Prove that you are the holder of the deposit key with zk (from another address)
4. Receive withdraw



Application 2: ZK-Rollups

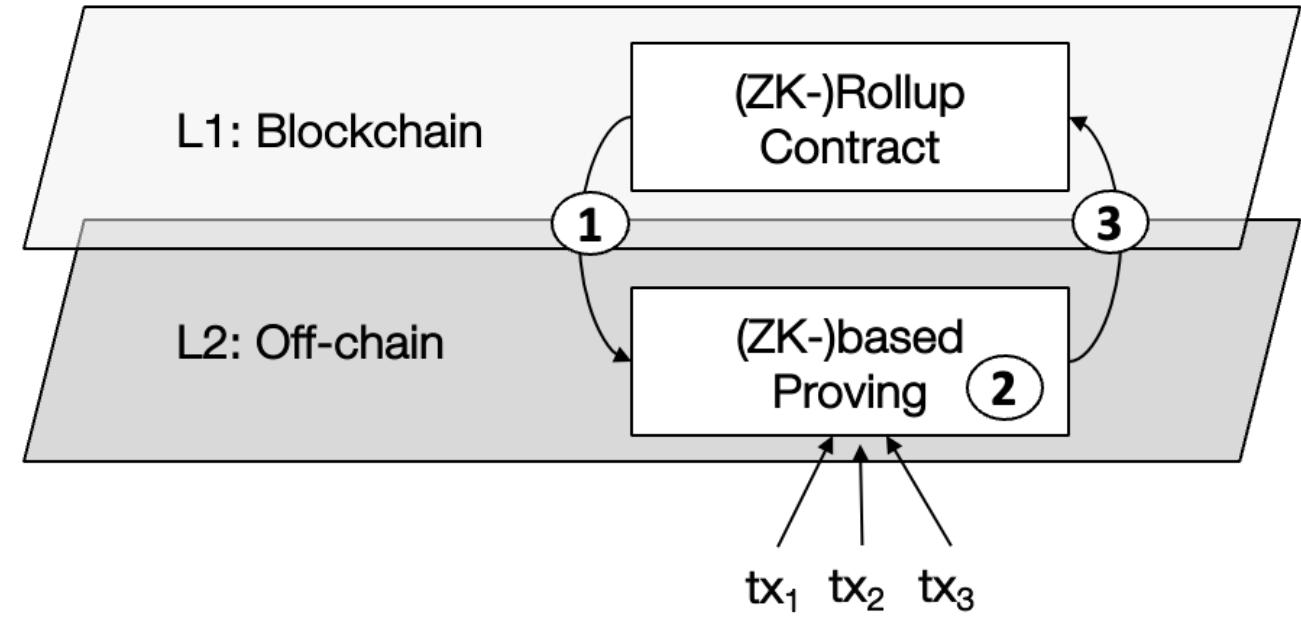
(ZK-)Rollups Overview

Objective: Reduce transaction costs through off-chain transaction aggregation

- Storage (compression),
- Computation (cheap verification)

Proof Correctness with

- Fraud Proofs (Mechanism Design), e.g., Arbitrum, Optimism
- Validity proofs (ZKP), e.g., zkSync, Polygon, Starknet



- ➊ Get state (accounts, balances) from L1.
- ➋ Aggregate transactions and create proof of computational correctness on L2.
- ➌ Verify proof and apply state to L1.

Example Architecture

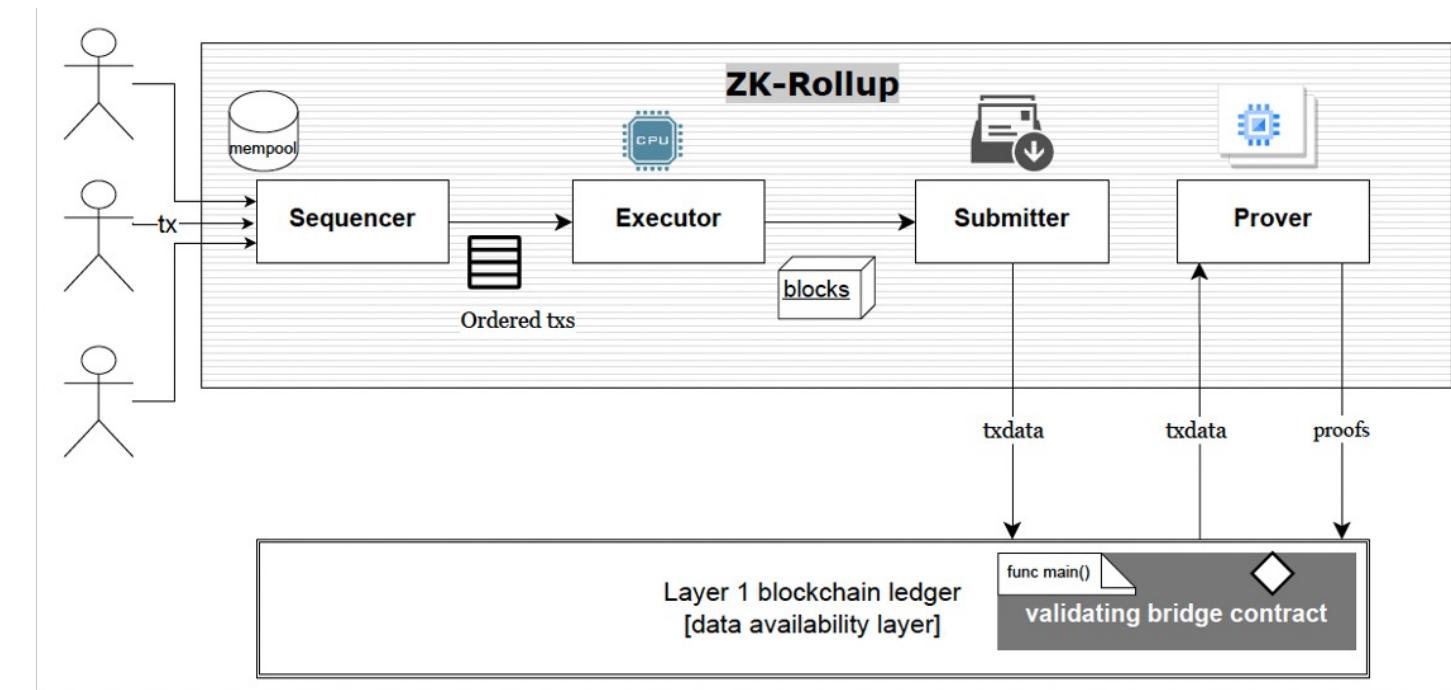
[1]

Sequencer: order transactions in preparation for execution.

Executors: construct transaction blocks from sequenced transactions.

Submitters: compute the hash of the Merkle tree's root and forward the state differences to L1.

Provers: actively monitor L1 checkpoint events, producing “validity proofs” with ZKPs.



[1] Motepalli, Shashank, Luciano Freitas, and Benjamin Livshits. "Sok: Decentralized sequencers for rollups." *arXiv preprint arXiv:2310.03616* (2023).

Example Architecture [1]

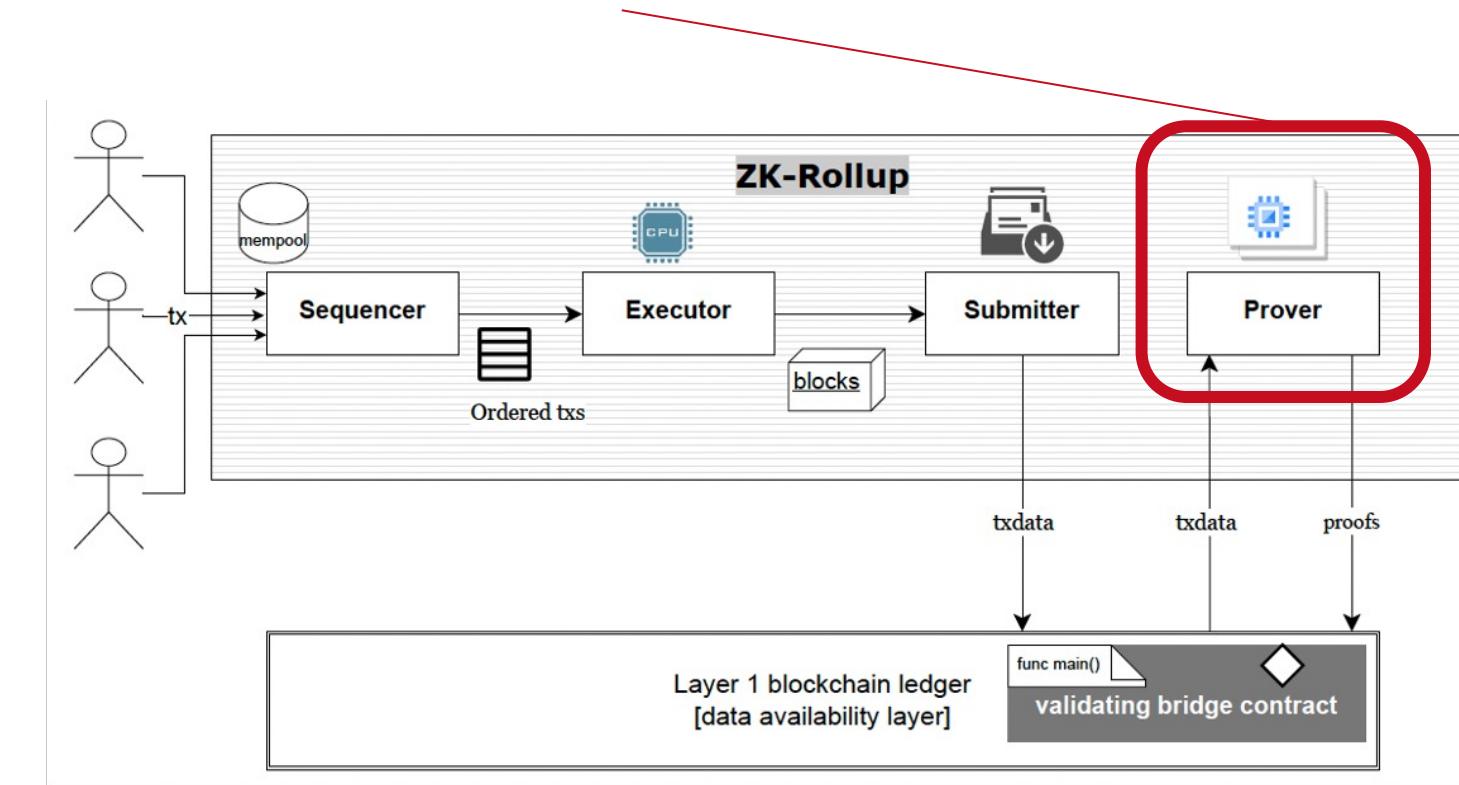
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Executors: construct transaction blocks from sequenced transactions.

Submitters: compute the hash of the Merkle tree's root and forward the state differences to L1.

Provers: actively monitor L1 checkpoint events, producing “validity proofs” with ZKPs.

- Proofs heavily rely on *Merkle Tree* operations.
- Optimization through *Recursive Proofs*, e.g., Nova, and *Efficient Hashing*, e.g., Poseidon.



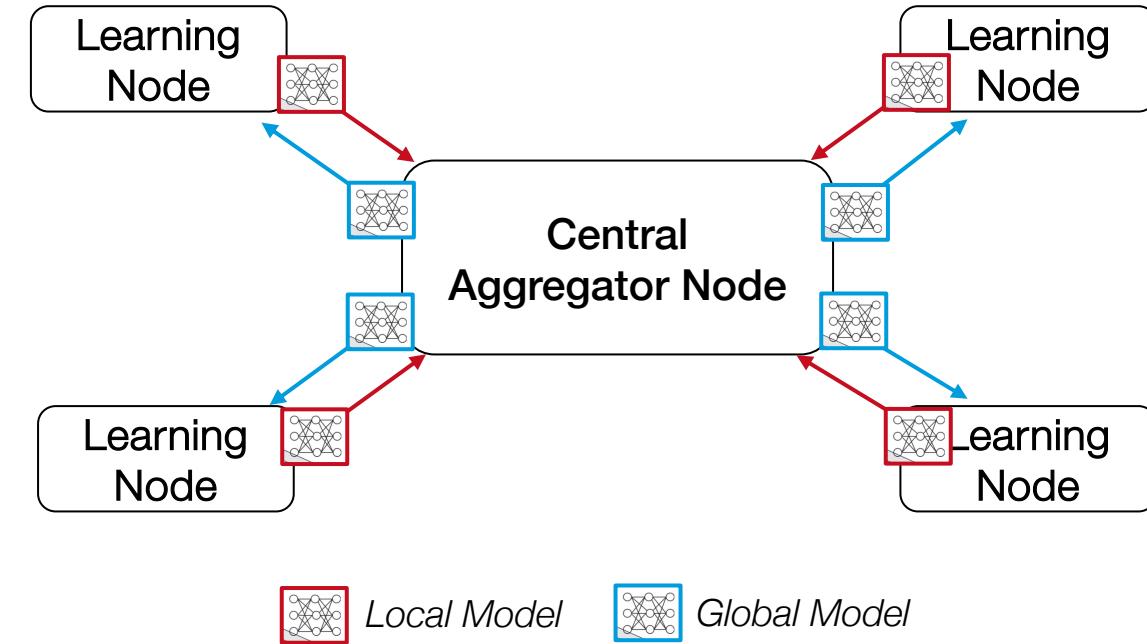
[1] Motepalli, Shashank, Luciano Freitas, and Benjamin Livshits. "Sok: Decentralized sequencers for rollups." *arXiv preprint arXiv:2310.03616* (2023).

Application 3: Verifiable Decentralized Federated Learning

Federated Learning

Learning nodes compute and submit *local model*.

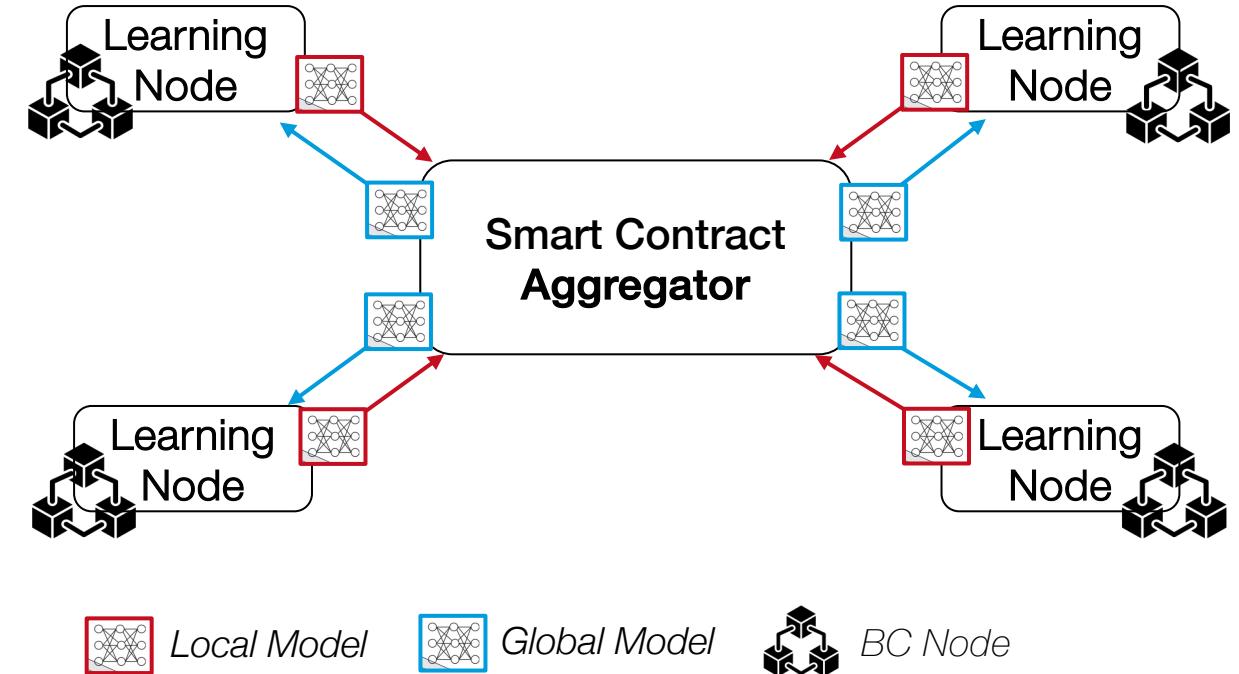
Aggregator node creates and returns *global model*.



Decentralized Federated Learning (+ Blockchain)

The aggregator is implemented as a smart contract.

Learning node submit local models through a blockchain client.

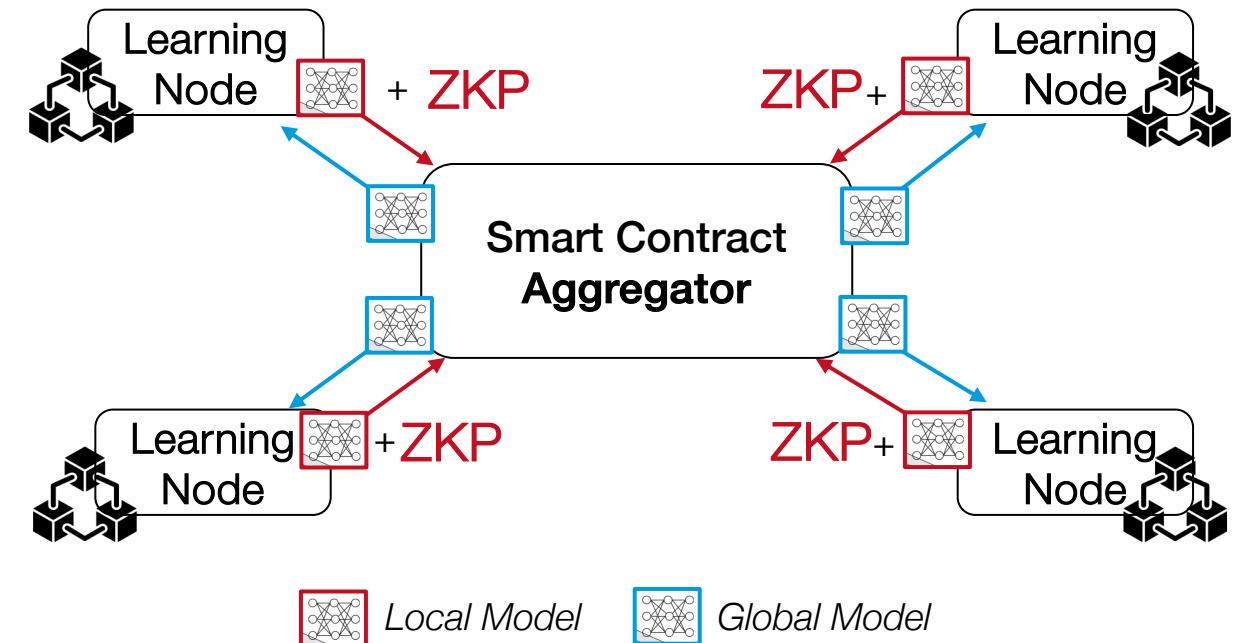


Verifiable Decentralized Federated Learning (+ ZKPs)

ZK-based local learning returns local model and computational proof.

Aggregator verifies ZKP before creating and returning global model.

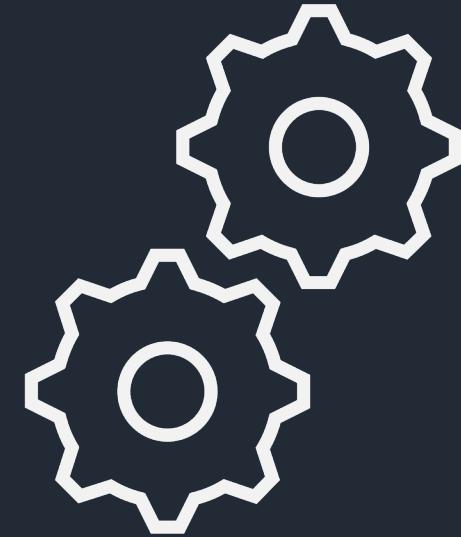
*...prevents **model poisoning** but adds high computational overhead.*



[1] J. Heiss, E. Grunewald, S. Tai, N. Haimerl, S. Schulte. *Advancing Blockchain-based Federated Learning through Verifiable Off-chain Computations*, IEEE Blockchain 2022

Other Application Contexts

- Netting in Energy Grids [3]
- Sensor Data Pre-processing in IoT scenarios [4]
- Blockchain Interoperability (zkBridges)
- Access Policy Evaluation
- ...



[3] J. Eberhardt, M. Peise., D.H. Kim, S. Tai. *Privacy-Preserving Netting in Local Energy Grids*, ICBC 2020

[4] J. Heiss, A. Busse, and S. Tai. *Trustworthy Pre-Processing of Sensor Data in Data On-chaining Workflows for Blockchain-based IoT Applications*, ICSOC 2021

Thanks for your attention!

We are looking forward to hear from you ☺

Please get in touch with us.

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