

# ZKDL Camp Topics

## Basic Topics (Preliminaries)

### 1. Mathematics for cryptographers.

- (a) Basics of number theory, RSA case study.
- (b) Definition of a group. Subgroups, cyclic groups, isomorphisms and automorphisms. Applications.
- (c) Vector spaces.
- (d) Polynomials.
- (e) Definition of a field. Finite fields.

### 2. Elliptic Curves.

- (a) Defining a group structure.
- (b) Points addition in affine form.
- (c) Scalar multiplication, effective implementation in  $O(\log_2(k))$ .
- (d) Twisted Curves.
- (e) Useful endomorphism.
- (f) Examples of widely used curves.

### 3. Elliptic Curve Pairings (*might simply redirect to the zksync lecture*).

- (a) Definition and applications.
- (b) Finite field extensions  $\mathbb{F}_{p^n}$ .
- (c) (*optional, possibly advanced topic*) Implementation details: divisors, ate pairing, Miller Loop.

### 4. Cryptographic Commitments.

- (a) Hash and Pedersen commitments.
- (b) Functional commitments: Polynomial commitments.
- (c) KZG commitment scheme.
- (d)  $\tau$  ceremony.

## Medium Topics

1. Introduction: What are zero-knowledge proofs? Basic examples.
2. Succinct Non-Interactive Arguments of Knowledge (SNARK): what succinctness means and security definitions.
3. Arithmetic Circuits. Rank-1 Constraint Systems. Quadratic Arithmetic Programs.
4. Programming SNARKs. Circom. Solving real-world problems with Circom and many practical examples.
5. Zero-knowledge proving systems case studies:
  - (a) Groth16
  - (b) Plonk
  - (c) Range proofs + Bulletproofs + Bulletproofs+ + Bulletproofs+ +
  - (d) STARKs

## **Advanced topics**

1. Low-level arithmetic and optimizations.
2. Halo2.
3. Nova, Supernova, Hypernova.
4. Folding schemes.