

# Lecture #5 Exercises

Distributed Lab

August 20, 2024



**Exercise 1.** Dmytro and Denis were watching a horse race. Confident in his ability to predict the outcome, Dmytro decided to commit to his prediction. However, in his haste, he forgot to use a blinding factor. Now, Dmytro is concerned that Denis might discover his prediction before the race ends, which would defeat the purpose of his commitment.

We define a dummy hash function  $H(a) = (a \cdot 13 + 17) \pmod{41}$ . Dmytro used a *hash-based commitment* and  $H$  as a hash function. Set of race horse numbers is  $(3, 5, 8, 15)$ . Help Denis to find out the horse number Dmytro have made a commitment to, if commitment equals  $C = 39$ .

- (A) 3.
- (B) 5.
- (C) 8.
- (D) 15.

**Exercise 2.** Denis made a setup (points  $G$  and  $U$ ) for a Pedersen commitment scheme and committed values  $(m, r) = (3, 7)$  to Dmytro by sending him  $\mathcal{C} = [3]G + [7]U$ . Dmytro did not verify the setup. Turns out that Denis knows that  $U = [6]G$ . Denis is planning to send a different message from the one he originally committed to to  $m_2 = 15$ . Which values  $(m_2, r_2)$  should he send to Dmytro at the opening stage?

- (A)  $(15, 5)$
- (B)  $(15, 7)$
- (C)  $(15, 4)$
- (D)  $(3, 5)$

**Exercise 3.** We define a dummy hash function  $H(a, b) = (a \cdot 3 + b \cdot 7) \pmod{41}$ . You have a Merkle tree built with depth 4 using hash function  $H$  with root equal 37. Position defines how leaves should be hashed:

- if left, then  $h_i \leftarrow H(h_{i-1}, \text{branch}[i])$
- if right, then  $h_i \leftarrow H(\text{branch}[i], h_{i-1})$

Which inclusion proof is valid for element 3?

- (A) branch: [4, 16, 13], position: [left, right, left]
- (B) branch: [1, 40, 3], position: [left, left, left]
- (C) branch: [5, 12, 13], position: [right, right, left]
- (D) branch: [4, 17, 13], position: [left, right, left]

**Exercise 4.** Given a polynomial  $p(x) = x^3 - 10x^2 + 31x - 30$ , Oleksandr wants to prove that  $p(2) = 0$ . To do that, according to the KZG commitment scheme, he constructs the quotient polynomial  $q(x)$  and wants to show that  $q(\tau) \cdot (\tau - 2) = p(\tau)$ . Assuming Oleksandr has conducted these steps correctly, what value of  $q(x)$  has Oleksandr calculated?

- (A)  $q(x) = 2x^2 + 4x - 6$
- (B)  $q(x) = x^3 - 10x^2 + 30x - 28$
- (C)  $q(x) = x^2 - 8x + 15$
- (D)  $q(x) = x^2 + 5x + 18$