

## Multi-label Learning:

## Background:

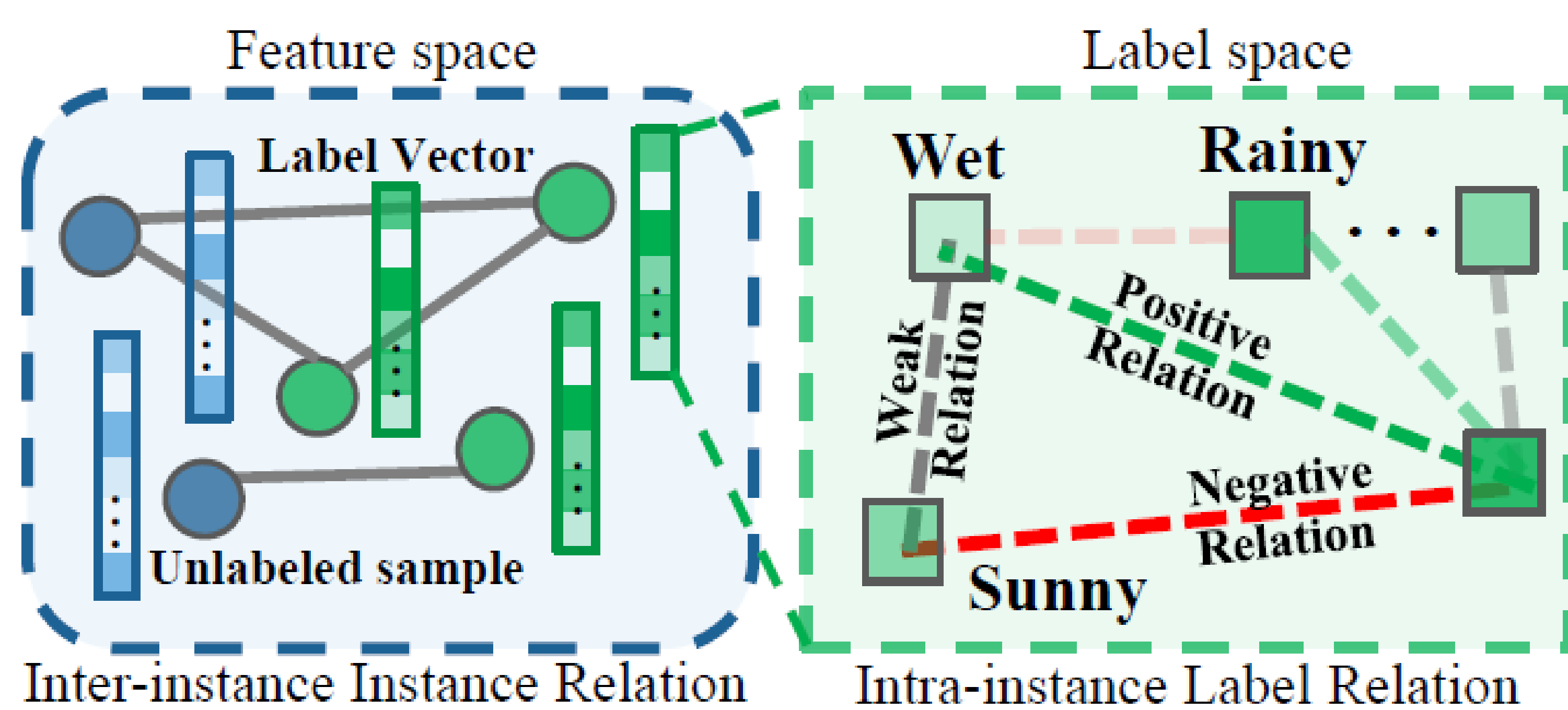
One object can be described by tens or hundreds of descriptions (e.g., color, shape, texture and category). It is critical and practical to predict all the labels from a single instance.

- Input: an instance
- Output: multiple predicted labels



## Challenges:

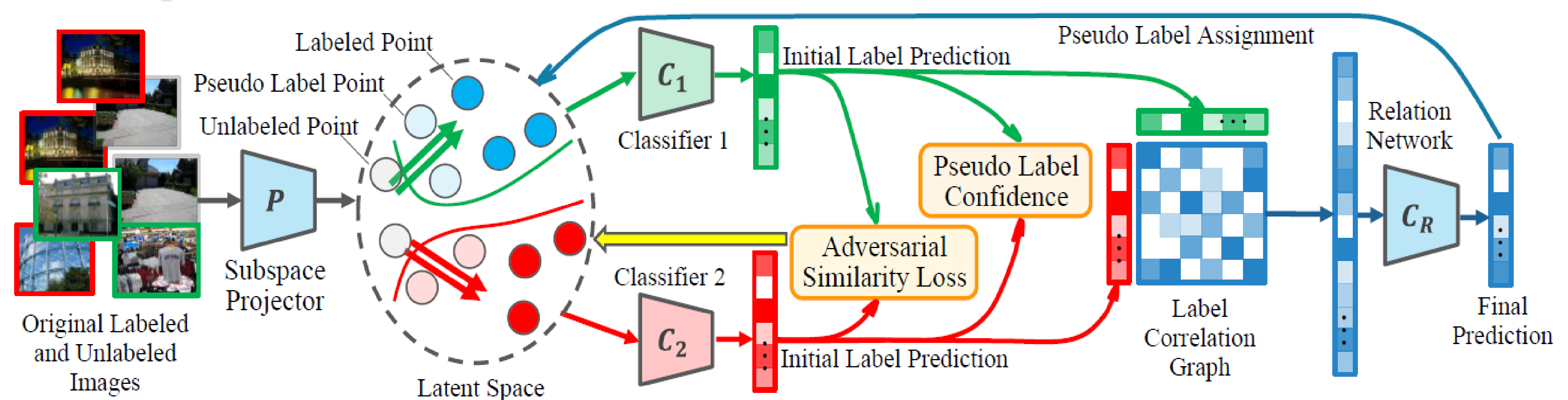
- Long-tail label distribution. The labels followed a long-tail distribution characteristic, which means some labels (e.g., *man-made*) are always show up while some labels are rarely be assigned (e.g., *fire*) .
- Distribution gaps between training and testing sets. The training sets cannot cover the entire feature space of testing.
- Label correlation is crucial for high accurate label prediction, while this knowledge is difficult, expensive, and challenging to obtain.



## Insights:

- Semi-supervised multi-label learning for multi-label prediction. Unlabeled samples are explored associated with labeled samples.
- The label-level correlation of each instance is important. Meanwhile, the label correlations residing inside both labeled and unlabeled samples could also provide crucial information. To this end, we want to explore the label correlations in unlabeled samples.

## Proposed Method:



- Two classifiers structure is deployed to align the distribution differences between labeled and unlabeled samples.

$$L_C(X_l, Y_l) = \frac{1}{2} [\|C_1(Z_l) - Y_l\|_F^2 + \|C_2(Z_l) - Y_l\|_F^2]$$

$$\min_{C_1, C_2} -L_{DA}(X_u) + \lambda L_C(X_l, Y_l) \quad , \quad L_{DA}(X_u) = d(C_1(Z_u), C_2(Z_u))$$

$$d(f_1, f_2) = \frac{1}{d_l} \sum_{k=1}^{d_l} |f_{1k} - f_{2k}|$$

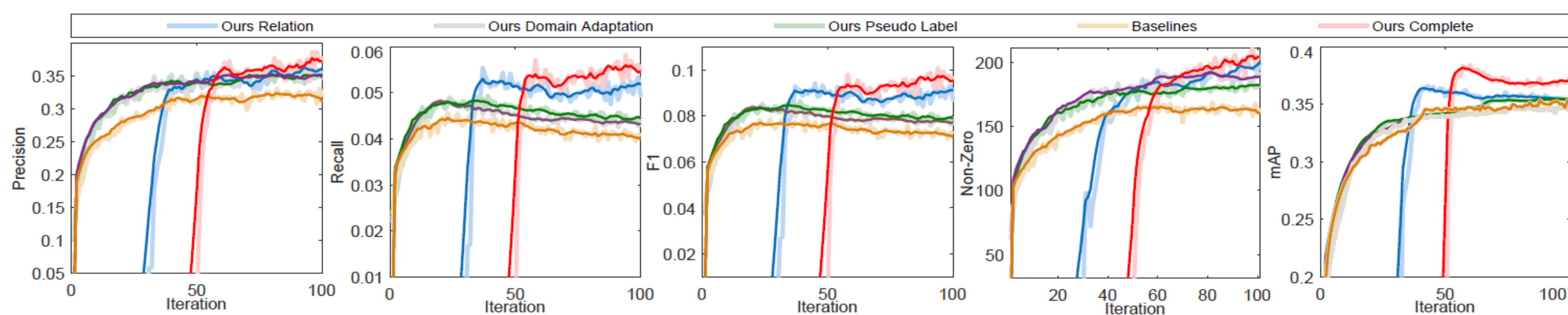
- Pseudo label is gradually assigned to unlabeled samples
- Label correlations are explored by relation networks

$$L_R = \sum_{i=1}^n \|y_i - C_R(C_1(P(x_i)) \cdot C_2(P(x_i))^\top)\|_2^2 \quad \min_{P, C_1, C_2, C_R} \frac{\alpha}{2} L_C + (1 - \alpha) L_R$$

## Experiments:

- Six datasets are used: MAD, Keck and Weizmann datasets.
- One is set as dictionary and another one is set as target dataset.

Data	Method	Pre	Rec	F1	N-R	MAP							Data	Method	Pre	Rec	F1	N-R	MAP
Corel	LR	0.2859	0.3211	0.3025	128	0.3630	SUN	LR	0.6209	0.1473	0.2457	102	0.6807	LR	0.7047	0.1548	0.2539	97	0.6616
	SSMLDR	0.2741	0.3366	0.3022	143	0.3410		SSMLDR	0.6879	0.1700	0.2726	102	0.6723	SSMLDR	0.6637	0.1481	0.2422	95	0.6581
	FastTag	0.3123	0.3657	0.3369	143	0.3871		FastTag	0.6816	0.1473	0.2457	102	0.6914	FastTag	0.6906	0.1522	0.2494	90	0.6706
	ML-PGD	0.2575	0.2911	0.2732	122	0.3727		ML-PGD	0.7110	0.1614	0.2631	101	<b>0.7087</b>	ML-PGD	0.6937	0.1471	0.2433	95	0.6829
	SAE	0.2962	0.3442	0.3184	141	0.3823		SAE	0.7183	0.1638	0.2668	98	0.7012	SAE	0.6978	0.1710	0.2747	100	0.6513
	AG2E	0.3011	0.3520	0.3245	157	0.3568		AG2E	0.7685	0.1765	0.2871	99	0.6778	AG2E	0.7125	0.1618	0.2637	88	0.6693
	Ours	<b>0.3154</b>	<b>0.3775</b>	<b>0.3437</b>	<b>148</b>	<b>0.3727</b>		Ours	<b>0.7966</b>	<b>0.1793</b>	<b>0.2923</b>	<b>102</b>	<b>0.6800</b>	Ours	<b>0.7512</b>	<b>0.1691</b>	<b>0.2866</b>	<b>93</b>	<b>0.6929</b>
	LR	0.3793	0.2038	0.2653	215	0.3440		LR	0.2010	0.0239	0.0428	157	0.0638	LR	0.2600	0.0307	0.0549	160	0.2693
ESP	SSMLDR	0.3294	0.1879	0.2267	226	0.3159	CUB	SSMLDR	0.3440	0.0473	0.0832	178	0.2329	SSMLDR	0.2926	0.0383	0.0677	166	0.2329
	FastTag	0.4011	0.1927	0.2617	208	0.3904		FastTag	0.2147	0.0379	0.0589	167	0.3144	FastTag	0.2231	0.0434	0.0726	143	0.2967
	ML-PGD	0.3239	0.2012	0.2482	210	0.4077		ML-PGD	0.3334	0.0451	0.0794	155	0.3288	ML-PGD	0.2392	0.0365	0.0635	117	0.1786
	SAE	0.3861	0.1743	0.2402	194	0.3842		SAE	0.3383	0.0514	0.0908	196	0.3255	SAE	0.2552	0.0469	0.0798	167	0.3102
	AG2E	0.3548	0.1525	0.2133	213	0.3730		AG2E	0.3409	0.0531	0.0911	190	0.3106	AG2E	0.2808	0.0451	0.0761	163	0.2692
	Ours	<b>0.3743</b>	<b>0.2189</b>	<b>0.2918</b>	<b>227</b>	<b>0.4105</b>		Ours	<b>0.3714</b>	<b>0.0548</b>	<b>0.0955</b>	<b>202</b>	<b>0.3542</b>	Ours	<b>0.2981</b>	<b>0.0486</b>	<b>0.0835</b>	<b>153</b>	<b>0.3308</b>
	LR	0.4287	0.2041	0.2765	199	0.4211		LR	0.8798	0.0821	0.1500	75	0.8626	LR	0.7555	0.0766	0.1392	66	0.8809
	IAP	SSMLDR	0.3491	0.2520	0.2927	229		0.3981	AWA	SSMLDR	0.7812	0.0858	0.1546	67	0.8346	SSMLDR	0.7017	0.0764	0.1378
FastTag		0.3446	0.2267	0.2908	227	0.3906	FastTag	0.7861		0.0827	0.1694	72	0.8791	FastTag	0.8610	0.0912	0.1649	81	0.8918
ML-PGD		0.3433	0.2282	0.3011	233	0.4067	ML-PGD	0.5319		0.0635	0.1393	68	0.8121	ML-PGD	0.4338	0.0623	0.1091	49	0.8677
SAE		0.5537	0.2260	0.2774	213	0.4379	SAE	<b>0.9683</b>		<b>0.0957</b>	<b>0.1742</b>	73	0.9397	SAE	0.9015	<b>0.0926</b>	<b>0.1679</b>	78	0.8918
AG2E		0.3829	0.2330	0.2897	229	0.4353	AG2E	0.8483		0.0827	0.1507	73	0.9033	AG2E	0.8347	0.0841	0.1476	71	0.8874
Ours		<b>0.4570</b>	<b>0.2531</b>	<b>0.3258</b>	<b>230</b>	<b>0.5148</b>	Ours	0.8689		0.0835	0.1523	75	<b>0.9441</b>	Ours	<b>0.9023</b>	0.0837	<b>0.1524</b>	<b>81</b>	<b>0.8985</b>



## Conclusion:

We proposed a novel Dual Relation Semi-supervised Multi-label Learning approach. Unlabeled samples are utilized to improve model robustness. The label correlations from both labeled and unlabeled samples are explored.