

Bacterial Dynamics in Curved Spaces

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The interplay between complex environments and active matter suggests a possibility to control and engineer active matter by carefully designing the confinement structures. It is now well established that confinement may influence transport, rheology, pressure, spatial distribution and collective motion of active matter. Curved confining walls, which are ubiquitous in biological systems, show their own, specific rich and intriguing effects on active matter. Here, using a double emulsion system, where the inner and outer droplet sizes can be independently controlled, we experimentally investigate the influence of curved confinement on an active bath of *Escherichia coli* bacteria. In particular, we analyze the fluctuations of the inner droplet using the framework of a stochastic “active noise” model, and show that the strength of active noise is not an intrinsic property of an active bath, but depends on the confinement curvature. **Our numerical simulations revealed the origin of this dependence on confinement.** Our results pose new challenge to active matter theory and suggest new methods to control active matter.

The interactions between active and passive objects are always intriguing. On the one hand, passive objects are often used as a probe to assess the properties, in particular activity, which are sometimes challenging to measure directly. On the other hand, the capabilities of activity to enhance mixing of fluids and transport of nutrients show great ecological significance and can potentially enable important biomedical applications [1–4].

On the most elementary level, the interaction between an active particle and a passive particle can be described as “scattering”. In this process, the active particle swims by the passive particle results in a closed-loop trajectory, due to the hydrodynamic head-rear symmetry of the model swimmer [5]. In the presence of a confining wall, the flow field generated by an active swimmer is modified, as if there is a mirror image of the swimmer, with force singularities pointing in opposite directions [6]. The head-rear symmetry is broken in the modified flow field, leading to net displacement of passive object in a single scattering event. Based on this picture, Mino et al. successfully modeled the confinement effect on the diffusivity of passive particles in active bath [7, 8]. Lagarde et al. focused their experiment more on the single scattering event, and found far field hydrodynamic interactions to be irrelevant compared to direct collisions [9]. The experiments mentioned above all revealed an important aspect of active baths: the effect on passive tracer diffusivity is stochastic and additive. This discovery has led to efforts to model active baths as a stochastic noise [10–13].

Confinement is known to have dramatic impact on active matter, with examples of pattern formation, directed flow and unusual mechanical properties [14–16].

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