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Interactive Point Set Joint Registration and Co-segmentation for Indoor Scenes

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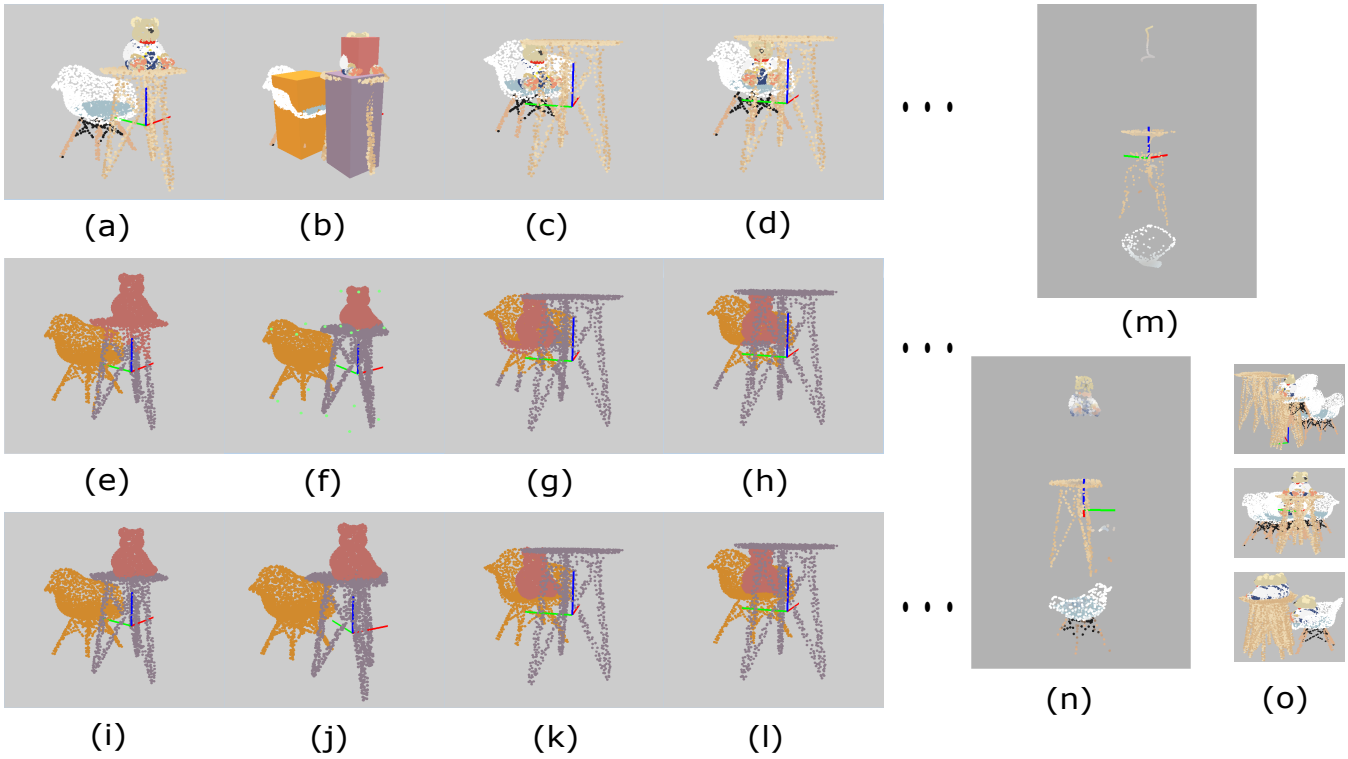

Figure 1: *(a)(b)(c)(d) are input point sets and user have initialized layout for (b) by interactively placing boxes in it. (m) shows the centroids of latent model. (e)(f)(g)(h) are segmentation result based on the instant parameters of latent model. (i)(j)(k)(l) are final segmentation result. (n) shows the final centroids of latent model. (o) verifys the accuracy of final transformation by aligning input sets to each object.*

Abstract

This paper presents a method of joint registration and co-segmentation for point sets of indoor scenes. We view the joint registration and co-segmentation as two problems heavily entangled with each other. To model such entangled problems, we treat the input point sets as samples from a latent generated model and bring up with a novel formulation based on Gaussian mixture model. By maximizing the posterior probability of the samples, we gradually recover the latent object model and object level segmentation and align the objects to the latent model(solve the registration). Alone with the formulation, we design a procedure of interaction that can help users to intuitively initialize the optimization. Our evaluation shows that our novel method is helpful and effective to do the joint registration and co-segmentation on point sets of indoor scenes.

Categories and Subject Descriptors (according to ACM CCS): I.3.8 [COMPUTER GRAPHICS]: Applications—I.4.8 [IMAGE PROCESSING AND COMPUTER VISION]: Scene Analysis—Range data

1. Introduction

In many researches and applications of indoor scenes the data of segmented and even annotated 3D indoor scenes are required as either data base or training data (e.g. [NXS12] [DSS12] [FRS*12] [CLW*14] [FSL*15]).
One way to build such data base is to interactively compose scenes from 3D shape models resulting in scenes with object segmentation and annotation naturally available, or to mannually segment and annotate existing scenes. This procedure can be tedious and time consuming, despite the efforts to improve the interaction experience(e.g. [MSL*11] [XCF*13]).
Another way is to automatically generate scenes from 3D shape models according to the input RGB or RGB-D images(e.g. [LZW*15] [CLW*14]). In such methods, a retrievial procedure is usually needed and inevitablely limit the result to a certain set of 3D models despite the actual 3D model in the input images.
We prefer a approach that helps us build such data set directly from the captured data. One of the major gap between the required data set and available scene capturing framework(e.g. [IKH*11]) is the general object level segmentation. We want to stress that a general object level segmentation problem should not be treated as an equivalence of multilabel classification problem since it is not limited to a certain set of objects. For 3D data, [JGSC15] used some simplified physical prior knowledge (i.e. the block based stability) to help acheiving the general objectness segmentation, while the work of [XHS*15] proposes a practical and rather complete framework to close the gap between the required data set and available scene capturing method. One of the observation in [XHS*15] is that the motion consistency of rigid object can serve as a strong evidence of general objectness. To exploit this fact, they employ a robot to do proactive push and use the movement tracking to verify and iteratively improve their object level segmentation result. Our work presented in this paper is trying to exploit the same observation from a different approach.
We intend to use the motion consistency that is naturally revealed by human activities along the time. Down to this approach, we are facing the choice of scanning scheme. One way is to record the change of the scene along with the human activities, another is to schedule a daily or even a once every half day sweep to only record the result of human activities but avoid the instant of human motion. The main challenge brought in by the second scheme is that we may not be able to solve the object correspondence by a local search due to the sparse sampling over time, but the very same challenge exists in the first scheme due to the exclusion caused by human bodies not to mention other additional process(e.g. tracking with severe oclussion) needed for human bodies. With the second scanning scheme, our original intention of building 3D scene data set from capturing naturally leads us to the problem of coupled joint registration and co-segmentation.
In this problem, registration and segmentaion are entangled in each other. On one hand the segmentation depends on the registration to connect the point clouds into series of rigid movement so that the objectness segmentation can be done based on the motion consistency, on the other hand, the registration depends on the segmentation to break the problem into a series of rigid joint registration instead of a joint registration with non-coherent point drift(A pair of points is close to each other in one point set but their correspondent pair of points in another point set is far from each other, in other words, the point drift of this pair is non-coherent. This happens when this pair of points actually belong to different objects.)
To model the problem, we employ a group of Gaussian mixture models and each of these Gaussian mixture models represents a potential object. This model unentangle the registration and segmentation in the way that the segmentation can be done by evaluate the probability of points belongs to the Gaussian mixture models and the registration can be done by evaluate rigid registration against each gaussain mixture models.
In summary our work makes following contributions:
Firstly, as far as we know we are the first work that bring up with the problem of point set joint registration and co-segmentation for indoor scenes.
Secondly, we come up with a Gaussian mixture model based formulation to simultaneously model both the registration and co-segmentation problem.
Thirdly, targeting the disadvantages of our formulation, we design a procedure of interaction and provide a practical tool for point set joint registration and co-segmentation based on it. We release the tool at `https://github.com/samhu1989/DevBundle`

2. Related Work

In this section we explain how our work is related to the previous works and how we draw experience from these previous works.

2.1. Point Set Registration with GMM Representation

There are a serious of works that uses gaussion mixture model as representation for point set to formulate the registration problem. [MS10] consider the registration of two point sets as a probability density estimation problem. They force the Gaussian mixture model centroids to move coherently as a group to preserve the topological structure of the point sets. Their method is appliable to both rigid registration and non-rigid registration. As we highlighted in section 1, our problem is different from the non-rigid registration considered in [MS10], the point drift could be non-coherent in our probelm. [JV11] summarized the works for point set registration using Gaussian mixture models and present a unified framework for the rigid and nonrigid point set registration problem. These works select one of the point set as the “model”. Unlike these works, [EKBHP14] treats all the point sets as data: they are all realizations of a Gaussian mixture and the registration is cast into a clustering problem. Comparing to these works, our work is most related to [EKBHP14]. Our formulation can be seen as an extention of the formulation of [EKBHP14] to simultaneously handle joint registration and co-segmentation.

2.2. Image segmentation and co-segmentation

[RKB04] is an influential work for interactive image segmentation. It uses two Gaussian mixture model, one for foreground and one for background. To initialize these two Gaussian mixture models, [RKB04] let user place a rectangle that contain the foreground. Our design of interaction draw on the experientce from [RKB04]. The difference is that our interaction is designed for 3D space and

can handle multiple objects segmentation rather than foreground-background segmentation. [TSS16] jointly recover cosegmentation and dense per-pixel correspondence in two images. Our work solve a similar problem for multiple 3D point sets.

2.3. Segmentation from Motion

The idea that motion can be strong hint for segmentation is used in many works. [XHS*15] employs a robot to do proactive push and track the motion to learn object segmentation. [LPR*16] use the motion in video and use the motion edge as training data to learn an edge detector. These methods lean on the motion that is continuous in time and can be tracked. Our method can handle motion that is not continuous in time.

3. Method Overview

3.1. Problem Statement

Given series of point sets which record the same group of rigid indoor objects with different layout. We intend to samutaneously partition the point sets into objects and align the points of same object to recover layouts for corresponding object. Figure 1 shows an example of input point clouds set.

3.2. Basic Formulation

To simutaneously model the joint registration and co-segmentation, we come up with a generative model as follows:

$$P(v_{mi}) = \sum_{k=1}^{K_n} p_k N(v_{mi}|\phi_{mn}(x_k), \Sigma_k) \tag{1}$$

which treat the i-th observed point v_{mi} from the m-th point set as a sample point generated by one of N object models. We can define:

$$\Theta = \{\{p_k, x_k, \Sigma_k\}_{k=1}^{\sum K_n}, \{\phi_{mn}\}_{m=1,n=1}^{MN}\}$$

as the parameter set of the generative model.
p_k is the weight of the k-th Gaussian.
x_k is the center of the k-th Gaussian.
Σ_k is the standard deviation of the k-th Gaussian.
There are $K_{all} = \sum K_n$ Gaussian models in total and among them K_n Gaussian models are treated as a group to represent n-th object.
V is the set of M input point sets.
v_{mi} is the i-th point of the m-th point cloud.
$\{\phi_{mn}\}$ are the functions of rigid transformation that transform the n-th group of gaussian centroids (representing the n-th object) to the space of m-th input point sets.
Each object model is represented by a group of K_n gaussian models.
Our goal of optimization is to maximize the probability of observed input sets sampled from the latent model.This problem can be solved in the framework of expectation-maximization. In particular, we bring in a latent parameter

$$Z = \{z_{mn}|m = 1...M, n = 1...N_m\}$$

such that $z_{mn} = k(k = 1...\sum K_n)$ assigns the observed point v_{mi} to the k-th component of Gaussian mixture model. We aim to maximize the expected complete-data log-likelihood:

$$f(\Theta|V,Z) = \mathbb{E}_Z[\ln P(V,Z;\Theta)|V] \tag{2}$$

The object can be written as:

$$\Theta = \arg\max \sum_Z P(Z|V,\Theta) \ln P(V,Z;\Theta) \tag{3}$$

Such formulation can be seen as an adaption of joint registration formulation in [EKBHP14], upon which we seperate Gaussian models into groups to express multiple objects and the latent parameter Z that assign observed points to gaussian models can naturally indicate the object level segmentation.
By the asssumption of independent and identically distributed of input points, we can write the objective to:

$$\Theta = \arg\max \sum_{mik} \alpha_{mik}(\ln p_k + \ln P(v_{mi}|z_{mi} = k;\Theta)) \tag{4}$$

where $\alpha_{mik} = P(z_{mi} = k|v_{mi};\Theta)$
By bringing in equation 1 and ingnoring constant terms, we can rewrite the objective as:

$$\Theta = \arg\max \sum_{mik} \alpha_{mik}(||v_{mi} - \phi_{mn}(x_k)||^2_{\Sigma_k} + \ln|\Sigma_k| - 2\ln p_k) \tag{5}$$

where the $|\cdot|$ denotes the determinant and $||x||^2_A = x^T A^{-1} x$. It is predefined that x_k is one of the gaussian centroid used to represent n-th object, which is why we apply transformation ϕ_{mn} on to the x_k. For the convenience of computation, we restrict the model to isotropic covariances, i.e.,$\Sigma_k = \sigma^2 I$ and I is the identity matrix.
Now, we can optimize this through iterating between estimating α_{mik} (Expectation-step) and maximizing $f(\Theta|V,Z)$ sequentially with respect to each parameters in Θ (Maximization-steps). These steps are:
E-step: this step estimates the posterior probability α_{mik} of v_{mi} to be a point generated by the k-th Gaussian model.

$$\alpha_{mik} = \frac{p_k \sigma_k^{-3} exp(-\frac{1}{2\sigma_k^2}||v_{mi} - \phi_{mn}(x_k)||^2)}{\sum_s^{K_{all}} p_s \sigma_s^{-3} exp(-\frac{1}{2\sigma_s^2}||v_{mi} - \phi_{mn}(x_s)||^2)} \tag{6}$$

M-step-a:this step update the transformations ϕ_{mn} that maximize $f(\Theta)$, given instant values for α_{mik}, x_k, σ_k. We only consider rigid transformations, making $\phi_{mn}(x) = R_{mn}x + t_{mn}$. The maximizer R^*_{mn}, t^*_{mn} of $f(\Theta)$ is the same with the minimizers of the following constrained optimization problems:

$$\begin{cases} \min_{R_{mn},t_{mn}} & ||(W_{mn} - R_{mn}X_n - t_{mn}\mathbf{e}^T)\Lambda_{mn}||^2_F \\ s.t. & R^T_{mn}R_{mn} = I, |R_{mn}| = 1 \end{cases} \tag{7}$$

where Λ_{mn} is $K_n \times K_n$ diagonal matrix with elements $\lambda_{mnk} = \frac{1}{\sigma_k}\sqrt{\sum_i^{I_m} \alpha_{mik}}$,$I_m$ is the number of point for the m-th input point set, $X_n = [x_1, x_2, ..., x_{K_n}]$ is the matrix stacked by the centroids of gaussian models that are predefined to represent the n-th object. $\mathbf{e}^T$ is a vector of ones, $||\cdot||_F$ denotes the Frobenius norm, and $W_{mn} = [w_{m1}, w_{m2}, ..., w_{mk}, ..., w_{mK_n}]$, in which w_{mk} is a weighted point as:

$$w_{mk} = \frac{\sum_{i=1}^{I_m} \alpha_{mik} v_{mi}}{\sum_{i=1}^{I_m} \alpha_{mik}} \tag{8}$$

This problem have a similar solution of in [EKBHP14]. The only difference is that we are estimating the transformation from latent models to the input point sets, since there are multiple group of x_k corresponding to multiple objects in our latent model. The optimal can be given by:

$$R^*_{mn} = U_{mn} C_{mn} V^T_{mn} \tag{9}$$

$$t^*_{mn} = \frac{1}{tr(\Lambda^2_{mn})} (W_{mn} - R_{mn} X_n) \Lambda^2_{mn} \mathbf{e} \tag{10}$$

where $[U_{mn}, S, V_{mn}] = svd(W_{mn} \Lambda_{mn} P_{mn} \Lambda_{mn} X^T_{mn})$ and $P_{mn} = I - \frac{\Lambda_{mn}\mathbf{e}(\Lambda_{mn}\mathbf{e})^T}{(\Lambda_{mn}\mathbf{e})^T \Lambda_{mn}\mathbf{e}}$,$I$ is identity matrix. $C_{mn} = diag(1, 1, |U_{mn}||V_{mn}|)$.

M-step-b: this step we update the parameters related to the Gaussian mixture model.

$$x^*_k = \frac{\sum_{m=1}^{M} \sum_{i=1}^{I_m} \alpha_{mik} (R^{-1}_{mn} v_{mi} - t_{mn})}{\sum_{m=1}^{M} \sum_{i=1}^{I_m} \alpha_{mik}} \tag{11}$$

where x_k is one of the Gaussian centroids that is predefined to represent n-th object.

$$\sigma^{*2}_k = \frac{\sum_{m=1}^{M} \sum_{i=1}^{I_m} \alpha_{mik} ||(v_{mi} - t_{mn} - R^*_{mn} x^*_k)||^2_2}{3 \sum_{m=1}^{M} \sum_{i=1}^{I_m} \alpha_{mik}} \tag{12}$$

$$p^*_k = \frac{\sum_{m,i} \alpha_{mik}}{M} \tag{13}$$

3.3. Bilateral Formulation

When considering features, we can add bilateral terms into the generative model.

$$P(v_{mi}, f_{mi}) = \sum_{k=1}^{K_n} p_k N(v_{mi} | \phi_{mn}(xv_k), \sigma v_k) N(f_{mi} | xf_k, \sigma v_f) \tag{14}$$

we measure the feature difference by a gaussian with diagnal Σ.

3.4. Interaction Design

Unfortunately, there are serveral parameters that can not be easily initialized in our formulation . In this subsection we first introduce our design of interaction, which is intuitive for users to input the semantic prior this way. We then explain how we can easily initlialize those parameters for our optimization based on the manual input.

As demonstrated in Figure 2, we let user choose one of the point sets and placing and editing boxes in it to indicate the layout for this point set. From this, we can easily initialize the total number of objects N and determine $\{K_n\}$ which is the numbers of Gaussian mixture models used to represent each object. These two paremeters are difficult to be initialized without semantic prior, but with the input of the users we can naturally initialize the N as the number of different color label and the K_n as

$$K_n = \frac{V_n}{\sum V_n} K_{all} \tag{15}$$

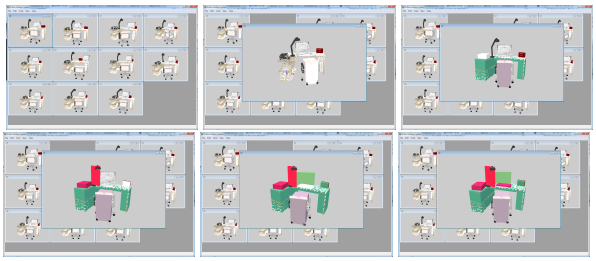

Figure 2: *From the first to the nineth, the nine images show the procedure of interaction: the user pick one point set and place boxes in it to indicate the layout for this point set. The box in white is the box currently under editing. The boxes in other colors are boxes placed to represent object layouts. One color represent one object. The interaction allows multiple boxes to represent same object.(e.g. the desk is represented by three boxes in same color)*

in which the V_n represent the total volume of the boxes in the n-th color and the K_{all} is initialized as $K_{all} = 0.5 * median(I_m)$ and $\{I_m\}$ are point numbers of M input point set. This is an emperical choice borrowed from [EKBHP14].

The expectation maximizaton framework is easily converge to a local optimal. To cope with this problem we further use this interaction as a soft constraint to guide the optimization. Such constraint is done by

4. Algorithms and Implementation Details

4.1. Expectation Conditional Maximization

Assuming the observed point clouds $\{V_m\}$ are independent and identically distributed, we can then write the (2) as:

$$\varepsilon(\Theta | V, Z) = \sum_{m,i,k} \alpha_{mik} (\log p_k + \log P(\phi_{nm}(v_{mi}) | z_{ji} = k; \Theta)) \tag{16}$$

In which the $\alpha_{mik} = P(z_{mi} = k | v_{mi}; \Theta)$,

Algorithm 1 Joint Registration and Co-segmentation (JRCS)

Input:
$\{V_m\}$:Observed point clouds
$\{\alpha^0_{mik}\}$:Initial posterior probabilities
Output:
Θ^q:Final parameter set

1. $q \leftarrow 0$
2. **repeat**
3. CM-step-a: Use α^q_{mik}, x^{q-1}_k to estimate $\{R^q_{mn}\}$ and $\{t^q_{mn}\}$
4. CM-step-b: Use α^q_{mik}, $\{R^q_{mn}\}$ and $\{t^q_{mn}\}$ to estimate the Gaussian centers x^q_k
5. CM-step-c: Use α^q_{mik}, $\{R^q_{mn}\}$ and $\{t^q_{mn}\}$ to estimate the covariances Σ^q_k
6. CM-step-d: Use α^q_{mik} to estimate the priors p^q_k
7. E-step: Use Θ^{q-1} to estimate posterior probabilities. $\alpha^q_{mik} = P(z_{mi} | v_{mi}; \Theta^{q-1})$
8. $q \leftarrow q + 1$
9. **until** Convergence
10. **return** Θ^q

4.2. Initialization Techniques

A key advantage motivates our formulation is that the soft correspondence can be initialized more flexiblely comparing to the typical initialization techniques such as landmark point pairs in registration.
The result of Clustering:

$$P(B_{mj} \in C_n)$$

Soft Correspondence Initialization
Then the α is initialized as:

$$\alpha_{ijk} = P(B_{mj} \in C_n)$$

on the condition that:

$$v_{ij} \in B_{mj} \wedge x_k \in O_n$$

5. Experiment and Discussion

5.1. Evaluation for Segmentation

5.2. Evaluation for Registration

5.3. Stress Tests on Noisy Data

5.4. User Study for Interaction

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