

### Exercise (12 points)

Clear all previous variables from the workspace by entering `clear` in the command window.

- (1) Run the script `init_point_mass_EOM.m` to initialize the model, and open the file `point_mass_EOM.slx`. (0 points)
- (2) The aircraft aerodynamics are implemented in `point_mass_EOM/aerodynamics`. Extract the equations for the lift and drag coefficients  $C_L$  and  $C_D$  as well as the expressions for lift and drag  $L$  and  $D$ . Write them down as functions of  $\alpha, V, \rho, S_{ref}$  and the constant terms. (4 points)

$$C_L = C_{L\alpha} \cdot \alpha + C_{L0}$$

$$C_D = K \cdot (C_L)^2 + C_{D0}$$

$$L = S_{ref} \cdot \frac{\rho}{2} \cdot V^2 \cdot C_L$$

$$D = S_{ref} \cdot \frac{\rho}{2} \cdot V^2 \cdot C_D$$

- (3) The propulsion system is modelled in `point_mass_EOM/propulsion`. Extract the equations for the thrust  $T$ , as well as for the propulsion components in x and z direction  $X_p$  and  $Z_p$ . Write them down as functions of  $\delta_T$  and constants (3 points)

$$T = T_0 + \delta_T \cdot T_{dT}$$

$$X_p = T \cdot \cos \alpha_T$$

$$Z_p = T \cdot \sin \alpha_T$$

- (4) Extract the equation for the change in velocity  $\dot{V}$  from the subsystem `point_mass_EOM/V_dot` and write it down as function of  $X_p, D, \gamma$  and constant terms. (1 point)

$$\dot{V} = \frac{X_p - D}{m} - g \cdot \sin \gamma$$

- (5) Extract the equation for the change in course  $\dot{\chi}$  from the subsystem `point_mass_EOM/chi_dot` and write it down as function of  $L, Z_p, \mu, V, \gamma$  and constant terms. (1 point)

$$\dot{\chi} = \frac{(L - Z_p) \cdot \sin \mu}{m \cdot V \cdot \cos \gamma}$$

- (6) Extract the equation for the change in climb angle  $\dot{\gamma}$  from the subsystem point mass EOM/gamma dot and write it down as function of  $L, Z_p, \mu, V, \gamma$  and constant terms. (1 point)

$$\dot{\gamma} = \frac{(L - Z_p) \cdot \cos \mu}{m \cdot V} - \frac{g \cdot \cos \gamma}{V}$$

- (7) Extract the equation for the change in altitude  $\dot{h}$  from the subsystem point mass EOM/h dot and write it down as function of  $V$  and  $\gamma$ . (1 point)

$$\dot{h} = V \cdot \sin \gamma$$

- (8) Describe in your own words, what happens in the subsystem point mass EOM/Integration? (1 point)

To do a integration process, from inputs  $h; \dot{\gamma}; \dot{X}; \dot{V}$  to outputs  $h; \gamma; X; V$ , which ~~are~~ go backwards and feedback the subsystem "aerodynamics".