### SGN-12006 Introduction to Image and Video Processing

#### **EXERCISE 6**

#### 16.11.2015 - 17.11.2015

## 1) Signal Creation

Create the following 128 x 128 gray-scale images:

- (a) Constant value 0.5 for whole image;
- (b) 20x20 white square in the middle;
- (c) Ramp from 0 to 1 in horizontal axis, constant in vertical axis.
- (d) Delta function at the center of the image;
- (e) Cosine signal having four periods in both directions; (help meshgrid)

All the images should be created using the full range 0 to 1, and without using any for or while loops.

### 2) DFT

- a) Perform the 2D Fourier transform on all the images in task 1. (help fftshift, fft2, log). Have a look at Ex6\_DFT.pdf for instruction of DFT in matlab.
- b) Explain what information you get from Fourier transform of an image.
- c) Consider DFT images from task 1, where is the energy concentrated and why?

# 2) Filtering in the Frequency Domain

Butterworth filters can be defined as:

(a) Butterworth low-pass filter: 
$$H(u,v) = \frac{1}{1 + \left(\frac{(D(u,v)}{D_0}\right)^{2n}}$$

(b) Butterworth high-pass filter: 
$$H(u, v) = 1 - \frac{1}{1 + \left(\frac{(D(u, v))}{D_0}\right)^{2n}}$$

where  $D_0$  is the so-called cut-off frequency distance.

$$D(u,v) = \sqrt{\left(u - M/2\right)^2 + \left(v - N/2\right)^2}$$
 with  $M \times N$  is the size of the image.

Use the given Butterworth low-pass filter (BWLPfilter.m) Choose  $D_0 = 2$ , n = 2 order and filter the image cameraman.tif with both (a) and (b) filters. Show images of the filters and the final filtered images.