

Time complexity analysis

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% Initial state
init_state(a). O(1)

% States O(1)
state(a).
state(b).
state(c).
state(d).
state(e).
state(f).
state(g).
state(h).
state(i).
state(j).
state(k).

% Accepting states O(1)
accept(b).
accept(c).
accept(d).
accept(e).
accept(g).
accept(h).
accept(j).

% Move O(1)
move(a, b, 0).
move(a, b, 2).
move(a, c, 1).

move(b, b, 0).
move(b, b, 2).
move(b, c, 1).

move(c, d, 0).
move(c, g, 1).
move(c, b, 2).
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move(d, e, 1).
move(d, b, 0).
move(d, b, 2).

move(e, f, 1).
move(e, f, 2).
move(e, d, 0).

move(g, h, 0).
move(g, g, 1).
move(g, j, 2).

move(h, i, 1).
move(h, b, 0).
move(h, b, 2).

move(j, k, 2).
move(j, b, 0).
move(j, c, 1).

% Function to go through the list and get the final state
go_through_Digits([], State, State). O(1)

% Recursive function
O(n), where n is the length of the list.
go_through_Digits([Digit|RestofDigits], State1, State2) :-
    (move(State1, NextState, Digit) -> O(1)
     NextState = NextState;
     NextState = State1),
    go_through_Digits(RestofDigits, NextState, State2).

% Verify if the list of digits leads to an accepting state
O(n), where n is the length of the list.
verify_number(Digits) :-
    init_state(StartState), O(1)
    go_through_Digits(Digits, StartState, FinalState), O(n), previous
    (accept(FinalState) -> O(1)
     writeln('yes');
     writeln('no'))

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% Change number to a list of digits
 $O(n) + O(n) \rightarrow O(2n) \rightarrow O(n)$ 
digit_list(N, L) :-
    atom_chars(N, Chars), %  $O(n)$  Convert the atom to a list of characters
    maplist(atom_number, Chars, L). %  $O(n)$  Convert each character to its
    numeric representation

 $O(2n) + O(n) \rightarrow O(3n) \rightarrow O(n)$ 
check(Number) :-
    digit_list(Number, Digits),  $O(2n)$ , previous
    verify_number(Digits).  $O(n)$ , previous

Overall the time complexity is  $O(n)$ 

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