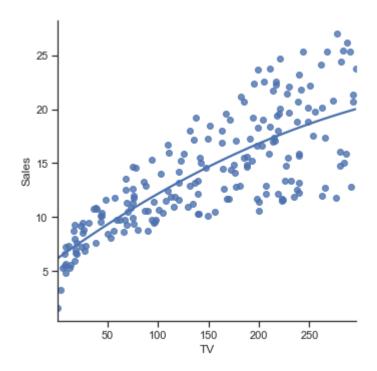
Московский государственный технический университет им. Н.Э. Баумана Кафедра «Системы обработки информации и управления»

Лабораторная работа №5 по дисциплине «Методы машинного обучения» на тему «Линейные модели, SVM и деревья решений.»

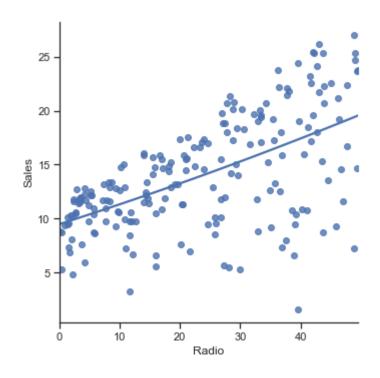
Выполнил: студент группы ИУ5-24М Зубаиров В. А.

```
[140]: import numpy as np
      import pandas as pd
      import seaborn as sns
      import matplotlib.pyplot as plt
      from sklearn import preprocessing, svm
      from sklearn import model selection
      from sklearn.model selection import train test split
      from sklearn.linear model import BayesianRidge
      from sklearn.tree import DecisionTreeClassifier, DecisionTreeRegressor, export graphviz
      from sklearn.metrics import r2 score
      %matplotlib inline
      sns.set(style="ticks")
      import warnings
      warnings.filterwarnings('ignore')
  [5]: data = pd.read csv("advertising.csv")
  [6]: data.head(2)
  [6]:
         TV Radio Newspaper Sales
      1 230.1 37.8
                       69.2 22.1
      2 44.5 39.3
                      45.1 10.4
  [7]: data.describe()
  [7]:
               TV
                     Radio Newspaper
                                          Sales
      count 200.000000 200.000000 200.000000 200.000000
      mean 147.042500 23.264000 30.554000 14.022500
      std
           85.854236 14.846809 21.778621
                                             5.217457
             0.700000 0.000000 0.300000 1.600000
      min
             74.375000 9.975000 12.750000 10.375000
      25%
      50% 149.750000 22.900000 25.750000 12.900000
      75% 218.825000 36.525000 45.100000 17.400000
      max 296.400000 49.600000 114.000000 27.000000
  [8]: data.info()
      <class 'pandas.core.frame.DataFrame'>
      Int64Index: 200 entries, 1 to 200
      Data columns (total 4 columns):
      # Column Non-Null Count Dtype
                _____
      0 TV
                 200 non-null float64
      1 Radio
                 200 non-null float64
      2 Newspaper 200 non-null float64
      3 Sales
                 200 non-null float64
      dtypes: float64(4)
      memory usage: 7.8 KB
```

- [9]: data.columns
- [9]: Index(['TV', 'Radio', 'Newspaper', 'Sales'], dtype='object')
- [12]: sns.lmplot(x="TV", y="Sales", data=data, order=2, ci=None)
- [12]: <seaborn.axisgrid.FacetGrid at 0x133706f10>

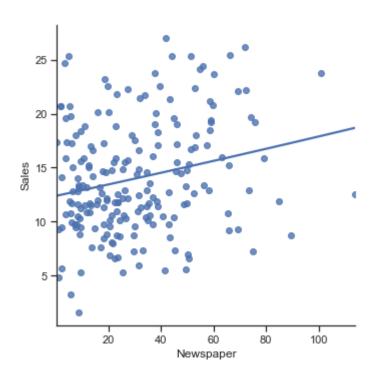


- [15]: sns.lmplot(x="Radio", y="Sales", data=data, order=2, ci=None)
- [15]: <seaborn.axisgrid.FacetGrid at 0x1357f9d90>



```
[16]: sns.lmplot(x="Newspaper", y="Sales", data=data, order=2, ci=None)
```

[16]: <seaborn.axisgrid.FacetGrid at 0x135878550>



[18]: data.corr()

[18]: TV Radio Newspaper Sales
TV 1.000000 0.054809 0.056648 0.782224
Radio 0.054809 1.000000 0.354104 0.576223
Newspaper 0.056648 0.354104 1.000000 0.228299
Sales 0.782224 0.576223 0.228299 1.000000

0.1. Между TV и Sales есть корреляция 0.78

```
[152]: x = data["TV"].values
y = data["Sales"].values
reg = BayesianRidge(fit_intercept=True).fit(x.reshape(-1, 1), y.reshape(-1, 1))
reg.coef_
reg.intercept_
```

[152]: 7.054854152265513

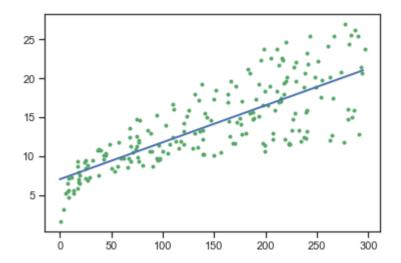
```
[153]: def func(w, b, x): return w*x + b
```

```
[154]: x_t = list(range(0, 300, 5))

y_t = [func(reg.coef_[0], reg.intercept_, x)  for x  in x_t]

y_t = reg.predict(x.reshape(-1, 1))
```

```
[155]: plt.plot(x, y, 'g.')
plt.plot(x_t, y_t, 'b', linewidth=2.0)
plt.show()
```



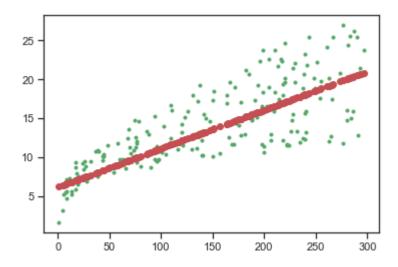
0.1.1. Модель линейной регрессии дала неплохой результат

0.2. SVM

[156]: from sklearn.svm import SVC, NuSVC, LinearSVC, OneClassSVM, SVR, NuSVR, LinearSVR

```
[157]: lin_SVR = LinearSVR(C=1.0, max_iter=10000)
lin_SVR.fit(x.reshape(-1, 1), y)
predict = lin_SVR.predict(x.reshape(-1, 1))
plt.plot(x, y, 'g.')
plt.plot(x, predict, 'ro')
```

[157]: [<matplotlib.lines.Line2D at 0x13e5a9b10>]



0.3. Деревья решений

```
[158]: dec tree = DecisionTreeRegressor(random state=1, max depth=5)
                                  dec tree.fit(data, data["Sales"])
                                  dec tree
[158]: DecisionTreeRegressor(ccp alpha=0.0, criterion='mse', max depth=5,
                                                                                               max features=None, max leaf nodes=None,
                                                                                             min impurity decrease=0.0, min impurity split=None,
                                                                                             min samples leaf=1, min samples split=2,
                                                                                              min weight fraction leaf=0.0, presort='deprecated',
                                                                                             random state=1, splitter='best')
[159]: dec predict = dec tree.predict(data)
[160]: from sklearn import tree
                                  tree.plot tree(dec tree, filled=True)
[160]: [Text(167.4, 199.32, 'X[3] \le 15.1 \rangle = 27.086 \rangle = 200 \rangle = 200 \rangle
                                  14.023'),
                                   = 10.67'),
                                   = 7.767'),
                                   Text(20.925, 90.6, 'X[0] \le 4.75 \times = 2.173 \times = 18 \times = 5.872'),
                                   = 2.4'),
                                   3.2'),
                                   Text(31.38750000000003, 54.35999999999985, 'X[3] <= 6.25\nmse =
                                 0.669 \text{ nsamples} = 16 \text{ nvalue} = 6.306').
                                   Text(36.61875, 18.1199999999999976, 'mse = 0.075\nsamples = 9\nvalue = 6.978'),
                                    Text(62.775000000000006, 90.6, 'X[3] \le 9.0 \text{ nmse} = 0.442 \text{ nsamples} = 27 \text{ nvalue} = 0.442 \text{ nvalue} =
                                 9.03'),
                                   Text(52.3125, 54.35999999999999985, 'X[3] \le 8.25 \times = 0.18 \times = 0.
                                  12 \text{ (nvalue} = 8.375'),
                                   7.825'),
                                   Text(73.2375, 54.3599999999999985, 'X[3] \le 9.55 \times = 0.034 \times = 0.
                                  15 \text{ nvalue} = 9.553'),
                                   9.386').
                                   Text(125.5500000000001, 126.839999999999, 'X[3] <= 12.55\nmse =
                                 2.031 \times = 80 \times = 12.302'
```

```
Text(94.16250000000001, 54.35999999999985, 'X[3] \le 10.55 \times = 10.
0.083 \text{ nsamples} = 19 \text{ nvalue} = 10.558').
    Text(99.39375, 18.1199999999999996, 'mse = 0.023 \nsamples = 10 \nvalue = 10.79'),
     Text(115.0875, 54.35999999999999985, 'X[3] \le 11.85 \times = 0.127 \times =
29\nvalue = 11.814'),
   11.565').
   Text(120.31875000000001, 18.11999999999999976, 'mse = 0.047\nsamples = 12\nvalue
= 12.167'),
    Text(146.475, 90.6, 'X[3] \le 13.8 \times = 0.703 \times = 32 \times = 13.781')
     Text(136.012500000000002, 54.35999999999985, 'X[3] \le 13.05 \text{ nmse} = 13.05 \text{ nmse}
0.091 \times 17 = 17 \times 10^{-1}
   12.789').
   13.338'),
   Text(156.9375, 54.359999999999985, 'X[3] \le 14.45 \text{ nmse} = 0.094 \text{ nsamples} =
  15\nvalue = 14.613'),
   14.175'),
   Text(162.16875000000002, 18.1199999999999976, 'mse = 0.026 \ nsamples = 11 \ nvalue
= 14.773'),
   Text(251.10000000000002, 163.0799999999998, 'X[3] <= 20.45\nmse =
  10.081 \text{ nsamples} = 75 \text{ nvalue} = 19.611'
   47\nvalue = 17.519'),
   = 16.348'),
   Text(177.8625, 54.3599999999999985, 'X[3] \le 15.65 \times = 0.084 \times = 
  14 \text{ nvalue} = 15.657'),
    Text(172.63125, 18.119999999999976, 'mse = 0.023\nsamples = 7\nvalue = 15.4'),
     15.914').
   Text(198.7875, 54.3599999999999985, 'X[3] \le 17.05 \times = 0.095 \times = 0.005 \times = 
  13 \text{ nvalue} = 17.092'),
    Text(193.55625, 18.1199999999999976, 'mse = 0.026\nsamples = 5\nvalue = 16.76'),
    Text(204.01875, 18.11999999999999976, 'mse = 0.025 \setminus nsamples = 8 \setminus nvalue = 17.3'),
     Text(230.175, 90.6, 'X[3] \le 19.1 \times = 0.505 \times = 20 \times = 19.1'
     Text(219.7125, 54.3599999999999985, 'X[3] \le 18.7 \times = 0.162 \times = 0
  10 \text{ nvalue} = 18.5'),
   Text(224.94375, 18.1199999999999976, 'mse = 0.002 \nsamples = 4 \nvalue = 18.95')
   Text(240.63750000000002, 54.35999999999985, 'X[3] <= 19.75\nmse =
0.128 \text{ nsamples} = 10 \text{ nvalue} = 19.7'
   20.075'),
```

 $Text(104.625, 90.6, 'X[3] \le 11.1 \times = 0.487 \times = 48 \times = 11.317')$

Text(272.0250000000003, 90.6, 'X[3] \leq 21.75\nmse = 0.581\nsamples = 16\nvalue = 21.744'),

Text(261.5625, 54.3599999999999985, 'X[3] \leq 21.0\nmse = 0.149\nsamples = 8\nvalue = 21.088'),

Text(256.33125, 18.119999999999976, 'mse = 0.002\nsamples = 4\nvalue = 20.725'),

Text(266.79375, 18.119999999999976, 'mse = 0.032\nsamples = 4\nvalue = 21.45'), Text(282.4875, 54.359999999999985, 'X[3] <= 22.5\nmse = 0.153\nsamples = 8\nvalue = 22.4'),

Text(277.25625, 18.119999999999976, 'mse = 0.042\nsamples = 5\nvalue = 22.16'), Text(287.71875, 18.119999999999976, 'mse = 0.08\nsamples = 3\nvalue = 22.8'),

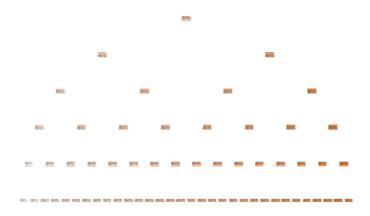
Text(313.875, 90.6, 'X[3] \leq 25.05\nmse = 0.984\nsamples = 12\nvalue = 24.958'),

Text(303.4125, 54.359999999999995, 'X[3] \leq 24.0\nmse = 0.133\nsamples = 6\nvalue = 24.1'),

Text(308.64375, 18.119999999999976, 'mse = 0.042\nsamples = 3\nvalue = 24.433'),

 $Text(324.33750000000003, 54.359999999999985, 'X[3] \le 25.85 \text{ nmse} = 0.361 \text{ nsamples} = 6 \text{ nvalue} = 25.817'),$

Text(319.10625, 18.119999999999976, 'mse = 0.002\nsamples = 4\nvalue = 25.425'),



0.4. Метрики качества

```
[161]: from sklearn.metrics import mean_absolute_error, mean_squared_error, □

→ mean_squared_log_error, median_absolute_error, r2_score

print("Метрики для линейной модели:\n")

print("Средняя абсолютная ошибка: ", mean_absolute_error(y, y_tt))
```

```
ргіпt("Средняя квадратичная ошибка: ", mean_squared_error(y, y_tt))
ргіпt("\n\nMetpuku для SVM-модели:\n")
ргіпt("Средняя абсолютная ошибка: ", mean_absolute_error(y, predict))
ргіпt("Средняя квадратичная ошибка: ", mean_squared_error(y, predict))
ргіпt("Коэффициент детерминации: ", r2_score(y, predict))

ргіпt("\n\nMetpuku для Decision Tree:\n")
ргіпt("Средняя абсолютная ошибка: ", mean_absolute_error(y, dec_predict))
ргіпt("Средняя квадратичная ошибка: ", mean_squared_error(y, dec_predict))
ргіпt("Коэффициент детерминации: ", r2_score(y, dec_predict))
```

Метрики для линейной модели:

Средняя абсолютная ошибка: 2.550919383216356 Средняя квадратичная ошибка: 10.512821002854928 Коэффициент детерминации: 0.6118688451058344

Метрики для SVM-модели:

Средняя абсолютная ошибка: 2.5708683334350892 Средняя квадратичная ошибка: 10.859652690875892 Коэффициент детерминации: 0.5990638916505333

Метрики для Decision Tree:

Средняя абсолютная ошибка: 0.14353164841694266 Средняя квадратичная ошибка: 0.03201810934980053 Коэффициент детерминации: 0.9988178980926156

0.5. Подбор гиперпараметров. Кросс-валидация

```
[164]: scores svm = cross validate(LinearSVR(C=1.0, max iter=10000),
                     x.reshape(-1, 1), y, cv=3, scoring=scoring)
       scores svm
[164]: {'fit time': array([0.03139281, 0.02713585, 0.02338099]),
       'score time': array([0.00076604, 0.00061393, 0.00054908]),
       'test mean': array([-2.54098772, -2.37148251, -3.1291242]),
       'test square': array([-11.0231287, -9.81978964, -15.84997398]),
       'test r2': array([0.60826634, 0.63516403, 0.38395142])}
[165]: scores dec = cross validate(DecisionTreeRegressor(random_state=1, max_depth=3),
                     data, data["Sales"], cv=5, scoring=scoring)
       scores dec
[165]: {'fit time': array([0.00271297, 0.0020709, 0.00206208, 0.00199294,
       0.00195193]),
       'score time': array([0.0018599, 0.00148034, 0.00148678, 0.00142694, 0.0014143
       'test mean': array([-0.72293478, -0.7307461, -0.66116873, -0.85487267,
       -0.91550049]),
       'test square': array([-0.64975012, -0.70991464, -0.63349151, -1.4104023]
       -1.08449788]),
       'test r2': array([0.97486214, 0.97589358, 0.97175881, 0.95176776, 0.95938815])}
[166]: print("Метрики для линейной модели:\n")
       print("Средняя абсолютная ошибка: ", np.mean(scores regr['test mean']))
       print("Средняя квадратичная ошибка: ", np.mean(scores_regr['test_square']))
       print("Коэффициент детерминации: ", np.mean(scores_regr['test_r2']))
       print("\n\nМетрики для SVM-модели:\n")
       print("Средняя абсолютная ошибка: ", np.mean(scores svm['test mean']))
       print("Средняя квадратичная ошибка: ", np.mean(scores_svm['test_square']))
       print("Коэффициент детерминации: ", np.mean(scores svm['test r2']))
       print("\n\nМетрики для Decision Tree:\n")
       print("Средняя абсолютная ошибка: ", np.mean(scores dec['test mean']))
       print("Средняя квадратичная ошибка: ", np.mean(scores dec['test square']))
       print("Коэффициент детерминации: ", np.mean(scores_dec['test_r2']))
```

Метрики для линейной модели:

Средняя абсолютная ошибка: -2.580423621885709 Средняя квадратичная ошибка: -10.693097277894969 Коэффициент детерминации: 0.601747959666948

Метрики для SVM-модели:

Средняя абсолютная ошибка: -2.6805314771806956

Средняя квадратичная ошибка: -12.23096410841425 Коэффициент детерминации: 0.5424605962417798

Метрики для Decision Tree:

Средняя абсолютная ошибка: -0.7770445553321956 Средняя квадратичная ошибка: -0.8976112886827845 Коэффициент детерминации: 0.9667340888852873

0.6. Оптимизация с помощью решетчатого поиска

```
[167]: from sklearn.model selection import GridSearchCV
[168]: n \text{ range} = np.array(range(1,10,1))
       tuned parameters = [{'max depth': n range}]
       tuned parameters
[168]: [{'max depth': array([1, 2, 3, 4, 5, 6, 7, 8, 9])}]
[169]: %%time
       clf gs = GridSearchCV(DecisionTreeRegressor(), tuned parameters, cv=5, scoring='r2')
       clf gs.fit(x.reshape(-1, 1), y)
      CPU times: user 48.9 ms, sys: 1.26 ms, total: 50.2 ms
      Wall time: 49.2 ms
[169]: GridSearchCV(cv=5, error score=nan,
               estimator=DecisionTreeRegressor(ccp_alpha=0.0, criterion='mse',
                                  max depth=None, max features=None,
                                  max_leaf_nodes=None,
                                  min impurity decrease=0.0,
                                  min impurity split=None,
                                  min samples leaf=1,
                                  min_samples_split=2,
                                  min weight fraction leaf=0.0,
                                  presort='deprecated',
                                  random state=None,
                                  splitter='best'),
               iid='deprecated', n jobs=None,
               param grid=[\{\text{max depth'}: array([1, 2, 3, 4, 5, 6, 7, 8, 9])\}],
               pre dispatch='2*n jobs', refit=True, return train score=False,
               scoring='r2', verbose=0)
[170]: # Лучшая модель
       clf gs.best estimator
[170]: DecisionTreeRegressor(ccp alpha=0.0, criterion='mse', max depth=3,
                    max features=None, max leaf nodes=None,
                    min impurity decrease=0.0, min impurity split=None,
```

min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, presort='deprecated', random_state=None, splitter='best')

[171]: clf_gs.best_score_

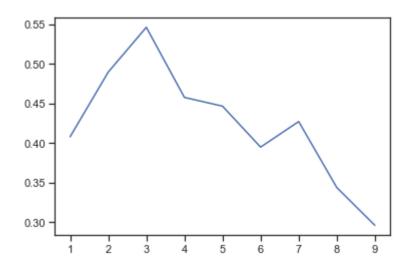
[171]: 0.5464056968965096

[172]: clf_gs.best_params_

[172]: {'max_depth': 3}

[173]: plt.plot(n_range, clf_gs.cv_results_['mean_test_score'])

[173]: [<matplotlib.lines.Line2D at 0x1365b10d0>]



0.6.1. Оптимизация SVM

[174]: param_grid = {'C': [0.1,1, 10, 100], 'epsilon': [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0]}

[175]: grid = GridSearchCV(LinearSVR(),param_grid,refit=True,verbose=2) grid.fit(x.reshape(-1, 1),y)

Fitting 5 folds for each of 40 candidates, totalling 200 fits

[CV] C=0.1, epsilon=0.1 ...

[CV] ... C=0.1, epsilon=0.1, total= 0.0s

[CV] C=0.1, epsilon=0.1 ...

[CV] ... C=0.1, epsilon=0.1, total= 0.0s

[CV] C=0.1, epsilon=0.1 ...

[CV] ... C=0.1, epsilon=0.1, total= 0.0s

[CV] C=0.1, epsilon=0.1 ...

[CV] ... C=0.1, epsilon=0.1, total= 0.0s

[CV] C=0.1, epsilon=0.1 ...

- [CV] ... C=0.1, epsilon=0.1, total= 0.0s
- [CV] C=0.1, epsilon=0.2 ...
- [CV] ... C=0.1, epsilon=0.2, total= 0.0s
- [CV] C=0.1, epsilon=0.2 ...
- [CV] ... C=0.1, epsilon=0.2, total= 0.0s
- [CV] C=0.1, epsilon=0.2 ...
- [CV] ... C=0.1, epsilon=0.2, total= 0.0s
- [CV] C=0.1, epsilon=0.2 ...
- [CV] ... C=0.1, epsilon=0.2, total= 0.0s
- [CV] C=0.1, epsilon=0.2 ...
- [CV] ... C=0.1, epsilon=0.2, total= 0.0s
- [CV] C=0.1, epsilon=0.3 ...
- [CV] ... C=0.1, epsilon=0.3, total= 0.0s
- [CV] C=0.1, epsilon=0.3 ...
- [CV] ... C=0.1, epsilon=0.3, total= 0.0s
- [CV] C=0.1, epsilon=0.3 ...
- [CV] ... C=0.1, epsilon=0.3, total= 0.0s
- [CV] C=0.1, epsilon=0.3 ...
- [CV] ... C=0.1, epsilon=0.3, total= 0.0s
- [CV] C=0.1, epsilon=0.3 ...
- [CV] ... C=0.1, epsilon=0.3, total= 0.0s
- [CV] C=0.1, epsilon=0.4 ...
- [CV] ... C=0.1, epsilon=0.4, total= 0.0s
- [CV] C=0.1, epsilon=0.4 ...
- [CV] ... C=0.1, epsilon=0.4, total= 0.0s
- [CV] C=0.1, epsilon=0.4 ...
- [CV] ... C=0.1, epsilon=0.4, total= 0.0s
- [CV] C=0.1, epsilon=0.4 ...
- [CV] ... C=0.1, epsilon=0.4, total= 0.0s
- [CV] C=0.1, epsilon=0.4 ...
- [CV] ... C=0.1, epsilon=0.4, total= 0.0s
- [CV] C=0.1, epsilon=0.5 ...
- [CV] ... C=0.1, epsilon=0.5, total= 0.0s
- [CV] C=0.1, epsilon=0.5 ...
- [CV] ... C=0.1, epsilon=0.5, total= 0.0s
- [CV] C=0.1, epsilon=0.5 ...
- [CV] ... C=0.1, epsilon=0.5, total= 0.0s
- [CV] C=0.1, epsilon=0.5 ...
- [CV] ... C=0.1, epsilon=0.5, total= 0.0s
- [CV] C=0.1, epsilon=0.5 ...
- [CV] ... C=0.1, epsilon=0.5, total= 0.0s
- [CV] C=0.1, epsilon=0.6 ...
- [CV] ... C=0.1, epsilon=0.6, total= 0.0s
- [CV] C=0.1, epsilon=0.6 ...
- [CV] ... C=0.1, epsilon=0.6, total= 0.0s
- [CV] C=0.1, epsilon=0.6 ...
- [CV] ... C=0.1, epsilon=0.6, total= 0.0s
- [CV] C=0.1, epsilon=0.6 ...
- [CV] ... C=0.1, epsilon=0.6, total= 0.0s
- [CV] C=0.1, epsilon=0.6 ...

```
[CV] ... C=0.1, epsilon=0.6, total= 0.0s
[CV] C=0.1, epsilon=0.7 ...
[CV] ... C=0.1, epsilon=0.7, total= 0.0s
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[CV] C=0.1, epsilon=0.8 ...
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[CV] ... C=1, epsilon=0.1, total= 0.0s
[CV] C=1, epsilon=0.1 ...
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[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers. [Parallel(n_jobs=1)]: Done 1 out of 1 | elapsed: 0.0s remaining: 0.0s

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[CV] ... C=1, epsilon=0.1, total= 0.0s
[CV] C=1, epsilon=0.1 ...
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[C V] C-1, cpsnon-0.1 ...

[CV] ... C=1, epsilon=0.1, total= 0.0s

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[Parallel(n jobs=1)]: Done 200 out of 200 | elapsed: 0.8s finished
```

```
[175]: GridSearchCV(cv=None, error score=nan,
              estimator=LinearSVR(C=1.0, dual=True, epsilon=0.0,
                          fit intercept=True, intercept scaling=1.0,
```

```
loss='epsilon insensitive', max iter=1000,
                           random state=None, tol=0.0001, verbose=0),
               iid='deprecated', n jobs=None,
               param grid={'C': [0.1, 1, 10, 100],
                      'epsilon': [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8,
                             0.9, 1.0]},
               pre dispatch='2*n jobs', refit=True, return train score=False,
               scoring=None, verbose=2)
[176]: grid.best estimator
[176]: LinearSVR(C=10, dual=True, epsilon=1.0, fit intercept=True,
             intercept scaling=1.0, loss='epsilon insensitive', max iter=1000,
             random state=None, tol=0.0001, verbose=0)
[177]: grid.best score
[177]: 0.5440492644611755
[178]: grid.best params
[178]: {'C': 10, 'epsilon': 1.0}
[182]: parameters = {"alpha 1": np.logspace(-13,-5,10),
               "alpha_2": np.logspace(-9,-3,10),
               "lambda 1": np.logspace(-10,-5,10),
               "lambda 2": np.logspace(-11,-4,10)}
       grid regr = GridSearchCV(BayesianRidge(), parameters, cv=3, n jobs=-1)
       grid regr.fit(x.reshape(-1, 1), y)
[182]: GridSearchCV(cv=3, error score=nan,
               estimator=BayesianRidge(alpha 1=1e-06, alpha 2=1e-06,
                             alpha init=None, compute score=False,
                             copy X=True, fit intercept=True,
                             lambda 1=1e-06, lambda 2=1e-06,
                             lambda init=None, n iter=300,
                             normalize=False, tol=0.001,
                             verbose=False),
               iid='deprecated', n jobs=-1,
               param grid={'alpha 1': array([1.00000000e-13, 7.74263683e-13,
       5.99484250e-...
                      'lambda 1': array([1.00000000e-10, 3.59381366e-10,
       1.29154967e-09, 4.64158883e-09,
           1.66810054e-08, 5.99484250e-08, 2.15443469e-07, 7.74263683e-07,
           2.78255940e-06, 1.00000000e-05]),
                      'lambda 2': array([1.00000000e-11, 5.99484250e-11,
       3.59381366e-10, 2.15443469e-09,
           1.29154967e-08, 7.74263683e-08, 4.64158883e-07, 2.78255940e-06,
           1.66810054e-05, 1.00000000e-04)},
               pre dispatch='2*n jobs', refit=True, return train score=False,
               scoring=None, verbose=0)
```

```
[186]: grid regr.best estimator
[186]: BayesianRidge(alpha 1=1e-05, alpha 2=1e-09, alpha init=None,
               compute score=False, copy X=True, fit intercept=True,
               lambda 1=1e-10, lambda 2=0.0001, lambda init=None, n iter=300,
               normalize=False, tol=0.001, verbose=False)
[187]: grid regr.best score
[187]: 0.6017531508217578
[188]: grid regr.best params
[188]: {'alpha 1': 1e-05, 'alpha 2': 1e-09, 'lambda 1': 1e-10, 'lambda 2': 0.0001}
[189]: reg = BayesianRidge(fit intercept=True, alpha 1=1e-05, alpha 2=1e-09, lambda 1=1e-10, \square
        \rightarrowlambda 2=0.0001).fit(x.reshape(-1, 1), y.reshape(-1, 1))
       y tt = reg.predict(x.reshape(-1, 1))
       \lim SVR = LinearSVR(C=1.0, max iter=10000, epsilon=1.0)
       lin SVR.fit(x.reshape(-1, 1), y)
       predict = lin SVR.predict(x.reshape(-1, 1))
       dec tree = DecisionTreeRegressor(random state=1, max depth=3)
       dec tree.fit(data, data["Sales"])
       dec predict = dec tree.predict(data)
[190]: print("Метрики для линейной модели:\n")
       print("Средняя абсолютная ошибка: ", mean_absolute_error(y, y_tt))
       print("Средняя квадратичная ошибка: ", mean_squared_error(y, y_tt))
       print("Коэффициент детерминации: ", r2 score(y, y tt))
       print("\n\nМетрики для SVM-модели:\n")
       print("Средняя абсолютная ошибка: ", mean_absolute_error(y, predict))
       print("Средняя квадратичная ошибка: ", mean squared error(y, predict))
       print("Коэффициент детерминации: ", r2 score(y, predict))
       print("\n\nМетрики для Decision Tree:\n")
       print("Средняя абсолютная ошибка: ", mean absolute error(y, dec predict))
       print("Средняя квадратичная ошибка: ", mean_squared_error(y, dec_predict))
       print("Коэффициент детерминации: ", r2 score(y, dec predict))
```

Метрики для линейной модели:

Средняя абсолютная ошибка: 2.5508292802546 Средняя квадратичная ошибка: 10.512794897173503 Коэффициент детерминации: 0.6118698089221382

Метрики для SVM-модели:

Средняя абсолютная ошибка: 2.5996867264932724 Средняя квадратичная ошибка: 11.18839596468356 Коэффициент детерминации: 0.586926758668624

Метрики для Decision Tree:

Средняя абсолютная ошибка: 0.7095532407407409 Средняя квадратичная ошибка: 0.7222188657407407 Коэффициент детерминации: 0.9733358303760538

0.7. После подбора параметров модели показали лучший результат, чем без подбора.