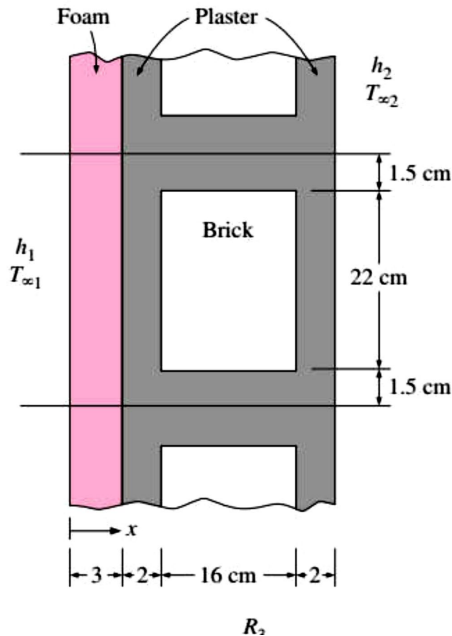


The rate of heat transfer through the composite wall analyzed in class is:

$$\dot{Q} = \frac{T_{\infty 1} - T_{\infty 2}}{R_{\text{tot}}} = \frac{20 - (-10) \text{ }^{\circ}\text{C}}{6,81 \text{ }^{\circ}\text{C/W}} = \mathbf{4,417 \text{ W}}$$



Thickness of the wall = 32cm

$$R_i = \frac{1}{h_i A} = \frac{1}{10 \times 0,25} = \mathbf{0,4 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Inner resistance)}$$

$$R_f = \frac{L_f}{k_f A} = \frac{0,3}{0,026 \times 0,25} = \mathbf{4,615 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Foam resistance)}$$

$$R_{pc1} = R_{pc2} = \frac{L_{pc1}}{k_p A_{pc1}} = \frac{0,02}{0,22 \times 0,25} = \mathbf{0,36 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Plaster resistance)}$$

$$R_{pc1} = R_{pc2} = \frac{L_{pc1}}{k_p A_{pc1}} = \frac{0,32}{0,22 \times 0,015} = \mathbf{96,97 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Plaster resistance in parallel)}$$

$$R_b = \frac{L_b}{k_b A} = \frac{0,32}{0,72 \times 0,22} = \mathbf{2,02 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Brick resistance in parallel)}$$

$$\frac{1}{R_{\text{tot}}} = \frac{1}{R_{pc1}} + \frac{1}{R_b} + \frac{1}{R_{pc2}} = \frac{1}{96,97} + \frac{1}{2,02} + \frac{1}{96,97} = \mathbf{0,516 \frac{\text{W}}{^{\circ}\text{C}}}$$

$$R_{\text{tot parall}} = \frac{1}{0,516} = \mathbf{1,938 \frac{^{\circ}\text{C}}{\text{W}}} \text{ (Total resistance in parallel)}$$

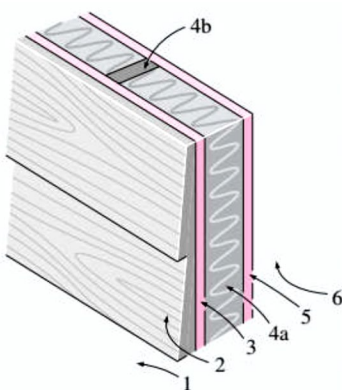
$$R_o = \frac{1}{h_2 A} = \frac{1}{50 \cdot 0,25} = 0,1 \frac{^\circ\text{C}}{\text{W}} \text{ (Outer resistance)}$$

$$R_{\text{tot}} = 0.4 + 4.615 + 0.36 + 0.36 + 1.938 + 0.1 = 7,773 \frac{^\circ\text{C}}{\text{W}} \text{ (Total resistance)}$$

$$\dot{Q} = \frac{T_{\infty 1} - T_{\infty 2}}{R_{\text{tot}}} = \frac{20 - (-10) \text{ } ^\circ\text{C}}{7,773 \text{ } ^\circ\text{C/W}} = \mathbf{3,86 \text{ W (Heat transfer through the composite wall)}}$$

By increasing the thickness of the brick from 16 cm to 32 cm, the total parallel resistance increases only of around $1 \frac{^\circ\text{C}}{\text{W}}$ so that the heat transfer through the wall decreases of 0,8 W (from 4.417 W to 3.86 W).

We can tell that increasing the thickness of the brick doesn't produce a significant effect in order to reduce the heat transfer, the better solution is increasing the thickness of the foam, which has a way higher resistance.



Determine the overall unit thermal resistance (the R_{value}) of a wood frame wall that is built around 38-mm 90-mm wood studs with a center-to-center distance of 400 mm. The 90-mm-wide cavity between the studs is filled with urethane rigid insulation. The inside is finished with 13-mm gypsum wallboard and the outside with 13-mm plywood and 13-mm 200-mm wood bevel lapped siding.

$$R_{\text{wood bevel}} + R_{\text{plywood(13mm)}} + R_{\text{gypsum wallboard}} + R_{\text{inside}} = 0,479 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}$$

With insulation

$$R_{\text{urethane r. f.}} = 0.98 \times \frac{90}{25} = 3.528 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}$$

$$R_{\text{outside}} = 0,03 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}$$

$$R'_{\text{tot}} = 3,528 + 0,339 + 0,03 = \mathbf{4,007 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}}$$

With wood stunds

$$R_{\text{plywood}} = 0,63 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}$$

$$R_{\text{outside}} = 0,3 \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}$$

$$\mathbf{R'_{\text{tot}} = 0,63 + 0,479 + 0,3 = \mathbf{1,379} \frac{\text{m}^2 \text{ } ^\circ\text{C}}{\text{W}}}$$