

Question 1:

Heat loss through a composite wall:

1.3m high and 5m wide wall consist of long 82 cm, 22 cm cross section horizontal bricks ($k = 0.72 \text{ W/m}^\circ\text{C}$) separated by 3cm thick plaster layers ($k = 0.22 \text{ W/m}^\circ\text{C}$).

There are also 2cm thick plaster layers on each side of the brick and a 3cm thick rigid foam ($k = 0.026 \text{ W/m}^\circ\text{C}$) on the inner side of the wall the indoor and the outdoor temperatures 20°C and -10°C and the convection heat transfer coefficients on the inner and the outer sides are $h_1 = 10 \text{ W/m}^2^\circ\text{C}$ and $h_2 = 40 \text{ W/m}^2^\circ\text{C}$ respectively. Assuming one dimensional heat transfer and disregarding radiation determine the rate of heat transfer through the wall.

answer:

$$R_{R\text{ frame}} = \frac{L_{\text{frame}}}{K_{\text{frame}} \times A_{1-\text{dimen}}} = \frac{0.103 \text{ m}}{0.1026 \text{ w/c} \times (0.1015 + 0.022 + 0.1015) \text{ m} \times 1 \text{ m}} = 4.1615 \%$$

$$R_{\text{ceiling}} = \frac{1}{h_1 \times A_{1-\text{dimen}}} = \frac{1}{10 \text{ w/c} \times (0.1015 + 0.022 + 0.1015) \text{ m} \times 1 \text{ m}} = 0.14 \%$$

$$R_{\text{brick}} = \frac{L_B}{K_B \times A_{B(1-\text{dimen})}} = \frac{0.32}{0.172 \text{ w/c} \times 0.129 \text{ m} \times 1 \text{ m}} = 2.02 \%$$

$$R_{\text{plaster up or down}} = \frac{L_P}{K_P + A_{P(1-\text{dimen})}} = \frac{0.32}{0.122 \text{ w/c} \times 0.1015 \times 1 \text{ m}} = 96.97 \%$$

$$\Rightarrow \frac{1}{R_{\text{total}}} = \frac{1}{R_{P.\text{up}}} + \frac{1}{R_B} + \frac{1}{R_{P.\text{down}}} = \frac{1}{96.97} + \frac{1}{2.02} + \frac{1}{96.97} = 0.5156 \text{ w/c}$$

$$\text{ie } R_{\text{total-parallel}} = \frac{1}{0.5156} = 1.9394 \%$$

$$R_{\text{left or right}} = \frac{L_{P.\text{left}}}{K_P \times A_{P(\text{left or right } 1-\text{dimen})}} = \frac{0.102 \text{ m}}{0.122 \times (0.1015 + 0.022 + 0.1015) \times 1} = 0.3636 \%$$

$$R_{\text{ceiling}} = \frac{1}{h_2 \times A_{1-\text{dimen}}} = \frac{1}{40 \times (0.1015 + 0.022 + 0.1015) \times 1 \text{ m}} = 0.1 \%$$

$$R_{\text{wall total } (1-\text{dimen})} = R_{1.\text{ceiling}} + R_{\text{plaster left}} + R_{\text{frame}} + R_{\text{total parallel}} + R_{\text{plaster right}} + R_{\text{ceiling}} = 12$$

$$0.14 \% + 4.1615 \% + 0.3636 \% + 1.9394 \% + 0.3636 \% + 0.1 \% = 7.7816 \%$$

$$R_{\text{wall total}} = 7.7816 \%$$

$$\dot{Q} = \frac{T_i - T_\infty}{R_{\text{wall, total}}} = \frac{20 - (-10)}{7,7816} = 3,855 \text{ W}$$

Comments: In the last question the thickness of wall was 16cm and then the R_{total} was around 6,81 C/W . In conclusion with increasing the thickness, R_{total} is increased and the heat transfer is decreased. Also, I should mentioned that we doubled the thickness of brick in a composite wall but the thermal resistance doesn't significantly increase and the rate of heat transferring doesn't decrease significantly.

Question 2:

Answers:

	wood	Insulation
outside air	0,03	0,03
wood Bevel (13mm x 20)	0,14	0,14
Polywood (13mm)	0,11	0,11
Urethane Rigid Foam (90)	1,10	$0,98 \times 90,25 = 3,528$
wood Studs (90mm)	0,63	N/A
Gypsum Board (13mm)	0,079	0,079
Inside surface	0,12	0,12

$$R_{\text{with wood}} = 0,03 + 0,14 + 0,11 + 0,63 + 0,079 + 0,12 = 1,109 \text{ m}^2\text{C/W}$$

$$R_{\text{with insulation}} = 0,03 + 0,14 + 0,11 + 3,528 + 0,079 + 0,12 = 4,107 \text{ m}^2\text{C/W}$$