

## Week 3 Assignment

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### Question 1

#### PART 1

$$R_{\text{wall.total}} = 6.81^{\circ}\text{C/W}$$

$$\begin{aligned} Q_{\text{dot}} &= 20 - (-10) / 6.81 \\ &= 4.41\text{W} \end{aligned}$$

#### PART 2

3m high and 5m wide wall consists of long 32cm 22cm cross section horizontal bricks ( $k=0.72\text{W/m}^{\circ}\text{C}$ ) separated by 3cm thick plaster ( $k=0.22\text{ W/m}^{\circ}\text{C}$ )

2cm thk plaster layers on each side of the brick and 3cm thk rigid foam ( $k=0.026\text{W/m}^{\circ}\text{C}$ ) on the inner side of the wall.  $T_1$  and  $T_2$  are  $20^{\circ}\text{C}$  and  $-10^{\circ}\text{C}$  respectively. And the convection heat transfer coefficients on the inner and outer sides are  $h_1=10\text{ W/m}^2\cdot^{\circ}\text{C}$  and  $h_2=40\text{W/m}^2$ , respectively.

$$\begin{aligned} R_{1\text{conv}} &= 1/h_1 \times A_1 = 1/10 \times (0.015+0.22+0.015) \times 1 \\ &= 0.4^{\circ}\text{C/W} \end{aligned}$$

$$\begin{aligned} R_{\text{foam}} &= L_{\text{foam}} / k_{\text{foam}} \times A_1 = 0.03 / [0.026 \times (0.015 + 0.22 + 0.015) \times 1] \\ &= 4.62^{\circ}\text{C/W} \end{aligned}$$

$$\begin{aligned} R_{\text{plaster.up}} &= R_{\text{plaster.down}} = L_{\text{p.up or dn}} / k_p \times A_{\text{p.up or p.dn}} \\ &= 0.32 / [0.22 \times 0.015 \times 1] \\ &= 96.88^{\circ}\text{C/W} \end{aligned}$$

$$\begin{aligned} R_{\text{brick}} &= L_{\text{brick}} / k_{\text{brick}} \times A_{\text{brick}} \\ &= 0.32 / [0.72 \times 0.22 \times 1] \\ &= 2.02^{\circ}\text{C/W} \end{aligned}$$

$$\begin{aligned} 1/R_{\text{total(parallel)}} &= [1/R_{\text{plaster.up}}] + [1/R_{\text{brick}}] + [1/R_{\text{plaster.down}}] \\ &= [1/96.88] + [1/2.02] + [1/96.88] \\ &= 0.516^{\circ}\text{C/W} \end{aligned}$$

$$R_{\text{total(parallel)}} = 1.94^{\circ}\text{C/W}$$

$$\begin{aligned} R_{\text{plaster.left}} &= R_{\text{plaster.right}} = 0.02 / [0.22 \times (0.015+0.22+0.015) \times 1] \\ &= 0.363^{\circ}\text{C/W} \end{aligned}$$

$$\begin{aligned} R_{2\text{conv.}} &= 1 / [40 \times (0.015+0.22+0.015) \times 1] \\ &= 0.1^{\circ}\text{C/W} \end{aligned}$$

$$R_{\text{wall.total}} = 0.4+4.62+0.363+1.94+0.363+0.1$$

$$= 7.79^{\circ}\text{C/W}$$

Heat transfer

$$\dot{Q} = T_1 - T_{\infty} / R_{\text{wall, total}}$$

$$= 20 - (-10) / 7.79$$

$$= 3.851\text{W}$$

By doubling the thickness of the brick in a composite wall does not change increase the thermal resistance of the whole wall, hence the rate of heat transfer does not significantly decrease.

## Question 2

	Wood	Insulation
Outside Air	0.03	0.03
Wood Bevel (13mmx200mm)	0.14	0.14
Polywood(13mm)	0.11	0.11
Urethane Rigif Foam Ins.(90mm)	No	$0.98 \times 90 / 25 = 3.528$
Wood studs (90mm)	0.63	No
Gypsum Board (13mm)	0.079	0.079
Inside surface	0.12	0.12

$$R'_{\text{with wood}} = (0.03 + 0.14 + 0.11 + 0.63 + 0.079 + 0.12)$$

$$= 1.109 \text{ m}^2 \text{ }^{\circ}\text{C/W}$$

$$R'_{\text{with insulation}} = (0.03 + 0.14 + 0.11 + 3.528 + 0.079 + 0.12)$$

$$= 4.007 \text{ m}^2 \text{ }^{\circ}\text{C/W}$$