

THE RADIATIVE HEAT TRANSFER

Every object produces radiative heat transfer, and it's difficult to calculate its.

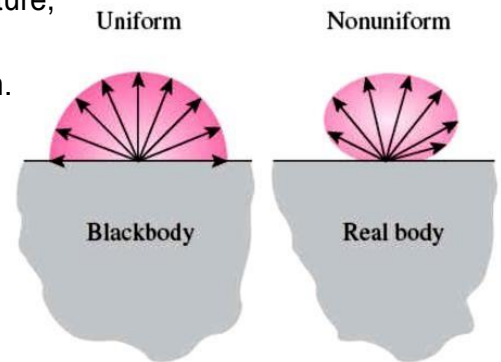
A **black-body** is an idealized body that emits the maximum amount of radiation: it is a perfect emitter and absorber of all incident radiation.

It has the highest possible emissive power at a certain temperature, has the same emissive power in every direction, but it hasn't the same emissive power at every wavelength.

The **radiation energy** emitted by a blackbody:

$$E_b(T) = \sigma T^4 \quad \text{w/m}^2 \quad \text{Blackbody emissive power}$$

$$\sigma = 5.670 \times 10^{-8} \quad \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4} \quad \text{Stefan-Boltzmann constant}$$



So, the emissive power of a black-body related to temperature is T^4 .

The **radiation intensity "I"** is the magnitude of radiation emitted (or incident) in a specified direction in space. Knowing it allows me to find the heat transfer between two surfaces:

$$E_b(T) = \pi I_b = \sigma T^4 \quad \text{w/m}^2$$

$$I_b(T) = \frac{E_b(T)}{\pi}$$

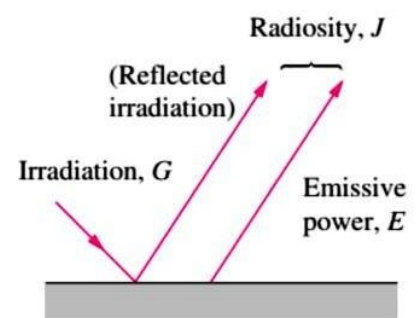
Diffuse radiation is a surface that has the same radiation in every direction.

Incident radiation is a surface that is receiving radiation.

Radiosity J is the sum of the Emissive power of an object and Reflected irradiation.

Is the quantity that represents the rate at which radiation energy leaves a unit area of a surface in all directions.

Irradiation G (for ex. the solar irradiation on a certain volume) is the radiation that is received, the radiation's flux on a surface.



Emissivity ϵ is how much radiation is emitted by a surface respect to a black-body. It depends on temperature and direction.

In a black-body $\epsilon=1$

$$\epsilon \text{ of an object's surface} = \frac{E \text{ of the object}}{E \text{ blackbody} \rightarrow \sigma T^4}$$

Synthesizing:

$$J_i = \left(\begin{array}{c} \text{Radiation emitted} \\ \text{by surface } i \end{array} \right) + \left(\begin{array}{c} \text{Radiation reflected} \\ \text{by surface } i \end{array} \right)$$

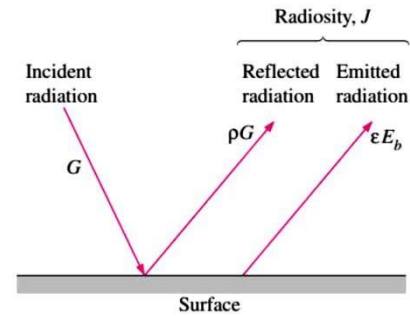
$$= \epsilon_i E_{bi} + \rho_i G_i$$

$$= \epsilon_i E_{bi} + (1 - \epsilon_i) G_i \quad (\text{W/m}^2)$$

$$\dot{Q}_i = \left(\begin{array}{c} \text{Radiation leaving} \\ \text{entire surface } i \end{array} \right) - \left(\begin{array}{c} \text{Radiation incident} \\ \text{on entire surface } i \end{array} \right)$$

$$= A_i (J_i - G_i) \quad (\text{W})$$

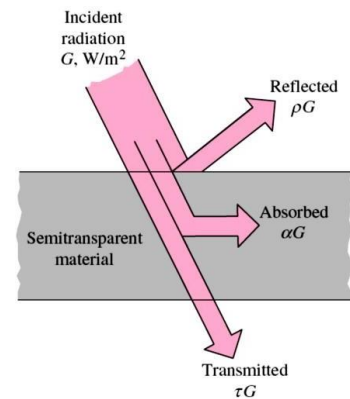
$$\dot{Q}_i = A_i \left(J_i - \frac{J_i - \epsilon_i E_{bi}}{1 - \epsilon_i} \right) = \frac{A_i \epsilon_i}{1 - \epsilon_i} (E_{bi} - J_i)$$



Absorptivity $a = \frac{\text{Absorbed radiation}}{\text{Incident radiation}} = \frac{G_{\text{abs}}}{G} \quad 0 \leq a \leq 1$

Reflectivity $\rho = \frac{\text{Reflected radiation}}{\text{Incident radiation}} = \frac{G_{\text{ref}}}{G} \quad 0 \leq \rho \leq 1$

Transmissivity $\tau = \frac{\text{Transmitted radiation}}{\text{Incident radiation}} = \frac{G_{\text{tr}}}{G} \quad 0 \leq \tau \leq 1$



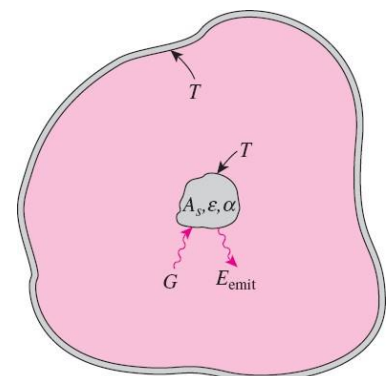
$$G = G_{\text{abs}} + G_{\text{ref}} + G_{\text{tr}}$$

$\alpha + \rho + \tau = 1$,but in the opaque surface $\tau=0$ (because nothing pass through an opaque surface)

There is also a relationship between α and ϵ : $\epsilon(T) = \alpha(T)$ **Kirchhoff's Law:**

the total hemispherical emissivity of a surface at temperature T is equal to its total hemispherical absorptivity for radiation coming from a blackbody at the same temperature.

$$G_{\text{abs}} = \alpha G = \alpha \sigma T^4 = E_{\text{emit}} = \epsilon \sigma T^4$$



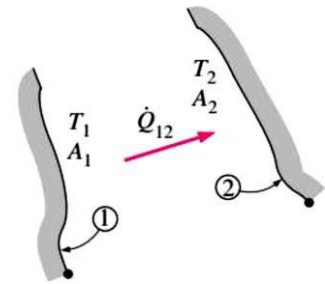
View Factor F_{12} is a geometrical quantity that represents the fraction of the emissive power/radiation leaving from surface 1 that is received by surface 2. It doesn't depend on the surface properties.

$$F_{12} = \frac{\text{q emitted by surface 1 and received by surface 2}}{\text{q emitted by surface 1}}$$

The net radiative heat exchange between black surface 1 and 2 is

$$\dot{Q}_{1 \rightarrow 2} = \left(\begin{array}{l} \text{Radiation leaving} \\ \text{the entire surface 1} \\ \text{that strikes surface 2} \end{array} \right) - \left(\begin{array}{l} \text{Radiation leaving} \\ \text{the entire surface 2} \\ \text{that strikes surface 1} \end{array} \right)$$

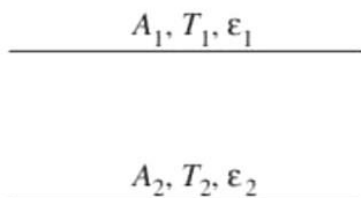
$$= A_1 E_{b1} F_{1 \rightarrow 2} - A_2 E_{b2} F_{2 \rightarrow 1} \quad (\text{W})$$



$$Q_{1 \rightarrow 2} = A_1 \cdot F_{12} \cdot \sigma (T_1^4 - T_2^4)$$

The net radiative heat exchange between gray/opaque surface 1 (that leaves) and 2 (that is receiving) is:

Infinitely large parallel plates



$$A_1 = A_2 = A$$

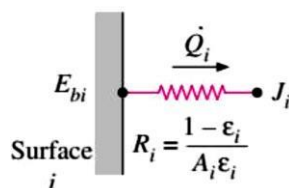
$$F_{12} = 1$$

$$\dot{Q}_{12} = \frac{A \sigma (T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$$

Radiative resistance

$$Q = A_i \frac{\epsilon_i}{1 - \epsilon_i} (E_{bi} - J_i) \Rightarrow Q = \frac{E_{bi} - J_i}{R_i} \quad \text{is the net heat exchange from surface } i \text{ with environmental}$$

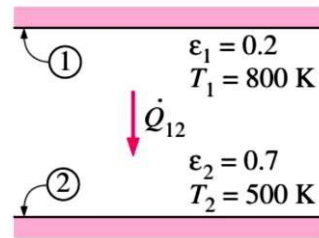
$$R_i = \frac{1 - \epsilon_i}{\epsilon_i A_i}$$



Exercise:

Calculate the heat exchange between the two parallel plates:

$$\dot{Q}_{12} = \frac{A\sigma(T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$$



$$Q_{12} = A \frac{5.670 \cdot 10^{-8} \cdot (800^4 - 500^4)}{\frac{1}{0.2} + \frac{1}{0.7} - 1} = A \cdot \frac{19680,57}{5,4286} = 3625,35 \cdot A \text{ [W]}$$

If the **two emissivities of the plates are 0.1:**

$$Q_{12} = A \frac{5.670 \cdot 10^{-8} \cdot (800^4 - 500^4)}{\frac{1}{0.1} + \frac{1}{0.1} - 1} = A \cdot \frac{19680,57}{19} = 1035,82 \cdot A \text{ [W]}$$

Conclusion:

With the same area and variation of temperature, increasing the emissivity it also increases the heat exchange between the two parallel plates