

Assignment 3

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Question 1

A wall: $h=3\text{m}$, $w=5\text{m}$ consists of long $32\text{m} \times 22\text{m}$ cross section horizontal bricks ($k=0.72\text{W/m}\cdot^\circ\text{C}$) separated by 3cm thick plaster layers ($k=0.22\text{W/m}\cdot^\circ\text{C}$).

There are also 2cm thick plaster layers on each side of the brick and foam thickness: 3cm with ($k=0.026\text{W/m}\cdot^\circ\text{C}$) on the inner side of the wall.

The indoor and the outdoor temperatures are 20°C and -10°C , and the convection heat transfer coefficients on the inner and outer sides are $h_1=10\text{W/m}^2\cdot^\circ\text{C}$ and $h_2=40\text{W/m}^2\cdot^\circ\text{C}$, respectively.

Assuming one dimensional heat transfer and disregarding radiation, determine the rate of heat transfer through the wall.

Every 25 cm of distance in vertical direction, a brick is in place. Therefore, every meter is 0.25m in height. $A=0.25\text{ m}^2$

$$R_i = R_{\text{conv}1} = \frac{1}{h_1 \cdot A} = \frac{1}{10 \cdot 0.25} = 0.4\text{ }^\circ\text{C/W}$$

$$R_1 (\text{foam}) = \frac{L(\text{foam})}{k(\text{foam}) \cdot A} = \frac{0.03}{0.026 \cdot 0.25} = 4.6\text{ }^\circ\text{C/W}$$

$$R_2=R_6 (\text{side plaster}) = \frac{L(\text{sideplaster})}{k(\text{sideplaster}) \cdot A} = \frac{0.02}{0.22 \cdot 0.25} = 0.36\text{ }^\circ\text{C/W}$$

$$R_3=R_5 (\text{center plaster}) = \frac{L(\text{centerplaster})}{k(\text{centerplaster}) \cdot A} = \frac{0.32}{0.22 \cdot 0.015} = 96.97\text{ }^\circ\text{C/W}$$

$$R_4 (\text{brick}) = \frac{L(\text{brick})}{k(\text{brick}) \cdot A(\text{brick})} = \frac{0.32}{0.72 \cdot 0.22} = 2.02\text{ }^\circ\text{C/W}$$

$$R_0 = R_{\text{conv}2} = \frac{1}{h_2 \cdot A} = \frac{1}{25 \cdot 0.25} = 0.16\text{ }^\circ\text{C/W}$$

$$\frac{1}{R(\text{parallel})} = \frac{1}{R_3} + \frac{1}{R_5} + \frac{1}{R_4} = \frac{1}{96.97} + \frac{1}{96.97} + \frac{1}{2.02} = 0.516\text{ }^\circ\text{C/W}$$

$$\text{Therefore, } R_{\text{parallel}} = \frac{1}{0.516} = 1.94\text{ }^\circ\text{C/W}$$

$$R_{\text{total}} = R_i + R_1 (\text{foam}) + R_2 + R_6 (\text{side plaster}) + R_{\text{parallel}} + R_0$$

$$R_{\text{total}} = 0.4 + 4.6 + 0.36 + 0.36 + 1.94 + 0.16 = 7.82\text{ }^\circ\text{C/W}$$

$$\text{Heat transfer through wall: } \dot{Q} = \frac{T(\text{inf}1) - T(\text{inf}2)}{R_{\text{total}}} = \frac{20 - (-10)}{7.82} = 3.84\text{ W}$$

Question 2

A wood frame wall that is built around 38mm x 90mm wood studs with a center-to-center distance of 400mm. The 90mm-wide cavity between the studs is filled with urethane rigid foam insulation. The inside is finish with 13-mm gypsum wallboard and the outside with 13-mm plywood and 13-mm x 200-mm wood bevel lapped siding. The insulated cavity constitutes 75% of the heat transmission area while the studs, plates, and sills constitute 21%. The headers constitute 4 % of the area, and they can be treated as studs.

Find the 2 *RUnit* values.

	WOOD	INSULATION
OUTSIDE AIR	0.03	0.03
WOOD BEVEL (13*20mm)	0.14	0.14
PLYWOOD (13mm)	0.11	0.11
URETHANE RIDGID FOAM INSULATION (90mm)	-	$0.98 \times 90 / 25 = 3.5$
WOOD STUDS (90mm)	0.63	-
GYPSUM BOARD (13mm)	0.079	0.079
INSIDE SURFACE	0.12	0.12
TOTAL m².C/W	1.11	3.98