Exercise:

Heat exchange between the two parallel plates:

How many shields with ε =0.1 should we add in order to have the new heat transfer rate to be 1% of the case without shields?

$$\begin{array}{c}
\varepsilon_1 = 0.2 \\
T_1 = 800 \text{ K} \\
\dot{Q}_{12} \\
\varepsilon_2 = 0.7 \\
T_2 = 500 \text{ K}
\end{array}$$

$$\dot{Q}_{12} = \frac{A\sigma(T_1^4 - T_2^4)}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1}$$

$$\dot{q} = \frac{\dot{Q}}{A}$$

 $\dot{q} = \frac{\dot{Q}}{A}$

$$\dot{q}_{12} = \frac{5.670 * 10^{-8} * (800^4 - 500^4)}{\frac{1}{0.2} + \frac{1}{0.7} - 1} = \frac{19680,57}{5.4286} = 3625,35 \quad [W]$$

If the two emissivities of the plates are 0.1:

$$\dot{q}_{12} = \frac{5.670*10^{-8}*(800^4 - 500^4)}{\frac{1}{0.1} + \frac{1}{0.1} - 1} = \frac{19680,57}{19} = 1035,82 \quad [W]$$

With the same area and variation of temperature, if I used a very low emissivity material (ϵ =0.1) I can reduce the heat transfer of 3 times.

Another solution to reduce the heat transfer is to put a shield between the two parallel plates. (multiple radiation shields)

① ③ ② ②
$$\epsilon_{1} = 0.2 \\ T_{1} = 800 \text{ K}$$

$$\epsilon_{3} = 0.1$$

$$\dot{q}_{12}$$

$$\dot{q}_{12}$$

$$\dot{Q}_{12, N \text{ shields}} = \frac{A\sigma(T_{1}^{4} - T_{2}^{4})}{\left(\frac{1}{\varepsilon_{1}} + \frac{1}{\varepsilon_{2}} - 1\right) + \left(\frac{1}{\varepsilon_{3, 1}} + \frac{1}{\varepsilon_{3, 2}} - 1\right) + \cdots + \left(\frac{1}{\varepsilon_{N, 1}} + \frac{1}{\varepsilon_{N, 2}} - 1\right)}$$

$$\left(\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1\right) + \left(\frac{1}{\varepsilon_{3,1}} + \frac{1}{\varepsilon_{3,2}} - 1\right) + \cdots + \left(\frac{1}{\varepsilon_{N,1}} + \frac{1}{\varepsilon_{N,2}} - 1\right)$$

$$\dot{q}_{12,1\text{shield}} = \frac{5.670*10^{-8}*(800^4 - 500^4)}{\left(\frac{1}{0.2} + \frac{1}{0.7} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right)} = \frac{19680,57}{5.426 + 19} = \frac{19680,57}{24.429} = 805.623 \text{ W} \qquad \text{using 1 shield}$$

$$\dot{q}_{12,\text{n. shields}} = \frac{5.670*10^{-8}*(800^4 - 500^4)}{\left(\frac{1}{0.2} + \frac{1}{0.7} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right)} = \frac{19680,57}{5.426 + 19 + 19} = \frac{19680,57}{43.429} = 453.167 \text{ W}$$
 using 2 shields

 $\dot{q}_{12,\text{n. shields}} = \frac{5.670*10^{-8}*(800^4 - 500^4)}{\left(\frac{1}{0.2} + \frac{1}{0.7} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right) + \left(\frac{1}{0.1} + \frac{1}{0.1} - 1\right)} = \frac{19680,57}{5.426 + 19 + 19 + 19} = \frac{19680,57}{62.429} = 315.247 \text{ W}$ using 3 shields. With these 3 shields, I have reduced the heat transfer od 10 times.

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*4)} = \frac{19680,57}{81.429} = 241.690\,\,\text{W} \qquad \text{using 4 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*5)} = \frac{19680,57}{100.429} = 195.965\,\,\text{W} \qquad \text{using 5 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*6)} = \frac{19680,57}{119.429} = 164.789\,\,\text{W} \qquad \text{using 6 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*7)} = \frac{19680,57}{138.429} = 142.171\,\,\text{W} \qquad \text{using 7 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*8)} = \frac{19680,57}{157.429} = 125.012\,\,\text{W} \qquad \text{using 8 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*9)} = \frac{19680,57}{176.429} = 111.550\,\,\text{W} \qquad \text{using 9 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*10)} = \frac{19680,57}{195.429} = 100.704\,\,\text{W} \qquad \text{using 10 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*11)} = \frac{19680,57}{214.429} = 91.781\,\,\text{W} \qquad \text{using 11 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*12)} = \frac{19680,57}{233.429} = 84.311\,\,\text{W} \qquad \text{using 12 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*14)} = \frac{19680,57}{252.429} = 77.965\,\,\text{W} \qquad \text{using 13 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*15)} = \frac{19680,57}{290.429} = 72.507\,\,\text{W} \qquad \text{using 14 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*15)} = \frac{19680,57}{290.429} = 67.764\,\,\text{W} \qquad \text{using 15 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*15)} = \frac{19680,57}{290.429} = 63.603\,\,\text{W} \qquad \text{using 16 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*16)} = \frac{19680,57}{309.429} = 63.603\,\,\text{W} \qquad \text{using 17 shields}$$

$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*16)} = \frac{19680,57}{309.429} = 59.923\,\,\text{W} \qquad \text{using 17 shields}$$

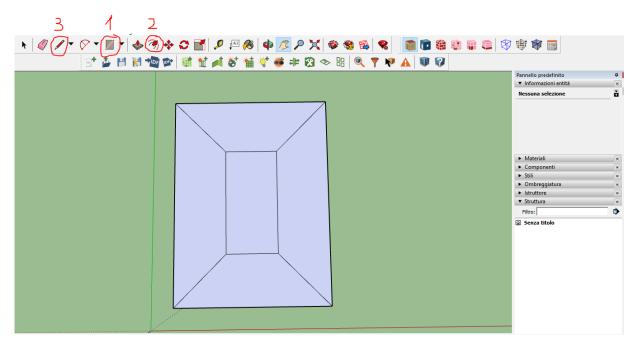
$$\dot{q}_{12,n.\,shields} = \frac{19680,57}{5.426+(19*16)} = \frac{19680,57}{3426+(19*16)} = \frac{19680$$

•••

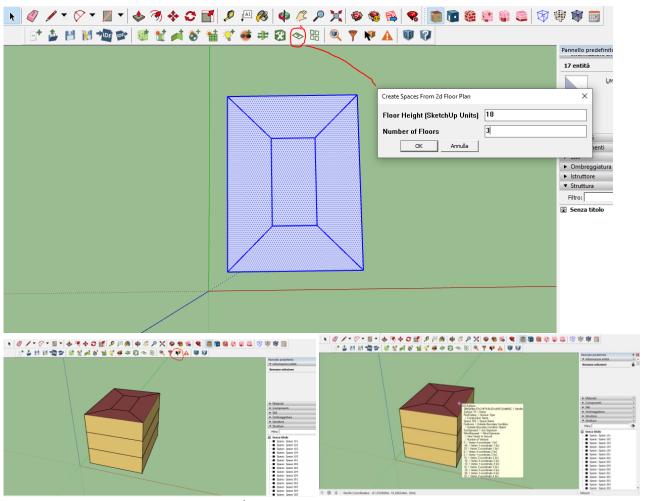
$$\dot{q}_{12,\text{n. shields}} = \frac{19680,57}{5.426 + (19*29)} = \frac{19680,57}{537.429} = 36.620 \text{ W}$$
 using 28 shields

$$\dot{q}_{12,\text{n. shields}} = \frac{19680,57}{5.426 + (19*29)} = \frac{19680,57}{556.429} = 35.369 \text{ W}$$
 using 29 shields

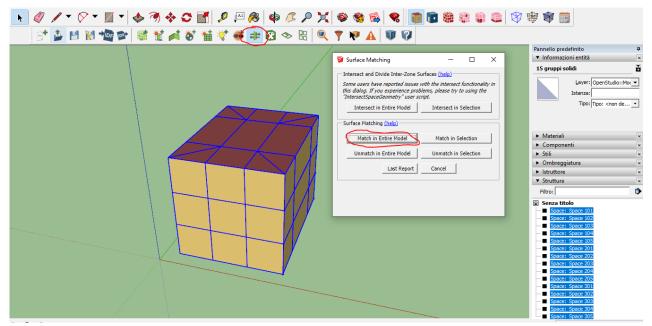
Using 28/29 shields with ϵ =0.1, I have reduced the initial heat transfer of 100 times.



I have created a rectangular with dimension 30x40 cm using as a tool the rectangular size, offset (of 10m through the center) and the pen.

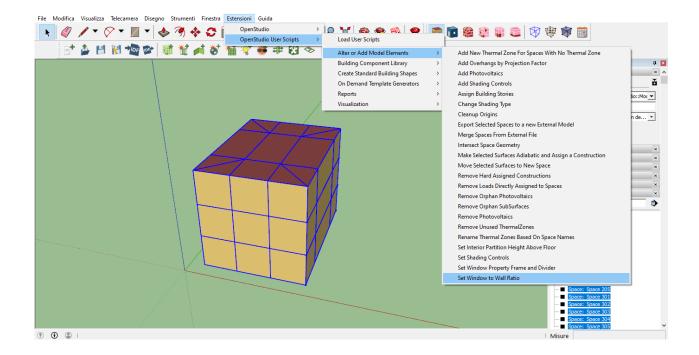


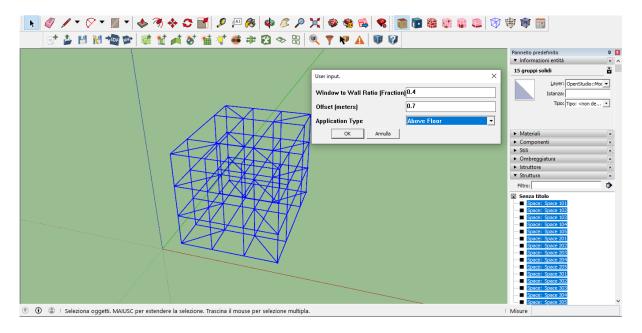
By using the tool Create Spaces From 2nd Floor Plan I have created a building of 3-floor height 10m. Selecting all the buildings and using Info Tool, I can see all the properties of each element that compose it.

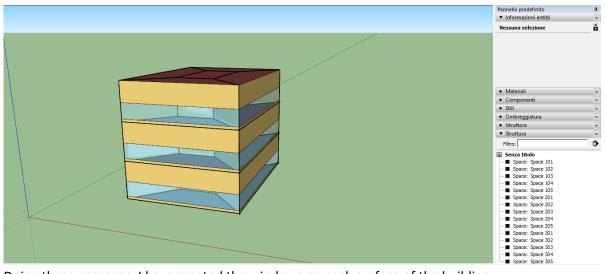


Selecting all the building >> Surface Matching >> Match the Entire Model.

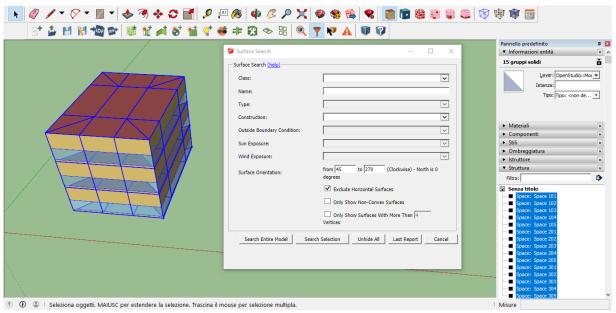
Doing these passages, in the following passages I won't create windows inside my building.



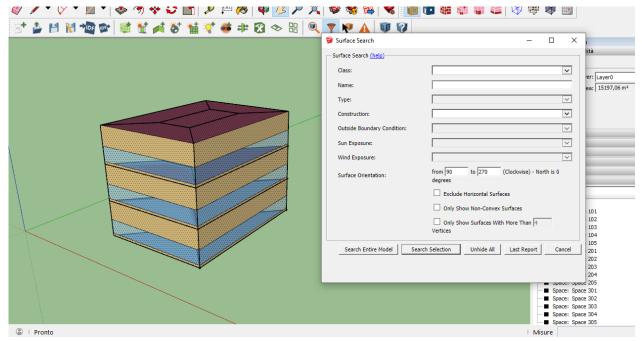




Doing these passages, I have created the windows on each surface of the building.

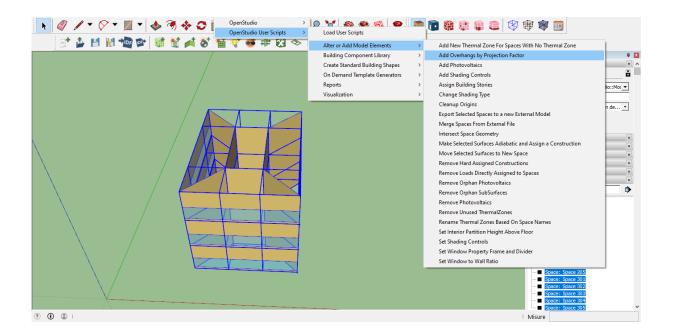


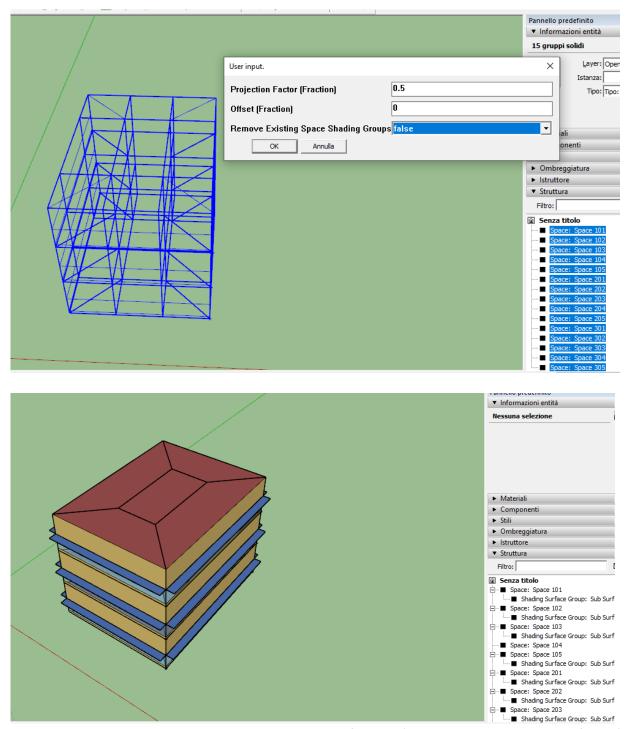
Doing so, and repeating this passage, I can exclude the north facade.



With the tool Search Surface, and pressed Search Selection, I should add external shading on the three surfaces (no on the north because I have excluded it.

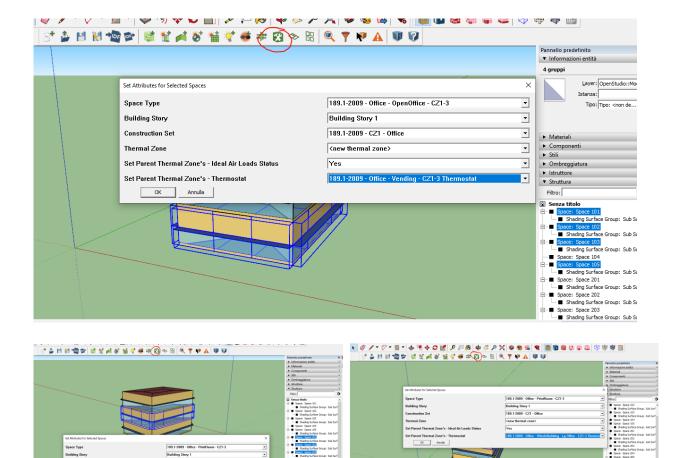
In my project, I could have missed and get wrong some passage, because I have an overhang on every façade, but during the next lessons I will correct it).





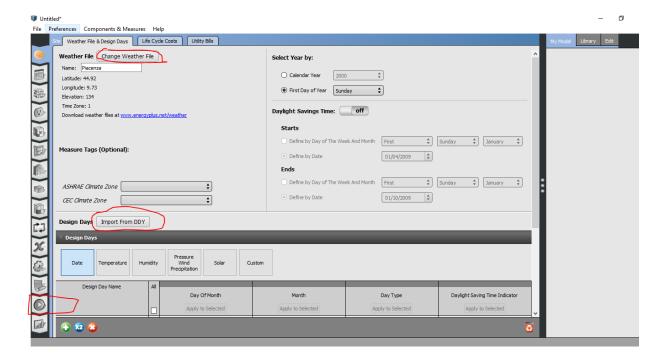
I put now the overhang that should go only on the three facades. (but it goes also on the north facade)

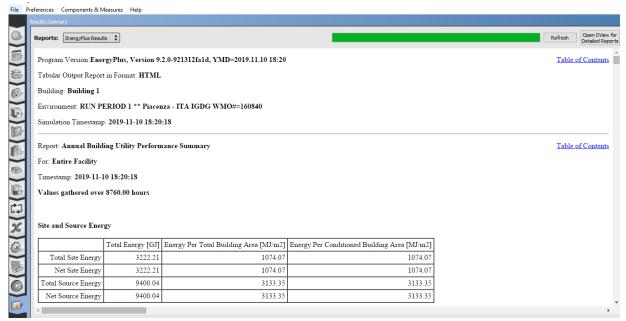
Now I start to select each thermal zone adding the specification: I start from the ground floor (Space 101,102,103,105)



In base of the function I want to put in the building, I can guess the number of people that will be into.

Now I can open Open Studio, insert the Weather File and the Design Days. Doing this, I have put the coordination of Piacenza. Then, I press Run.





Here I can see the Results Summary of my building.