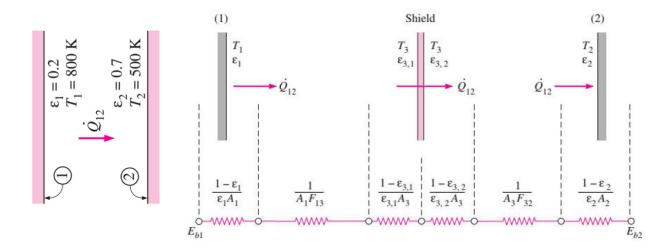
Task 1

Considering the same example you solved in the previous assignment (radiative heat transfer between two parallel plates), how many shields with epsilon = 0.1 should you add in order to have the new heat transfer rate to be 1% of the case without shields?



ANSWER

Without shield, $\varepsilon_1 = 0.2$ and $\varepsilon_2 = 0.7$,

$$\dot{Q}_{12} = \frac{E_{b1} - E_{b2}}{\frac{1 - \varepsilon_1}{A\varepsilon_1} + \frac{1}{AF_{12}} + \frac{1 - \varepsilon_2}{A\varepsilon_2}} = \frac{A\sigma(T_1^4 - T_2^4)}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1}$$

With N shield $\varepsilon_3 = 0.1$

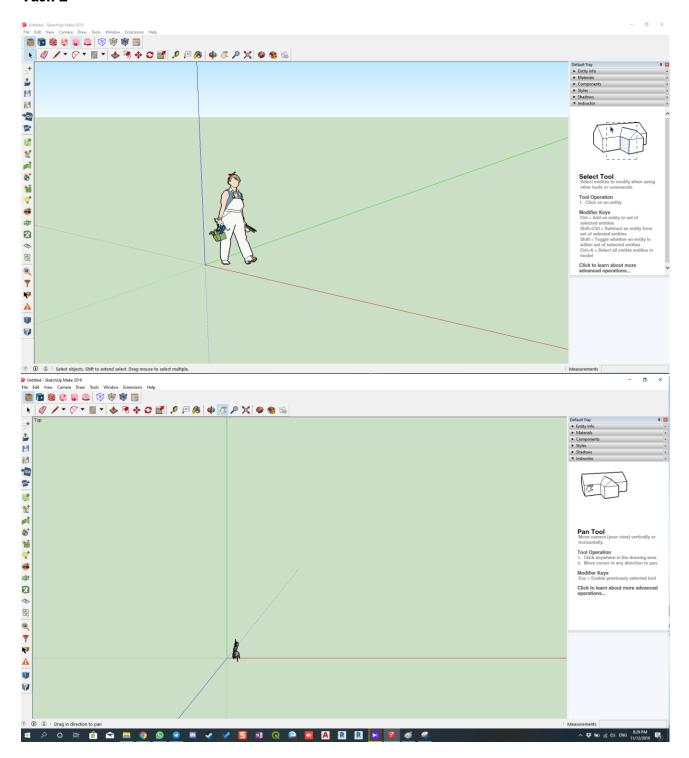
$$\begin{split} \dot{\boldsymbol{Q}}_{12Nshields} &= \frac{E_{b1} - E_{b2}}{\frac{1 - \varepsilon_1}{A\varepsilon_1} + \frac{1}{AF_{13}} + \frac{1 - \varepsilon_3}{A\varepsilon_3} + N \times \left(\frac{1 - \varepsilon_3}{A\varepsilon_3} + \frac{1}{AF_{33}} + \frac{1 - \varepsilon_3}{A\varepsilon_3}\right) + \frac{1 - \varepsilon_3}{A\varepsilon_3} + \frac{1}{AF_{32}} + \frac{1 - \varepsilon_2}{A\varepsilon_2} \\ &= \frac{A\sigma(T_1^4 - T_2^4)}{\left(\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_3} - 1\right) + N\left(\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_3} - 1\right) + \left(\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_2} - 1\right)} \\ &= \frac{A\sigma(T_1^4 - T_2^4)}{\left(\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1\right) + (N + 1)\left(\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_3} - 1\right)} \end{split}$$

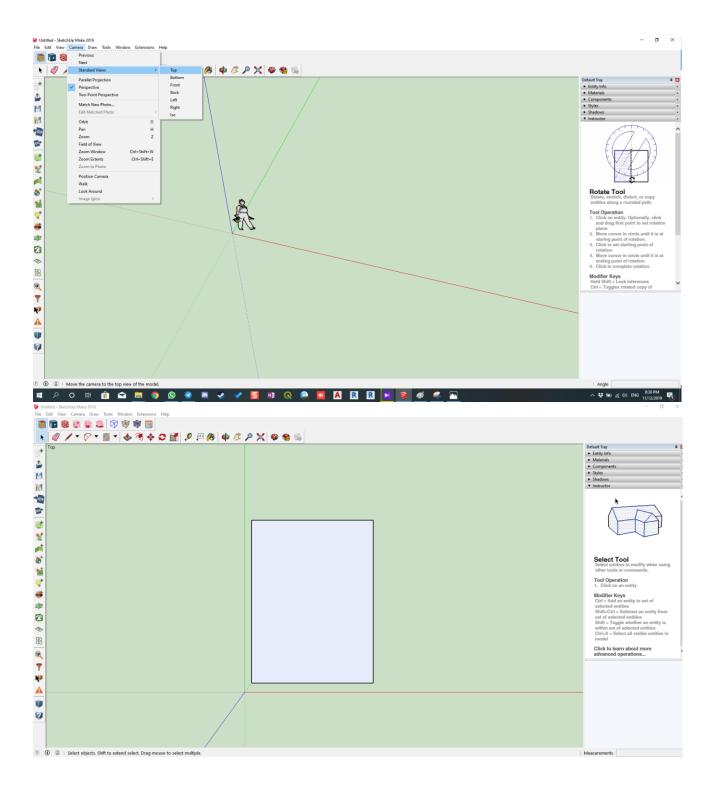
$$\frac{\dot{\boldsymbol{Q}}_{12Nshields}}{\dot{\boldsymbol{Q}}_{12}} = \frac{\left(\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1\right) + (N+1)\left(\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_3} - 1\right)}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1} = 1 + (N+1)\frac{\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_3} - 1}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1} = 100$$

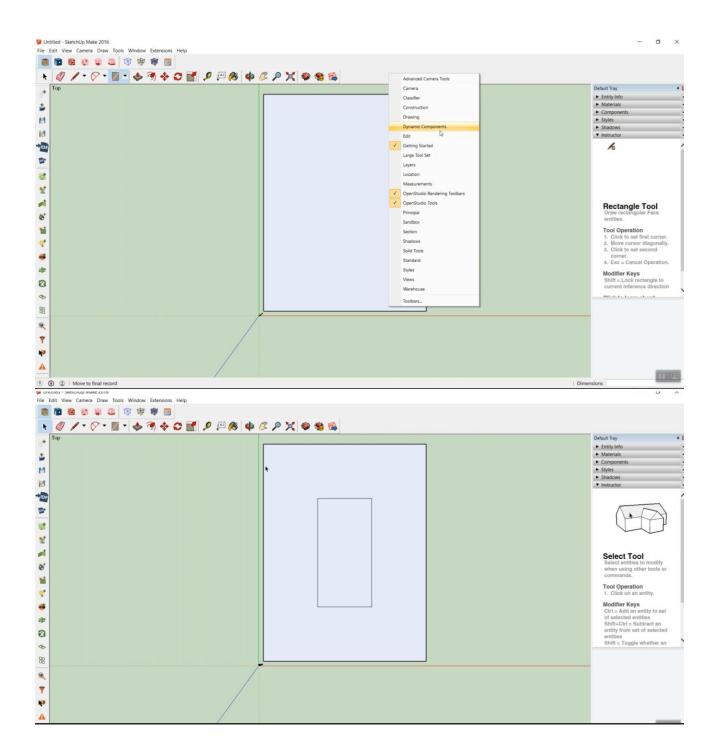
$$\iff \mathbf{N} = 99 \times \frac{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1}{\frac{1}{\varepsilon_3} + \frac{1}{\varepsilon_3} - 1} - 1 = 99 \times \frac{\frac{1}{0.2} + \frac{1}{0.7} - 1}{\frac{1}{0.1} + \frac{1}{0.1} - 1} - 1 \approx 27.3$$

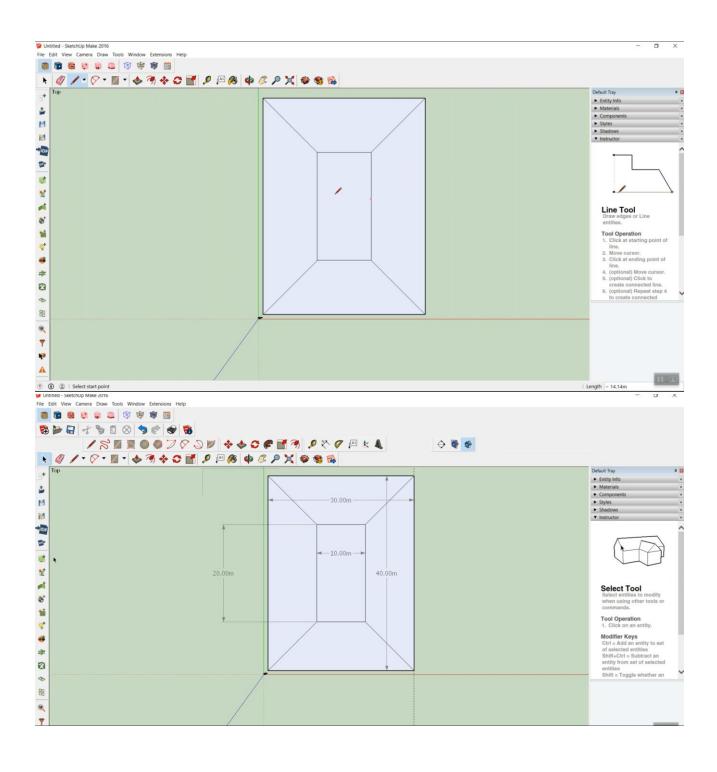
Conclusion: 27 shields can be added.

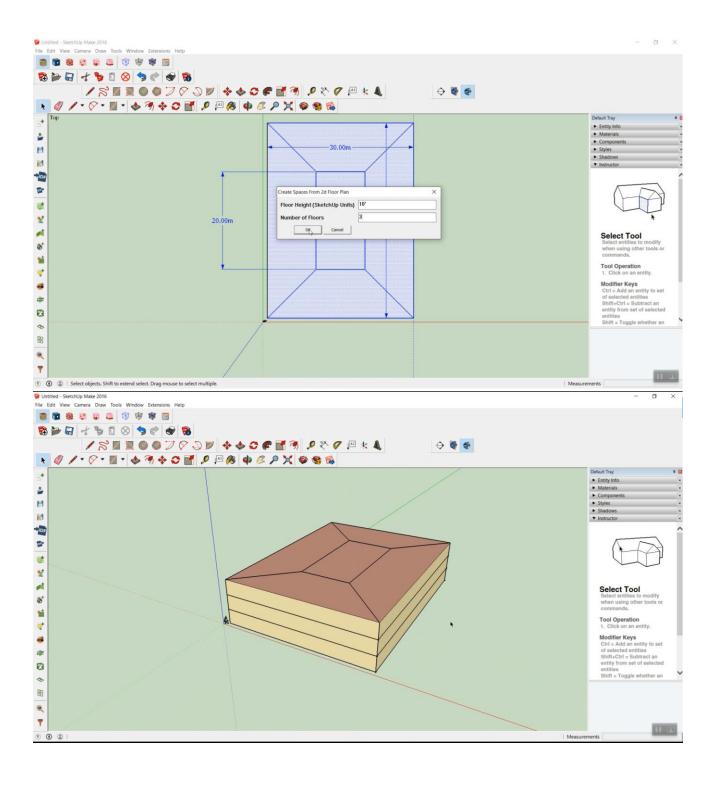
Task 2

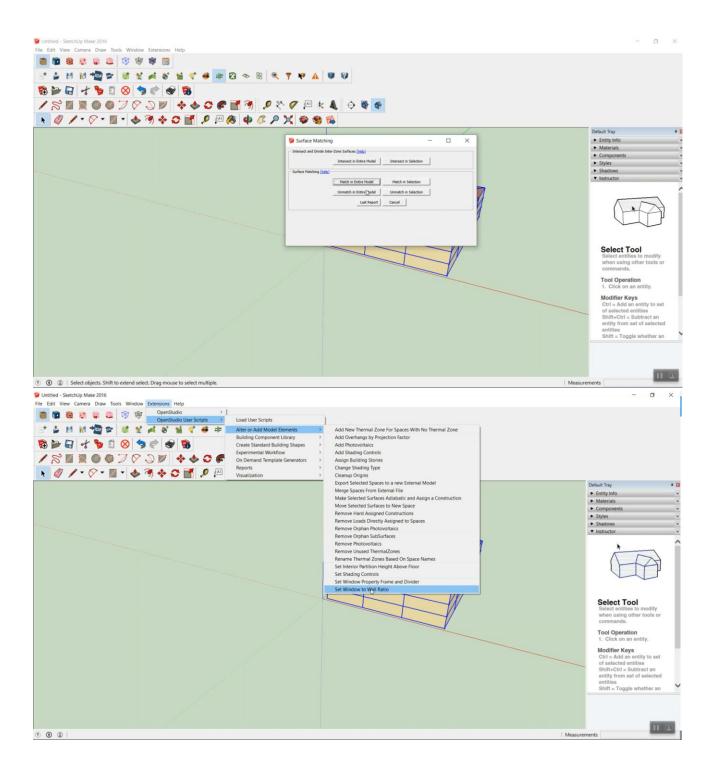


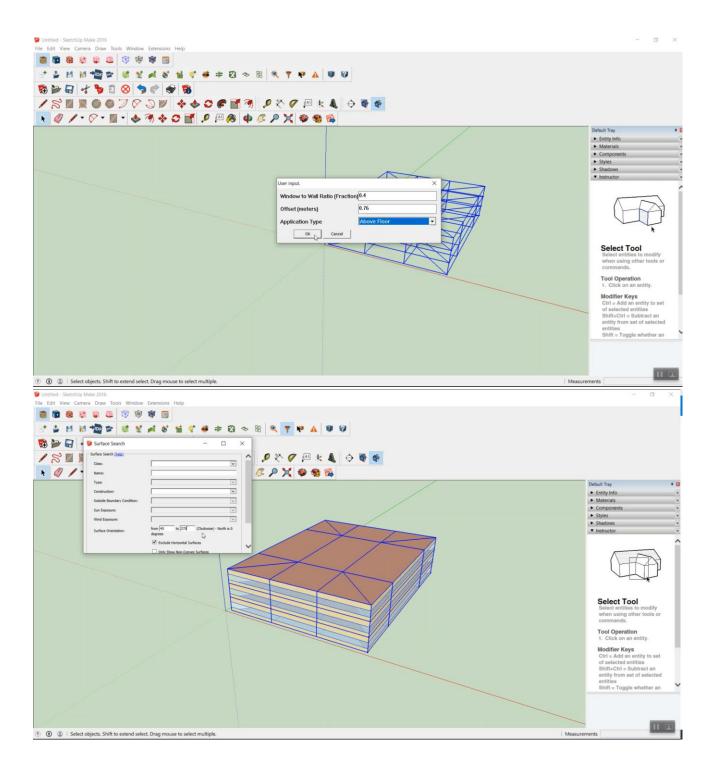


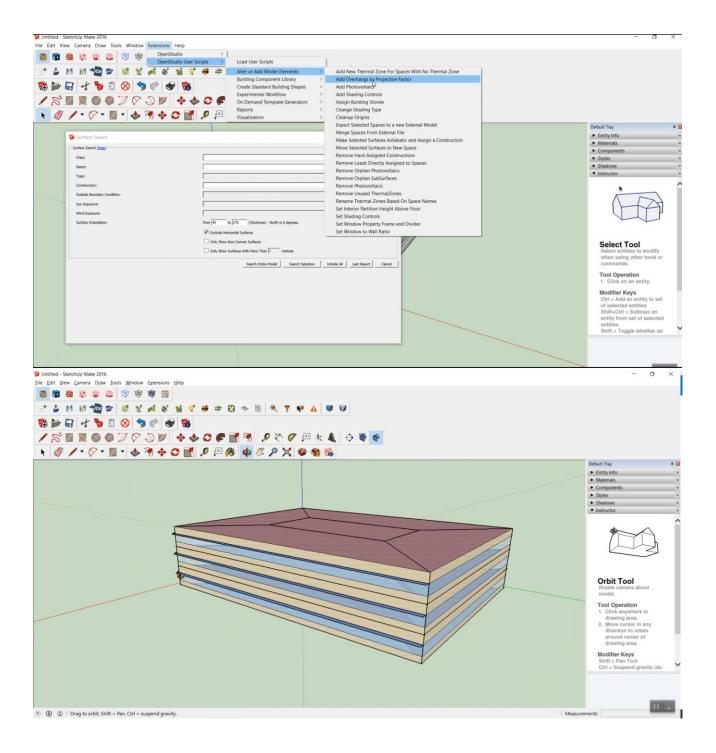


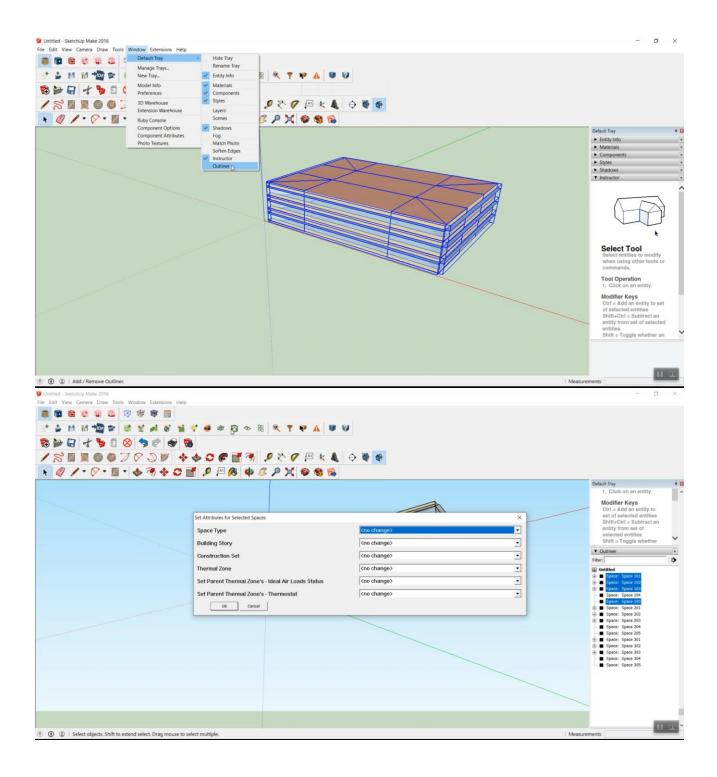


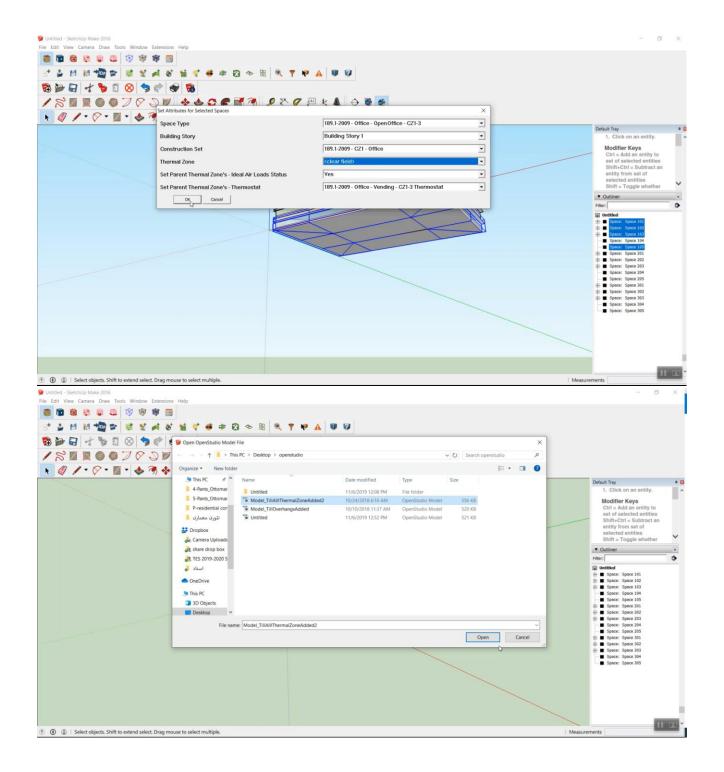


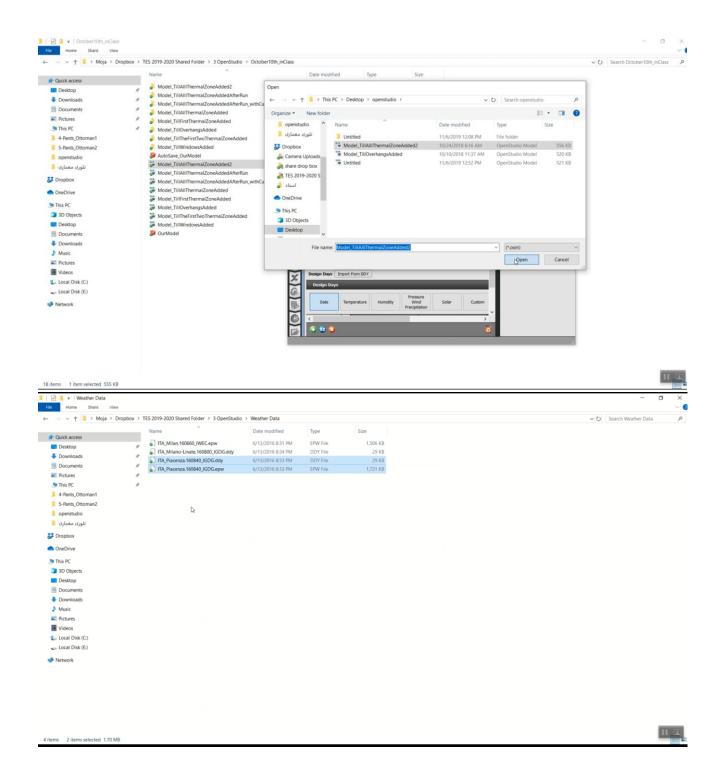


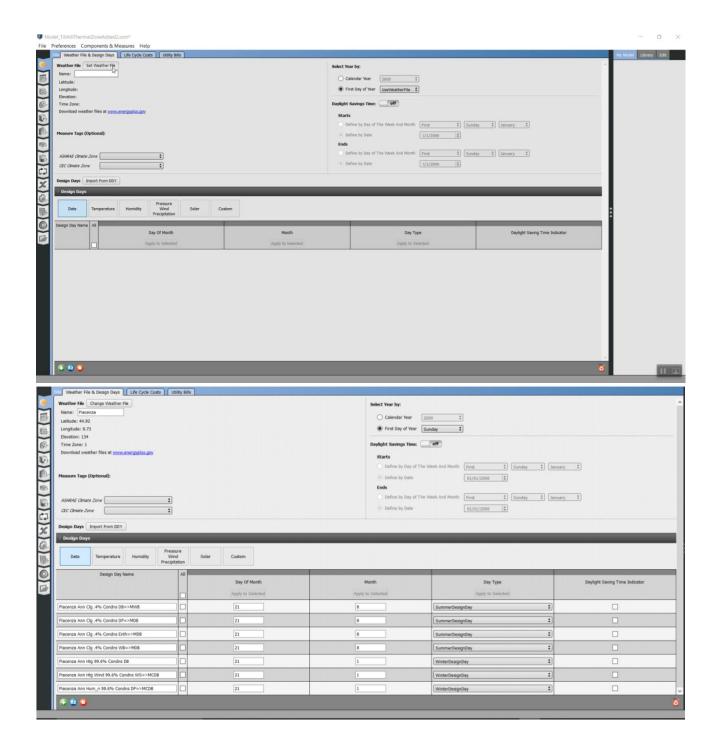


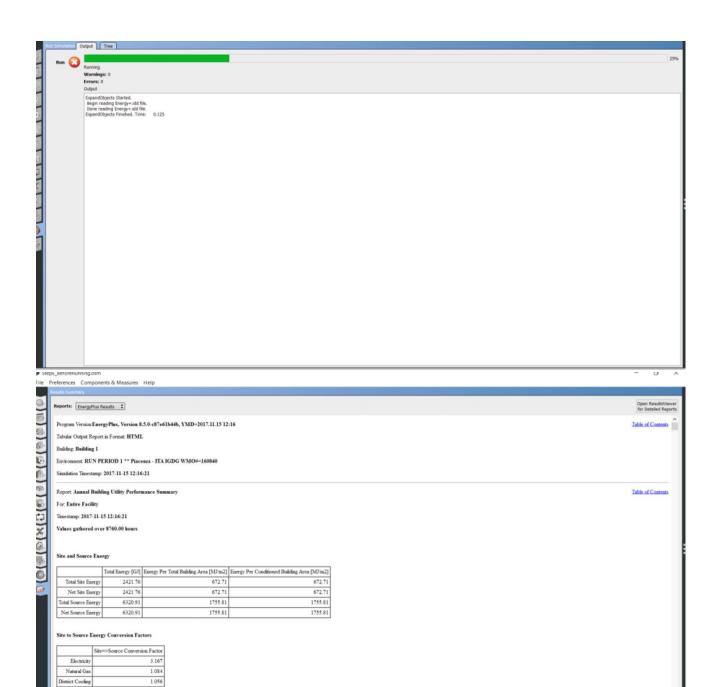












1.056

3.613

District Heating