

A 3 m high and 5 m wide wall consists of long **32 cm 22 cm** cross section horizontal bricks ($k = 0.72 \text{ W/m} \cdot ^\circ\text{C}$) separated by 3 cm thick plaster layers ($k = 0.22 \text{ W/m} \cdot ^\circ\text{C}$).

There are also 2 cm thick plaster layers on each side of the brick and a 3-cm-thick rigid foam ($k = 0.026 \text{ W/m} \cdot ^\circ\text{C}$) on the inner side of the wall. The indoor and the outdoor temperatures are 20°C and -10°C , and the convection heat transfer coefficients on the inner and the outer sides are $h_1 = 10 \text{ W/m}^2 \cdot ^\circ\text{C}$ and $h_2 = 40 \text{ W/m}^2 \cdot ^\circ\text{C}$, respectively. Assuming one-dimensional heat transfer and disregarding radiation, determine the rate of heat transfer through the wall.

$$R_i = \frac{1}{10 \times 0.25} = 0.4 \text{ } ^\circ\text{C/W}$$

$$R_f = \frac{0.03}{0.026 \times 0.25} = 4.62 \frac{^\circ\text{C}}{\text{W}}$$

$$R_{p_{up}} = R_{p_{down}} = \frac{L_{p_{c1}}}{k_p \times A_{p_{c1}}} = \frac{0.32}{0.22 \times 0.015} = 96.97 \frac{^\circ\text{C}}{\text{W}}$$

$$R_b = \frac{L_b}{k_b \times A_b} = \frac{0.32}{0.72 \times 0.22} = 2.02 \frac{^\circ\text{C}}{\text{W}}$$

$$\frac{1}{R_{tot_{parallel}}} = \frac{1}{R_b} + \frac{1}{R_{p_{up}}} + \frac{1}{R_{p_{down}}} = \frac{1}{2.02} + 2 \times \left(\frac{1}{96.97} \right) = 0.52 \text{ } ^\circ\text{C/W}$$

$$\rightarrow \frac{1}{R_{tot_{parallel}}} = 0.52 \text{ W}/^\circ\text{C} \rightarrow R_{tot_{parallel}} = \frac{1}{0.52} = 1.92 \text{ } ^\circ\text{C/W}$$

$$R_{P_1} = R_{P_2} = \frac{L_{p_1}}{k_p \times A_{p_1}} = \frac{0.02}{(0.22 \times 0.25)} = 0.363 \text{ } ^\circ\text{C/W}$$

$$R_{\downarrow o} = \frac{1}{h_o \times A} = \frac{1}{40 \times 0.25} = 0.1 \text{ } ^\circ\text{C/W}$$

$$R_{total} = R_i + R_o + 2 \times R_{P_1} + R_{tot_{parallel}} + R_{foam}$$

$$R_{total} = 7.78 \text{ } ^\circ\text{C/W}$$

$$Q = T/R_{total} = \frac{30}{7.78} = 3,86 \text{ W}$$

Finalize the composite wall question by finding the heat transfer rate

$$R_{total} = 6.81 \text{ }^{\circ}\frac{C}{W}$$

$$Q = T/R_{total} = \frac{30}{6.81} = 4,405W$$

Brick Thickness And Thermal Resistance does not increase equally proportionol

- Determine the overall unit thermal resistance (the R -value) and the overall heat transfer coefficient (the U -factor) of a wood frame wall that is built around 38-mm 90-mm wood studs with a center-to-center distance of 400 mm. The 90-mm-wide cavity between the studs is filled with Urithane rigid insulation. The inside is finished with 13-mm gypsum wallboard and the outside with 13 mm plywood and 13-mm 200-mm wood bevel lapped siding. The insulated cavity constitutes 75 percent of the heat transmission area while the studs, plates, and sills constitute 21 percent. The headers constitute 4 percent of the area, and they can be treated as studs.
- Find two R unit values.

	Wood	Insulation
Outside Air	0.03	0.03
Wood bevel l.	0.14	0.14
plywood(13mm)	0.11	0.11
Urithane Rigid foam Ins.	No	$0.98 \times 90 / 25 = 3.53$
Wood studs	0.63	No
Gypsum board	0.079	0.079
Inside surface	0.12	0.12

$$R'_{withWood} = 0.03 + 0.14 + 0.11 + 0.63 + 0.079 + 0.12 = 1.109 \text{ } m^2 \cdot ^{\circ}\frac{C}{W}$$

$$R'_{withIns} = 0.03 + 0.14 + 0.11 + 3.53 + 0.079 + 0.12 = 4.007 \text{ } m^2 \cdot ^{\circ}C/W$$