

WEEK 3 SUBMISSION

QUESTION 1:

In this week's assignment you should first finalize the composite wall question by finding the heat transfer rate, and then solve the same question while the thickness of the brick is increased to 32 cm and comment on the results

ANSWER 1:

$$k_{\text{brick}} = 0.72 \text{ W/m}^\circ\text{C}$$

$$k_{\text{plaster}} = 0.22 \text{ W/m}^\circ\text{C}$$

$$k_{\text{foam}} = 0.026 \text{ W/m}^\circ\text{C}$$

$$T_1 = 20^\circ\text{C}$$

$$T_2 = 10^\circ\text{C}$$

$$h_1 = 10 \text{ W/m}^2^\circ\text{C}$$

$$h_2 = 25 \text{ W/m}^2^\circ\text{C}$$

$$R_{\text{conv1}} = 1/h_1A = 1/10 \cdot (0.015 + 0.22 + 0.015) \cdot 1 = 0.4^\circ\text{C/W}$$

$$R_{\text{foam}} = L_{\text{foam}}/k_{\text{foam}}A = 0.03/0.026 \cdot (0.015 + 0.22 + 0.015) \cdot 1 \approx 4.6154^\circ\text{C/W}$$

$$R_{\text{plaster left}} = R_{\text{plaster right}} = L_{\text{plaster left}}/k_{\text{plaster}}A_{\text{plaster left}} = 0.02/0.22 \cdot (0.015 + 0.22 + 0.015) \cdot 1 = 3.6364^\circ\text{C/W}$$

$$R_{\text{plaster up}} = R_{\text{plaster down}} = L_{\text{plaster up}}/k_{\text{plaster}}A_{\text{plaster up}} = 0.16/0.22 \cdot 0.015 \cdot 1 \approx 48.4849^\circ\text{C/W}$$

$$R_{\text{brick}} = L_{\text{brick}}/k_{\text{brick}}A_{\text{brick}} = 0.16/0.72 \cdot 0.22 \cdot 1 \approx 1.101^\circ\text{C/W}$$

$$\therefore 1/R_{\text{total parallel}} = 1/R_{\text{plaster up}} + 1/R_{\text{brick}} + 1/R_{\text{plaster down}} = 1/48.4849 + 1/1.101 + 1/48.4849 \approx 0.9495^\circ\text{C/W}$$

$$\therefore R_{\text{total parallel}} = 1/0.9495 \approx 1.0532^\circ\text{C/W}$$

$$R_{\text{conv2}} = 1/h_2A = 1/40 \cdot (0.015 + 0.22 + 0.015) \cdot 1 = 0.1^\circ\text{C/W}$$

$$R_{\text{total}} = R_{\text{conv1}} + R_{\text{foam}} + R_{\text{plaster left}} + R_{\text{total parallel}} + R_{\text{plaster right}} + R_{\text{conv2}} = 0.4 + 4.6154 + 3.6364 + 1.0532 + 3.6364 + 0.1 = 13.4414^\circ\text{C/W}$$

$$\therefore Q = T_1 - T_2 / R_{\text{total}} = 20 - 10 / 13.4414 \approx 0.744 \text{ W}$$

If we increase the thickness of the brick to 32cm, then following the same procedures we had above, the result will be:

$$R_{\text{total}} = 14.4946^\circ\text{C/W}$$

$$\therefore Q = T_1 - T_2 / R_{\text{total}} = 20 - 10 / 14.4946 \approx 0.69 \text{ W}$$

So, from the result we could see that by just increase the thickness of the brick will not significantly increase the thermal resistance of the wall.

QUESTION 2:

You should solve again the simplified wall calculation procedure replacing the glass fiber one with urethane rigid foam and while replacing the fiberboard with plywood and find

the two R_{unit} values

ANSWER 2:

We could find the R values by checking table:

Outside Air	0.03
Wood Bevel(13mm*200mm)	0.14
Glass fiber	$0.7 \times 90 / 25 = 2.52$
Urethane Rigid Foam Ins.(90mm)	$0.98 \times 90 / 25 = 3.528$
Mineral fiber batt(90mm)	$0.66 \times 90 / 25 = 2.376$
Wood Stud(90mm)	0.63
Plywood(13mm)	0.11
Gypsum Board(13mm)	0.079
Inside Surface	0.12

When replacing the glass fiber with Urethane rigid foam,

$$R_{\text{foam}} = 0.03 + 0.14 + 3.528 + 2.376 + 0.63 + 0.079 + 0.12 = 6.903^{\circ}\text{C/W}$$

When replacing the fiberboard with plywood,

$$R_{\text{plywood}} = 0.03 + 0.14 + 2.52 + 2.376 + 0.63 + 0.11 + 0.12 = 5.926^{\circ}\text{C/W}$$