

1 Introduction

A concurrent datatype is ... A concurrent datatype offers encapsulation of concurrency and makes writing concurrent programs simpler.

For example, the `MenWomen` object is a concurrent datatype that captures a classical synchronization problem. In this problem, some processes need to pair with other processes by exchanging their identities. Figure 1 is an interface of a concurrent datatype for the `MenWomen` problem.

```
trait MenWomenT{  
  def manSync(me: Int): Int  
  def womanSync(me: Int): Int  
}
```

Figure 1: Interface

The safety and liveness properties are essential to the correctness of concurrent datatypes. The safety property states that the behaviour of the concurrent object should observe some invariant. For example, if a process with identity 1 calling `manSync` returns 2, then the process with identity 2 should call `womanSync` and return 1. The liveness property states that the concurrent object should not refuse to synchronize when a synchronization is possible between one or more processes. For example, a system with one process calling `manSync` and one process calling `womanSync` should not deadlock.

In this paper, we examine the above two correctness properties for various concurrent datatypes. In addition, we provide a few CSP implementations for objects commonly used in concurrent programming, which can be used in future CSP projects.

1.1 Linearization test

To verify the correctness of a concurrent datatype, one can carry out the Linearization test described in [TODO: Reference]. The linearization testing framework measures each call's starting and returning time to get a history of function calls and returns. Then for the observed history, the testing framework attempt to find a series of synchronization point that obeys the safety property. If the framework can not find a valid synchronization point series, then the concurrent datatype implementation is wrong.

In this remaining section we shall look at a few history from the `MenWomen` object. The timeline in Figure 2 visualizes the function call history of two process `T1` and `T2`. `T1` first calls `manSync`, then `T2` calls `womanSync`. A synchronization occurs between `T1` and `T2`. `T1` returns the identity of process `T2` then `T2` returns the identity of process `T1`.

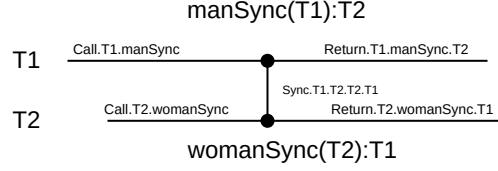


Figure 2: Visualized history of T1 calling `manSync` and T2 calling `womanSync`

In Figure 3, both processes calls `manSync`, and no synchronization is possible. Note that the liveness condition is not invalidated even if the system deadlocks in this case.

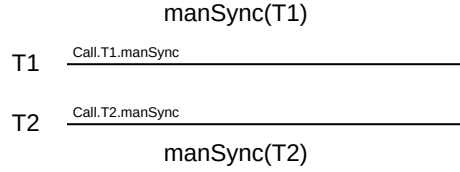


Figure 3: Visualized history of both T1 and T2 calling `womanSync`

Scheduling is one of the reasons validating a history can be complicated. In Figure 4, process T3 calls `manSync` first but gets descheduled. Then T1 calls `manSync` and synchronizes with T2 which later calls `womanSync`. To find a valid series of synchronization point, the linearization framework usually needs to search a large state.

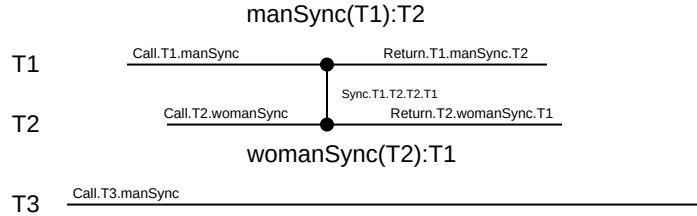


Figure 4: Visualized history of T3 get descheduled

1.2 Checking safety property using CSP

The history can be captured as a trace of a CSP system. In addition to performing the function body, each function call sends a `Call` event before the function body and a `Return` event after the function body. Figure 5 is the definition of `Call` and `Return` channel in CSP. The definition of the channel usually need to include the identity of the calling process, the function called, and its parameter.

```

--identity of the calling process
--function called by the process
channel Call : TypeThreadID . TypeOps
--identity of the calling process
--function called by the process
--return value of the function call
channel Return: TypeThreadID . TypeOps . TypeThreadID

```

Figure 5: Definition of call

To check the safety property, we check that a testing system built from some processes using the concurrent datatype refines a specification process built from the object definition in CSP trace model.

A generic and scalable system is used for the testing system to generate possible histories of processes using concrete datatype. Each process in the testing system can call any function from the concurrent object with any arguments allowed. It is important each process can choose to terminate. Otherwise, the testing system only models a system that runs forever, given that there is no deadlock. We shall see how this affects bug finding in a concurrent datatype in later objects.

The specification generates all valid histories. The process uses the same number of linearizer processes synchronizing on events from the **Sync** channel. Event from the **Sync** channel should include information from all participating processes, and Figure 6 is the **Sync** channel definition for ... Each linearizer process repeatedly calls a function, synchronize with zero or some processes, and returns according to the calling argument and extra information from the synchronization point. To match the definition of the generic and scalable testing system, each linearizer process can also choose to terminate.

```

--Identity of thread calling ManSync
--Return of ManSync
--Identity of thread calling WomanSync
--Return of WomanSync
channel Sync: TypeThreadID . TypeThreadID . TypeThreadID . TypeThreadID

```

Figure 6: Definition of call

We shall see a concrete testing system and specification process in the Men-Women section.

1.3 Checking liveness property using CSP

For liveness property, we check the same generic and scalable testing system refines the same specification process, but in the failure model. Suppose all

process calls `manSync`. Since a linearizer process calling `manSync` sends `Return` event only after synchronizing `Sync` event with another linearizer process calling `womanSync`, the linearizer will refuse to return any function call, which is an expected behavior. One can use a datatype-specific specification process that does not explicitly use any synchronization points. However, reusing the linearizer process is easier.

2 Common Objects

2.1 Shared Variable

The usage of shared variables is common in concurrent datatypes. For example, some concurrent datatypes may temporarily store the identity of a waiting process. However, CSP is more like a functional programming language and does not support mutable variables.

A recursive process in CSP can capture the behaviour of a shared variable. The recursive process holds the value of the variable in its parameter. At any time, the variable process is willing to answer a query for the variable value in channel `getValue`. Alternatively, the process can receive an update on the variable value in channel `getValue`, after which the function recurses with the new variable value.

Because it is natural for a concurrent datatype to use multiple shared variables, the global variable is implemented as a CSP module in Figure 7 to allow better code reuse. The module requires two parameters. `TypeValue` is the set of possible values for the variable, and `initialValue` is the value before any process modifies the variable. An uninitialized variable module is also available in the same Figure 7, with the only difference that the variable non-deterministically chooses an initial value from `TypeValue` at start time. `runWith` is a convenient helper function to run a given process `P` with the `Var` process. If the parameter `hide` is true, `runWith` function hides all events introduced by the shared variable. In later chapters, we will see how the `runWith` function helps reduce the code complexity of the synchronization object implementation.

Figure 8 is an example of two processes using a shared variable. The first line in the example creates a shared variable `VarA` with value ranging from 0 to 2 and initialized with 0. Process `P` increments `VarA` modulo 3 forever and process `Q` reads `VarA` forever. Process `P` interleaves with process `Q`, and the combined process is further synchronized with the variable `VarA` process. In the resulting process `System`, changes to `VarA` made by process `P` is visible to process `Q`.

2.2 Semaphore

A Semaphore is a simple but powerful concurrent primitive. This thesis shall describe and use a simplified binary semaphore from [TODO: Reference], which removes interrupts and timeout operations.

```

--set of possible value for the variable
--initil value for the variable
module ModuleVariable(TypeValue, initialValue)
  Var(value) = getValue!value → Var(value)
               □ setValue?value → Var(value)
  chanset = {getValue, setValue}
exports
  --(Bool, Proc) → Proc
  runWith(hide,P) = if hide then (Var( initialValue ) [|chanset|] P) \ chanset
                     else Var( initialValue ) [|chanset|] P
  channel getValue, setValue: TypeValue
endmodule

module ModuleUninitVariable(TypeValue)
  Var(value) = getValue!value → Var(value)
               □ setValue?value → Var(value)
  chanset = {getValue, setValue}
exports
  runWith(hide,P) =
    if hide then ((~| x:TypeValue • Var(x)) [| chanset |] P) \ chanset
    else (~| x:TypeValue • Var(x)) [| chanset |] P
  channel getValue, setValue: TypeValue
endmodule

```

Figure 7: CSP implementation of global variable process module

A binary semaphore can either be raised or lowered. A **down** function call raises the semaphore regardless of the semaphore state. If a process calls the **down** method when the semaphore is raised, the semaphore becomes unraised. However, if the semaphore is unraised, the process waits until another process calls **up** and proceeds to put down the semaphore. Depending on the initial state of the semaphore, a binary semaphore can be further categorized as a mutex semaphore or a signalling semaphore.

Modelling a semaphore is simple in CSP. A process may call **up** function or **down** function via channel **upChan** or channel **downChan** respectively. The semaphore is modelled by a process implemented by two mutually recursive functions **Semaphore(True)** and **Semaphore(False)**. The semaphore process representing an unraised state accepts a **upChan** event by any process and proceeds to the raised process. The semaphore process representing a raised state can either accept a **upChan** event and recurse to the raised process, or accept a **downChan** event and proceed to the unraised process.

Like the shared variable in the earlier subsection, the semaphore is encapsulated in a CSP module. To create a semaphore, one needs to supply two arguments. **TypeThreadID** is the set of identities of processes that use this semaphore.

```

instance VarA = ModuleVariable({0..2},0)
P = VarA::getValue? a → VarA::setValue!((a+1)%3) → P
Q = VarA::getValue? a → Q
System = VarA::runWith(false,P||Q)

```

Figure 8: CSP Example of a process using a shared variable

`initialState` is a boolean value indicating the starting state of the semaphore. If `initialState` is true, the semaphore is raised initially. Otherwise, the semaphore is lowered.

```

module ModuleSemaphore(TypeThreadID, initialState)
  --Raised
  Semaphore(True) = downChan? id → Semaphore(False)
                  □ upChan? id → Semaphore(True)
  --Unraised
  Semaphore(False) = upChan? id → Semaphore(True)

  chanset = {upChan, downChan}
exports
  --runWith::(Bool,Proc) → Proc
  runWith(hide,P) = (Semaphore [| chanset |] P) \
                    (if hide then chanset else {})
  channel upChan, downChan: TypeThreadID
endmodule

```

Figure 9: Implementation of a binary semaphore in CSP

2.3 Monitor

A Monitor is another powerful concurrent primitive. This thesis will also use a simplified monitor from [TODO:reference].

Usually, code protected by the monitor is wrapped inside a `synchronized` block. In Figure 10, `op1` uses `synchronized` to prevent race condition on the variable `a`. To run a `synchronized` block in CSPM, the process first needs to synchronize with the monitor process on a `waitEnter` event, which works as a certificate to run code inside block. After running the code inside `synchronized` block, the process sends a `Exit` event to notify the monitor process that it is exiting.

Inside a `synchronized` block, the process can also perform `wait`, `notify`, and `notifyAll`. The method `op2` in Figure 10 first increments `b`, wait to be notified, and decrements `b`. So the shared variable `b` here counts the number of processes waiting to be notified. The method `op3` notifies one waiting process and `op4` notifies all waiting processes.

```

class MonitorExample {
  private var a = 0;
  def op1():Unit = synchronized{
    a+=1;
  }

  private var b = 0;
  def op2():Unit = synchronized{
    b+=1;
    wait();
    b-=1;
  }

  def op3():Unit = synchronized{
    notify ();
  }

  def op4():Unit = synchronized{
    notifyAll ();
  }
}

```

Figure 10: Description

In the CSP implementation, a waiting process first synchronizes a **Wait** event with the monitor process to indicate that the process calls **wait** and no longer hold the running certificate. The process can then be waked up with **waitNotify** or spuriously by a event **SpuriousWake** from the monitor process. Finally the process needs to reobtain the certificate **WaitEnter** to resume execution. In practice, the **wait** function is often guarded with a while loop to prevent spurious wakeup. Again CSPM does not have a built-in while loop, and a generic while statement is implemented in continuation pass style. (Maybe leave this continuation pass style while loop in appendix?)

Note that both **WaitNotify** and **SpuriousWake** events come from the monitor process. And when a process calls **notify** or **notifyAll**, it needs to synchronize with the monitor process. This is because normally a process does not know how many processes are waiting. If a process calling **notify** directly synchronizes with a waiting process, then the notifying process will block if there are no waiting process. Similarly a process calling **notifyAll** does not know how many process it should wake up.

The monitor process has two states. The monitor process allows different set of events in two different states. When there is no running process, the monitor can allow a free process to enter its synchronized block by synchronizing on a **waitEnter** event with the process. When there is a running process, the

server process should respond to method calls from the running process, but the monitor should not allow another process to obtain the monitor lock. In either state, the monitor process can spuriously wake up a waiting process.

//Should I split some functions into respective paragraphs here. Or use line number.

```

module ModuleMonitor(ThreadsID)
channel
  Notify, NotifyAll, Exit, Wait,
  WaitNotify, WaitEnter, SpuriousWake: ThreadsID

chanset = { Notify, NotifyAll, Exit, Wait, WaitNotify, WaitEnter, SpuriousWake }

--A list of event for every event e in s
repeat(ch, s) =
  if s={} then SKIP
  else ch? a:s → repeat(ch, diff(s, {a}))

--cur is current active running thread
--waiting is a set of threads waiting to be notified
active(cur, waiting) =
  --current running thread notify
  Notify.cur → (
    if waiting={} then
      --do nothing if no thread is waiting
      active(cur, {})
    else
      --wakeup a process
      WaitNotify? a:waiting →
        active(cur, diff(waiting, {a}))
  ) □
  --current running thread notifyAll
  NotifyAll.cur → (
    repeat(WaitNotify, waiting);
    active(cur, {})
  ) □
  --current running thread exit
  Exit.cur → (
    inactive(waiting)
  ) □
  --current running thread wait
  Wait.cur → (
    inactive(union(waiting, {cur}))
  ) □
  --spurious wakeup
  waiting ≠ {} & SpuriousWake? a:waiting → (

```



```

    active(cur, diff(waiting, {a}))
  )

--when no active thread is running
inactive(waiting) =
  --pick a thread that is ready to enter
  WaitEnter? a → (
    active(a, waiting)
  ) □
  --spurious wakeup
  waiting ≠ {} & SpuriousWake? a:waiting → (
    inactive(diff(waiting, {a}))
  )

exports
  --Given a process that uses the monitor
  --Return the process synchronized with the monitor server process
  --If hide is true, monitor channels are hidden
  runWith(hideSpurious, hideInternal, P) =
    let hideset0 = if hideInternal then chanset else {} within
    let hideset1 = if hideSpurious then hideset0 else diff(hideset0, {SpuriousWake}) within
    (inactive({}) [|chanset|] P) \ hideset1

  --java-like synchronized function
  synchronized(me, P)=
    WaitEnter.me →
    P;
    Exit.me →
    SKIP

  enter(me) =
    WaitEnter.me →
    SKIP

  exit(me) =
    Exit.me →
    SKIP

  --notify()
  notify(me) =
    Notify.me →
    SKIP

  --notifyAll()
  notifyAll(me) =

```

```

NotifyAll . me →
SKIP

--wait()
wait(me) =
  Wait . me → ((
    WaitNotify . me →
    WaitEnter . me →
    SKIP
  ) □ (
    SpuriousWake . me →
    WaitEnter . me →
    SKIP
  )
)

whileWait(me,cond) =
  while(cond)(wait(me);SKIP)
endmodule

```

Figure 11: Implementation of Monitor in CSP

3 MenWomen

For simplicity, a process calling **ManSync** is called a man process, and a process calling **WomanSync** is called a woman process.

3.1 Implementation

One way to implement the MenWomen object is to use a monitor and a shared variable indicating the stage of synchronization. Figure 12 is a Scala implementation of the MenWomen object with monitor.

- A man process enters the synchronization and waits until the current stage is 0. Then in stage 0, the man process sets the global variable **him** inside the **tMenWomen** object to its identity. Then the man process notifies all processes so that a waiting woman process can continue. Finally, the man process waits for stage 2.
- A women process enters the synchronization and waits until the current stage is 1. The woman process sets the global variable **her** to its identity and returns the value of global variable **him**.
- In stage 2, the waiting man process in stage 0 is wakened up by the woman process in stage 1. The man process notifies all waiting processes and returns the value of **her**.

The code snippet in Figure 12 is a Scala implementation of the MenWomen process using a monitor by Gavin Lowe. With the shared variable and monitor module, the Scala code is further translated to a CSP code in Figure 13. With the convention described in the introduction section, every function call begins with a Call event containing all parameters. And every function call ends with a Return event containing the return value.

```
class MenWomen extends MenWomenT{
  private var stage = 0
  private var him = -1
  private var her = -1

  def manSync(me: Int): Int = synchronized{
    while(stage != 0) wait()
    him = me; stage = 1; notifyAll()
    while(stage != 2) wait()
    stage = 0; notifyAll(); her
  }

  def womanSync(me: Int): Int = synchronized{
    while(stage != 1) wait()
    her = me; stage = 2; notifyAll();
  }
}
```

Figure 12: Scala implementation of the MenWomen process using a monitor

```
instance VarStage = ModuleVariable({0,1,2},0)
instance VarHim = ModuleUninitVariable(ThreadID)
instance VarHer = ModuleUninitVariable(ThreadID)
instance Monitor = ModuleMonitor(ThreadID)
manSync(me) =
  Call ! me! ManSync →
  Monitor::enter(me);
  Monitor::whileWait(me, \ ktrue,kfalse •
    VarStage::getValue?x →
    if x≠0 then ktrue else kfalse
  );
  VarHim::setValue! me →
  VarStage::setValue! 1 →
  Monitor::notifyAll (me);
  Monitor::whileWait(me, \ ktrue,kfalse •
    VarStage::getValue?x →
    if x≠2 then ktrue else kfalse
  );
```

```

    VarStage::setValue ! 0 →
    Monitor::notifyAll (me);
    VarHer::getValue ? ans →(
    Monitor::exit (me);
    Return ! me ! ManSync ! ans →
    SKIP
    )
womanSync(me)=
    Call ! me ! WomanSync →
    Monitor::enter(me);
    Monitor::whileWait(me, \ ktrue,kfalse •
        VarStage::getValue ? x →
        if x≠1 then ktrue else kfalse
    );
    VarHer::setValue ! me →
    VarStage::setValue ! 2 →
    Monitor::notifyAll (me);
    VarHim::getValue ? ans →(
    Monitor::exit (me);
    Return ! me ! WomanSync ! ans →
    SKIP
    )

```

Figure 13: CSP implementation of the MenWomen

3.2 Linearization Test

Recall that in the testing system, each process can call any function provided by the concurrent datatype or choose to terminate. In the CSP implementation a helper function is used. `chaosP(P)` runs the process `P` that terminate with `SKIP` any number of time. With the helper function, the process `P` only needs to non-deterministically choose to perform `manSync` or `womanSync` with its identity.

All processes in the testing system interleaves with other processes and synchronize with the processes of shared variables and the process of the monitor. Since the testing system should only include `Call` and `Return` events, all other events are hidden using the first two boolean flags in `runWith` defined in earlier subsection.

```

Thread(me)=chaosP(manSync(me) □ womanSync(me))
System(All)=runWith(True,True,||| me:All • Thread(me))

```

Figure 14: CSP implementation of the testing processes and system

Similarly, a linearizer process can non-deterministically choose to perform `manSync`, synchronize with another linearizer process calling `womanSync`, and

return with the identity it received from the **Sync** event. Also, the linearizer can choose to call **womanSync** or terminate. **Linearizers(All)** puts all linearizers processes in parallel.

The **Linearizers** function creates a combined linearizer process in three steps. First it put all linearizer process in parallel using Replicated Generalized Parallel in CSPM. Specifically, General Parallel uses three argument, the linearizer identity set, the linearizer process, and a synchronization alphabet set. The synchronization alphabet set for a process identity is the set of **Sync** event where the process identity appears on first or third argument. If the a linearizer process wants to send a event in its synchronization alphabet set, the process must synchronize with all other linearizer process whose synchronization alphabet set include this event. Then **Linearizers** runs the paralleled process with the specification process of **Sync** event. For **MenWomen** object, the synchronization is stateless and only requires the return value is the identity of the other process. Finally, like the testing system, all **Sync** event are hidden to provide all valid histories.

```

Lin(All,me)= (
  Call ! me! ManSync →
  Sync ! me? mereturn ? other? otherreturn →
  Return ! me! ManSync! mereturn →
  Lin(All,me)
)□(
  Call ! me! WomanSync →
  Sync ? other? otherreturn ! me? mereturn →
  Return ! me! WomanSync! mereturn →
  Lin(All,me)
)□STOP

LinEvents(All,me)=union({
  ev | ev←{Sync},
  let Sync.t1.a.t2.b=ev within
    countList(me,<t1,t2>)=1 and
    member(t1, All) and
    member(t2, All)
}, {Call.me, Return.me})

Linearizers (All)=(|| me: All • [LinEvents(All,me)] Lin(All,me)) [|{Sync}|] Spec)
\ {Sync}

```

Figure 15: CSP implementation of the testing processes and system

Figure 16 visualizes how the linearizer process can generate the trace that corresponds to the history described in Figure 2, where one process calls **manSync** and another process calls **womanSync**. And 17 visualizes the linearizer deadlocks

as required if both processes calls `manSync`.

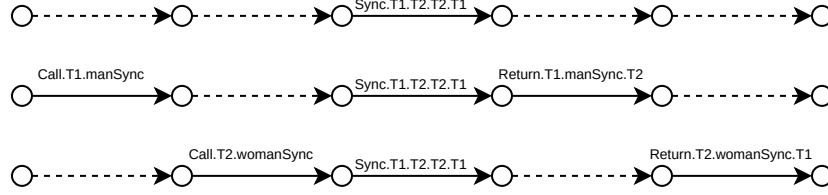


Figure 16: Linearizers generating the history where one process calls `manSync` and another process calling `womenSync`

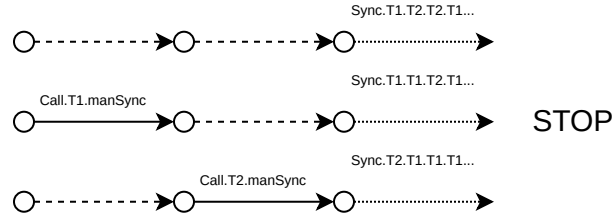


Figure 17: Linearizers generating the history where one process calls `manSync` and another process calling `womenSync`

Finally, we perform the test using trace refinement for safety property and failure refinement for liveness. As expected, the correct implementation passes all tests.

```
System2=System({T1,T2})
Spec2Thread=Linearizers({T1,T2})
assert Spec2Thread  $\sqsubseteq_T$  System2
assert Spec2Thread  $\sqsubseteq_F$  System2

System3=System({T1,T2,T3})
Spec3Thread=Linearizers({T1,T2,T3})
assert Spec3Thread  $\sqsubseteq_T$  System3
assert Spec3Thread  $\sqsubseteq_F$  System3
```

Figure 18: CSP implementation of the testing processes and system

3.3 A faulty version

We shall examine another MenWomen implementation in Figure 19. One key difference in this faulty MenWomen object is that it uses `Option` data in the

shared variables to store the identity of the process calling `manSync` and the process calling `womanSync`.

```
class FaultyMenWomen extends MenWomenT{
  private var him: Option[Int] = None
  private var her: Option[Int] = None

  def manSync(me: Int): Int = synchronized{
    while(him.nonEmpty) wait()
    him = Some(me); notifyAll()
    while(her.isEmpty) wait()
    val Some(res) = her
    her = None; notifyAll()
    res
  }

  def womanSync(me: Int): Int = synchronized{
    while(her.nonEmpty) wait()
    her = Some(me); notifyAll()
    while(him.isEmpty) wait()
    val Some(res) = him
    him = None; notifyAll()
    res
  }
}
```

Figure 19: Faulty Scala implementation of MenWomen object

The safety property test shows that this implementation handles scheduling carelessly. This implementation fails the test $\text{Spec2Thread} \sqsubseteq_T \text{System2}$, and FDR provides a trace that violates the safety property specification, shown in Figure 20. FDR further allows the user to expand the hidden τ events in the testing system, which are normally processes' interaction with shared variable and monitor. By understanding the expanded trace in CSP, we can find an equivalent way to trigger the bug in Scala.

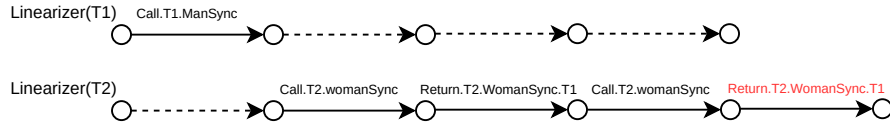


Figure 20: Trace

- A process `T1` calls `manSync`. On first line, since the shared variable `him` is initially `None`, `T1` skips the `wait`, set `him` to `Some(T1)` and waits for a process calling `womanSync`.

- A process **T2** calls **womanSync** and returns **T1**. At this stage, there is no waiting process waiting to run **womanSync** and the shared variable is not **None**. So **T2** does not wait at any point, notifies all waiting process, and returns.
- Before **T1** reenters the **synchronized** block, process **T2** calls **womanSync** again. **him** has not been reset by **T1** yet. So **T2** pairs with **T1** again, which should not be allowed.

4 ABC

With an ABC object, three processes can exchange data with each other two processes. More specifically, one process calling **aSync**, one process calling **bSync**, and one process calling **cSync** synchronizes. Then each of the three processes returns with the arguments of two other processes. For simplicity, we shall call a process calling **syncA** as an A-process, a process calling **syncB** as a B-process, and a process calling **syncC** as a C-process.

One of the challenges to check an ABC object is the large number of states in the CSP model. In this section, we shall see how the linearizer process can be optimized and the efficiency of a explicit linearization point test.

4.1 Implementation

Figure 21 is a Scala implementation of a ABC object with semaphore. In each round of synchronization,

- Initially semaphore **aClear** is raised. An A-process acquires semaphore **aClear**, sets the shared variable **a** to its parameter, raises semaphore **bClear** and waits to acquire semaphore **aSignal**. A B-process and a C-process behaves similarly in turn, except they use different semaphores and shared variables.
- After a C-process raises semaphore **aSignal**, the A-process is able to continue. The A-process reads the shared variable **b** and **c**, raises the semaphore **bSignal**, and returns **b** and **c**. Likewise, B and C also take the value of two other shared variable and raise respective semaphores in turn.

Using the shared variable and semaphore module, it is easy to translate the Scala implementation to a CSP implementation.

```
class ABC[A,B,C] extends ABCT[A,B,C]{
  // The identities of the current (or previous) threads.
  private var a: A = _
  private var b: B = _
  private var c: C = _

  // Semaphores to signal that threads can write their identities .
```



```

private val aClear = MutexSemaphore()
private val bClear, cClear = SignallingSemaphore()

// Semaphores to signal that threads can collect their results .
private val aSignal, bSignal, cSignal = SignallingSemaphore()

def syncA(me: A) = {
  aClear.down      // (A1)
  a = me; bClear.up // signal to b at (B1)
  aSignal.down     // (A2)
  val result = (b,c)
  bSignal.up       // signal to b at (B2)
  result
}

def syncB(me: B) = {
  bClear.down      // (B1)
  b = me; cClear.up // signal to C at (C1)
  bSignal.down     // (B2)
  val result = (a,c)
  cSignal.up       // signal to c at (C2)
  result
}

def syncC(me: C) = {
  cClear.down      // (C1)
  c = me; aSignal.up // signal to A at (A2)
  cSignal.down     // (C2)
  val result = (a,b)
  aClear.up        // signal to an A on the next round at (A1)
  result
}
}

```

Figure 21: Scala implementation of the ABC using semaphores

4.2 Testing

Similar for the MenWomen object, a testing system is defined through any number of working processes and a specification is built from a `Sync` channel, linearizer processes, and a synchronization alphabet set.

One key difference of method in `ABC` object is that processes can call with any argument from the set `TypeData`, whereas in `MenWomen` object, processes can only call with their identity. As shown in Figure 22 So inside `chaosP`, the processes also chooses an argument with general non deterministic choice.

```

Thread(me)=chaosP(
  □x:TypeData • (
    SyncA(me,x)
    □ SyncB(me,x)
    □ SyncC(me,x)
  )
)

```

Figure 22: Definition of processes in the testing system.

Using the standard linearization testing technique, the `Sync` channel in Figure 23 is used to represent the synchronization of three involved threads. For example, the event $Sync.t_1.a.b.c.t_2.d.e.f.t_3.g.h.i$ represents the synchronizations of three threads, t_1, t_2, t_3 , in which the first process t_1 calls `aSync` with a and returns (b, c) , the second process t_2 calls `bSync` with d and returns (e, f) , and last process t_3 calls `cSync` with g and returns (h, i) . The `Sync` specification process, shown in the same figure, should then check that for each synchronization point, the return value of each functional call is the pair of arguments of the two other function call. Finally a linearizer process is defined in a similar format.

```

--thread identity calling ASync. ASync parameter a. ASync return pair (b,c)
--thread identity calling BSync. BSync parameter b. BSync return pair (a,c)
--thread identity calling CSync. CSync parameter c. CSync return pair (a,b)
channel Sync: TypeThreadID . TypeData . TypeData . TypeData .
              TypeThreadID . TypeData . TypeData . TypeData .
              TypeThreadID . TypeData . TypeData . TypeData

Spec = Sync ? aid ? a ? b ? c
      ? bid : diff (TypeThreadID, {aid}) ! b ! a ! c
      ? cid : diff (TypeThreadID, {aid, bid}) ! c ! a ! b
      → Spec

```

Figure 23: Definition of `Sync` channel and `Sync` specification for linearizers

4.2.1 Speeding up model compilation

Consider the specification process with three processes. Let M be the size of the set of all possible arguments. Consider the trace in Figure 26, where process `T1` calls `aSync` with `A`, `T2` calls `bSync` with `B`, `T3` calls `cSync` with `C`. Then they synchronization.

```

--Linearizer for a process
Lin(All,me)=(
  --me synchronizes as thread A
  Call ! me!ASync? a →
  Sync ! me!a? b? c? t2:diff(All,{me})? t2b? t2a? t2c? t3:diff(All,{me,t2})? t3c? t3a? t3b →
  Return ! me!ASync! b! c →
  Lin(All,me)
) □ (
  --me synchronizes as thread B
  Call ! me!BSync? b →
  Sync ? t2:diff(All,{me})? t2b? t2a? t2c! me! b? a? c? t3:diff(All,{me,t2})? t3c? t3a? t3b →
  Return ! me!BSync! a! c →
  Lin(All,me)
) □ (
  --me synchronizes as thread C
  Call ! me!CSync? c →
  Sync ? t2:diff(All,{me})? t2b? t2a? t2c? t3:diff(All,{me,t2})? t3a? t3b! me! c? a? b →
  Return ! me!CSync! a! b →
  Lin(All,me)
)

```

Figure 24: Definition of linearizer process

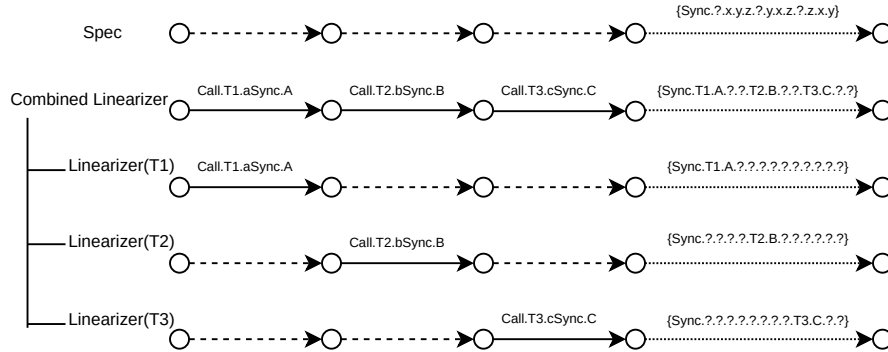


Figure 26:

The last transition in the diagram is the **Sync** event between three processes. Above the edge is the set of possible **Sync** event that every process accepts. Each linearizer accepts $3^2 * M^8$ possible **Sync** event. The combined linearizer accepts M^6 sync event. However, according to the sync specification, only one **Sync** event is valid.

With the above analysis, it is tempting to reduce the redundancy in **Sync**

```

System3=System({T1,T2,T3})
System4=System({T1,T2,T3,T4})
System5=System({T1,T2,T3,T4,T5})

Spec3Thread=Linearizers({T1,T2,T3})
Spec4Thread=Linearizers({T1,T2,T3,T4})
Spec5Thread=Linearizers({T1,T2,T3,T4,T5})

assert Spec3Thread  $\sqsubseteq_T$  System3
assert Spec4Thread  $\sqsubseteq_T$  System4
assert Spec5Thread  $\sqsubseteq_T$  System5

assert Spec3Thread  $\sqsubseteq_F$  System3
assert Spec4Thread  $\sqsubseteq_F$  System4
assert Spec5Thread  $\sqsubseteq_F$  System5

```

Figure 25: Test

event. optimize the individual lineariser by using the information from the specification process. Instead of choosing all possible remaining arguments, the individual lineariser could choose arguments that are correct according to the specification process. Figure 27 includes part of the simplified code. This change does not reduce the number of transitions in the resulting specification, but it helps FDR build the process faster.

```

channel Sync: TypeThreadID . TypeThreadID . TypeThreadID .
                TypeData . TypeData . TypeData

Lin(All,me)= (
  Call ! me!ASync? a →
  Sync ! me? t2:diff(All,{me})? t3:diff(All,{me,t2}) ! a? b? c →
  Return ! me!ASync! b! c →
  Lin(All,me)
) ...

```

Figure 27: Simplified definition of Sync channel and part of simplified linearizer

With the above optimization, the testing finishes quickly for both test cases.

4.3 Faulty version

Recall that in Java and Scala, raising a semaphore immediately allows another thread waiting to acquire the semaphore to continue. So it is essential to take a copy of the two other arguments before raising the semaphore.

On the other hand, what if the implementation of `syncA` does not take a copy of the argument? It turns out that the faulty `ABC` object passes tests for three processes but fails the linearisation test with at least four threads.

4.3.1 Explanation of the error case

For the test `Spec4Thread` \sqsubseteq_T `System4`, FDR displays a trace of the testing system that violates the specification. From the trace, it seems that process `T1` synchronizes with `T2` and `T3` in the first round, and should return `(B,C)`, but `(E,F)`, the argument in the second round is returned. By expanding the τ event and translate CSP traces into program traces, it is possible to see what goes wrong in the faulty version when there are four threads.

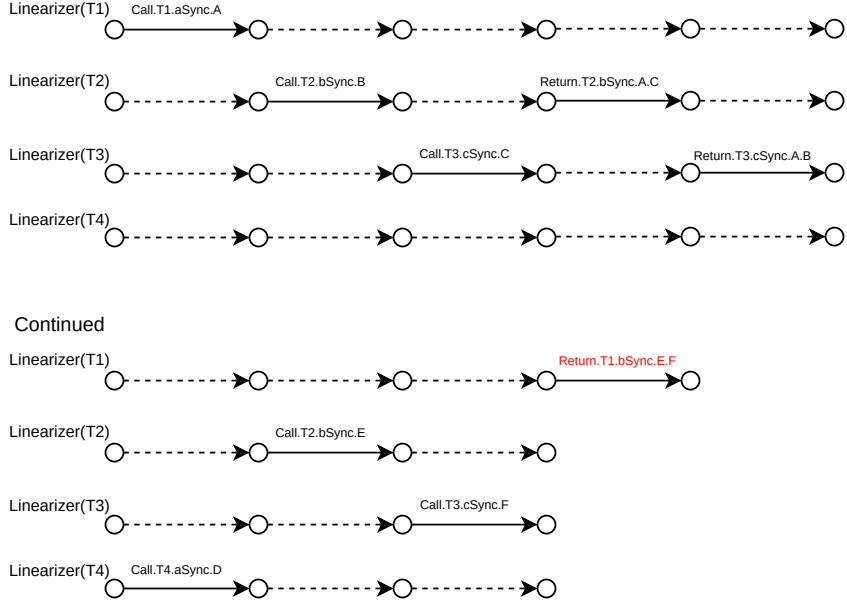


Figure 28: Trace that violates the specification

- In the first round of synchronization, process T_A , T_B , T_C call `aSync`, `bSync` or `cSync` respectively, and put down its argument in turn.
- Process T_A raises `bSignal`. Before T_A exits, the other two processes T_B , T_C returns. Now T_A should return argument of T_B and T_C .
- Another round of synchronization starts. Thread T_D , T_B , T_C call `aSync`, `bSync` or `cSync` respectively, and overwrites the shared variable `a,b,c` in turn.
- Now T_A returns with `(b,c)` from the second round, which may not be the argument of `bSync` and `cSync` in the first round.

4.3.2 Conclusion

In the above section, we tested a semaphore based concurrent datatypes. With the testing result, we showed that it is important to be reminded that a thread waiting for the semaphore to raise can immediately continue and overwrite shared variables, after the semaphore is raised by another process.