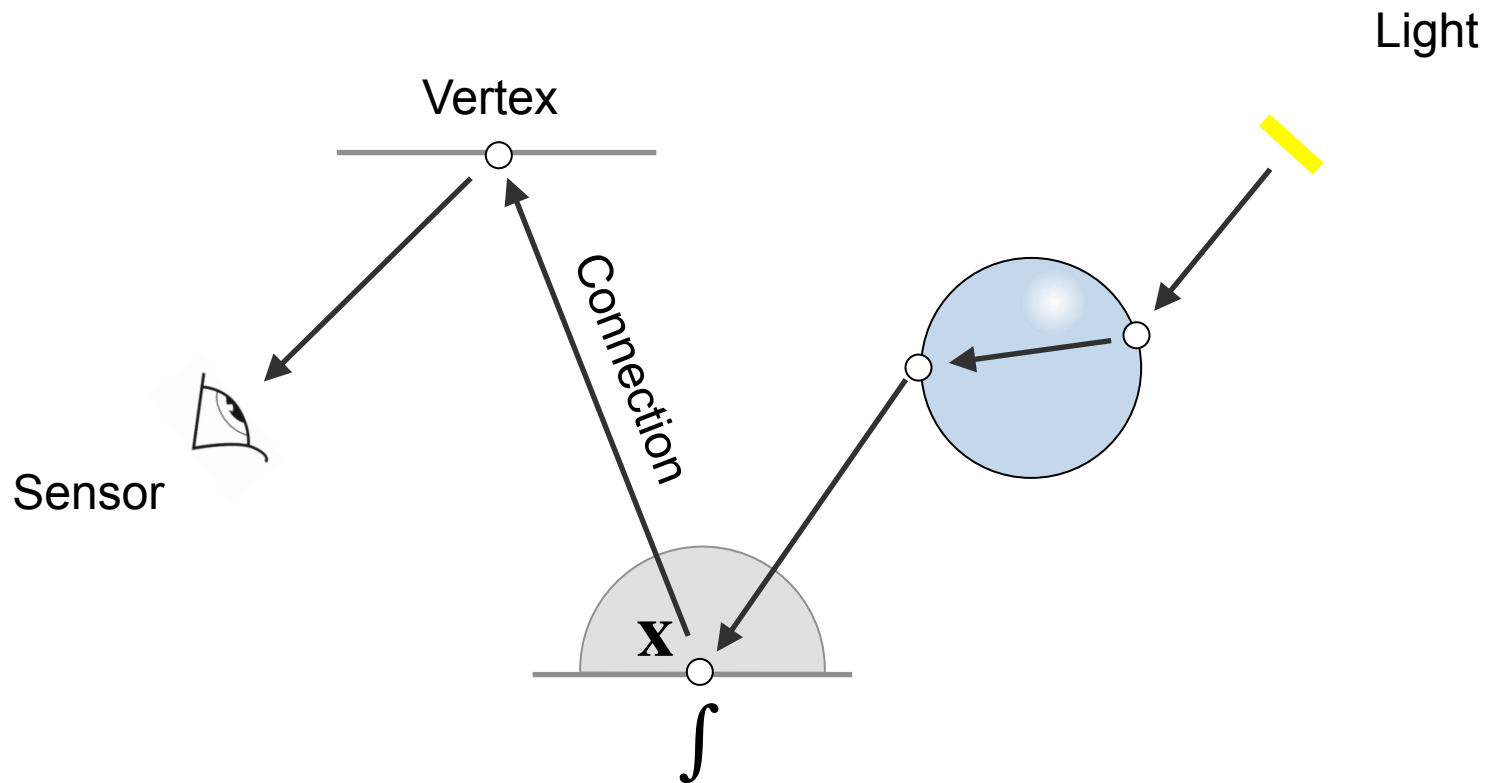


Photon Mapping

Today

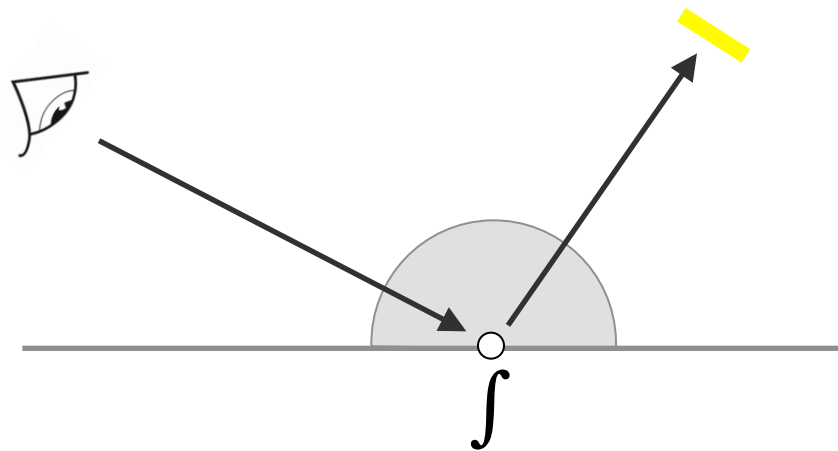
- Motivation
- Idea: Starting light paths at the light
- Methods
 - Light tracing
 - Bi-directional path tracing
 - Photon Mapping
 - Instant Radiosity

Path space jargon



Example 1: Small lights

- Small light sources imply a small hit chance
- Solution: Next-event estimation
- Pre-condition: We know what is a light



What is hard for Path tracing

- Two examples:
 - Occlusion (key hole-like)
 - Specular (caustics)

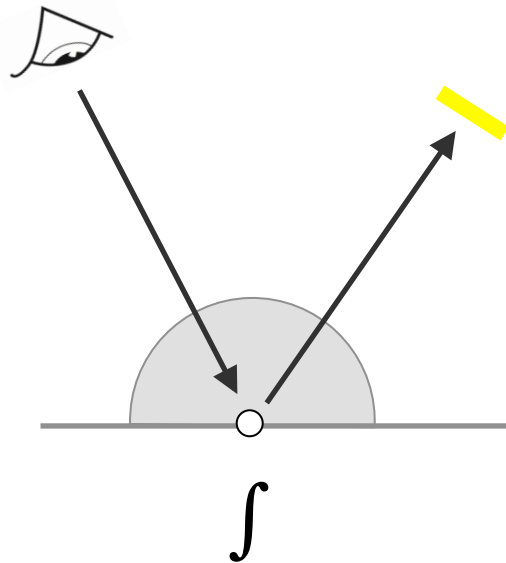


Small lights

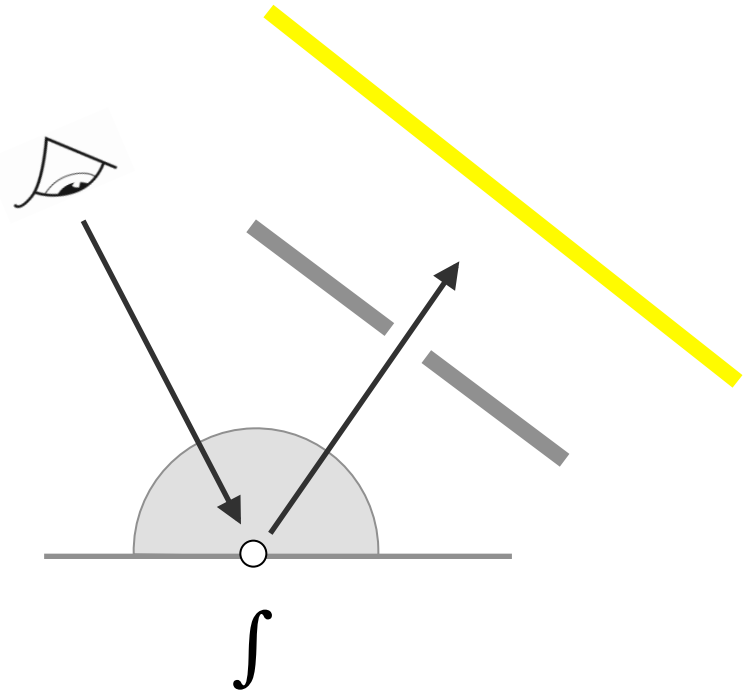


Limits of next-event estimation

Small light: Fine!



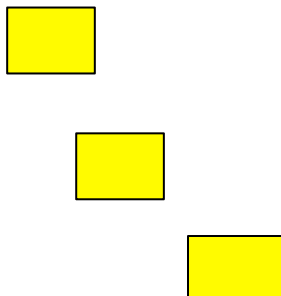
Large light, small holes, now what?



Roulette in spherical domain

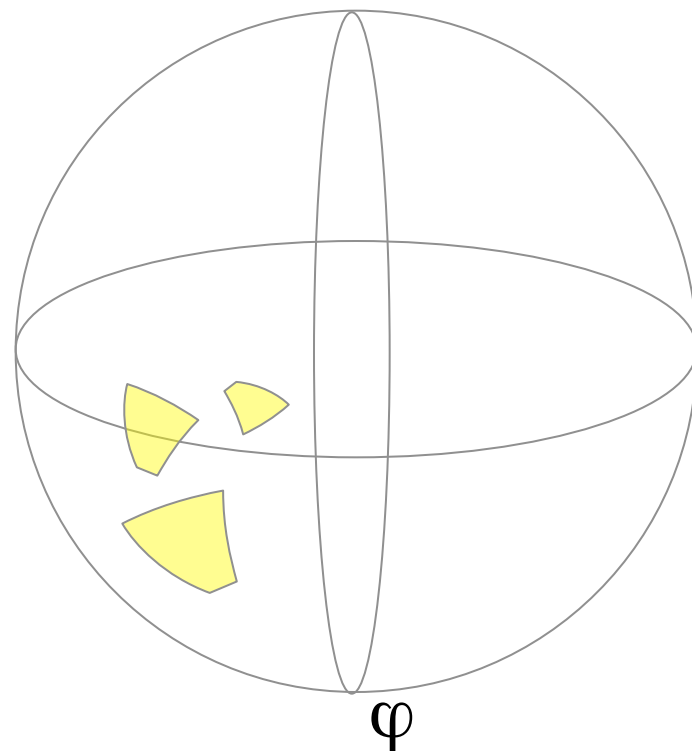
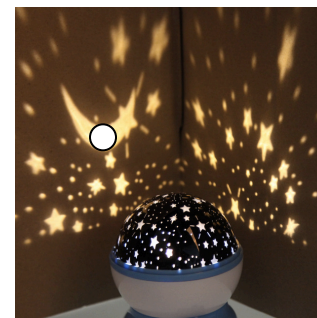
 θ

		0		00	
		1	2	3	
American roulette	1st 12	4	5	6	
		7	8	9	
		10	11	12	
		13	14	15	
	2nd 12	16	17	18	
		19	20	21	
		22	23	24	
		25	26	27	
	3rd 12	28	29	30	
		31	32	33	
		34	35	36	
		2-1	2-1	2-1	



0		00																																			
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	2-1	
1st 12												2nd 12												3rd 12													
1-18						Even						Red						Black						Odd						19-36							
American roulette																																					

Θ

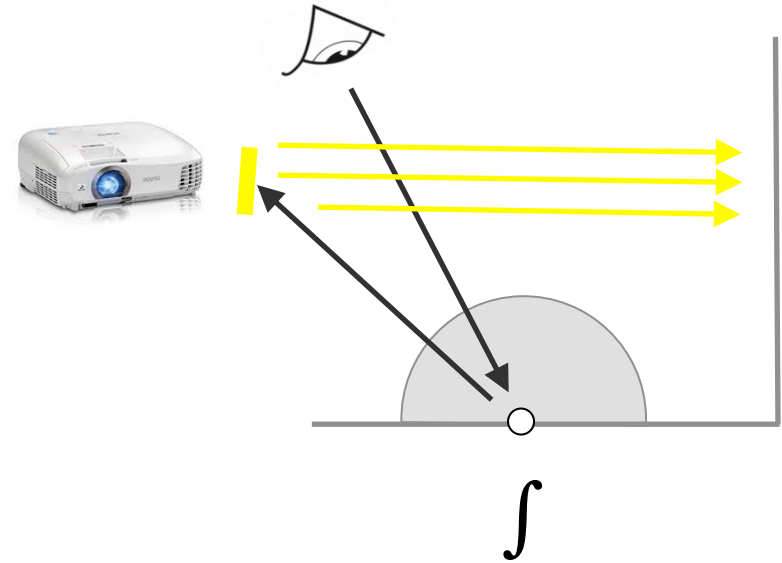
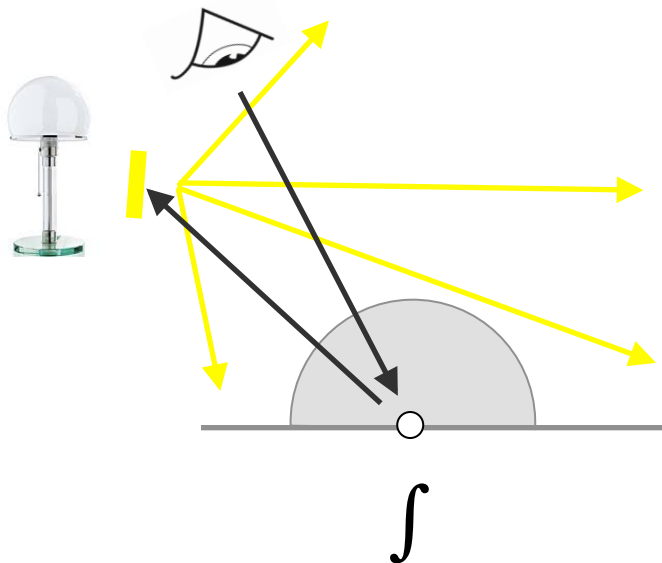
 φ 

Projector



Next-event cant help

- The projector send in very few directions only
- Connecting to it is useless most if the time

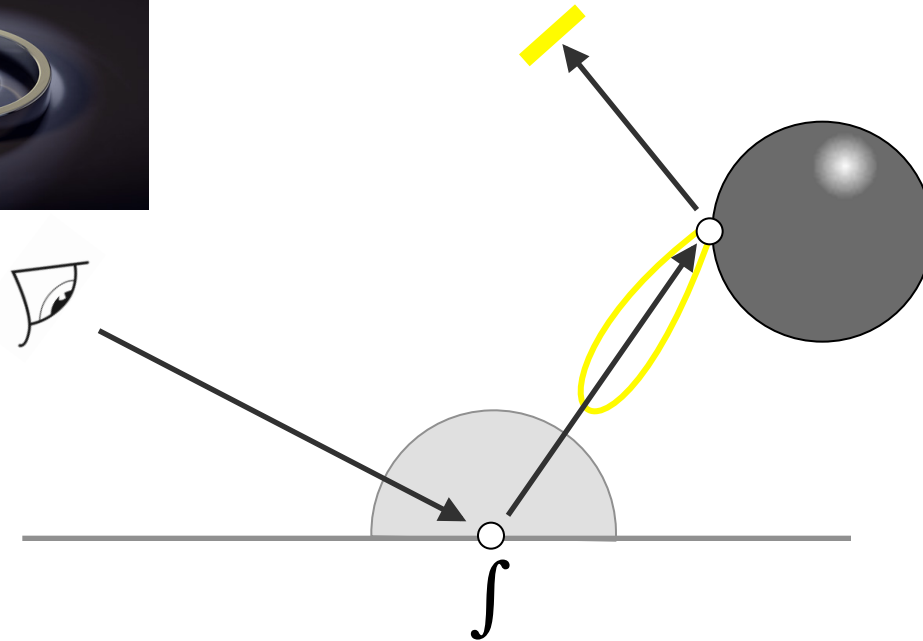


Reflective caustic

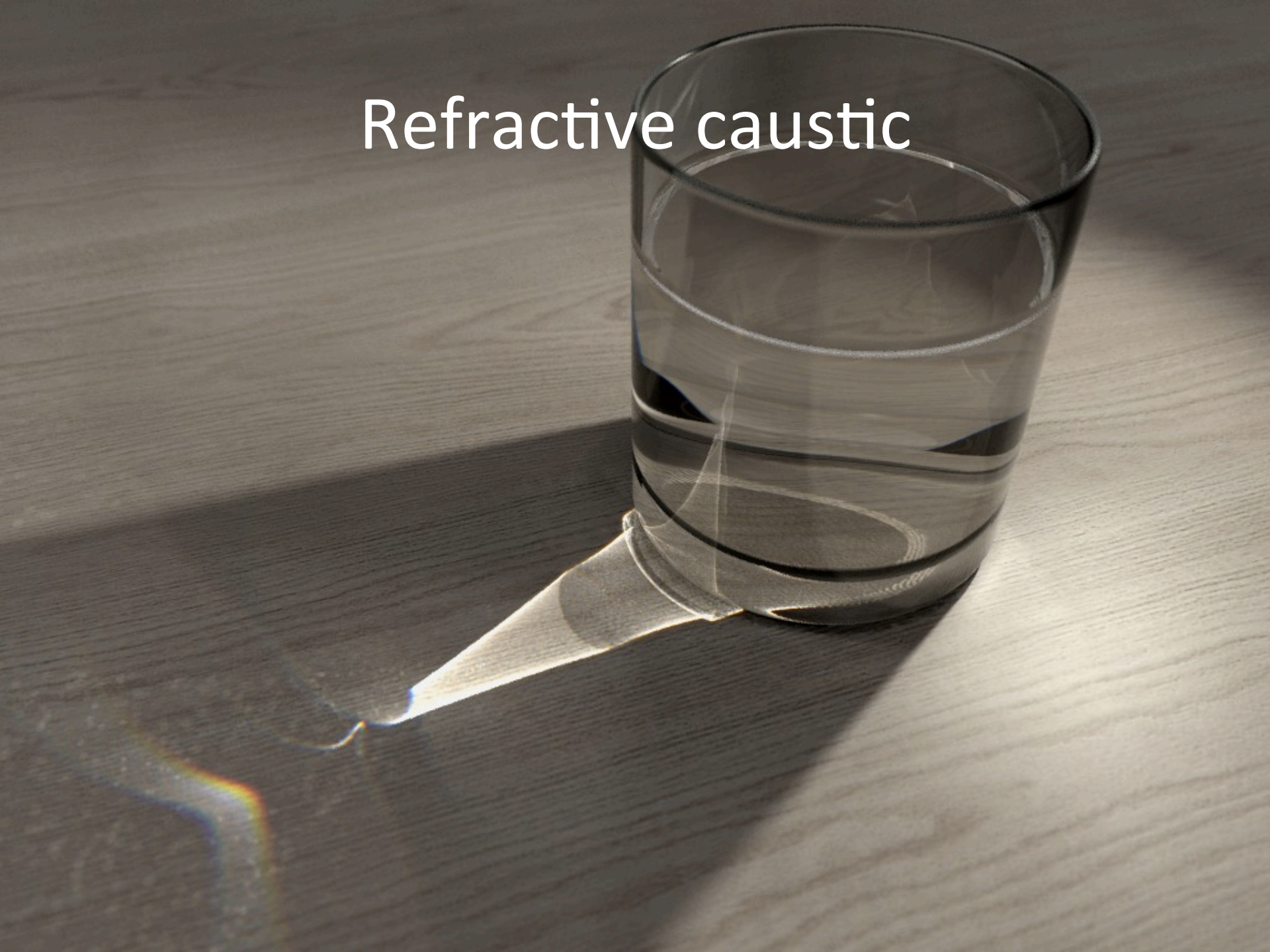


Example 2: Caustics

- A **caustic** is similar to a small light sources
- No obvious way to find it

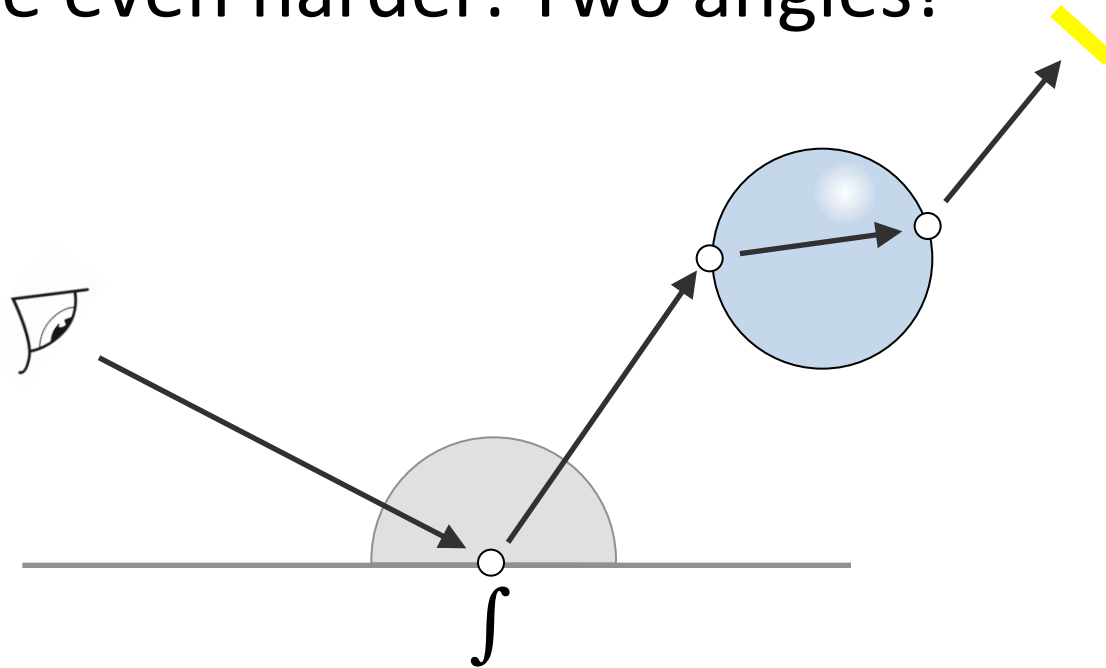


Refractive caustic



Example 2: Caustics

- A **caustic** is similar to a small light source
- No obvious solution
- Refractive even harder: Two angles!

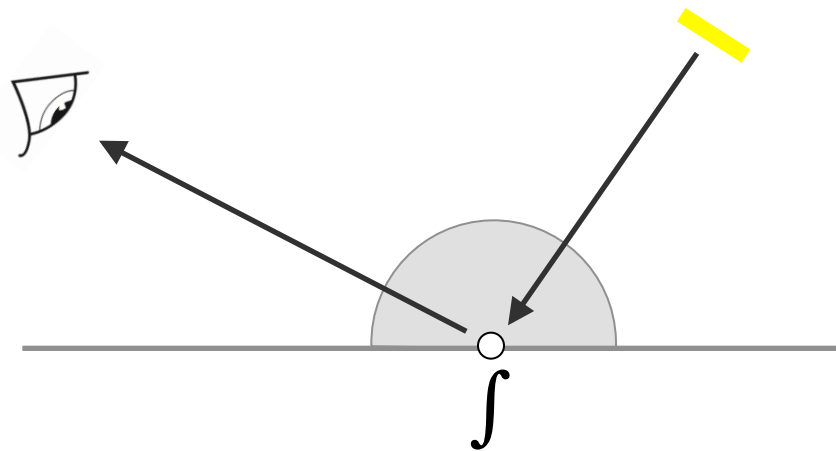


What is hard for path tracing?

- Paths of the form LSDE, LSSDE, etc
- Light that undergoes one or more specular reflections and then a diffuse bounce
- Reflective or refractive caustics

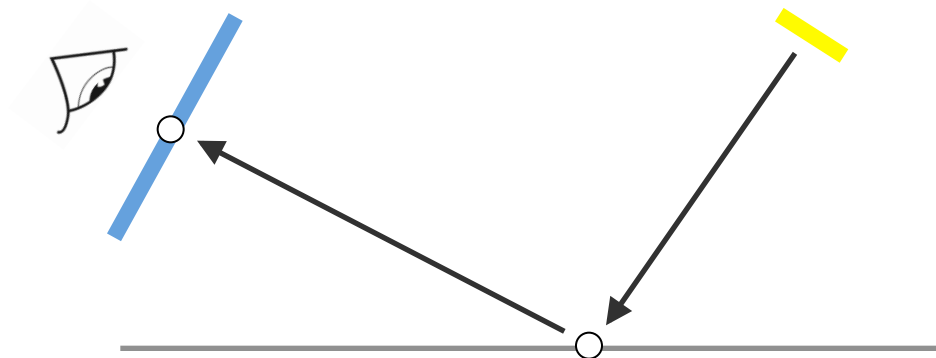
Solution: Light tracing method

- Start path at the light
- Trace rays through the scene
- In the end **project** onto sensor



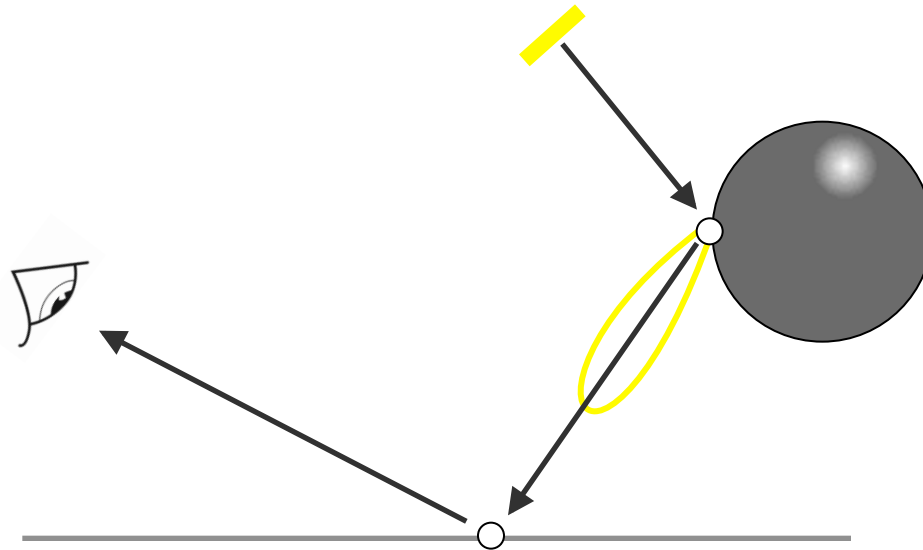
Light tracing

- Need next-event estimation at final vertex
- Sensor is even smaller than light
- Finding it by chance even less likely



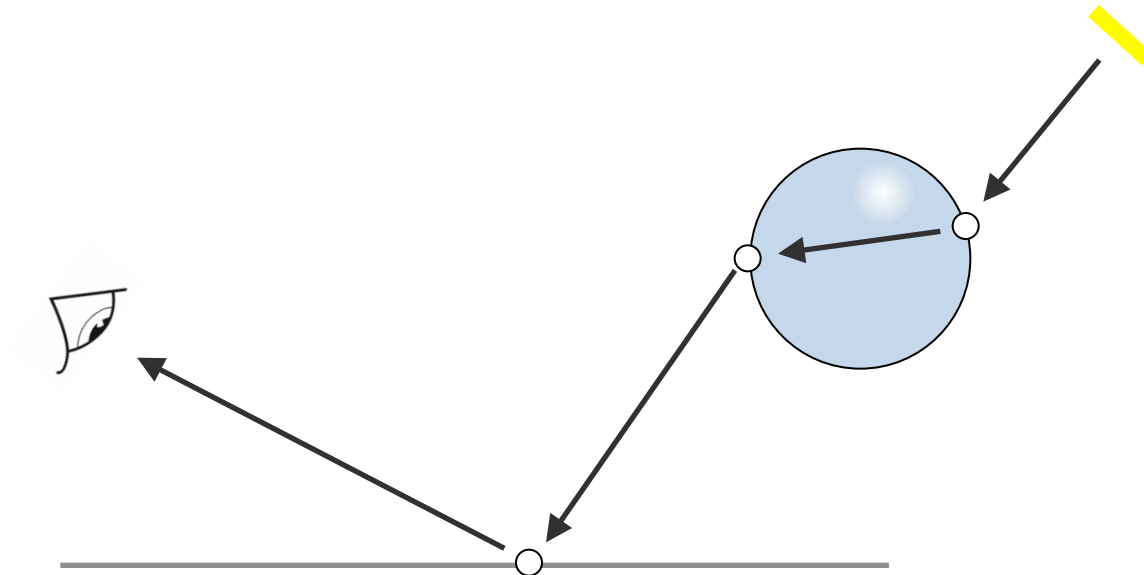
Light tracing for a reflective caustic

- Works quite well

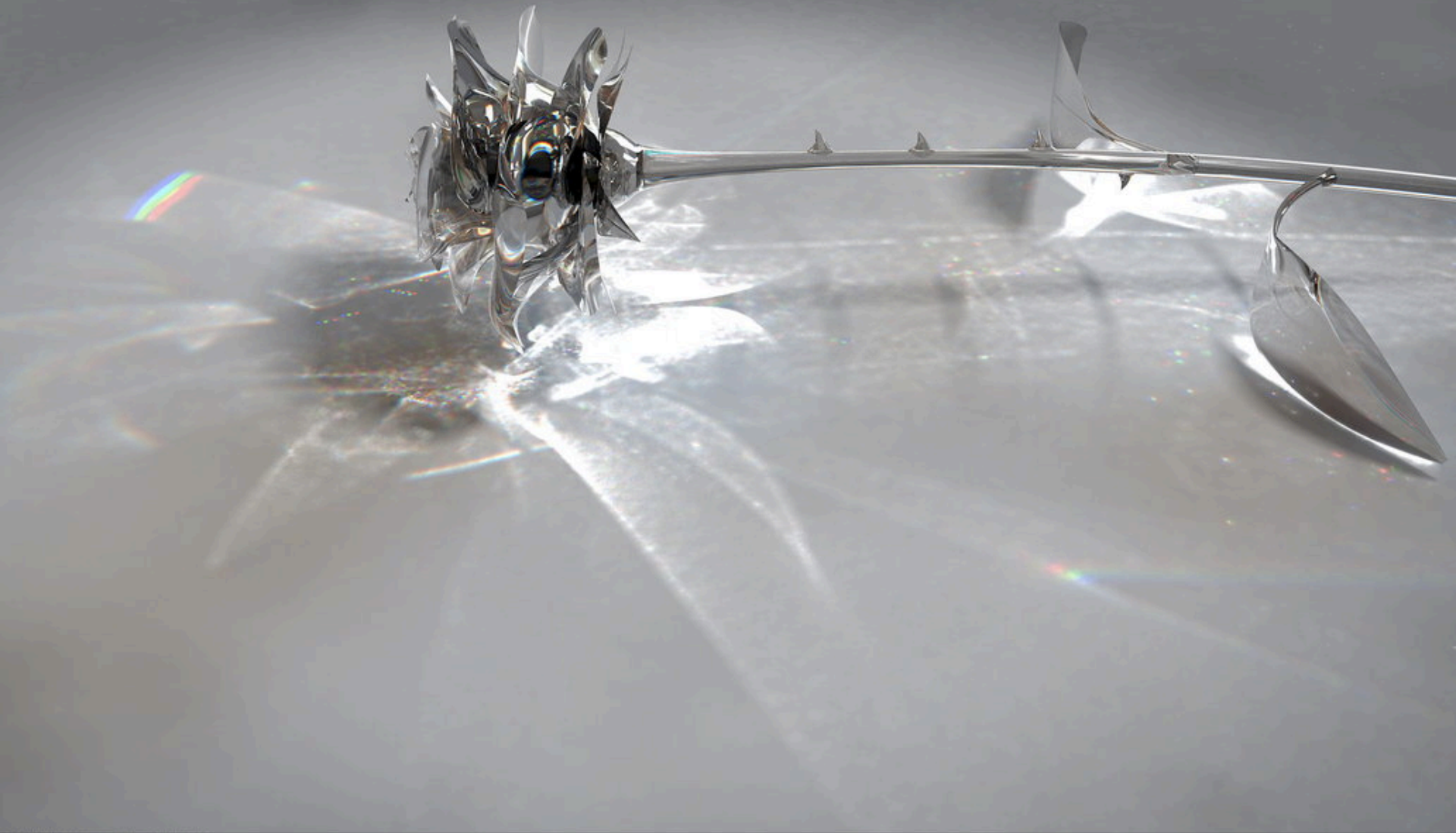


Light tracing for a refractive caustic

- Works quite well

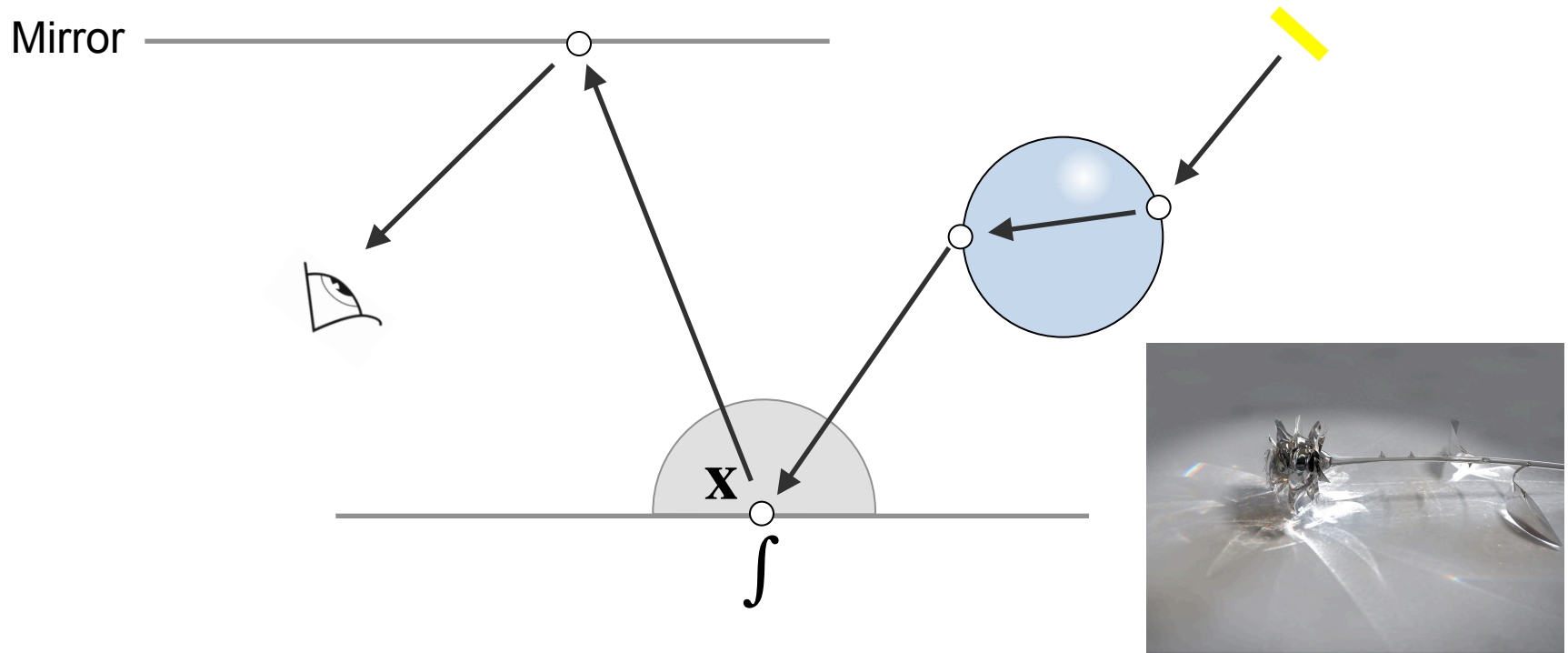


Reflection of a caustic



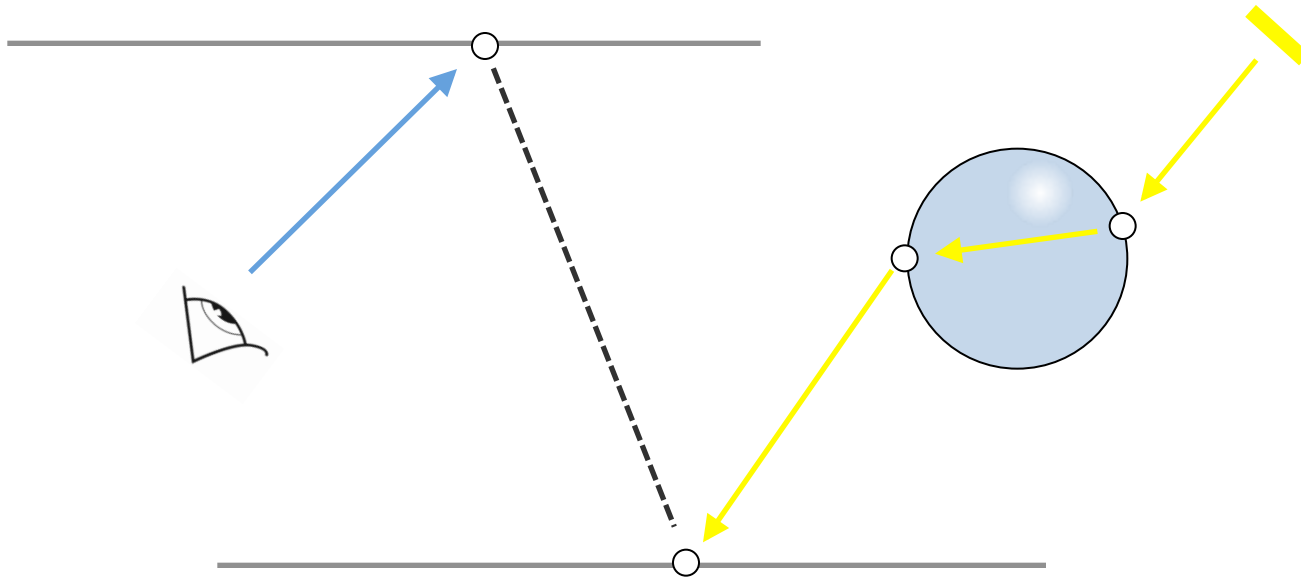
Caustics in a mirror

- Very hard!
- How could we know at \mathbf{x} how to go on?



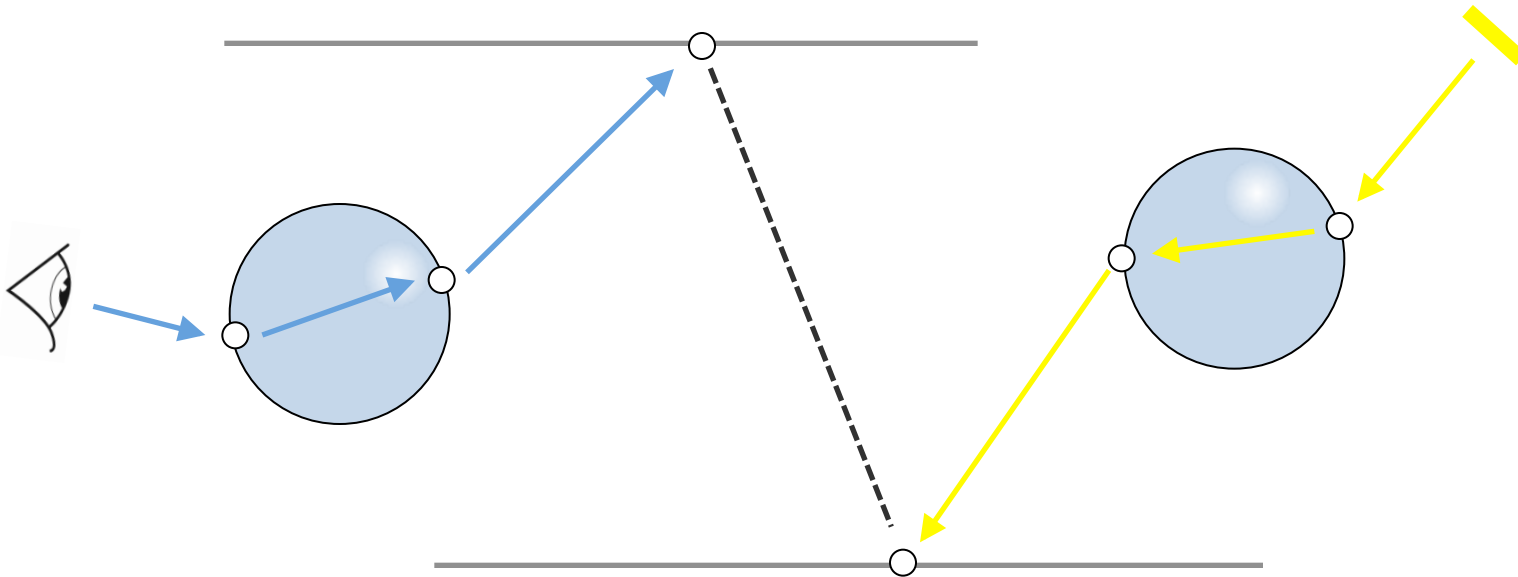
Bi-directional path tracing

- Start a path both at the eye and the light
- Connect the ends



Bi-directional path tracing

- Start a path both at the eye and the light
- Connect the ends

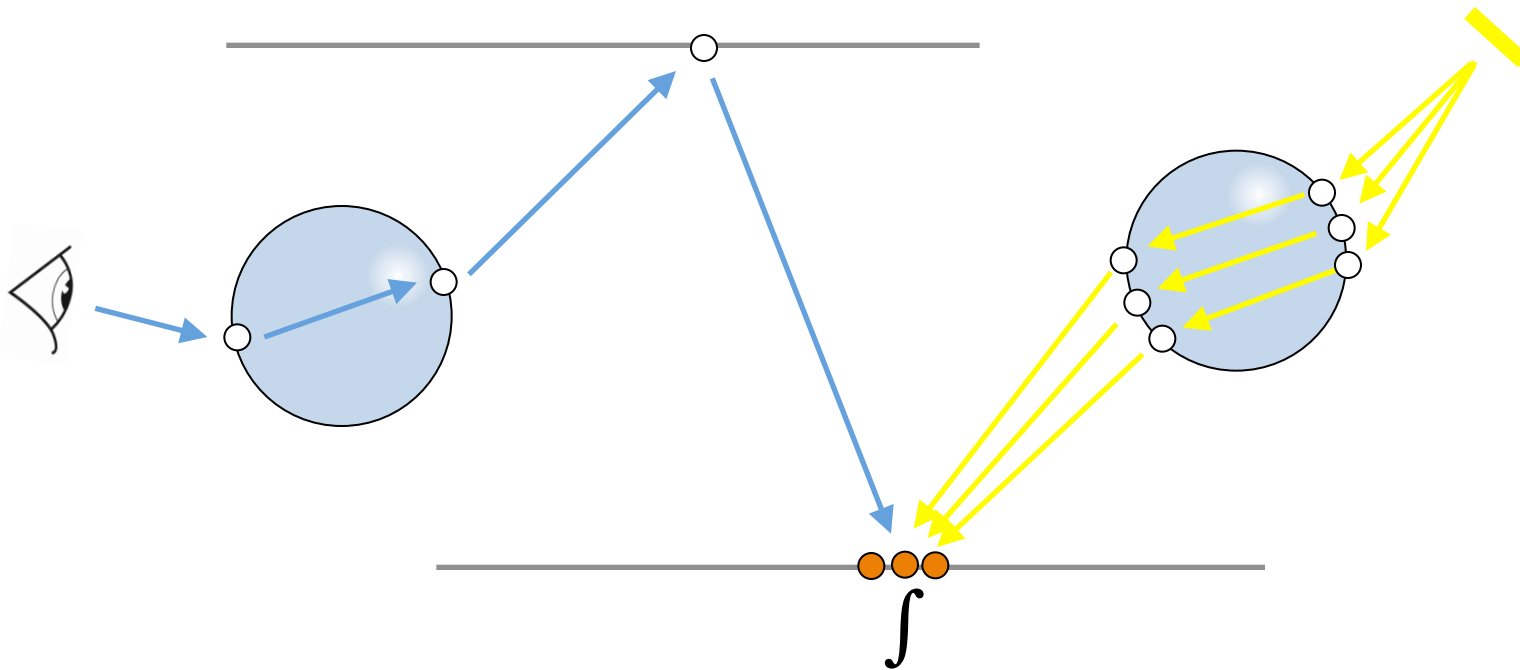


Photon mapping

- When eye paths connect to light paths we don't care about their path, only about the vertex
- Idea:
 - Store end-vertices from the light
 - Re-use from the eye

Photon mapping

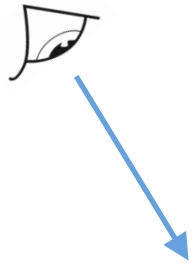
- Start many rays at the light, store last vertex
- Re-use from the eye



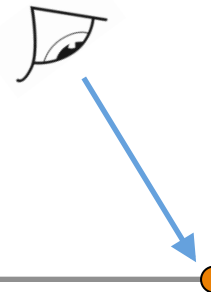
Density estimation

- Photon are just a list of 3D points
- How to convert into $L_i(\mathbf{x}, \omega)$?
- Find how many are nearby!

Many photons: bright

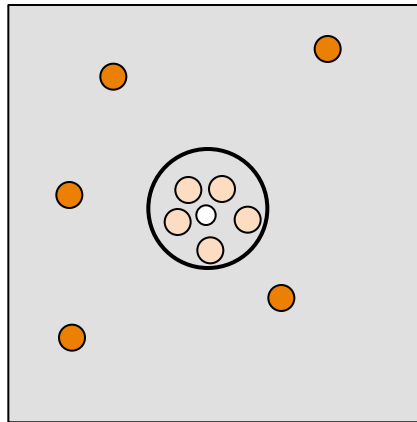


Fewer photons: bright



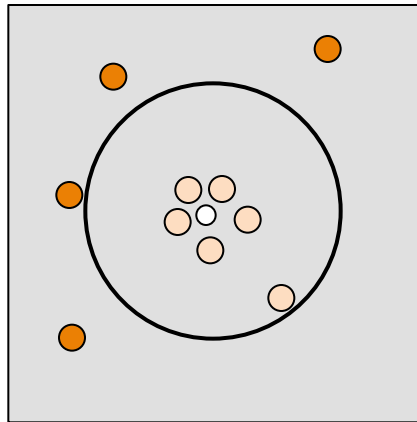
Two options: Option 1

- Find the nearest k
- See how large their radius r is
- Large a is small density and low L



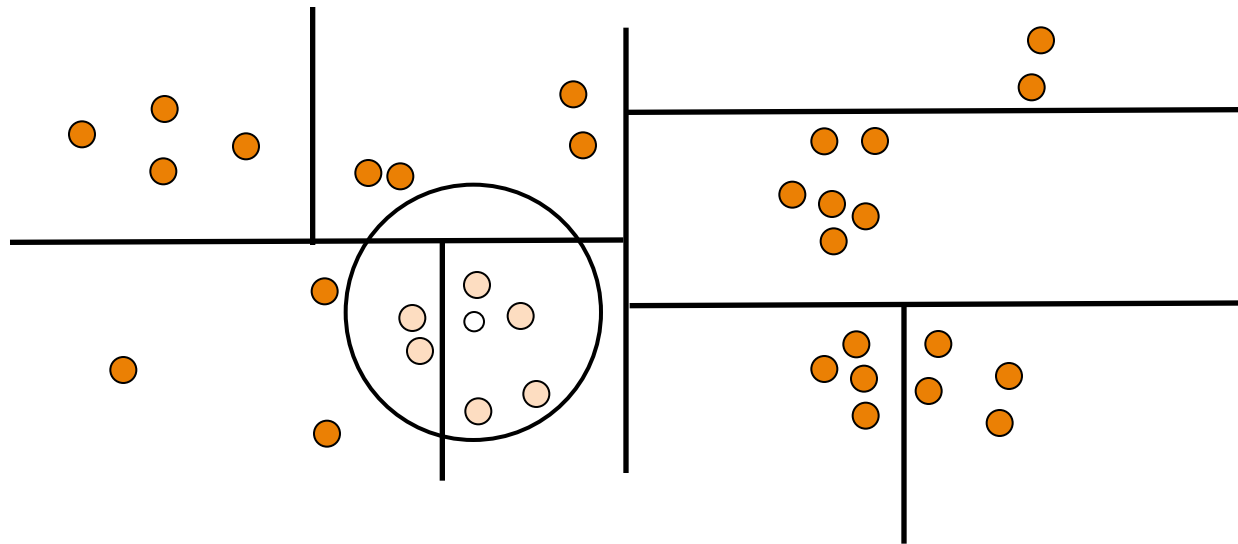
Two options: Option 2

- Fix a radius r
- Count how many k are in this radius
- Large k is high density and high L



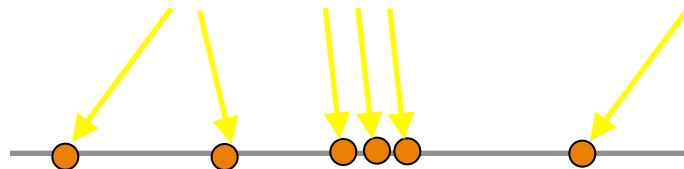
How to find k nearest?

- Spatial bounding structures
- $k d$ tree
- Can find k NN in $\log(n)+k$ time for n points



■ BRDF in PM

- The light also depends on the direction
- Photons also store from where they came
- Like this, can take direction into account



Instant radiosity

- Two passes
 - Instead of doing density estimation, just consider each photon a light sources
 - Proceed with your usual rendering pipeline with shadow maps to light from these
- Can even be OpenGL and shadow mapping
- Can work in real-time
- Closest to real-time GI we got for now

Real-time 5 ys ago



Recap

- Can also start from the light
- Sometimes better
- Bias / Variance / Consistence
- Three ways to to this
 - Light tracing
 - Path Tracing
 - Instant radiosity
 - Bi-Directional Ray Tracing
 - Photon Mapping