

# CS2100 CheatSheet

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## C programming

### Data Types

- int (integer): 4 bytes, -2,147,483,648 ( $-2^{31}$ ) to 2,147,483,647 ( $2^{31} - 1$ )
- float (real number): 4 bytes
- double (real number): 8 bytes
- char (character): 1 byte, enclosed in pair of single quotes eg. 'a'

### Preprocessor Directives

- Include libraries eg. `#include <math.h>`, need to compile with `-lm` if imported math lib
- Macro expansions eg. `#define PI 3.142 //use CAPS for macro` Macro expansions do a textual substitution

### Input/Output

Input/Output statements:

- `scanf`( format string, input list );
- `printf`( format string );
- `printf`( format string, print list )

Format Specifiers

Placeholder	Variable Type	Function Use
<code>%c</code>	char	<code>printf / scanf</code>
<code>%d</code>	int	<code>printf / scanf</code>
<code>%f</code>	float or double	<code>printf</code>
<code>%f</code>	float	<code>printf</code>
<code>%lf</code>	double	<code>scanf</code>
<code>%e</code>	float or double	<code>printf (for scientific notation)</code>

Examples

- `-%5d`: displays integer with width 5, right justified
- `-.8.3f`: display real number, width of 8, 3dp, right justified

### Operators

#### Equals operator

= has the side effect of returning the value assigned

### Arithmetic Operators and Precedence

Operator Type	Operator	Associativity
Primary expression operators	<code>() expr++ expr--</code>	Left to right
Unary operators	<code>* &amp; + - ++expr --expr (typecast)</code>	Right to left
Binary operators	<code>* / % + - &lt;&gt; &lt;= &gt;= == != &amp;&amp;   </code>	Left to Right
Assignment operators	<code>= += -= *= /= %=</code>	Right to left

### Mixed-Type Arithmetic Operations

- `int m = 10/4;` means `m = 2;`
- `float p = 10/4;` means `p = 2.0;`
- `int n = 10/4.0` means `n = 2;`
- `float q = 10/4.0` means `q = 2.5;`
- `r = -10/4.0;` means `r = -2;`

### Type Casting

```
syntax: (type) expression
int aa = 6; float ff = 15.8;
float pp = (float) aa / 4;    means pp = 1.5;
int nn = (int) ff / aa;      means nn = 2;
float qq = (float) (aa / 4); means qq = 1.0;
```

### Remainder

% is remainder in C

- `- a = 10 % 4 → a = 2`
- `- a = -10 % 4 → a = -2`

### Booleans

No boolean types in C, use integers ie

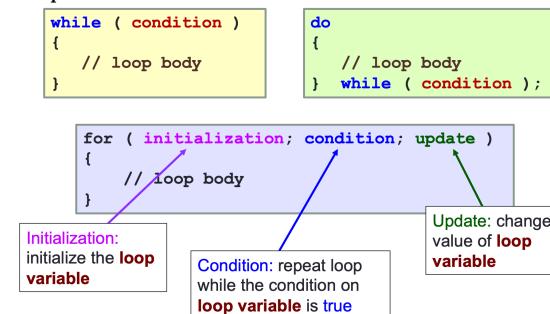
- 0 represents false
- any other integer (usually 1) represents true

### Operator Precedence

Operator Type	Operator	Associativity
Primary expression operators	<code>() [] . -&gt; expr++ expr--</code>	Left to Right
Unary operators	<code>* &amp; + - ++expr --expr (typecast) sizeof</code>	Right to Left
Binary operators	<code>* / % + - &lt;&gt; &lt;= &gt;= == != &amp;&amp;   </code>	Left to Right
Ternary operator	<code>? :</code>	Right to Left
Assignment operators	<code>= += -= *= /= %=</code>	Right to Left

Note that precedence of `&&` is greater than that of `||`.  
`&&` and `||` use short-circuit evaluation

### Loops



For `for` loops in C, declaration of the loop variable has to be before the `for` loop

### Number Systems

#### Data Representation

- bit: 0 or 1
- byte: 8 bits

- word: Multiple of bytes, 4 for mips

N bits can represent up to  $2^N$  values, from 0 –  $(2^N - 1)$

To represent M values,  $\lceil \log_2 M \rceil$  bits are required

In C,

- Prefix 0 for octal, eg 032 represents (32)<sub>8</sub>

- Prefix 0x for hexadecimal, eg 0x32 represents (32)<sub>16</sub>

### Conversion from Decimal to Base R

$$(43)_{10} = (101011)_2$$

2   43
2 21 rem 1 ← LSB
2 10 rem 1
2 5 rem 0
2 2 rem 1
2 1 rem 0
0 rem 1 ← MSB

$$(0.3125)_{10} = (.0101)_2$$

Carry
0.3125 × 2 = 0.625
0.625 × 2 = 1.25
0.25 × 2 = 0.50
0.5 × 2 = 1.00

### Binary to Octal and Hexa shortcuts

- Binary to Octal: partition in groups of 3, take the value of the groups
- Octal to Binary: reverse - Binary to Hexa: partition in groups of 4, take the value of the groups
- Hexa to Binary: reverse, convert hexa to binary, extend to 4 digits if needed

### ASCII code

Integers (0 – 127) and characters are 'somewhat' interchangeable in C

### Negative Numbers

3 representations

1. Sign-and-Magnitude

2. 1s complement

3. 2s complement

### Sign and Magnitude

Sign is represented by sign bit; 0 for + and 1 for -

First bit is sign bit, other 7 bits are read as normal

- Largest value:  $2^{n-1} - 1$

- Smallest value:  $-2^{n-1} + 1$

- 2 zeroes:  $+0 = 00000000$  and  $-0 = 10000000$

- Range:  $2^{n-1} - 1$  to  $-2^{n-1} + 1$

To negate the number, just invert sign bit

### 1s Complement

Negated value of  $x$  is given by  $-x = 2^n - x - 1$

- Largest value:  $2^{n-1} - 1$

- Smallest value:  $-2^{n-1} - 1$

- 2 zeroes:  $+0 = 00000000$  and  $-0 = 11111111$

- Range:  $-(2^{n-1} - 1)$  to  $2^{n-1} - 1$

To negate a number, invert all bits

Note that the first bit still represents the sign: 0 for positive and 1 for negative.

## 2s Complement

Negated value of  $x$  is given by  $-x = 2^n - x$

- Largest value:  $2^{n-1} - 1$

- Smallest value:  $-2^{n-1}$

- Range:  $-2^{n-1}$  to  $2^{n-1} - 1$

To negate a number, invert all bits, then add 1

For fractions same thing, flip then add one to LSB

Note that MSB still represents the sign, and that MSB "has a value" of  $-2^{n-1}$

## Sign Extension

For 1s and 2s complement: Extend sign bit

For SAm: Pad 0s after the sign bit

## Arithmetics

### 2s Complement Addition and Subtraction

Algorithm for adding integers  $A$  and  $B$

1. Perform binary addition on the two numbers

2. Ignore the carry out of MSB

3. Check for overflow, overflow occurs if the 'carry in' and 'carry out' of the MSB are different. Or if the result is opposite sign of  $A$  and  $B$

### 1s Complement Addition and Subtraction

Algorithm for adding integers  $A$  and  $B$

1. Perform binary addition on the two numbers

2. If there is a carry out of the MSB, add 1 to the result (at the LSB)

3. Check for overflow

## Overflows

Overflows are a result of addition/subtraction going beyond the range of numbers

- positive add positive  $\rightarrow$  negative

- negative add negative  $\rightarrow$  positive

## Excess Representation

Allows the range of values to be distributed evenly between positive and negative values, using a simple translation (subtraction)

$$\text{Excess representation} = \text{Value} + \text{excess}$$

eg for excess-8, rep = Value + 8

For 4-bit numbers, usually use excess-7 or excess-8

## Real numbers

### Fixed point representation

Number of bits allocated for whole number part and fractional part are fixed

- Advantage: Easier computation

- Disadvantage: smaller range for a given precision

### Floating point representation

IEEE 754 Floating-Point Representation

3 components: sign, exponent, mantissa (fraction)

Similar to standard form

Radix is assumed to be 2

1. Single Precision (32-bit): 1-bit sign, 8-bit exponent with excess-127, 23-bit mantissa

2. Double Precision (64-bit): 1-bit sign, 11-bit exponent with excess-1023, 52-bit mantissa

Mantissa normalised with an implicit leading bit 1

eg. -6.5 in decimal

$$-6.5_{10} = -110.1_2 = -1.101_2 * 2^2$$

IEEE 754: 1 10000001 10100000000000000000000000000000<sub>2</sub> = C0D00000<sub>16</sub>

## Pointers and Functions

### Pointers

Can refer to the address of a variable by using the *address of operator*, & %p is used as the format specifier for addresses, addresses are printed out in hexadecimal format

### Pointer Variables

Variable that contains the address of another variable.

### Declaring a Pointer

Syntax:

type \*pointer\_name

- pointer\_name is the name of the pointer (Good practice to name a pointer with suffix \_p or \_ptr)

- type is the data type of the variable this pointer may point to  
eg. int \*a\_ptr declares a pointer to an int named a\_ptr

### Assigning Value to a Pointer

```
int a = 123;
int *a_ptr; // declaring an int pointer
a_ptr = &a;

int a = 123;
int *a_ptr = &a; // initialising a_ptr
```

### Accessing Variable through Pointer

Once a\_ptr points to a, can access a through a\_ptr using *indirection operator*, (or dereferencing operator) \*

ie. a\_ptr\* === a

Note that

- int \*a\_ptr is a declaration of a pointer to an int with the name a\_ptr  
- \*a\_ptr is the value AT the address stored in a\_ptr

### Incrementing Pointers

Incrementing a pointer means that the pointer will look at the NEXT chunk of data,

ie. incrementing an int/ float ptr increases value by 4, incrementing a char ptr increases value by 1, incrementing double ptr increases value by 8

Note remember to assign the pointer variable an address before using if not it would be pointing somewhere unknown

## User Defined Functions

Function Definitions follow the following syntax

```
return_type name(p1_type p1_name, p2_type p2_name, ...){  
    // function body  
}
```

Function prototypes follow the following syntax (names of params not needed)

```
return_type name(p1_type, p2_type, ...);
```

Good practice to put function prototypes at the top before main() function, after preprocessor directives. Function definitions after main() function

Without function prototype, compiler assumes default return type of int

### Pass-by-Value and Scope Rule

In C, actual parameters are passed to formal parameters by a mechanism called *pass-by-value*

- Formal parameters and variables are local to the function they are declared in

- Local parameters and variables are only accessible in the function they are declared in (Scope rule)

- When function is called, activation record is created in call stack and memory is allocated for the local parameters and variables of the function

- Once done, activation record is removed, memory allocated is released

- Local params and variables of a function exist in memory only during execution of function and are known as *automatic variables*

- In contrast, *static variables* live in memory even after the function is executed

Then how to allow a function to return more than one value or modify values of variables defined outside of it?

- Using functions with pointer parameters

## Arrays, Strings, Structures

### Arrays

Declaration: element type, array name size, eg, int c[30];

Initialising: arrays can be initialised at time of declaration

**size of arrays**

// a[0]=54, a[1]=9, a[2]=10  
int a[3] = {54, 9, 10};

// size of b is 3 with b[0]=1, b[1]=2, b[2]=3  
int b[] = {1, 2, 3};

// c[0]=17, c[1]=3, c[2]=10, c[3]=0, c[4]=0  
int c[5] = {17, 3, 10};

int e[2] = {1, 2, 3}; // warning issued: excess elements

int f[5];  
f[5] = {8, 23, 12, -3, 6}; // too late to do this;  
// compilation error

Note what happens when fewer initial values are provided.

array name refers to the address of the first element  
eg. int a[10]; // a = &a[0]

### Array Assignment

Array name is a fixed pointer, it points to the first element in the array and cannot be altered

```
int source[10] = { 10, 20, 30, 40, 50 };
int dest[10];
dest = source; //illegal
```

Instead use a loop to loop through elements and copy them over, or use `memcpy()` in `<string.h>` library

### Array params in functions

Function prototype: `int sumArray(int [], int);`

Function Definition:

```
int sumArray(int arr[], int size) { ... }
int sumArray(int arr[8], int size) { ... }
```

- 8 is ignored by the compiler because array parameters are passed in as pointers, must pass in size as a separate parameter

- Therefore, alternative function prototype: `int sumarray(int *, size)` and alternative function definition: `int sumArray(int *arr, int size) {...}`

- This also means that any function can modify an array it receives

### Strings

- Array of chars  $\neq$  string, need to append null character
- String is an array of chars terminated by a null character, (\0, ascii value 0)
- `char fruit_name[] = "apple";` ↓
- `char fruit_name[] = {'a', 'p', 'p', 'l', 'e', '\0'};`

### String IO

Input:

1. `fgets(str, size, stdin)` // reads size - 1 char, or until (including) newline
2. `scanf("%s", str);` // reads until whitespace
- Don't use `gets()`, can result in buffer overflow
- `fgets()` can read in newline character if there is enough space, need to replace it with null character

```
fgets(str, size, stdin);
len = strlen(str);
if (str[len - 1] == '\n') {
    str[len - 1] = '\0';
}
```

Output:

1. `puts(str);` // terminates with new line
2. `printf("%s\n", str);`

### String Functions

1. `strlen(s)`, returns number of chars in s
2. `strcmp(s1, s2)`, compares ASCII values of chars in s1 and s2, return negative int if s1 < s2 and positive if s1 > s2, 0 if same
3. `strncmp(s1, s2, n)`, compares first n characters of s1 and s2
4. `strcpy(s1, s2)`, copies s2 into s1, must use this because cannot assign, unless at declaration. If s2 too long can cause buffer overflow
5. `strncpy(s1, s2, n)`, copies first n chars from s2 to s1

All the functions use null character, without it could result in illegal access of memory

### Structures

Structures allow grouping of members of different types  
A group can be a member of another group  
Groups are also called structure types

Struct Definition:

```
typedef struct {
    int acctNum;
    float balance;
} account_t;
```

- Remember the ; at the end!
- Types must be defined before declaring variables of that type
- No memory is allocated to a type
- Put struct definitions before function prototypes but after preprocessor directives

### Accessing members of a structure variable

- Use the dot (.) operator

eg:

```
result_t result;
result.stuNum = 123456;
result.score = 62.0;
result.grade = 'D';

card_t card = { 123456, {30, 6} };
card.expiryDate.year = 2021;
```

### Reading a Structure member

Structure members are read in individually

```
result_t result;
printf("Enter student number, score and grade: ");
scanf("%d %f %c", &result.stuNum, &result.score, &result.grade);
```

Unlike arrays, can do assignment with structures, eg if result has already been initialised, `result.stuNum = result1.stuNum` is valid

### Structures and Functions

Returning structure from function

Can return a struct as you would for other types

Structures as parameters

- Uses pass-by-value, entire structure is copied over
- To modify a structure's content, need to pass address of structure to function, using & operator
- Therefore to access members need to use `(*player).name`, for example. - Note that dot operator (.) has higher precedence than indirection operator (\*), therefore the () are needed
- `(*ptr_name).member` can be rewritten as `ptr_name->member`

### MIPS

#### Overview

Mips uses Load-Store architecture, ie. both instructions and data are stored in memory

- Limit memory operations

- Rely on registers (mips has 32) for storage during execution  
Note that Registers have no data type!!

### Arithmetic Operations

Addition and Subtraction

eg. `texttadd $s0, $s1, $s2`, adds \$s1 and \$s2 and stores in \$s0  
eg. `texttsub $s0, $s1, $s2`, subtracts \$s2 from \$s1 and stores in \$s0

Immediate operations

Immediate values are constants, 16-bit, source2 is a constant instead  
Values ranges from  $[-2^{15} \text{ to } 2^{15} - 1]$ , 16-bit 2s comp

Register Zero

\$0 always has a value of 0

Can be used to assign values eg `f = g`, by writing `add $s0, $s1, $zero`, f in \$s0, g in \$s1

### Logical Operators

View Registers as 32 raw bits instead of a number

Logical operation	C operator	Java operator	MIPS instruction
Shift Left	<code>&lt;&lt;</code>	<code>&lt;&lt;</code>	<code>sll</code>
Shift right	<code>&gt;&gt;</code>	<code>&gt;&gt;, &gt;&gt;&gt;</code>	<code>srl</code>
Bitwise AND	<code>&amp;</code>	<code>&amp;</code>	<code>and, andi</code>
Bitwise OR	<code> </code>	<code> </code>	<code>or, ori</code>
Bitwise NOT	<code>~</code>	<code>~</code>	<code>nor</code>

#### AND

a	b	a AND b
0	0	0
0	1	0
1	0	0
1	1	1

#### OR

a	b	a OR b
0	0	0
0	1	1
1	0	1
1	1	1

#### NOR

a	b	a NOR b
0	0	1
0	1	0
1	0	0
1	1	0

#### XOR

a	b	a XOR b
0	0	0
0	1	1
1	0	1
1	1	0

Shift Left

- `sll` (shift left logical): Move all bits in a word to the left by a number of positions; fill the emptied positions with zeroes.

- has the effect of multiplying number by  $2^n$ , where n is the number in the immediate field

Shift Right

- `srl` (shift right logical): Move all bits in a word to the right by a number of positions; fills the emptied positions with zeroes.

- divide number by  $2^n$

AND

-  $a \wedge 0 \implies 0$

-  $a \wedge 1 \Rightarrow a$

- use above two properties for masking, set positions to be ignored to 0, set positions of interest to 1  
OR

-  $a \vee 0 \Rightarrow a$

-  $a \vee 1 \Rightarrow 1$

- use above two properties for setting bits, set position to be set to 1

## NOR

- Can be used to implement NOT instruction  
- NOR with 0

## XOR

- Can also be used to implement NOT instruction  
- XOR with 1  
- Has XORI instruction but no NORI, to keep instruction set small

## Large constant

- How to load a 32 bit constant into a register  
- use lui instruction to set upper 16 bits (lower 16 bits would be set to 0)  
- then use ori instruction to set lower bits, (16 bit immediate would be 0-extended to 32-bit)

Note that logical operators 0 extend immediates to 32 bits whereas arithmetic operations sign-extend(extend first bit)

## Memory Instruction

### Load Word

- eg lw \$t0, 4(\$s0) - address = value of \$s0 + 4, eg 8000 stored in \$s0, then address = 8004  
- Memory word at Mem[8004] loaded into \$t0, ie Mem[8004] - Mem[8007]

### Store Word

- eg sw \$t0, 12(\$s0) - address = value of \$s0 + 12, eg 8000 stored in \$s0, then address = 8012  
- Content of \$t0 stored into the word at Mem[8012], ie, 8012 - 8015

- Note that offset must be a multiple of 4 (because word is 4 bytes in mips)  
- MIPS does not allow unaligned load and stores with lw and sw, need to use pseudo-instructions ulw and usw  
- Other load-store instructions include load byte (lb) and store byte (sb), used for chars and char arrays, for these instructions, offset no need multiple of 4

## Decisions

1. Conditional (branching)
2. Unconditional (jump)

## Branching

BEQ, branch on equal

- eg beq \$r1, \$r2, label

- go to the statement labeled label if value in \$r1 is equal to value in \$r2

BNE, branch not equal

- eg bne \$r1, \$r2, label

- go to the statement labeled label if values aren't equal

## Jump

- processor always follows the branch

- eg j label

Note that label is an "anchor" in code. Labels are not instructions

- Later on labels will be converted to numbers, ie PC relative addressing for branch and truncated address for jump

Common technique: when there is only one branch, ie if with no else, then invert the conditional for more succinct code

## Inequalities

For branch on less than or branch on greater than, use slt

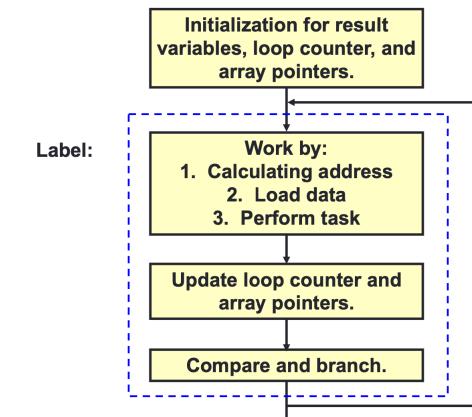
- slt (slti): set on less than eg slt \$t0, \$s1, \$s2, sets \$t0 to 1 if \$s1 < \$s2 or 0 otherwise

- use slt with beq or bne to achieve blt or bgt (reverse \$s1 and \$s2 in slt)

blt \$s1, \$s2, L

slt \$t0, \$s1, \$s2 # these two instructions equivalent to above  
bne \$t0, \$zero, L

## Arrays and loops



Can use pointers instead of index to make code shorter.

- index need to increment, shift left twice (if 4 bytes like int) unless array of chars, then add to base address  
- using pointers, set pointer to base address, increment by 4 each time (if int/ float etc), or increment by 1 if char array

## Encoding Instructions

Constraints are to encode all instructions in 32 bits, and make them as regular as possible

1. R-format (Register format: op \$r1, \$r2, \$r3)
2. I-format (Immediate format: op \$r1, \$r2, Immd)
3. J-format (Jump format: op Immd)

## Instruction Address

- Instructions stored in memory
- Instructions are 32-bits long
- Instructions are word-aligned

Program Counter (PC) is a special register that keeps the address of the instruction being executed by processor

## Branch Instruction Encoding

Immediate is only 16-bits, addresses are 32 bits. Immediate is not long enough

- Specify target address **relative to PC**

- Since instructions are word aligned, can treat the immediate as number of words away from PC

- Can branch up to  $2^{15}$  words away from PC,  $2^{17}$  bytes

Branch Calculation:

If the branch is **not taken**:

$$PC = PC + 4$$

( $PC + 4$  is address of next instruction)

If the branch is **taken**:

$$PC = (PC + 4) + (\text{immediate} \times 4)$$

Note: immd field specifies number of words to jumps, which is the **same** as the number of instructions to skip over

## J-format

For jumps, can jump anywhere in memory, not small jumps so cannot use PC-relative addressing

Want to specify a 32-bit address to jump to, but cannot due to 6-bit opcode  
Getting the address:

1. Start with 26-bits
2. Instructions are word aligned, so last two bits are always 00, can omit (like branching), now have 28-bit
3. Choose **4 most significant bits from PC+4**, cannot jump to anywhere in memory but should be sufficient. Max jump range: 256MB boundary

## Summary

- Branches and load/store are both I-format instructions, but branch use **PC-relative addressing** while load/store uses **base addressing**

- Jumps use **pseudo-direct addressing**

- shifts use R-format, but other immediate instructions use I-format

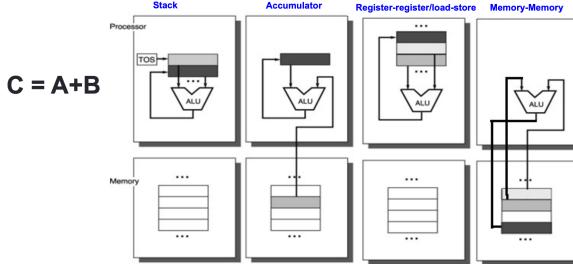
## Instruction Set Architecture

### 5 concepts of ISA design

1. Data Storage
2. Memory Addressing Modes
3. Operations in Instruction Set
4. Instruction Formats
5. Encoding the Instruction Set

### 1. Data Storage

Stack	Accumulator	Register (load-store)	Memory-Memory
Push A	Load A	Load R1,A	Add C, A, B
Push B	Add B	Load R2,B	
Add	Store C	Add R3,R1,R2	
Pop C		Store R3,C	



## 2. Memory Addressing Mode

- Given  $k$  bit address, address space is of size  $2^k$
- Each memory transfer consists of one word of  $n$  bits

Processor contains:

- Memory Address Register (MAR):  $k$ -bit address bus between processor and memory (one direction CPU → mem)
- Memory Data Register (MDR):  $n$ -bit data bus (bidirectional for read and write)
- control lines: eg read/write control

## Endianness

The relative ordering of the bytes in a multiple-byte word stored in memory

- Big-endian: MSB stored in lowest address
- Little-endian: LSB stored in lowest address

Eg. For 0xDE AD BE EF

- Big-endian: 0: DE, 1: AD, 2: BE, 3: EF
- Little-endian: 0: EF, 1: BE, 2: AD, 3: DE

NOTE: Ordering **within** bytes are not affected, only ordering **between** bytes

## Addressing Modes

In MIPS, 3 addressing modes

1. Register: Operand is in register
2. Immediate: Operand is specified in instruction directly
3. Displacement: Operand is in memory with address calculated as Base + Offset (lw/sw)

## 4. Instruction Format

Instruction Length:

- Variable length: More flexible (but complex) and compact instruction set, requires multi-step fetch and decode
- Fixed length: Easier fetch and decode, simplify pipelining and parallelism, but instruction bits are scarce

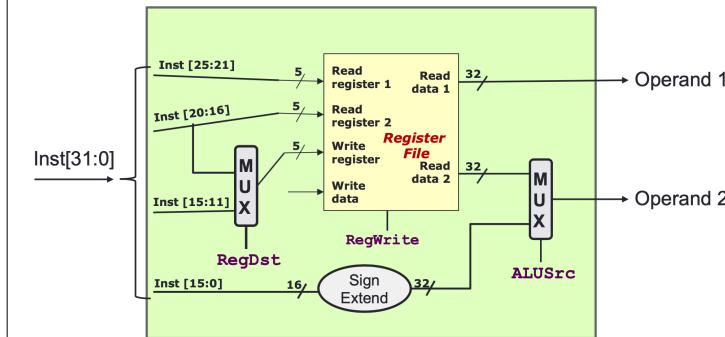
## 5. Encoding the Instruction Set

Things to be decided:

- No. of registers
- No. of addressing modes
- No. of operands in instruction

Expanding Opcode scheme for fixed length instructions

- Opcode has variable length for different instructions
- Eg. 16 bit fixed length instruction, 2 types of instructions, 1 operand and 2 operand, each operand takes 5 bits
- Type A: 6-bit opcode, 2\*5-bit operand
- Type B: 11-bit opcode, 1\*5-bit operand
- To maximise no. of instructions: Give more 6-bit prefixes to type B
- To minimise no. of instructions: Give more opcodes to type A

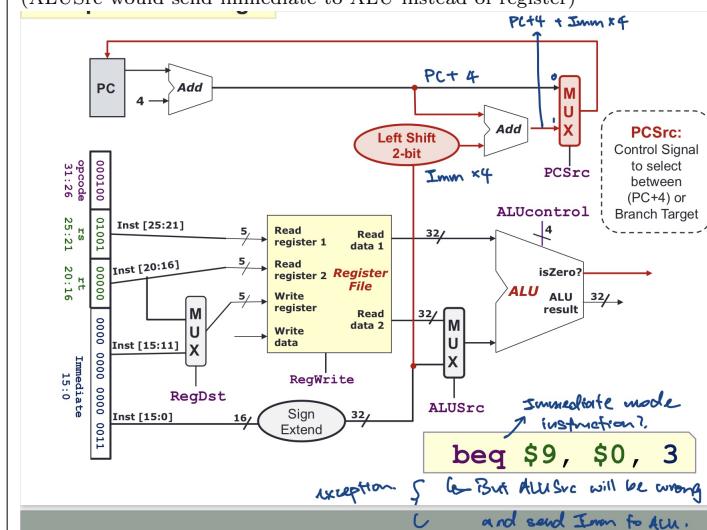


## 3. ALU Stage aka EX stage

- takes in 2 32-bit numbers
- outputs 32-bit result and 1 bit signal isZero for branching
- 4-bit control signal called ALUcontrol

Exception Branch instructions

- need to perform 2 calculations: Branch outcome and target address
- current circuit would be wrong because branching is I-format instruction (ALUSrc would send immediate to ALU instead of register)



## 4. Memory Stage

Only load and store instructions need to perform operations in this stage.

- Use memory address calculated by ALU stage
- Read or write to data memory

All other instructions remain idle

Data memory

- Inputs: memory address, data to be written (Write Data) for store instructions
- Output: Data read from memory for load instructions
- Control: Read and write controls

R W

1 undefined (should not have this case)

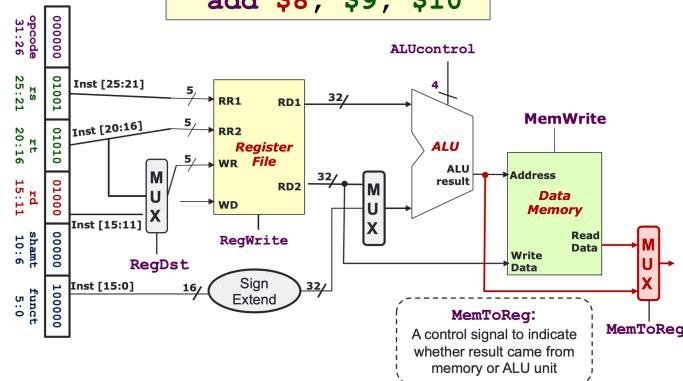
0 1 write

1 0 read

0 0 nothing

For store instructions, need to connect RD2 (rt) to Write Data.

Need to choose between output from Read Data and output from ALU stage



NOTE: MemToReg mux is mounted upside down ie. 1 is Read Data, 0 is ALU result

## 5. Register Write Stage

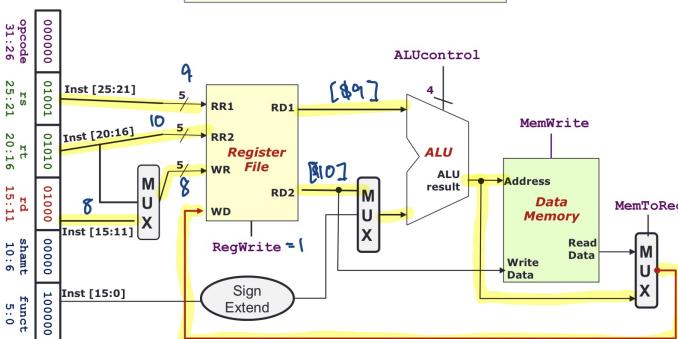
Write to register (stores, arithmetics, loads, slt, etc)

Just connect correct result to Register File Write Data input.

- Control: RegWrite, 1 write 0 nothing

## 5.5 Register Write Stage: Routing

**add \$8, \$9, \$10**



Control Signal	Execution Stage	Purpose
<b>RegDst</b>	Decode/Operand Fetch	Select the destination register number
<b>RegWrite</b>	Decode/Operand Fetch RegWrite	Enable writing of register
<b>ALUSrc</b>	ALU	Select the 2nd operand for ALU
<b>ALUControl</b>	ALU	Select the operation to be performed
<b>MemRead / MemWrite</b>	Memory	Enable reading/writing of data memory
<b>MemToReg</b>	RegWrite	Select the result to be written back to register file
<b>PCSrc</b>	Memory/RegWrite	Select the next PC value

- Generate all of these signals using opcode (and funct, for R-type) using combinational circuit

### PCSrc

Note only need opcode (that it is a branch instruction) but also if the branch is taken (isZero == 1).

- Therefore, need to combine the two signals using AND gate

### ALUControl

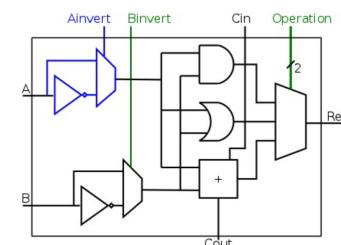
All control signals other than ALUControl can be generated from opcode only (the signals are the same for all R-type), only ALUControl needs funct code (as opcode is 0 for all R-type)

- only exception is shifts?

ALUcontrol	Function
0000	AND
0001	OR
0010	add
0110	subtract
0111	slt
1100	NOR

- 4 control bits are needed:

- **Ainvert**:  
■ 1 to invert input A
- **Binvert**:  
■ 1 to invert input B
- **Operation (2-bit)**:  
■ To select one of the 3 results



Picture shows 1 "slice" of 32-bit ALU. Can think of actual ALU as 32 slices back to back

NOTE: SUB is implemented by inverting all bits in B, setting first  $C_{in}$  to 1  

$$A + B' + 1 = A + 2s \text{ comp of } B$$

### Multilevel Decoding

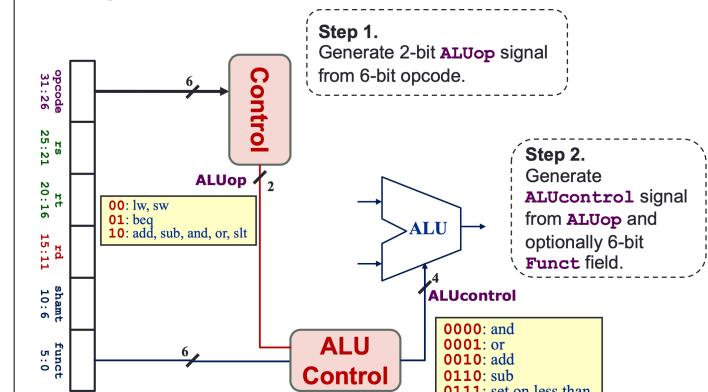
- Use some of the input to reduce cases, then generate full output
- Simplifies design process, reduce size of main controller, speedup circuit

### Intermediate Signal: ALUop

- Use opcode to generate 2-bit ALUop signal

Instruction	ALUop	What
lw/sw	00	ADD
beq	01	SUB
R-type	10	depends on funct

Use ALUop signal and funct field from R-type to generate 4-bit ALUcontrol

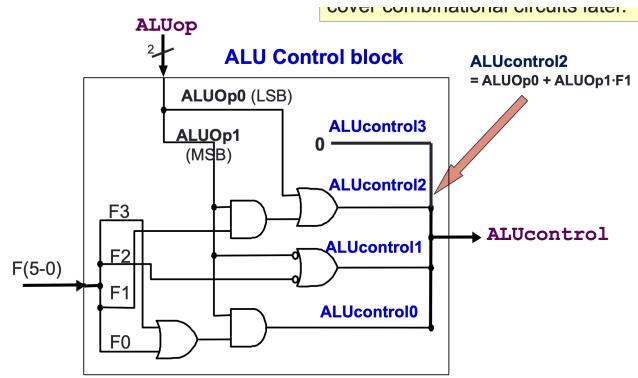


Opcode	ALUop	Instruction Operation	Funct field	ALU action	ALU control
lw	00	load word	xxxxxx	add	0010
sw	00	store word	xxxxxx	add	0010
beq	01	branch equal	xxxxxx	subtract	0110
R-type	10	add	10 0000	add	0010
R-type	10	subtract	10 0010	subtract	0110
R-type	10	AND	10 0100	AND	0000
R-type	10	OR	10 0101	OR	0001
R-type	10	set on less than	10 1010	set on less than	0111

- Table of Opcode, funct field and corresponding ALUop and ALUcontrol signals

	ALUop		Funct Field (F[5:0] == Inst[5:0])						ALU control
	MSB	LSB	F5	F4	F3	F2	F1	F0	
lw	0	0	X	X	X	X	X	X	0 1 1 0
sw	0	0	X	X	X	X	X	X	0 0 1 0
beq	0	X	1	X	X	X	X	X	0 1 1 0
add	1	0	X	X	X	0	0	0	0 0 1 0
sub	1	0	X	X	X	0	0	1	0 1 1 0
and	1	0	X	X	X	0	1	0	0 0 0 0
or	1	0	X	X	X	0	1	0	0 0 0 1
sll	1	0	X	X	X	1	0	1	0 1 1 1

- Table of how to generate each bit of ALUControl



- Circuit of ALUControl Block

$$ALUControl0 = (ALUop_1 \cdot F_3) + (ALUop_1 \cdot F_0) = ALUop_1 \cdot (F_0 + F_3)$$

$$ALUControl1 = (ALUop_1 \cdot F_2)'$$

$$ALUControl2 = ALUop_0 + ALUop_1 \cdot F_1$$

$$ALUControl3 = 0$$

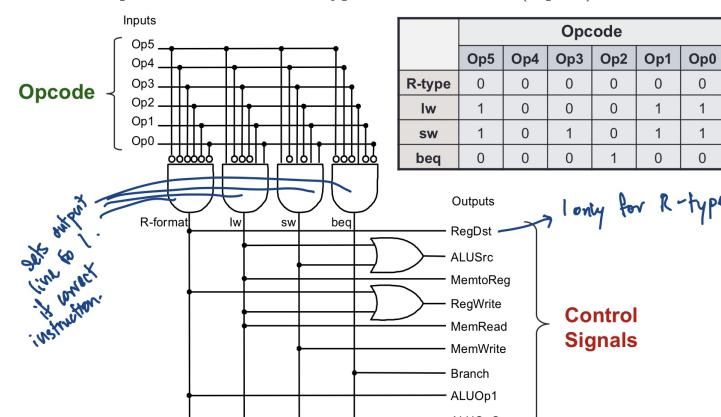
#### Control Design

	RegDst	ALUSrc	MemTo Reg	Reg Write	Mem Read	Mem Write	Branch	ALUop	
								op1	op0
R-type	1	0	0	1	0	0	0	1	0
lw	0	1	1	1	1	0	0	0	0
sw	X	1	X	0	0	1	0	0	0
beq	X	0	X	0	0	0	1	0	1

- Table of control signals for various instructions (outputs)

	Opcode ( Op[5:0] == Inst[31:26] )						
	Op5	Op4	Op3	Op2	Op1	Op0	Value in Hexadecimal
R-type	0	0	0	0	0	0	0
lw	1	0	0	0	1	1	23
sw	1	0	1	0	1	1	2B
beq	0	0	0	1	0	0	4

- Table of opcode for the various types of instructions (inputs)



#### Instruction Execution

- 1. Read contents of register or memory
- 2. Perform computation
- 3. Write results

Perform all within a clock period to prevent reading a storage element when it is being written

#### Single Cycle Implementation

- All instructions take one cycle - Cycle must be at least as long as slowest instruction
- All instructions take as much time as slowest instruction

#### Multicycle Implementation

- Break up instructions into execution steps (IF, ID, EX, MEM, WR)
  - Each execution step takes 1 clock cycle  $\Rightarrow$  cycle time much shorter
  - Cycle must be long enough to accommodate longest step
  - Each step takes as much time as longest step
  - Instructions take variable number of clock cycles to complete execution
- Not covered

#### Pipelining

- One step per clock cycle
- Execute different steps of multiple instructions simultaneously

#### Boolean Algebra

##### Precedence of Operators

- Not (')
- And (.)
- Or (+)

##### Boolean Algebra Laws

TODO: add pictures here

#### Duality

If AND/OR operators and identity elements 0/1 in a Boolean Equation are interchanged, it remains valid

#### Theorems

TODO: add picture here

#### Standard Form

Every boolean expression can be expressed in SOP or POS.

- Literals: Boolean variable or complemented form, eg. x or  $x'$
- Product Term: single literal or a product (AND) of several literals, eg x or  $x.y.z'$
- Sum Term: single literal or a sum (OR) or several literals, eg x or  $x+y+z$
- Sum-of-Products (SOP): product term or sum (OR) of product terms, eg x,  $x.y.z'$ ,  $x + y.z$ ,
- Product-of-Sums (POS): sum term or product (AND) of sum terms, eg x,  $x+y+z'$ ,  $x.(x+y)$

#### Minterm and Maxterm

- Minterm of n variables is a **sum term** that contains n literals from all the variables

e.g. for two variables x, y, minterms are  $x'.y'$ ,  $x'.y$ ,  $x.y'$ ,  $x.y$