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Math Stats 7<sup>th</sup> WMS What Is Statistics?

The following notes are from *Mathematical Statistics with Applications*, 7<sup>th</sup> ed. by Wackerly, Mendenhall & Scheaffer.

# What Is Statistics?

# 1.1 Introduction

#### 1.1 Definition (statistics).

**Statistics** is a theory of information with inference-making as its objective.

#### 1.1 Remark (The objective of statistics).

The objective of statistics is to make an inference about a population based on information contained in a sample from that population and to provide an associated measure of goodness for the inference.

## 1.2 Definition (population).

A *population* is the large body of data that is the target of our interest.

#### 1.3 Definition (sample).

A *sample* is a subset selected from a population.

# 1.2 Characterizing a Set of Measurements: Graphical Methods

### 1.1 Note (relative frequency histogram).

Given data set [2.1, 2.4, 2.2, 2.3, 2.7, 2.5, 2.4, 2.6.2.6, 2.9] we can construct the *relative frequency histogram*:

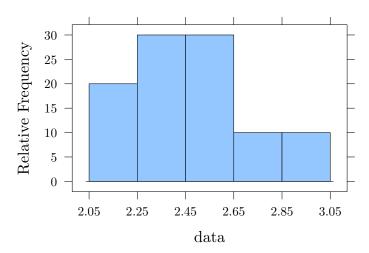


Figure 1: Relative Frequency Histogram

- 2 out of the 10 values, [2.1, 2.2], lie between 2.05 and 2.25.
- 3 out of the 10 values, [2.4, 2.3, 2.4], lie between 2.25 and 2.45.
- 3 out of the 10 values, [2.5, 2.6, 2.6], lie between 2.45 and 2.65.
- 1 out of the 10 values, [2.7], lies between 2.65 and 2.85.
- 1 out of the 10 values, [2.9], lies between 2.85 and 3.05.

#### 1.2 Remark.

When choosing the intervals of a histogram:

- 1. Choose so that it is impossible for a measurement to fall on a point of division. The idea is to separate the data into distinct buckets and look at what perecentage of the total data set is contained in each bucket. The 'buckets' correspond to the chosen intervals. If intervals are chosen such that a data point falls exactly between two intervals, then it's ambiguous as to which interval the data point lies in.
- 2. You could choose an interval that contains every data point but this defeats the purpose of using the histogram to visualize the relative frequency of data in the data set. You could also choose many small intervals which each contain at most one data point but this would defeat the purpose of broadly visualizing the relative frequency of data in the data set. The number of intervals should scale appropriately with the size of the data set.

#### 1.2 Note.

The probability that an arbitrary value from a data set will lie in a given interval of a relative frequency histogram for that data set is equal to the percentage of the total area of the histogram lying over that interval.

#### 1.1 Example.

The total area of the histogram of Fig.1 is:

$$(2.25 - 2.05) \cdot 0.2 + (2.45 - 2.05) \cdot 0.3 + (2.65 - 2.45) \cdot 0.3 + (2.85 - 2.65) \cdot 0.1 + (3.05 - 2.85) \cdot 0.1 = 0.2$$

The area of the histogram in the interval [2.05, 2.45] is:

$$(2.25 - 2.05) \cdot 0.2 + (2.45 - 2.05) \cdot 0.3 = 0.1$$

So, based on this histogram, the probability that an arbitrary data point lies between 2.05 and 2.45 is 0.1/0.2 = 0.5 = 50%.

# 1.3 Characterizing a Set of Measurements: Numerical Methods

#### 1.4 Definition (mean).

Given a data set  $[y_1, y_2, \dots, y_n]$ , the **mean** of the data set is given by:

$$\bar{y} = \frac{1}{n} \sum_{i=1}^{n} y_i$$

### 1.1 Notation $(\bar{y})$ .

When the data set is a sample, the mean is denoted  $\bar{y}$ , read "y bar".

#### 1.2 Notation $(\mu)$ .

When the data set is a population, the mean is denoted  $\mu$ .

#### 1.5 Definition (population variance).

Given a population  $[y_1, y_2, \dots, y_n]$ , the **population variance** of the population is given by:

$$\sigma^{2} = \frac{1}{n} \sum_{i=1}^{n} (y_{i} - \mu)^{2}$$

### 1.6 Definition (sample variance).

Given a sample  $[y_1, y_2, \ldots, y_n]$ , the **sample variance** of the population is given by:

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (y_{i} - \bar{y})^{2}$$

Math Stats 7<sup>th</sup> WMS List of Notation A

# Appendix

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