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1 Building Abstractions with Procedures

Definition (computational process).

Abstract beings that inhabit computers.

Definition (data).

Computational processes manipulate other abstract things called ***data*** as they evolve.

Definition (program).

A pattern of rules by which the evolution of a computational process is directed.

Definition (programming language).

That in which programs are carefully composed from symbolic expressions that prescribe the tasks we want our computational processes to perform.

Definition (bug, glitch).

Small errors.

Definition (debug).

Remove bugs.

Programming in Lisp

See the [appendix](#).

Appendix

A Notes on LISP

A.1 McCarthy 1960

Recursive Functions of Symbolic Expressions and Their Computation by Machine, Part I

LISP:

- LISt Processor
- Developed for the IBM 704 computer by the Artificial Intelligence group at M.I.T.
- Designed to facilitate experiments with a proposed system called the *Advice Tracker*:
 - a machine that could be instructed to handle declarative as well as imperative sentences and could exhibit “common sense” in carrying out its instructions.
 - originally proposed in November 1958.
- main requirement was a programming system for manipulating expressions representing formalized declarative and imperative sentences so that the Advice Taker system could make deductions.

Definition (conditional statement).

A *conditional expression* has the form

$$(p_1 \rightarrow e_1, p_2 \rightarrow e_2, \dots, p_n \rightarrow e_n)$$

where each p_i is a propositional expression and each e_i is an expression of any kind.

It is read “if p_1 then e_1 , else if p_2 then e_2 , else ... else if p_n then e_n . ”

Determining the value, starting from $i = 1$:

- If p_i is undefined or if $i = n$ and p_n is false, then the value is *undefined*.
- If p_i is true, then the value is e_i .
- If p_i is false, check p_{i+1} .

Example.

- $(1 < 2 \rightarrow 4, 1 > 2 \rightarrow 3) = 4$
- $(2 < 1 \rightarrow 4, 2 > 1 \rightarrow 3, 2 > 1 \rightarrow 2) = 3$
- $(2 < 1 \rightarrow 4, T \rightarrow 3) = 3$
- $(2 < 1 \rightarrow \frac{0}{0}, T \rightarrow 3) = 3$
- $(2 < 1 \rightarrow 3, 4 < 1 \rightarrow 4)$ is undefined.
- $(2 < 1 \rightarrow 3, 4 < 1 \rightarrow 4)$ is undefined.

Example.

- $|x| = (x < 0 \rightarrow -x, T \rightarrow x)$
- $\delta_{ij} = (i = j \rightarrow 1, T \rightarrow 0)$
- $\text{sgn}(x) = (x < 0 \rightarrow -1, x = 0 \rightarrow 0, T \rightarrow 1)$

Example (recursive functions).

- $n! = (n = 0 \rightarrow 1, T \rightarrow n \cdot (n + 1)!)$
- $\text{gcd}(m, n) = (m > n \rightarrow \text{gcd}(n, m), \text{rem}(n, m) = 0 \rightarrow m, T \rightarrow \text{gcd}(\text{rem}(n, m), m))$
- $\text{sqrt}(a, x, \epsilon) = (|x^2 - a| < \epsilon \rightarrow x, T \rightarrow \text{sqrt}(a, \frac{1}{2}(x + \frac{a}{x}), \epsilon))$

Example (propositions).

- $p \wedge q = (p \rightarrow q, T \rightarrow F)$
- $p \vee q = (p \rightarrow T, T \rightarrow q)$
- $\neg p = (p \rightarrow F, T \rightarrow T)$
- $p \supset q = (p \rightarrow q, T \rightarrow T)$

Definition (function).

A **function** has the form

$$\lambda((x_1, \dots, x_n), \mathcal{E})$$

where (x_1, \dots, x_n) is a list of n variables and \mathcal{E} is a form of those variables.

Example.

$$\lambda((x, y), y^2 + x)(3, 4) = 19$$

Remark.

Variables occurring in the list of variables are dummy or bound variables. We may change the names of the bound variables in a function expression without changing the value of the expression, provided that we make the same change for each occurrence of the variable and do not make two variables the same that previously were different.

Example.

$$\lambda((x, y), y^2 + x) = \lambda((u, v), v^2 + u)$$

Definition ($\text{label}(a, \mathcal{E})$).

$\text{label}(a, \mathcal{E})$ denotes the expression \mathcal{E} provided that occurrences of a within \mathcal{E} are to be interpreted as referring to the expression as a whole.

Example.

λ -notation is inadequate for naming functions defined recursively. For example, we can convert

the definition

$$\text{sqrt}(a, x, \epsilon) = (|x^2 - a| < \epsilon \rightarrow x, T \rightarrow \text{sqrt}\left(a, \frac{1}{2}\left(x + \frac{a}{x}\right), \epsilon\right))$$

into

$$\text{sqrt} = \lambda((a, x, \epsilon), (|x^2 - a| < \epsilon \rightarrow x, T \rightarrow \text{sqrt}\left(a, \frac{1}{2}\left(x + \frac{a}{x}\right), \epsilon\right)))$$

but the right-hand side cannot serve as an expression for the function because there would be nothing to indicate that the reference to sqrt within the expression stood for the expression as a whole.

The *label* notation makes explicit what symbol in \mathcal{E} should refer to the statement itself. Thus we can write

$$\text{label}(\text{sqrt}, \lambda((a, x, \epsilon), (|x^2 - a| < \epsilon \rightarrow x, T \rightarrow \text{sqrt}\left(a, \frac{1}{2}\left(x + \frac{a}{x}\right), \epsilon\right))))$$

as a name for our sqrt function.

A.2 LISP 1.5 Programmer's Manual

LISP 1.5 Programmer's Manual

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