CCE5225 Assignment II PGM 2020-21

January 30, 2021

1 Assignment - Probabilistic Graphical Models

- 1.0.1 Year 2020-2021- Semester I
- 1.0.2 CCE5225
- 1.1 #### Developed by Adrian Muscat, 2020

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Submit a pdf version (with the attached plagiarism form) of the final jupyter notebook (as a turn-it-in job on VLE) and the jupyter notebook itself separately (as an assignment job on VLE)

```
[1]: import numpy as np
     import pickle
     import re
     from skmultilearn.problem_transform import BinaryRelevance
     from sklearn.utils._testing import ignore_warnings
     from sklearn.exceptions import ConvergenceWarning
     from sklearn.model_selection import GridSearchCV
     from sklearn.preprocessing import LabelEncoder, OneHotEncoder,
      \hookrightarrowMultiLabelBinarizer
     from sklearn.linear_model import LogisticRegression
     from sklearn.multioutput import ClassifierChain
     import pandas
     from collections import Counter
     def saveAnswer(obj, name):
         answer_file = open(f'saved_answers/{name}.pkl', 'wb')
         pickle.dump(obj, answer_file)
         answer_file.close()
     def trimSubClasses(labels):
         pattern = re.compile(r'.+?(?=_\d+(?!.))')
         # Ensure each object label does not contain a suffix of regex pattern ''_{\perp} \setminus d''_{\perp}
      → (such as car_1, person_3, etc, returning car, person, etc instead)
         labels = [[label if not pattern.match(label) else pattern.match(label).
      →group(0) for label in row] for row in labels]
```

return labels [2]: infile = open('MLC_data_2020_21.pkl','rb') data = pickle.load(infile, encoding='latin1') infile.close() [3]: train_obj_labels = trimSubClasses(data['development']['object_labels']) train_out_labels = data['development']['output_labels'] train_geo_feat = data['development']['geometric_features'] test_obj_labels = trimSubClasses(data['test']['object_labels']) test_out_labels = data['test']['output_labels'] test_geo_feat = data['test']['geometric_features']

2 Section 1: Preparing the data

2.1 Part 1

```
[4]: # 1.a. Computing the mean output label count per example, per dataset
     \rightarrow (development and test)
     average_out_count_train = 0
     average_out_count_test = 0
     for row in train_out_labels:
         average_out_count_train += len(row)
     for row in test out labels:
         average_out_count_test += len(row)
     average_out_count_train /= len(train_out_labels)
     average_out_count_test /= len(test_out_labels)
     print('Answer to 1.a:')
     print('Mean output labels per row (train set): ', average_out_count_train)
     print ('Mean output labels per row (test set): ', average_out_count_test)
     saveAnswer({
         'train_average_out': average_out_count_train,
         'test_average_out': average_out_count_test
     }, '1a')
```

```
Answer to 1.a:
Mean output labels per row (train set): 2.1584763696214435
Mean output labels per row (test set): 2.148496240601504
```

```
[5]: # 1.b. Flatten the output labels to a 1-d array, computing the distribution for → both datasets
```

```
# Flatten the labels into a 1D array
flat_out_train = np.concatenate(train_out_labels)
flat_out_test = np.concatenate(test_out_labels)
# Count the numbers of each label
train_out_counts = Counter(flat_out_train)
test_out_counts = Counter(flat_out_test)
# Create dataframes from each counter object above.
train_out_counts_df = pandas.DataFrame.from_dict(train_out_counts,_
→orient='index')
train_out_counts_df.index.name = 'Label distribution in development (train) set'
test_out_counts_df = pandas.DataFrame.from_dict(test_out_counts, orient='index')
test_out_counts_df.index.name = 'Label distribution in test set'
print("Results for 1.b:")
display(train_out_counts_df)
display(test_out_counts_df)
saveAnswer({
    'train out counts': train out counts df,
    'test_out_counts': test_out_counts_df
}, '1b')
```

Results for 1.b:

0 Label distribution in development (train) set next_to 1411 at_the_level_of 926 near 2276 behind 1055 opposite 267 359 on in_front_of 1102 above 117 under 432 far from 376 593 against outside_of 43 beyond 42 around 34 56 in 69 along 22 none

Label distribution in test set

0

```
270
in_front_of
                                  136
against
next_to
                                  359
at_the_level_of
                                  227
near
                                  578
under
                                  101
behind
                                  270
far from
                                  100
                                   88
on
opposite
                                    66
above
                                    31
                                    16
along
                                    5
beyond
around
                                    8
                                    18
in
outside_of
                                    8
none
                                    5
```

```
[6]: # 1.c. Computing the composite output labels (without flattening like in 1.b)
     \rightarrow for both datasets.
     # Same as above, compute the occurances of each composite output label.
     # Unlike above, we first need to transform each row from an unhashable list to \Box
     \rightarrowa hashable tuple object.
     train cmp out counts = Counter(map(tuple, train out labels))
     test_cmp_out_counts = Counter(map(tuple, test_out_labels))
     train_cmp_out_counts_df = pandas.DataFrame.from_dict(train_cmp_out_counts,_u
     →orient='index')
     train_cmp_out_counts_df.index.name = 'Composite output label distribution in_
     test_cmp_out_counts_df = pandas.DataFrame.from_dict(test_cmp_out_counts,__
     →orient='index')
     \texttt{test\_cmp\_out\_counts\_df.index.name} = \texttt{'Composite output label distribution in}_{\sqcup}
     ⇔test set'
     print('Results for 1.c:')
     display(train_cmp_out_counts_df)
     display(test_cmp_out_counts_df)
     saveAnswer({
         'train_out_counts': train_cmp_out_counts_df,
         'test_out_counts': test_cmp_out_counts_df
     }, '1c')
```

Results for 1.c:

```
(behind, opposite, near)
                                                          3
    (on,)
                                                        135
    (in front of, near)
                                                        269
    (near, behind)
                                                         31
    (opposite, beyond)
                                                          1
    (in_front_of, opposite, under)
                                                          1
    (outside_of, next_to, at_the_level_of, near)
                                                          1
    (in_front_of, next_to, opposite, near)
                                                          1
    (against, at_the_level_of)
                                                          1
    [317 rows x 1 columns]
                                                       0
    Composite output label distribution in test set
    (in_front_of, against)
                                                       7
    (next_to, at_the_level_of, near)
                                                     132
    (under,)
                                                      53
    (at_the_level_of,)
                                                       9
    (in_front_of, next_to, at_the_level_of, near)
                                                       2
    (above, next_to, against, behind, near)
                                                       1
    (in, on)
                                                       1
    (in_front_of, next_to, against)
    (around, against, near)
    (next_to, at_the_level_of, far from)
    [166 rows x 1 columns]
[7]: # 1.d Computing the co occurrence probability distribution of the training set.
    def computeProbabilityMatrix(matrix):
         # Get all the unique labels from the input matrix.
        labels = np.unique(np.concatenate(train_out_labels))
         # Create the output matrix for the probabilities.
        distribution = pandas.DataFrame(np.zeros(((len(labels)), (len(labels)))),
     distribution.index.name = 'co occurrence probabilities'
         # Get all co occurrences
        for sample in matrix:
            for target in labels:
                 if target in sample:
                    for prep in sample:
                         distribution[target][prep] += 1
```

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Composite output label distribution in developm...

(next_to, at_the_level_of, near)

```
targetCount = 0
    coCount = 0
    # Calculate the probabilities by dividing the 2nd labels co occurrences_{\sqcup}
→with the 1st labels total occurrences
    for target in labels:
        for prep in [label for label in labels if label != target]:
            targetCount = distribution[target][target]
            coCount = distribution[prep][target]
            distribution[prep][target] = coCount / targetCount
        # Set the targets to 0 to avoid bias
        distribution[target] [target] = 0
    return distribution
probDistribution = computeProbabilityMatrix(train_out_labels)
display(probDistribution)
saveAnswer({
    'coOccurrenceProbMatrix': probDistribution
}, '1.d')
```

	above	against	along	around	\
co occurrence probabilities					
above	0.000000	0.034188	0.000000	0.000000	
against	0.006745	0.000000	0.008432	0.008432	
along	0.000000	0.072464	0.000000	0.000000	
around	0.000000	0.147059	0.000000	0.000000	
at_the_level_of	0.006479	0.109071	0.019438	0.000000	
behind	0.032227	0.067299	0.019905	0.001896	
beyond	0.047619	0.023810	0.000000	0.000000	
far from	0.026596	0.000000	0.002660	0.000000	
in	0.017857	0.232143	0.000000	0.000000	
in_front_of	0.012704	0.060799	0.019964	0.000000	
near	0.029438	0.027241	0.023726	0.000000	
next_to	0.017009	0.096386	0.039688	0.000000	
none	0.000000	0.000000	0.000000	0.000000	
on	0.013928	0.571031	0.000000	0.000000	
opposite	0.022472	0.041199	0.000000	0.000000	
outside_of	0.046512	0.069767	0.000000	0.000000	
under	0.000000	0.324074	0.002315	0.016204	

	at_the_le	vel_of	beł	nind b	eyond	far f	rom \	
co occurrence probabilities								
above	0.	051282	0.290	0.0	17094	0.085	470	
against	0.	170320	0.119	9730 0.0	01686	0.000	000	
along	0.	260870	0.304	1348 0.0	00000	0.014	493	
around	0.	000000	0.058	3824 0.0	00000	0.000	000	
at_the_level_of	0.	000000	0.032	2397 0.0	01080	0.019	438	
behind		028436	0.000	0.0	23697	0.152	607	
beyond		023810	0.595		00000	0.452		
far from		047872	0.428		50532	0.000		
in		000000	0.000		00000	0.000		
in_front_of		036298	0.061		09074	0.159		
near		315466	0.259		02636	0.000		
next_to		532955	0.141		00709	0.002		
none		000000	0.000		00000	0.002		
on		000000	0.002		00000	0.000		
		172285	0.142		11236	0.000		
opposite		093023	0.302		00000	0.037		
outside_of								
under	0.	011574	0.087	963 0.0	02315	0.011	5/4	
								,
	in	in_from	it_oi	nea	r ne	xt_to	none	\
co occurrence probabilities	0 000547	0.44		0 57045		05100	0 0	
above	0.008547		19658	0.57265		05128	0.0	
against	0.021922		12985	0.10455		29342	0.0	
along	0.000000		L8841	0.78260		11594	0.0	
around	0.000000		00000	0.00000		00000	0.0	
at_the_level_of	0.000000		13197	0.77537		12095	0.0	
behind	0.000000		34455	0.55924		.88626	0.0	
beyond	0.000000		38095	0.14285		23810	0.0	
far from	0.000000	0.46	88085	0.00266		07979	0.0	
in	0.000000	0.00	00000	0.00000	0.0	00000	0.0	
in_front_of	0.000000	0.00	00000	0.54537	2 0.1	.89655	0.0	
near	0.000000	0.26	34060	0.00000	0 0.5	12742	0.0	
next_to	0.000000	0.14	18122	0.82707	3 0.0	00000	0.0	
none	0.000000	0.00	00000	0.00000	0.0	00000	0.0	
on	0.069638	0.05	50139	0.03621	2 0.0	05571	0.0	
opposite	0.000000	0.26	39663	0.62921	3 0.1	79775	0.0	
outside_of	0.000000	0.39	95349	0.44186	0.3	02326	0.0	
under	0.000000	0.06	37130	0.16435	2 0.0	46296	0.0	
	on	opposit	te ou	itside_of	u	nder		
co occurrence probabilities				_				
above	0.042735	0.05128	32	0.017094	0.00	0000		
against	0.345700	0.01855		0.005059		6088		
along	0.000000	0.00000		0.000000		4493		
around	0.000000	0.00000		0.000000		5882		
at_the_level_of	0.000000	0.04967		0.004320		5400		
behind	0.000948	0.03601		0.012322		6019		
= = == == == == ==	3.000010	0.0000						

```
beyond
                          0.000000 0.071429
                                              0.000000 0.023810
                          0.000000 0.026596
far from
                                              0.026596 0.013298
                          0.446429 0.000000
                                              0.000000 0.000000
in
in_front_of
                          0.016334 0.065336
                                              0.015426 0.026316
                          0.005712 0.073814 0.008348 0.031195
near
                          0.001417 0.034018 0.009213 0.014174
next to
none
                          0.000000 0.000000 0.000000 0.000000
                          0.000000 0.000000 0.000000 0.000000
on
                          0.000000 0.000000 0.003745 0.018727
opposite
                                              0.000000 0.000000
                          0.000000 0.023256
outside_of
                          0.000000 0.011574
                                              0.000000 0.000000
under
```

2.2 Part 2

```
[8]: #2.a Transform the object and geometrical features into an input matrix.
     # Trim the file names from the inputs.
     train_trimmed = np.array(train_obj_labels)[:, 1:]
     test_trimmed = np.array(test_obj_labels)[:, 1:]
     # Transform the features into one-hot encoded.
     obj_encoder = OneHotEncoder(sparse=False)
     obj_encoder = obj_encoder.fit(train_trimmed)
     train_input_matrix = obj_encoder.transform(train_trimmed)
     test_input_matrix = obj_encoder.transform(test_trimmed)
     # Append the geometrical features onto the obtained one-hot features.
     train_input_matrix = np.append(train_input_matrix, train_geo_feat, axis=1)
     test_input_matrix = np.append(test_input_matrix, test_geo_feat, axis=1)
     saveAnswer({
         'train_input_matrix': train_input_matrix,
         'test_input_matrix': test_input_matrix
     }, '2.a')
     XTrain = train_input_matrix
     XTest = test_input_matrix
```

```
[9]: # 2.b Transform the output features into a multi-label output matrix.

# Use a multi-label binarizer to one-hot encode and reduce multiple features
into a single vector.

out_one_hot = MultiLabelBinarizer()
out_one_hot = out_one_hot.fit(train_out_labels)

train_output_matrix = out_one_hot.transform(train_out_labels)

test_output_matrix = out_one_hot.transform(test_out_labels)
```

```
saveAnswer({
    'train_output_matrix': train_output_matrix,
    'test_output_matrix': test_output_matrix
}, '2.b')

yTrain = train_output_matrix
yTest = test_output_matrix
```

2.3 Part 3

```
[10]: # 3 Functions for calculating accuracy metrics
      def getMatrix(predictions, truths):
          # Generate a single confusion matrix for all labels
          tp = 0
          fp = 1
          fn = 2
          tn = 3
          # Initialise an empty array.
          matrix = [0, 0, 0, 0]
          # Over each prediction-truth pair, update the confusion matrix for that \Box
       \rightarrow label.
          for (plabel, tlabel) in np.nditer([predictions, truths], flags=['refs_ok']):
              if plabel == 1 and tlabel == 1: matrix[tp] += 1
              elif plabel == 1 and tlabel == 0: matrix[fp] += 1
              elif plabel == 0 and tlabel == 1: matrix[fn] += 1
              elif plabel == 0 and tlabel == 0: matrix[tn] += 1
          return matrix
      def getMatrices(predictions, truths, num_labels):
          # Generate a multi-label confusion matrix
          tp = 0
          fp = 1
          fn = 2
          tn = 3
          # Initialise an empty set of arrays.
          matrices = [[0, 0, 0, 0] for i in range(0, num_labels)]
          it = np.nditer([predictions, truths], flags=['multi_index', 'refs_ok'])
          # Over each prediction-truth pair, update the confusion matrix for that
       \rightarrow label.
```

```
for plabel, tlabel in it:
        i = it.multi_index[1] # This is the label index
        if plabel == 1 and tlabel == 1: matrices[i][tp] += 1
        elif plabel == 1 and tlabel == 0: matrices[i][fp] += 1
        elif plabel == 0 and tlabel == 1: matrices[i][fn] += 1
        elif plabel == 0 and tlabel == 0: matrices[i][tn] += 1
   return matrices
# 3.a Accuracy (intersection over union)
def getAccuracy(predictions, truths):
   # Get the overall accuracy
   matrix = getMatrix(predictions, truths)
   correct = matrix[0] + matrix[3] # tp + tn
   total = sum(matrix) # tp + fp + fn + tn
   return correct / total
# 3.b Precision
def getPrecision(predictions, truths):
   # Get the overall precision
   matrix = getMatrix(predictions, truths)
   positives = matrix[0] # tp
   positiveGuesses = matrix[0] + matrix[1] # tp + fp
   return positives / positiveGuesses
# 3.c Recall
def getRecall(predictions, truths):
   # Get the overall recall
   matrix = getMatrix(predictions, truths)
   positives = matrix[0] # tp
   allPositives = matrix[0] + matrix[2] # tp + fn
   return positives / allPositives
# 3.d Per-label precision
def getMultiLabelPrecision(predictions, truths):
   # Get the per-label precision
   matrices = getMatrices(predictions, truths, len(truths[0]))
   precisions = [0 for i in range(len(matrices))]
   for i, (tp, fp, fn, tn) in enumerate(matrices):
```

```
p = tp + fp
precisions[i] = (tp / p) if p != 0 else 0

return precisions

# 3.e Per-label recall

def getMultiLabelRecall(predictions, truths):
    # Get the per-label recall
    matrices = getMatrices(predictions, truths, len(truths[0]))

recalls = [0 for i in range(len(matrices))]

for i, (tp, fp, fn, tn) in enumerate(matrices):
    allPositives = tp + fn
    recalls[i] = (tp / allPositives) if allPositives != 0 else 0

return recalls
```

3 Section 2

3.1 Part 1

```
[11]: # 4.a Develop a binary-relevance model set using logistic regression, first
       → trained through cross-validation and then training the best br model on the
       \rightarrow whole training set.
      parameters = [
          {
              'classifier': [LogisticRegression()],
              'classifier__solver': ['sag', 'saga'],
              'classifier__C': [1.0, 0.5, 1.5],
              'classifier__max_iter': [250, 500, 100],
              'classifier__class_weight': [None, 'balanced'],
              'classifier__warm_start': [True],
              'classifier__random_state': [12]
          }
      ]
      clf = GridSearchCV(BinaryRelevance(), parameters, scoring='accuracy', __
      →verbose=2, n_jobs=4)
      clf.fit(XTrain, yTrain)
      display(clf.best_params_, clf.best_score_)
      print(f'Best estimator achieved an accuracy score of {clf.best_score_} and ∪
       →trained in {clf.refit_time_:.2f} sec')
```

```
predictions = clf.predict(XTest).todense()
saveAnswer({
    'trained_model': clf,
    'predictions': predictions
}, '4.a')
Fitting 5 folds for each of 36 candidates, totalling 180 fits
[Parallel(n_jobs=4)]: Using backend LokyBackend with 4 concurrent workers.
[Parallel(n_jobs=4)]: Done 33 tasks
                                          | elapsed: 1.1min
[Parallel(n_jobs=4)]: Done 154 tasks
                                          | elapsed: 4.8min
[Parallel(n_jobs=4)]: Done 180 out of 180 | elapsed: 5.6min finished
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear model/ sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
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converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
```

```
converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear model/ sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
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  warnings.warn("The max_iter was reached which means "
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/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
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converge
  warnings.warn("The max_iter was reached which means "
/home/zachc/.local/lib/python3.8/site-packages/sklearn/linear_model/_sag.py:329:
ConvergenceWarning: The max_iter was reached which means the coef_ did not
converge
  warnings.warn("The max_iter was reached which means "
{'classifier': LogisticRegression(max_iter=500, random_state=12, solver='sag',_
 →warm_start=True),
 'classifier__C': 1.0,
 'classifier__class_weight': None,
 'classifier__max_iter': 500,
 'classifier__random_state': 12,
 'classifier__solver': 'sag',
 'classifier__warm_start': True}
0.0338582981958941
```

Best estimator achieved an accuracy score of 0.0338582981958941 and trained in

10.93 sec

```
[12]: # 4.b Metrics on the trained models from 4.a
     # Next, compute the metrics accordingly.
     brAcc = getAccuracy(predictions, yTest)
     brPre = getPrecision(predictions, yTest)
     brRec = getRecall(predictions, yTest)
     brPrePerLabel = getMultiLabelPrecision(predictions, yTest)
     brRecPerLabel = getMultiLabelRecall(predictions, yTest)
     # In the case of the multi-label metrics, convert them into dataframes for
      \rightarrow readability.
     brPrePerLabel = pandas.DataFrame(brPrePerLabel, index=out_one_hot.classes_,_
      brRecPerLabel = pandas.DataFrame(brRecPerLabel, index=out_one_hot.classes_,_
      print(f'Accuracy: {brAcc}')
     print(f'Precision: {brPre}')
     print(f'Recall: {brRec}')
     display(brPrePerLabel)
     display(brRecPerLabel)
     saveAnswer({
         'accuracy': brAcc,
         'precision': brPre,
         'recall': brRec,
         'multiPrecision': brPrePerLabel,
         'recPerLabel': brRecPerLabel
     }, '4.b')
```

Accuracy: 0.8857253427686864 Precision: 0.6102719033232629 Recall: 0.2650918635170604

BR Precision above 0.000000 against 0.000000 along 0.000000 around 0.000000 at_the_level_of 0.000000 behind 0.681818 beyond 0.000000 far from 0.625000 0.000000 in_front_of 0.672131 near 0.597605 0.000000 next_to

```
0.000000
none
                     0.000000
οn
                     0.000000
opposite
                     0.000000
outside_of
                     1.000000
under
                 BR Recall
                  0.000000
above
                  0.000000
against
along
                  0.000000
around
                  0.000000
at_the_level_of
                  0.000000
behind
                  0.222222
beyond
                  0.000000
far from
                  0.050000
                  0.00000
in
in_front_of
                  0.151852
near
                  0.863322
                  0.000000
next_to
                  0.000000
none
on
                  0.000000
                  0.000000
opposite
outside_of
                  0.000000
under
                  0.009901
```

3.2 Q5: Construct a bayesian network

Aim is to construct a bayesian network using the above-generated co occurrence probability distribution.

3.2.1 Associated labels

First would be to identify the strongest-pairing labels to other labels (and vice-versa to obtain dead-end labels/pairs).

Immediately, it can be concluded that every variable is independent of none.

Otherwise, getting the co occurrences with the a probability of at least 0.4, we get to following:

[13]:		target	prep	P(target prep)
	0	next_to	near	0.827073
	1	at_the_level_of	next_to	0.812095
	2	along	next_to	0.811594
	3	along	near	0.782609
	4	at_the_level_of	near	0.775378
	5	opposite	near	0.629213
	6	beyond	behind	0.595238
	7	above	near	0.572650
	8	on	against	0.571031
	9	behind	near	0.559242
	10	in_front_of	near	0.545372
	11	next_to	at_the_level_of	0.532955
	12	near	next_to	0.512742
	13	far from	in_front_of	0.468085
	14	beyond	far from	0.452381
	15	in	on	0.446429
	16	outside_of	near	0.441860
	17	far from	behind	0.428191

Based on the above, dependencies can be drawn from the pairs to form a basic bayesian network, modelling the probability that any one state will also include any other connected state.

There are also two cyclic links from the above, which need to be removed. Doing so leaves the following.

The graph is divided into two components, with the near label being the root of the greatest of the two graphs. It does not include the around or under labels, which did not have a very strong dependency on the graph nodes. none is also not shown as it is not dependent on any other label (since none cannot be derived/derive any other label).

This leaves the above graph, which can be converted into a chain order for training the bayesian chain classifier.

```
['above' 'against' 'along' 'around' 'at_the_level_of' 'behind' 'beyond'
'far from' 'in' 'in_front_of' 'near' 'next_to' 'none' 'on' 'opposite'
'outside_of' 'under']
```

Derived chain order from above network is:

```
'in_front_of', 'far from', 'beyond', 'outside_of', 'against', 'on', 'in',
     'none', 'around', 'under']
[15]: # 6: Retrain the model using the bayesian network
     # bccParams = clf.best_params_
     # bccParams = {str(key).replace('classifier__', ''): val for key, val in_
      →bccParams.items()}
     # del bccParams['classifier']
     @ignore_warnings(category=ConvergenceWarning)
     def getFittedBCC(x, y, order):
         chainParams = {
             'order': [
                 order.
             ]
         }
         clf = GridSearchCV(ClassifierChain(LogisticRegression()), chainParams)
         return clf.fit(x, y)
     bccClf = getFittedBCC(XTrain, yTrain, chain_order_1)
     bccPredictions = bccClf.predict(XTest)
[16]: print(f'Best chain: {bccClf.best_params_["order"]}')
     # Get the metrics
     bccAcc = getAccuracy(bccPredictions, yTest)
     bccPre = getPrecision(bccPredictions, yTest)
     bccRec = getRecall(bccPredictions, yTest)
     bccPrePerLabel = getMultiLabelPrecision(bccPredictions, yTest)
     bccRecPerLabel = getMultiLabelRecall(bccPredictions, yTest)
     # Convert them into dataframes
     bccPrePerLabel = pandas.DataFrame(bccPrePerLabel, index=out_one_hot.classes_,_
      bccRecPerLabel = pandas.DataFrame(bccRecPerLabel, index=out_one_hot.classes_,_
      # Concatenate the final BCC metrics with the BR metrics for comparison.
     finalPerLabelPre = pandas.concat([brPrePerLabel, bccPrePerLabel], axis=1)
     finalPerLabelRec = pandas.concat([brRecPerLabel, bccRecPerLabel], axis=1)
```

['near', 'next_to', 'along', 'at_the_level_of', 'opposite', 'above', 'behind',

finalPerLabelMetrics = pandas.concat([finalPerLabelPre, finalPerLabelRec],_

 \rightarrow axis=1)

```
print('\nFinal metrics:')
display(finalMetrics)
print('\nFinal per-label metrics:')
display(finalPerLabelMetrics)

saveAnswer({
    'bnChain': bccClf.best_params_['order'],
    'classifier': bccClf,
    'finalMetrics': finalMetrics,
    'finalPerLabelMetrics': finalPerLabelMetrics
}, '6')
```

Best chain: [10, 11, 2, 4, 14, 0, 5, 9, 7, 6, 15, 1, 13, 8, 12, 3, 16]

Final metrics:

BR BCC
Accuracy 0.885725 0.888545
Precision 0.610272 0.560268
Recall 0.265092 0.548994

Final per-label metrics:

	BR Precision	BCC Precision	BR Recall	BCC Recall
above	0.000000	0.600000	0.000000	0.096774
against	0.000000	0.389831	0.000000	0.338235
along	0.000000	1.000000	0.000000	0.125000
around	0.000000	1.000000	0.000000	0.125000
at_the_level_of	0.000000	0.432886	0.000000	0.568282
behind	0.681818	0.632124	0.222222	0.451852
beyond	0.000000	0.000000	0.000000	0.000000
far from	0.625000	0.518072	0.050000	0.430000
in	0.000000	0.500000	0.000000	0.111111
in_front_of	0.672131	0.514894	0.151852	0.448148
near	0.597605	0.692542	0.863322	0.787197
next_to	0.000000	0.511848	0.000000	0.601671
none	0.000000	0.000000	0.000000	0.000000
on	0.000000	0.522936	0.000000	0.647727
opposite	0.000000	0.200000	0.000000	0.015152
outside_of	0.000000	0.000000	0.000000	0.000000
under	1.000000	0.532710	0.009901	0.564356

4 Q7: Evaluation of results

The performance results for both models are quite interesting, in that both achieved a near-equal accuracy of 89%. BCC sees a decline in precision of 5% compared to BR, suggesting it returns fewer quality results compared to the BR model. Looking at the per-label distribution, however,

shows that the BCC model in fact performs better on most labels. The BR model did not make any predictions on some labels, only predicting with a handful of labels.

BCC saw the largest improvement in terms of recall, with an overall score of 55% compared to the 27% of the BR model. Looking at the per-label recall shows that the BR model only predicted positives for a handful of labels. BCC seemed to make a greater variety of predictions, going for labels which the BR model didn't make any predictions on.

The above results suggest that the BR model tended towards only a handful of labels as possible predictions, likely due to it not correlating any possible relations between the labels. BCC does not seem to face this issue, being able to make multiple label predictions for a single sample and trying other labels as predictions. This is in large part to the order of labels in which it is trained as derived from the bayesian network modelled above. Based on these results, it appears as though the BCC definitely improved over the BR model based on the higher recall and precision, with a relatively smaller reduction in precision. This can be an acceptable tradeoff depending on the nature of the multi-label problem, the relationships between the labels presented and what metrics will be more favourable in that problem. For those which do not see any relation between many/all of the labels, it might be suitable to use the Binary Relavance model. For those problems which have multiple intercompatible labels (such as this scenario where near might frequently be classified alongside next_to), having a model such as the Bayesian Chain Classifier being aware of those relationships may show improved performance as it did here.