Algorithm performs  $28 \text{ n}^2 + 30 \text{ n} \log^2 2 \text{ n} + 78 \text{ operations}$ . Determine its asymptotic time complexity (among all valid options select the most commonly used notation)

- O(28 n^2 + 30 n log^2 n + 78)
- O(n<sup>2</sup>)
- O(n^2 + n log^2n)
- O(28 n^2)

All constants are insignificant in big O notation, so this expression is equivalent to  $n^2 + n \log^2 n$ , moreover, since  $O(n^2) > O(n \log^2 n)$  we can drop the second term, the final result is  $O(n^2)$ 

What is the time complexity of this algorithm? Please provide the most accurate estimation

```
1 var count = 0;
for (int i = 1; i < n*n; i *= 3)
count++;
```

- O(n^2)
- O(n)
- 0(1)
- O(n log n)
- O(log n)
- O(log^2 n)

This loop iterates over values  $1, 3, 9, ..., 3^k < n^2$ , where  $3^{k+1} \ge n^2$ . So we make k operations, and the value of k is:  $\log(3^k) < \log(n^2) \Rightarrow k < \log(n^2) = 2\log(n) \Rightarrow k = O(\log(n))$ 

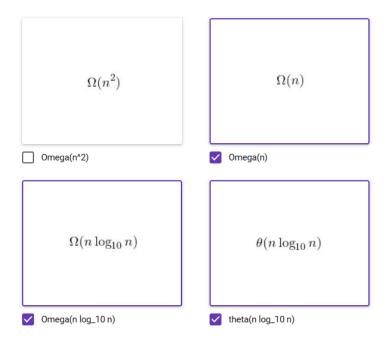
What is the time complexity of this function? Please provide the most accurate estimation

```
foo(arr):
    n = length(arr)
    for i from 0 to n-1:
        swapped = false
        for j from 0 to n-1-i:
            if arr[j] > arr[j+1]:
                swap(arr[j], arr[j+1])
                swapped = true
        if not swapped:
            break
    return arr
O(n^2)
```

- O(n log n)
- O(n)
- O(n^3)

This is bubble sort implementation, time complexity of which is  $O(n^2)$ 

```
f(n) = n + n \log_{-}10 n
Select all classes to which f(n) belongs
```





Intuitively, omega is "greater or equal than", theta is "equal to", O is "smaller or equal than"

- 1)  $\Omega(n^2)$  is **not correct**, because  $n \log_{10} n$  grows slower than  $n^2$
- 2)  $\Omega(n)$  is **correct** since  $n \log_{10} n$  grows faster than n
- 3)  $\Omega(n \log_{10} n)$  is **correct**, since it is equal to the function we have
- 4)  $\Theta(n \log_{10} n)$  is **correct**, since it is equal to the function we have
- 5)  $\Theta(n \log_2 n)$  is **correct**, since base of the log does not matter, so this equal to our function
- 6)  $O(n \log_{10} n)$  is **correct**, since it is equal to our function
- 7) O(n) is **not correct**, since n grows slower than  $n \log_{10} n$ , so it is not greater or equal to f(n)
- 8)  $O(n^2)$  is **correct**, since  $n^2$  grows faster than  $n \log_{10} n$

#### Quiz 2

Which iterator type allows both forward and backward traversal but not random access?

$\cap$	Forward	Iterato
$\smile$		

Bidirectional Iterator

Contiguous Iterator

Random Access Iterator

Forward iterator allows only forward traversal, and contiguous and random access iterators both provide random access, so the answer is **bidirectional iterator** 

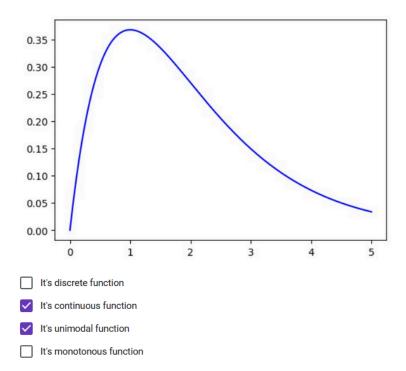
Suppose that in <b>multiplicative</b> approach of dynamic array implementation we grow the capacity by a factor of 1.5 instead of 2. What would be the impact on the performance?	
No difference in performance	
Lower memory wastage but higher amortized insertion cost	
Higher memory wastage but lower amortized insertion cost	
○ Insertions will always be O(1)	
Since we allocate less memory after each rehash, less memory could remain unused, the same time we will ran out of free space more frequently, therefore a higher amort insertion cost	
A sorting algorithm is considered <b>stable</b> if:	
It sorts elements in O(n log n) time	
It does not use extra memory	
It preserves the relative order of equal elements	
It always sorts in ascending order	
This is just the definition	
Suppose we want sort an array of objects, that are easy to compare, but really computationally heavy to swap. Which of this 3 quadratic sorting algorithms would be the most efficient in this case?	
O Bubble sort	
Selection sort	
○ Insertion sort	
Both bubble and insertion sorts do $O(n^2)$ swaps in the worst case, but selection sort does $O(n)$ swaps.	always
Which of the following lines would sort vector vec of Student objects by GPA in descending order?	
<pre>struct Student { std::string name; double gpa; };</pre>	
std::sort(vec.begin(), vec.end(), [](Student a, Student b) { return a.gpa < b.gpa; });	
<pre>std::sort(vec.begin(), vec.end(), [](const Student &amp;a, const Student &amp;b) { return a.gpa &gt; b.gpa; });</pre>	
std::sort(vec.begin(), vec.end());	
std::sort(vec.begin(), vec.end(), std::greater<>());	

Last 2 options are not correct, since default comparators we will be sorting students by the first value, in particular by their name. Among first 2 options the first one will sort them in ascending order, so the second option is correct.

Which data structure is commonly used to implement a priority queue?
○ Linked List
Binary Heap
Oictionary
○ Stack
In priority queue we want to be able to insert values, get the smallest element, and to be able to delete it. All this operations are exactly what binary heap provides.
What is the average time complexity for finding the k-th smallest element using D&C approach?
<ul><li>O(n)</li></ul>
O(nlogn)
O(nlogk)
O(n^2)

The algorithm for that is similar to quick sort, but instead of recursively going into both parts we go into only to the side that contains k-th element, so the average time complexity is linear

Choose all correct facts about this function



This is not a discrete function, since we see that it is defined for non integer values, but it is a continuous function. This function has only 1 extremum, therefore it is unimodal. And lastly, it is not monotonous, since in increases, and then decreases

Given the following program what would be it's output?

```
a = [1, 1, 3, 4, 6, 7, 7, 7, 10, 11]
L = -1
R = 10
while (R - L > 1):
 M = (L + R) // 2
 if (a[M] >= 7):
  R = M
 else:
  L = M
print(L, R)
\bigcirc 34
45
O 57
O 67
78
79
```

In this implementation of binary search we are moving right boundary if the element is greater or equal to 7. Therefore in the end R would be placed on the first instance of 7, which

has the index 5. And the condition for stopping the loop is that difference between L and R is not greater then 1. Therefore L would be equal to 5 - 1 = 4. Answer is  $\bf 4 \ \bf 5$ 

	rted array of size n and q queries to check whether a given element rray. What would be the time complexity of answering all the
O(n log	+ q log q)
O(n log	+ n log q)
O(q log	
O(n log	
O(n+q)	
=	ted so we can use binary search for finding each element. One binary search work time, and since we run it 1 time for each of the q queries, the time complexity is
search? f - monotono f can be con	the complexity for finding such x that: $f(x) = 0$ using continuous binary as function, $f(a) = -5$ , $f(b) = 5$ and $f(a) = -5$ , $f(b) = -5$
O(log n)	
O(log(b-	- log(eps))
O(log(b	))
O(log(b	) + log(eps))
decreasing	g binary search while $r-l>\varepsilon$ to get the required precision. And since we are he distance between r and l by a factor 2 on each iteration, we will have to do erations, which by properties of logarithm is equal to $\log(b-a)-\log(\varepsilon)$
Quiz 4	
	re of SinglyLinkedList <int64> and SinglyLinkedListNode<int64> in is the length of the list? (assuming 64-bit architecture)</int64></int64>
O 16; 16	
<ul><li>16n; 16</li></ul>	
O 16n; 8	
O 16; 8	
8n; 16	
8; 16	

int 64 occupies 8 bytes, and in SinglyLinkedListNode we have to store 2 of them, 1 for the value, and 1 for the pointer to the next node. So the size of SinglyLinkedListNode would be 16 bytes. And therefore the size of SinglyLinkedList would be  $16 \cdot n$  bytes

Which STL structures can be used to implement a stack?
✓ std::deque
✓ std::vector
std::queue
✓ std::list
Deque can be used to implement the stack, since it has both push_back and pop_back operations. Same thing with vector. Queue however is not suitable, since it does not allow pop_back operations. And finally list is suitable here, because again, we can both add and delete elements to the back.
A stack is used to check if a sequence of k types of brackets is a correct bracket sequence (every bracket is given by its type - a number between 1 and k - and if it's opening or closing). What is the time complexity of the algorithm?
○ O(n + k)
O(n)
O(k)
O(nk)
The algorithm for doing that is iterating over the sequence, and maintaining a stack with opened brackets. Since operations with stack are $O(1)$ the time complexity would be just $O(n)$ , because of iterating over the sequence.
Consider some array of 5 positive numbers. Let's call a subsegment "good" if its sum is no more than 10. Let $f(L)$ be the number of "good" segments of the form [L; R]. Which of the following are valid values of $f(L)$ ?
[0, 0, 0, 0, 0]
<b>[</b> 5, 4, 3, 2, 1]
[1, 2, 3, 2, 1]
[1, 3, 2, 1, 2]
[1, 3, 3, 1, 1]

Option [1,3,2,1,2] is definitely invalid because for the last position of L there exists only 1 segment. Option [1,3,3,1,1] is invalid because after moving from L=3 to L=4 value of f(L) could not have decreased more then by 1. That is because if we had some valid segment [L;R], then segment [L+1;R] would also be valid since we have decreased the sum. So the only segment that we lose is when L=R.

All other options satisfy this criteria so they are valid.

A fully persistent stack is initially empty. How many nodes are there after 3 push and 2 pop operations?

3

Persistent stack creates new node after each push, and doesn't change the amount of nodes during pop. So the answer is 3

#### Quiz 5

Which operations with std::set<int> X can be performed in worst-case O(log n)?

union(X, Y)

get kth order statistic (kth element in ascending order)

insert element

check if X contains x

find the number of elements less than or equal to m

Insert and contains are  $O(\log n)$ . All other operations are not doable in this time complexity

Consider a function H(K). What conditions should H(K) always satisfy to be a **hash** function?

H(K1) = H(K2) => K1 = K2

H(K1) != H(K2) => K1 != K2

K1 != K2 => H(K1) != H(K2)

K1 = K2 => H(K1) = H(K2)

The main issue with hashes is that there might be collisions, so that for different values  $K_1$  and  $K_2$ , we have same hashes. So option 3 is incorrect. Also, from this it follows that option 1 is incorrect because by having the same hashes we can not deduct that the values are the same. Both other options are correct because hash function is deterministic, so for same values it would always produce the same result.

Which of the following is a collision for this hash function?

```
int N = 97, p = 3;
int hash(std::string key) {
   int hash = 0;
   int p_pow = 1;
   for (auto c : key) {
      hash = (hash + (c - 'a') * p_pow) % N;
      p_pow = (p_pow * p) % N;
   }
   return hash;
}

   'aq', 'aaaq'
   'aba', 'abaa'
   'baab', 'bab'
   None of the above
```

Carefully looking into the code, we see that for each character a value of 'a' is subtracted, so if we have symbol 'a' in our string it will not be significant in the final value of the hash. So both strings in the second option will have the same hash, cause they have character 'b' on the same position

A hash table contains 5000 elements and has capacity 2<sup>15</sup> = 32768. What is the approximate **load factor** of this hash table?

0.0004

0.0032

0.1526

6.5536

333.33

2500

 $\frac{5000}{32768} \approx 0.1526$ 

factor reaches 1. The hash table is initially empty. What's the <b>average</b> time complexity of n insert operations?
O(n sqrt(n))
O(n^2)
O(n)
<ul><li>O(n log n)</li></ul>
Let's say we have n elements and the capacity is now 2n. We are making n insertions. On average first one will take $\frac{2n}{n}$ , second will take $\frac{2n}{n-1}$ and so on. Overall we will have $2n\left(\frac{1}{n}+\frac{1}{n-1}+\ldots+\frac{1}{1}\right) \leq 2n\log n$ , thus, $O(n\log n)$
An array a is fixed. You are given queries: for a given segment [LR], calculate f(a[L], a[L+1],, a[R]). For which f can this problem be solved using the prefix approach? (choose all that apply)
✓ product
gcd
✓ sum
min

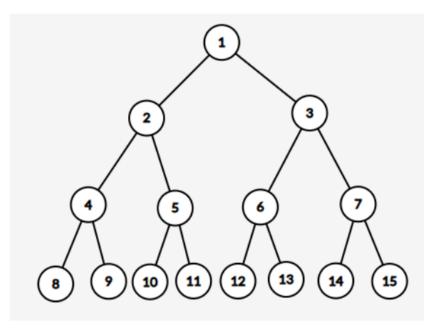
Consider a hash table with open addressing which is rebuilt only when its load

Operations that have an inverse operation are suitable here, therefore product and sum.

There is a segment tree for the sum, built on a 8-element array.

You are going to change the value of the element on the position 2 in the array (0-indexed).

What nodes will be updated?

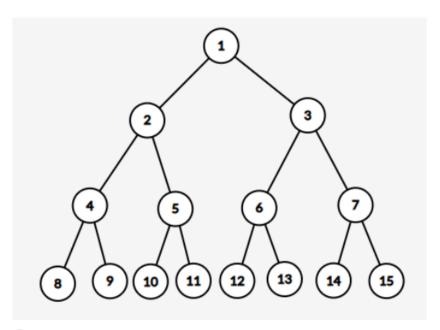


- 0 1, 2, 5, 10
- 0 1, 3, 6, 13
- 0 1, 3, 7, 14
- 0 1, 2, 4, 9
- 0 1, 2, 4, 8

We will update all the nodes on the path from vertex 10 to the root, therefore 1, 2, 5, 10

There a is segment tree for the minimum, built on an 8-element array. \*

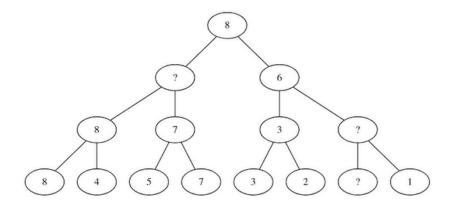
You are asking minimum on the segment [1..5] (0-indexed). What nodes will be used for the result?



- 5, 6, 9
- 5, 9, 14
- 0 6,7,10
- 0 2,3
- 4, 5, 6
- 7, 11, 12
- O 2,6
- 0 6, 8, 11

All the nodes that are entirely inside of the query segment will be used. In this case it will be node 9, 5, 6.

On the picture, there is a segment tree for the maximum. What are the values in the missing nodes?



- 8, 5, 3
- 7,1,6
- 8, 6, 6
- 7,1,1
- 0 8, 4, 4

The first missing value is 8, since value in the node is maximum of its children, so  $\max(7, 8) = 8$ . Next up we have 2 nodes on the right. The upper one must contain value 6, since it's parent has value 6, which should be the maximum of both children, but left child has value 3. And lastly the lower node should also contain value 6 following the same logic.

Given an array a of length n and a function f, we need to answer the following queries:

- calculate f on a[L...R];
- set a[i] = x.

For which f can we answer these queries in O(log n) using a segment tree?

- √ f(a[L...R]) = a\_L \* a\_{L+1} \* ... \* a\_R
- $f(a[L...R], x) = number of L <= i <= R such that a_i >= x$
- f(a[L...R], x) = smallest L <= i <= R such that a\_i >= x
- f(a[L...R]) = the number of L <= i <= R such that a\_i = 0
- f(a[L...R]) = a\_L ^ (a\_{L+1} ^ (... ^ (a\_R)...)) % M

Product is trivial, smallest i such that  $a_i \geq x$  is done having segment tree for maximum and using the idea of descending. The number of zeros is done using segment tree for sum, and changing 0 values to 1, and all others to 0.

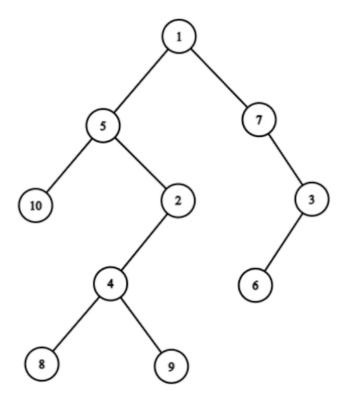
O 11
O 18
O 15
27
O 20
O 22
Initially there are $8+4+2+1=15$ vertices, on each update we add new nodes on the way from the root to the leaf, which is 4. So after 3 updates we will add 12 vertices resulting in 27 vertices in total.
Quiz 7
Consider a tree T with $\bf n$ vertices. How many <b>edges</b> does T have? Let's call a sequence $(v_1, v_2,, v_k)$ , $k \ge 2$ a <b>path</b> if for any $1 \le i < k$ , $(v_i, v_{i+1})$ is an edge in T. Paths $(v_1, v_2,, v_k)$ and $(v_k,, v_2, v_1)$ are considered to be the same. How many <b>paths</b> does T have?
O n-1; n^2
2n; n(n-1)/2
n; n^2
O 2n; 2^n
n; n(n-1)/2
n-1; n(n-1)/2
n(n-1)/2; n^2
Tree is a connected graph without cycles, so there should be at least $n-1$ edge to make it connected, and there can be no more than $n-1$ edge, since otherwise there would be cycles. There is exactly 1 path between each pair of vertices, so the number of paths is the number of pairs of vertices we can choose. This is simply $\binom{n}{2} = \frac{n \cdot (n-1)}{2}$ Answer is $n-1$ ; $\frac{n \cdot (n-1)}{2}$

A persistent segment tree is built on an array of length 8. How many vertices are

there after 3 modifications?

What is the next node in the traverse order?

- 1) LVR
- 2) VLR
- 3) LRV



- UVR: 4, VLR: 5, LRV: 7
- UVR: 1, VLR: 5, LRV: 7
- UVR: 1, VLR: 8, LRV: 6
- UVR: 4, VLR: 1, LRV: 8
- LVR: 1, VLR: 4, LRV: 5
- UVR: 5, VLR: 8, LRV: 6
- UVR: 5, VLR: 4, LRV: 1
- UVR: 4, VLR: 8, LRV: 5
- UVR: 5, VLR: 1, LRV: 7

The order of traversal for the whole tree for all 3 cases:

- 1) LVR: 10, 5, 8, 4, 9, **2, 1**, 6, 3, 7
- 2) VLR: 1, 5, 10, **2**, **4**, 8, 9, 7, 3, 6
- 3) LRV: 10, 8, 9, 4, **2, 5**, 6, 3, 7, 1
- So the answer is 1, 4, 5

In a binary tree T of size n, let L and R be the **left** and the **right** subtrees of a vertex v respectively. Let H(L) be the height of the left subtree, S(L) be its size; same for R. Which of these conditions imply that T is balanced?

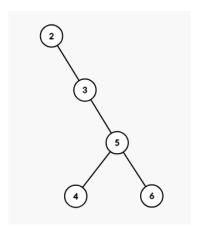
- ✓ for all v, |S(L) S(R)| < 1</p>
- T has at least n/2 leaves
- or all v, |H(L) H(R)| < 2025
- ✓ for all v, |H(L) H(R)| < 1</p>
- for all v, |S(L) S(R)| < 2025

All options with inequalities are correct, since tree is balanced if the height is  $O(\log n)$ , and it can be shown that if for every vertex difference in size, or height between children does not exceed some constant C, in our case 1 or 2025, then the height of such tree is  $O(\log n)$ 

A BST is initially empty. Values are inserted in the following order: 2, 3, 5, 4, 6. What is the resulting **height** of the BST (height defined as the number of edges on the longest path from root to leaf)?

- $\bigcirc$  1
- O 2
- 3
- O 4
- O 5

The tree would look like:



So it can be seen that the height is 3.

	rval [0; M], where M is sufficiently greater than n, and inserted into the BST at is the expected value of the resulting height?
0	O(1)
•	O(log n)
0	O(sqrt(n))
0	O(n)
nsei	rting random values that are uniformly distributed would

A BST is initially empty. n values are chosen randomly and uniformly from the

Inserting random values that are uniformly distributed would result in expected  $O(\log(n))$  height, since each inserted element is equally likely to split the remaining elements into subgroups that are kind of balanced. This resembles the quick sort where we randomly pick a pivot element.

Let `std::set s = {2, 1, 4, 5, 2, 3}'.

What are the results of

1) `lower\_bound(3) - begin()`;

2) `upper\_bound(4) - begin()`?

2, 3

2, 4

2, 5

3, 3

3, 4

3, 5

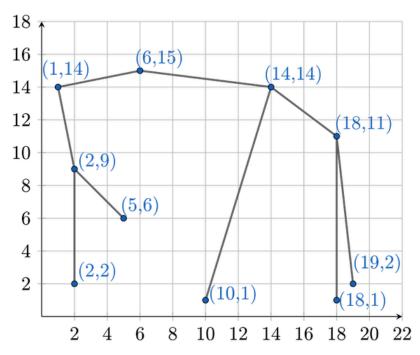
4, 3

4, 4

4, 5

Set would look like  $\{1, 2, 3, 4, 5\}$ . Lower bound would find element 3, since it is the first element not less than 3. Begin points at the first element. So the result of subtraction is 2 Upper bound would find element 5, since it is the first element greater than 4. And again, since begin points at the first element the result would be 4.

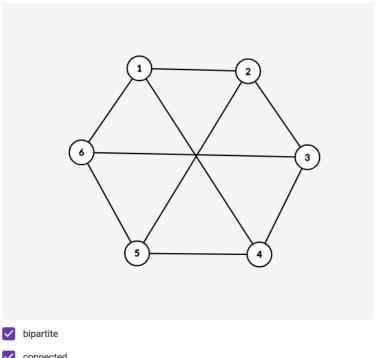
You are given the following treap T. It is split by key k=4 into trees L and R. What is the depth of L?



- $\bigcirc$  0
- O 1
- 2
- O 3

Splitting by k=4 we get 3 elements in tree L: (1, 14), (2, 9), (2, 2). The height of the tree would be 2.

The graph below is ... (choose all correct statements)



connected

acyclic

a tree

regular

This graph is clearly connected, since it has only 1 connectivity component.

This graph is regular, since each vertex has an equal amount of edges.

This graph is bipartite, since we can color vertices from 1 to 6 with alternating colors, and no 2 adjacent vertices will have the same color.

This graph is not acyclic, since there are clearly cycles in it, for example 1-4-5-6-1 This graph is not a tree, since it is not acyclic.

What's the maximum possible number of bridges in a graph on 10 vertices? Articulation points?

0 10; 10

9;8

9;9

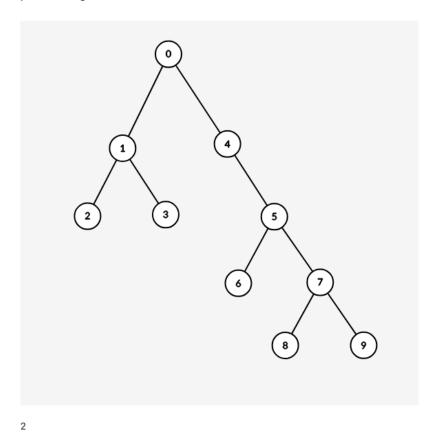
0 10;8

8;55

If we remove the bridges from the graph, it will split into several connectivity components, the maximum we can get is 10, because there are 10 vertices, so the maximum amount of bridges would be 9. An example of such graph is path graph.

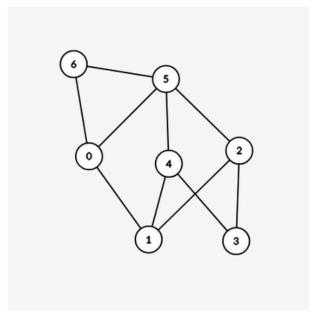
For articulation points same example with path graph works, this way we get 8 articulation points (all vertices except endpoints)

How many centroids does the following tree have? Write the answer as a single positive integer



There are 2 centroids: 4 and 5, since for each of them if we remove it, the remaining trees would have not more than  $\lfloor \frac{n}{2} \rfloor$  vertices

BFS is run on this graph, starting from vertex 0 and processing neighbors in ascending order. What is the maximum size of the queue?



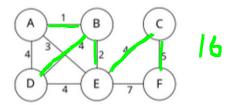
- 2
- 3
- 4
- O 5
- O 6
- O 7

Queue on each step:  $\{0\} \rightarrow \{1,5,6\} \rightarrow \{5,6,2,4\} \rightarrow \{6,2,4\} \rightarrow \{2,4\} \rightarrow \{4,3\} \rightarrow \{3\} \rightarrow \{\}\}$ Therefore the maximum size of queue is 4, after considering vertex 1

Given a graph with O(V) edges and integer edge weights varying from 1 to sqrt(V), which of the following algorithms will solve the SSSP problem with the best time complexity?

- O-k BFS
- Dijkstra with linear search
- Dijkstra with priority queue

We have a sparse graph, so dijkstra with linear search would't work here. 0-k BFS works in O(kV), and in this case  $k = \sqrt{V}$ , so  $O(V\sqrt{V})$ , and since Dijkstra with priority queue works in  $O(V \log V)$ , it would be more optimal here What's the weight of the MST of this graph? Write the answer as a single integer



16

Go over edges in ascending order, take those which reduce the amount of connectivity components.

Take AB (+1), take BE (+2), skip AE, take AD (+4), skip BD, skip DE, take CE (+4), take CF (+5), skip EF

Total: 1 + 2 + 4 + 4 + 5 = 16

Given a graph with all edge weights being 0 or 1, what's the time complexity of finding its MST?

- ( ) O(VE)
- O(V + E)
- O(E log V)
- O(V^2)

In this case we can just use BFS

Suppose all but 2 edges in a graph have different weights. What's the maximum number of MSTs it can have?

- ()
- 2
  - ( ) 3
  - ( ) 4

We can get different MSTs when we have several edges to choose from, since we are considering them in ascending order, it happens when 2 edges have the same weight. There is only 1 such pair of edges, so picking either of them would result in different MST

How many edges are there in a complete directed graph with n vertices?
○ n^2
<ul><li>n(n-1)</li></ul>
○ 2n
○ n-1
For each of n vertices there are n - 1 vertices to make an edge $\Rightarrow n \cdot (n-1)$
How many fundamental cycles in an undirected graph with 10 vertices, 18 edges and 3 connected components?
O 7
○ 8
O 9
O 10
<ul><li>11</li></ul>
O 12
Using formula from the lecture we get 18 - $10 + 3 = 11$
In a DAG with n vertices and no edges, how many different topological orders are there?
O 1
○ n
O n^2
● n!

Since there are no edges, any permutation would be valid  $\Rightarrow n!$ 

	If we build a DP solution using the formula $dp[i] = dp[i-1] + dp[i-2]$ , what is the time complexity of computing $dp[n]$ ?
	<ul><li>O(n)</li></ul>
	O(2^n)
	O(n^2)
	O(log n)
	We calculate dp[i] in $O(1)$ , we need to calculate value of dp for all i from 0 to n $\Rightarrow n \cdot O(1) = O(n)$
	How many different paths are there from vertex 1 to vertex n in a DAG where edges exist only from i to i+1 and from i to i+2?
(	∩^2
(	
(	2^(n-1)
(	n-th fibbonaci number

Let dp[i] be the amount of paths from 1 to i, there are 2 options how we could get to vertex i: from i - 1 or from i - 2. Therefore dp[i] = dp[i-1] + dp[i-2], which is the formula for fibbonaci numbers

A turtle can only move one right or down. The number in each cell indicates the number of coins in this cell. What's the maximum number of coins it can collect on its way from the top left to the bottom right corner? Give the answer as a single integer

0	3	5	2
7	4	8	3
6	9	3	7
8	4	6	0

32

Lets calculate dp:

 $0\ 3\ 8\ 10$ 

7 11 19 22

13 22 25 32

 $21\ 26\ 32\ 32$ 

What's the asymptotic complexity of computing the binomial coefficient {n \choose k} using dynamic programming?

( ) O(n^k)

( ) O(n)

O(n + k)

O(nk)

C[n][k] can be recalculated as C[n-1][k]+C[n-1][k-1], so we recalculate dp in O(1), and there are  $n \cdot k$  values in total, therefore O(nk)

Consider an array A of n integers with the sum 30. It's known that for any 1 <= k <= 30, there exists a subsequence of A with sum k. What is the minimum possible value of n? Give the answer as a single integer

5

Lower bound: n = 5

Proof: Suppose for n=4 we can choose 30 different subsequences with different sums. But there are  $2^4=16$  possible subsequences of A, therefore we can not choose 30 different subsequences

Example for n = 5:  $A = \{1, 2, 4, 8, 16\}$ 

What is the Levenshtein distance between "cat" and "tram"? Give the answer as a single integer

3

 $cat \rightarrow tat \rightarrow trat \rightarrow tram$ 

Consider a variation of question 1 where the turtle can move in all 4 directions, and instead of coins, the numbers represent the damage received when visiting the corresponding cell; the goal is to minimize the total damage. What's the time complexity of the solution for a matrix of size n\*m?

- O(n+m)
- O(n^2)
- O(n\*m\*log(n+m))
- O((n+m)\*log(n+m))
- () O(nm)

Represent the grid as graph, and find shortest path using dijkstra

#### Quiz 12

How many permutations on 5 elements are there?

120

5! = 120

In how many ways can n=5 be decomposed into positive integer summands? Decompositions that differ only by the order of summands are considered the same.

7

Lets just consider all the options: $1+1+1+1+1$ $1+1+1+2$ $1+1+1+2$ $1+2+2$ $1+1+3$ $1+4$ $2+3$ $5$
Given a bitset of n bits, which of the following operations can be done in O(1), assuming n fits into one machine word?
flip all bits
get next bitset in lexicographical order
get kth bit
flip last 1-bit to 0
All options are correct, since n fits into one machine word, and any operation with machine word works in $\mathcal{O}(1)$
What's the time complexity of finding a minimal weight Hamiltonian path?
O(n^2*2^n)
O(n*2^n)
O(2^n)
O(n*n!)
O(n!)
Fastest algorithm is $O(n^2 \cdot 2^n)$ , check the lecture
What is time complexity of algorithm that iterates over all pairs of bit masks and their submasks?
○ 2 <sup>n</sup> n
<ul><li>3<sup>n</sup></li></ul>
○ 4^n
2^(n^2)
Same thing, the algorithm is described in the lecture