ALMOST REAL: AN INVESTIGATION INTO THE METAPHYSICS OF VIRTUAL REALITY.
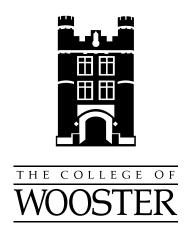
EXAMPLE INDEPENDENT STUDY THESIS

Presented in Partial Fulfillment of the Requirements for
the Degree Bachelor of Arts In Computer Science and
Philosophy in the
Department of Math and Computer Science at The College of
Wooster

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ABSTRACT

This interdisciplinary independent study thesis is divided into five chapters. The first chapter "On Virtual Realism" will outline the author's unique formulation of virtual realism, the ontological thesis that experiences in virtual reality are non-illusory, and that virtual objects truly exist in an equivalent sense to physical objects. Next, "Idealism and Virtual Reality" will describe the metaphysical implications of the idealism of British empiricist George Berkeley and the Yogācāran school of Mahayana Buddhism with respect to a virtual realist project. Although Berkeley and the Yogācāran philosopher Vasubandhu differ in several respects, both author's projects are ultimately sympathetic to the aims of virtual realism. However, the Yogācāran idealism ultimately proves to be the superior choice for the virtual realist. The next chapter "Virtual physicalism" will posit a physicalist reply to the idealism of Vasubandhu and argue for a physicalist account of reality and virtual reality using Occam's razor as inspired by Saul Kripke's argumentation in his article Mad pain and Martian pain. Having established the merits of physicalist account of reality over the idealist standpoint, the remainder of this section will focus on how the metaphysical commitments of physicalism impact a virtual realist worldview. The fourth chapter will describe the implementation of an immersive virtual environment using physicalist principles and discuss how awareness of the virtual nature of a virtual reality environment impacts an agent's experience of said environment. Of specific interest to this project is how ideas from physicalist metaphysics can aid virtual reality designers in crafting non-player character experiences which do not fall victim to the uncanny valley phenomenon (Masahiro Mori's hypothesis that very human-like but slightly imperfect digital entities elicit feelings of eeriness and revulsion among some observers). The fifth chapter describes the methodology and results of a usability study which attempts to measure the effectiveness of these philosophical principles in helping designers remedy the uncanny valley phenomenon in their creations.

This work is dedicated to the future generations of Wooster students.

ACKNOWLEDGMENTS

I would like to acknowledge Prof. Lowell Boone in the Physics Department for his suggestions and code.

VITA

Publications

Fields of Study Major field: Computer Science and Philosophy

Specialization: Human Computer Interactions, Metaphysics, Virtual Reality

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Preface

The purpose of this document is to provide you with a template for typesetting your IS using LaTeX. LaTeX is very similar to HTML in the sense that it is a markup language. What does this mean? Well, basically it means you need only enter the commands for structuring your IS, i.e., identify chapters, sections, subsections, equations, quotes, etc. You do not need to worry about any of the formatting. The `woosterthesis` class takes care of all of the formatting.

Here is how I plan on introducing you to LaTeX. The Introduction gives some reasons for why one might find LaTeX superior to MS Word^TM. Chapter 3 will demonstrate how one starts typesetting a document and works with text in LaTeX. Chapter 4 discusses the creation of tables and how one puts figures into a thesis. Chapter 5 talks about creating a bibliography/references section and an index. There are three Appendices which discuss typesetting mathematics and computer program code. The Afterword will discuss some of the particulars of how a LaTeX document gets processed and what packages the `woosterthesis` class uses and are assumed to be available on your system.

Hopefully, this document will be enough to get you started. If you have questions please refer to **? ? ? ? ?**], or **?**].
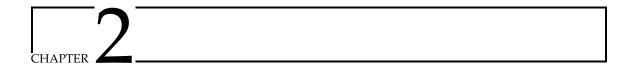
CHAPTER 1

INTRODUCTION

So why would you want to use LaTeX instead of Microsoft Word™? I can think of several reasons. The main one for this author is that LaTeX takes care of all of the numbering automatically. This means that if you decide to rearrange material in your IS, you do not have to worry about renumbering or references. This makes it very easy to play around with the structure of your thesis. The second reason is that it is ultimately faster than Word™. How? Well, after a week or so of using LaTeX you will begin to remember the commands that you use frequently and won't have to use the LaTeX pallet in TeXShop or TeXnicCenter. So you can just type everything including the mathematics, where with Word™ you would have to use the Equation Editor.

I have also tried to make things more efficient by organizing the example folder as follows. There is a `username.tex` file which you will want to rename using your username and which is what you will enter all of the information about your IS into. `username.tex` also has explanations about other files that you might need to edit. In addition there are folders for chapters, appendices, styles, and figures. This structure is there to try and reduce file clutter and to help you stay organized. There should also be a .bib file which you can use as a model for your own .bib file. The .bib file has your bibliographic information.

LaTeX is really easy to learn. For an average IS, the author will only need to learn a handful of commands. For this small bit of effort, you get a tremendous amount of flexibility and a very beautiful document. The following chapters will introduce some of the common things a student might need to do in a thesis.

CHAPTER 2

Are Virtual Things Real?

2.1 Definitions

At first glance, the question, an answer to the question "virtual things real?" appears trivial. Clearly, the pokemon in my handheld game are nothing more than a series of electromagnetic patterns. The same could be said of any sense-experience we have. Before we can investigate the claim "are virtual worlds real?", we must first establish what we mean by the claim. In his article *The Virtual and the Real*, David Chalmers describes the term virtual as having several commonplace definitions. One common meaning of the term"virtual", claims the phrase"virtual X" means something along the lines of"as if X but not X" . On that reading, virtual reality is an unreal as-if reality, and virtual reality is no more reality than a virtual kitten is a kitten. [?] While this definition is widely cited in dictionaries and other authoritative sources of definitions, it does not reflect the termâĂŹs contemporary definition. The advent of modern computer technology has resulted in a second widely used definition of the term"virtual". When used in discussions regarding computing, English speakers tend to mean something along the lines of "a computer-based version of X" when talking about a"virtual X. Under this more contemporary description, virtual reality can be a sort of reality, just a virtual bank is a real bank (insofar as it fulfills all of the roles and functionalities we typically associate with an organization with the label of"bank"). For many readers, this recitation of definitions may appear pedantic. However, the dual definitions of the term"virtual" suggests that perhaps the opposition towards virtual realism is in part motivated by linguistics, just as proponents of the identity thesis in the philosophy of mind struggle with the inherent dualist bias in how English speakers and Western Philosophy think about these ideas. I will discuss this view of mine at greater length at later points in this paper, however for now I will merely say the first term should not be applied to descriptions

of computer systems that instantiate via a combination of hardware and software an environment in which an agent can interact with entities described by software instructions. To apply the first term to these sorts of systems implies either confusion about the nature of these systems or an attempt to argue against virtual realism by begging the question. The second definition presented by Chalmers encompasses a wide array of systems and environments. These spaces range from the permanent and all-encompassing environment depicted in the 1999 science fiction movie *The Matrix* to the ephemeral argumentation of the hit Android and iOS game, *Pokemon Go*. In *Matrix as Metaphysics*, Chalmers argues that"if we are in a Matrix, most of our ordinary beliefs (e.g. that there are tables) are true: if we discovered that we are in a Matrix, instead of saying that there are no tables, we should say instead that tables are computational objects made of bits". Chalmers describes this view as *digitalism*, the claim that (1) Virtual objects really exist and are computational objects; (2) Events in virtual worlds are largely computational events that really take place. (3) Experiences in virtual reality are non-illusory. (4) Virtual experiences are as valuable as non-virtual experiences. In contrast to this view is the digital irrealist thesis, which claims that (1) Virtual objects do not really exist. (3) Experiences in virtual reality are illusory. [**?**]. We shall be using two positions throughout this project as the two primary conflicting views on this topic. However, before we weigh the merits of virtual realism against its opposition, we must first have an account of what is real. This question has been an active battleground for philosophers since the field's inception, 2000 years ago. Most accounts of the real fall either into the dualist, idealist or materialist camps. Substance dualists (SD) hold that there exist two discrete types of substance, physical substance and mental substance. Materialism is the claim that physical matter is the fundamental substance in the universe. This view is opposed by idealism, the claim that ideas or mental substance is fundamental material of reality. The idealist claims that the universe is purely mental, mentally constructed, or otherwise immaterial in nature. All of these positions are theoretically compatible with either virtual realism or virtual realism. However, each view comes with a series of caveats and ontological commitments which may be a deal breaker for many who hold said view.

2.1.1 ARE VIRTUAL OBJECTS REAL?

Virtual realism is unproblematic for the idealist, who asserts that all of reality is immaterial mental substance (in other words, ideas). However, Idealism is a highly outlandish view and difficult for many to wrap their heads around. Why ought we accept this view? The classical Western idealist position was first formalized by Bishop George Berkeley. Berkeley's rejection of the existence of

physical substance is based upon the claim that we can perceive only our own ideas. Berkeley continues by arguing given that no inert substance (such as matter) can have ideas and since matter is an inert substance has sensible qualities, our understanding of matter is by definition contradictory in nature. Berkeley continues by claiming a denial of the claim "If sensible qualities are perceivable, then they must be ideas" in conjunction with his previous assertion that we can perceive only our own ideas implies a conception of matter that is epistemologically inaccessible and hence meaningless. [1] We shall use a similar line of argumentation to justify a virtual realist conception of reality. Virtual objects are weapons, people, buildings and other entities within a virtual environment. These entities are instantiated within the memory of a digital computer by a data structure. Data structures consist of a series of values electromagnetically stored within the memory of the computer. When interpreted by a specific programming language, these values specify the number of bytes to allocate for a given instance or instances of a particular abstract object and specify a series of operations which can be applied to the data stored within the allocated memory. Every action in a given virtual world has a corresponding action within one or more data structure within the memory of the computer which is instancing said virtual world. These data structures can cause the computer to output electromagnetic data which can be transformed by other hardware into images, sounds and other forms of sense data. These electromagnetic emissions also enable it to communicate via wired or wireless connection with other computer systems. Humans and other conscious agents with the appropriate can perceive these electromagnetic emissions as sense-data. Clearly, data structures (via the hardware they are instantiated within) seem to have some level of causal powers. Computers fly jets, drive cars, perform surgery and drive multi-million user cross-continental worlds like EVE Online and World of Warcraft. Yet, books, movies and other forms of media also cause real world events. People clearly have strong emotional The virtual irrealist might claim that these data structures derive their causal power from the programmer who created them or the algorithm which generated them instead of arising from the data structures themselves. Under this view, data structures (and hence virtual objects) are ultimately patterns of interactions between different entities consisting of physical matter whose arrangement is set forth by the actions of a conscious entity. However, the same could be said of books and other other forms of media which the digital realist claims not to constitute real entities (or at least is not committed by definition to claiming). One direction for mitigating this problem is to bite the bullet and adapt a fictionalist stance, which holds that all fictional worlds are real in so much as we can say $\exists X$ where X is some fictional entity within world Y. This line of reasoning is resembles modal realism, the

position which claims that all possible worlds are as real as the actual world.[2] One proponent of this position is David Lewis. Lewis holds

One of the two major schools in Mahayana Buddhism, Yogacara is a form of Buddhistism noted for its denial of the existence of external objects [3] . Literally translated, the term Yogacara means "the practice of yoga", this name reflects the school's origins in metaphysical speculation into the nature of yoga and mediation practices. Many advanced mediation practices involve focusing on ones awareness of purely mental entities, the connection between these expertises and the achievement of Enlightenment motivates the Yogacara's idealist understanding of the universe. Yogacaran metaphysics can be characterized by the term *Cittamatra* (English: "consciousness only"), one of the school's other names. Yoagacarans believe that nothing exists besides mental things. This radical form of idealism seems highly counterintuitive and illogical. However, there are many persuasive arguments for this abnormal view. When somebody suffering from cataracts looks at the moon, they have the experience of seeing the moon as if it were covered in hairs. But clearly a hairy moon is no more real than a moon made out of cheese. Yet for the individual suffering from cataracts, their experience of a hairy moon is just as real as the experience of a desolate rocky moon was for the crew of Apollo eleven. So how do we account for what the person is seeing? Yogacaran philosopher Vasubandhu argues that the person with cataracts is aware of a mental image (deemed an impression) that manifests itself as an external object when there is no such thing outside of the mind. This view is motivated by representationalism, the notion that we "what we are directly aware of in waking memory sensory experience is not the external object, but rather a mental image that resembles the object and is caused by sense-object contact" [3].

In contrast to the "impression only" idealism of the Yogacara, the representationalist viewpoint is compatible with the existence of external objects (i.e: a realist standpoint). Vasubandhu argues that the world is nothing but unreal impressions, analogous to the unreal hairs on the moon *seen* by the cataract sufferer.

Vasubandhu continues by denying the existence of spatial locations. Both realists and idealists like Vasubandhu describe experiences in terms of physical objects, but these experiences could also be explained in terms of images containing colors and shapes. Each of these color/shape images can be described as baring different relations to each other(left, right, etc) [3]. This visual change will change over time, but an observer will eventually discover that certain visual features will reoccur periodically in a predicable manner. From these patterns, an agent can construct a phenomenal language that maps onto the all of the visual elements we typically describe in spatial terms. This language may be awkward, but it is the only means to describe these types of experiences in a

manner that is amicable to both realists and idealists. This phenomenal language mirrors how computer systems describe and represent entities within a virtual space. Using this language, the realist can object to Vasubandhu's claim with the inter-subjective agreement [3]. This argument centered around the fact that, barring special cases in which the experience is solely an impression (i.e: in the hairy moon example) agents seem to have remarkably similar sensory experiences. The realist claims that the different between these special impression-only experiences and *normal* sensory experience is that there is only a inter-subjective agreement in the latter scenario. In other words, the majority of observers are in agreement about the nature of the sensory experience and there are publicly accessible signifiers that can explain the minority's differences in sensory experience of the phenomena in question. From these facts, the realist claims, we can infer that normal sensory experience is independent of the observer's mind and therefore physical objects must exist. Another reply to Yogacaran idealism available to the realist is the argument from efficacy. This counterargument involves comparing sensory experiences which are known to be merely impressions with what are said to be normal sensory experiences. The normal sensory experiences will have clearly observable casual effects on the observer while the impressions have no lasting casual impact on the agent or their surroundings.

Vasubandhu counters these realist arguments with the phenomena of the *pretas*, beings cursed to consume urine, blood and other vile things. Vasubandhu explains that karma causes the pretas to perceive an ordinary river as brimming with fowl liquids just as it causes the sinner to perceive the existence of demons and other guardians of hell. The pretas also present a counterexample to the inter-subjective agreement, the impression of a river of filth and demons is not merely the sensory-experience of a single entity, but rather the phenomenal experience of everyone who has done evil in their past life.

Having shown shared karmic experience is an adequate substitute for physical substance for explaining the phenomena of intersubjective agreement. Vasubandhu continues by arguing that spatio-temporal determinacy can be explained without positing the existence of physical objects. Vasubandhu cites dreams as an example of mere impressions the realist might claim exhibit spatio-temporal determinacy and efficacy. Dream entities clearly seem to have a discrete location at a given time within the dream world. Similarly, erotic dreams can have the same sorts of physical effects as an analogous intimate encounter outside of a dream state. [3].

For many, Vasubandhu's counterexamples will hardly seem sufficient to justify such an outlandish scheme as to propose the nonexistence of physical matter. After all, if we accept a Buddhist concept of
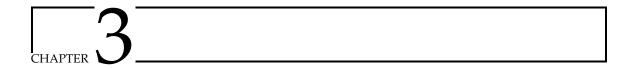
karma, we are still left with two competing theories of experience: the impressions only explanation in terms of karmic seeds and the theory of karmic casual laws. [3] Vasubandhu employs the *principle of lightness*, a principle from Buddhist philosophy which states that "given two competing theories each of which is equally good at explaining and predicting the relevant phenomena, choose the lighter theory, that is, the theory which posits the least number of unobservable entities" [3]. This principle motivates Vasubandhu's move to idealism, why should one posit the existence of material elements when the impressions-only theory has equal explanatory power? Realism introduces unnecessary complexity into our account of existence.

2.2 Awareness and Virtual Reality

A major factor when discussing the realism of a virtual environment is the agent or user's knowledge about said system. A user's sense of reality is highly dependent on their past experiences and subjective conception of reality. Just as the prisoners in Plato's allegory of the cave believe the shadows on the wall to be real, an agent who was born and raised experiencing only the sense-data of digital environment like the one depicted in the movie *The Matrix* will view sense-data from this machine as real, regardless of how unnatural or unreal it might appear to a human from "real world". Knowledge of whether one is a "brain in a vat" or within the "real world" is a major factor in determine of whether one doubts the reality of their experience.

2.2.1 Materialism and VR

Materialism holds that only finite physical substance embodies reality. For the materialist to accept virtual realism, they must adapt a strictly empiricist epistemological view, claiming sense-data is the sole source of justified true beliefs about the universe. For a materialist with this view, whatever they experience as the world around them is the world around them. A materialist born and raised in the Matrix would have no means (barring glitches in the Matrix) of deducing that she is experiencing sense-data that has been fed to her by a complex computer system. However, this view also is friendly to claims of virtual realism about contemporary VR technology. The output from a VR system is sense-data too. Interactions with objects in VR still have

CHAPTER 3

QUANTIFYING THE REALNESS OF VIRTUAL WORLDS

3.1 INTRODUCTION

Computer graphics have progressed immensely since the dawn of 3d computer graphics. Modern day computers are capable of rendering 3d models with with millions of polygons and employ complex shaders (computer programs that determine which colors and textures are used to draw the model) and other effects to create life-like images. However, realism in computer graphics is not merely a measure of the amount number of polygons or complexity of the shaders, physics engine or lighting effects. Small details like the uniqueness of terrain and objects, a lack of diversity in texture pattern and quality and other factors can have a significant impact on whether an environment appears realistic to a user. In this section, we shall survey and critique contemporary methods for quantitatively measuring realism in 3d computer worlds and posit our own measurement scheme.

The term "realistic" compasses a wide array of subjective and objective qualities. One key factor in determining whether an experience in a 3d environment is realistic for a user is immersion. Authors in the field of digital communication and human-computer factors use the term âĂIJimmersionâĂİ to describe a wide array of characteristics a digital space might have. Many authors use the term immersion to measure the ability of the system to "shut out:" or "pull" the user out of their awareness of physical reality. Slater and Wilbur (1997) note that an environment is more likely to feel immersive if it: a) offers high fidelity simulations through multiple sensory modalities, b) finely maps a userâĂŹs virtual bodily actions to their physical body's counterparts, and c) removes the participant from the external world through self-contained plots and narratives. These factors point to importance of sense of presence in making an immersive experience. However, other authors attempt to measure i through realistic graphics. Some researchers in this field attempt to quantify realism by taking

snapshots of virtual environments and measuring aspects of the resulting images such as gradient variance, color variance and shadow softness [4]. Others leverage qualitative data collected from user interviews to compare levels of realism between different virtual worlds and across hardware platforms. In this paper, we shall use the latter approach to measuring realness of virtual worlds. Our argument for the superiority of this methodology hinges on the fact that static screen-shots fail to account for the impact of animation, field of view, audio effects, type of control peripherals and other key aspects of user-experience on the immersiveness of an experience. A virtual environment's immersiveness is not merely a product of its graphics engine, physics engine and other software components but rather a composite of the proper application of software techniques and game design paired with a hardware system that well complements these software factors. As a result, it is improper to discuss the reality or immersive properties of a piece of software independently of the hardware platform it is running on top of.

3.2 EMOTION AND IMMERSION

As described in introduction to this section, the realism of a virtual environment is a holistic measurement of the immersiveness of the player's experience within the game world. Games with inferior graphics systems but which feature a highly captivating story or game play mechanic are easier to lose oneself within then a bland game with state-of-the-art graphics. Central to a game or other form of simulation's ability to captivate a user is its capacity to invoke an emotional response in a user or player. Games with primitive graphics and game mechanics can still have powerful emotive power, Aerith's death in the 1997 JRPG (Japanese RPG) Final Fantasy VII still prompts strong emotional reactions, despite its primitive character models and linear gameplay in comparison with modern day games in the same genre. [**?**] Clearly, the ability to invoke emotion is not something that can be measured using surface roughness or other such technical metrics. Storytelling is an essential aspect in creating an immersive experience. However, there are many games without plots that also offer a highly immersive experience for players. One such game is Minecraft, which offers players a 3d sandbox environment in which they must survive in a hostile world while building and exploring a procedurally generated voxel world containing caves mountains and countless other environments. This game features relatively primitive shaders and lighting effects and has a very minimal plot and few NPCs, yet the game still offers a highly immersive and addictive player experience. Players denote thousands of hours to building detailed and complex structures within the game world and express genuine stress and unease when faced with the in-game monsters,

Figure 3.1: Final Fantasy 7 Aerith Death Cutscene

despite their unrealistic appearances. [**?**] [**?**] A game's capacity to elicit an emotional response in

Figure 3.2: Minecraft Gameplay

the user is an essential and undeniable factor in its immersive qualities. We argue for

3.3 AN EXAMPLE OF MAKING A NEW SECTION AND GIVING IT A SHORT NAME

The \chapter and \subsection commands work in exactly the same manner. Each new chapter must have \chapter[short name]{chapter name} as its first line.

"Hey, wait a minute. What if I need to refer to that section? How can I do that?" It's actually as simple as adding\label{labelname} at the end of the \chapter command like\section[My new section]{An example of making a new section and giving it a short name}\label{sec:newsec}. Now I can refer to Section 3.3 by typing \ref{sec:newsec}. You can label just about anything and

Figure 3.3: Minecraft Hostile NPCs (source: http://www.minecraftlover.com)

refer to the label to get an automatically generated number for the item. This means that you need to come up with a labeling scheme before you start writing and stick with it.

Some other things you'll need to be able to do include italicizing and bolding text and creating lists. These are also easy to accomplish. For example I can use \emph or \textit to italicize text. To italicize homework I would enter \emph{homework} or \textit{homework} to produce *homework*. To obtain **bold** text you would use the \textbf command. And what about lists?

There are several kinds of lists (enumerated, itemized, and descriptive) and each has its own place and environment. An enumerated list is good for outlining or ordered lists:

```
\begin{enumerate}
\item First main idea
\begin{enumerate}
\item First subpoint
\item\label{enum:1b} Second subpoint
\end{enumerate}
\item Second main idea
\end{enumerate}
```

1. First main idea
    (a) First subpoint
    (b) Second subpoint
2. Second main idea

The itemized list is good for unordered lists or bullet points:

```
\begin{itemize}
\item Idea
\item Idea
\item Idea
\item Idea
\end{itemize}
```

- Idea
- Idea
- Idea
- Idea

And the descriptive list is good for definitions; however, `amsthm` already has a definition environment, and you will most likely not need the description environment. In any event, here is an example:

```
\begin{description}
\item[First item:] Idea
\item[Second item:] Idea
\item[Third item:] Idea
\end{description}
```

> **First item:** Idea
>
> **Second item:** Idea
>
> **Third item:** Idea

Notice the use of brackets in the last example. The brackets are optional and the text in the brackets is used as the label for the item. You should also note that you can label an item for later reference see 1b. There are several options for changing the format of the list environments and a package, `paralist`, for customizing lists which are described in section 3.3 of **?**].

3.4 THEOREMS, DEFINITIONS, EXAMPLES, OH MY!

The next thing you'll probably need to do is enter definitions, theorems, and examples. Below you will find some examples. On the left you will see the text typed into the document and on the right what it looks like when formatted. These examples are intended to give you a sense of what type of mathematical expressions LaTeX handles. You should look at Appendix **??** for a more complete discussion of entering mathematics. In the beginning you will not know all of the commands that you need to enter. Don't worry. Each of the suggested editors has a palette that shows you a picture of what you want and puts the correct commands into the document when you click the picture. As you look at these examples, keep it in mind that some of them use some user defined commands which can be found in `styles/personal.tex`. Now lets look at Definition 3.1 **??**, Theorem 3.1, and equation 3.3.

```
\begin{defn}[One of Ramanujan's
 third order mock theta
 functions]\label{def1}
 \begin{equation}\label{introf(q)}
 f(q)=1+\sum_{y=1}^{\infty}
 \frac{q^{y^2}}{(1+q)^2(1+q^2)^2
 \cdots (1+q^y)^2}.
 \end{equation}\end{defn}
```

Definition 3.1 ONE OF RAMANUJAN'S THIRD ORDER MOCK THETA FUNCTIONS:

$$f(q) = 1 + \sum_{y=1}^{\infty} \frac{q^{y^2}}{(1+q)^2(1+q^2)^2 \cdots (1+q^y)^2}. \qquad (3.1)$$

```
\begin{thm}[Watson's
transformation of
$f(q)$]\label{introwatthm}
\begin{equation}\label{introf}
\qrfac{q}{\infty}
\sum_{y=0}^{\infty} q^{y^2}
 \qrfac[-2]{- q}{y}=1+
\sum_{y=1}^{\infty}
\frac{(-1)^{y}
4q^{(3/2)y^2+
(1/2)y}}{(1+q^{y})}.
\end{equation}\end{thm}
```

Theorem 3.1 (Watson's transformation of $f(q)$).

$$(q)_\infty \sum_{y=0}^{\infty} q^{y^2} (-q)_y^{-2} = 1 + \sum_{y=1}^{\infty} \frac{(-1)^y 4q^{(3/2)y^2+(1/2)y}}{(1+q^y)}. \qquad (3.2)$$

This is a more complicated example which uses the \substack command to have multiple summation criteria.

```
\begin{align}\label{m.1diasumtwo}
\left[NUM\right]_1^{(\fl)}(q;b;
\bvec{x})=&\ q\sum\limits_{
\substack{ 0\leq r,t
\leq\fl-1}}
q^{r+t}\sum\limits_
 {\substack{{\lambda
 \vdash (r+t)}\\
 \lambda/1^r\in V_t\\
 \ell(\lambda)\leq \fl-1}}
 \mathrm{s}_{(b,\lambda)}
 (\bvec{x}).\end{align}
```

$$[NUM]_1^{(\ell)}(q;b;\mathbf{x}) = q \sum_{0 \leq r,t \leq \ell-1} q^{r+t} \sum_{\substack{\lambda \vdash (r+t) \\ \lambda/1^r \in V_t \\ \ell(\lambda) \leq \ell-1}} \mathrm{s}_{(b,\lambda)}(\mathbf{x}). \qquad (3.3)$$

Another thing that one might need to do is create piecewise definitions. This can be accomplished by using the cases environment. This example also uses the \intertext command to put text between displayed equations.

```
\begin{subequations}\label{2c1BP}
\begin{alignat}{2}\label{2c1BPa}
A_{y_1}:=&\begin{cases}
 1 &\text{for $y_1=0$},\\
\frac{-1)^{y_1}
4q^{y_1}q^{\binom{y_1}{2}}}
{\qrfac{q}{2y_1}(1+q^{y_1})}
&\text{for $y_1>0$}\end{cases}\\
\intertext{and} B_{y_1}:=&
\qrfac[-1]{-q}{y_1}\qrfac[-1]
{-q}{y_1}=\qrfac[-2]{-q}{y_1}
&.\label{2c1BPb}\end{alignat}
\end{subequations}
```

$$A_{y_1} := \begin{cases} 1 & \text{for } y_1 = 0, \\ \frac{-1)^{y_1} 4q^{y_1} q^{\binom{y_1}{2}}}{(q)_{2y_1}(1+q^{y_1})} & \text{for } y_1 > 0 \end{cases} \qquad (3.4a)$$

and

$$B_{y_1} := (-q)_{y_1}^{-1} (-q)_{y_1}^{-1} = (-q)_{y_1}^{-2} \qquad . \qquad (3.4b)$$

Finally, if you need to incorporate examples into your thesis you can do it using the example environment, as seen in Example 3.1.

```
\begin{ex}[An example example]
\label{ex:ex}
This is an example of including an
 example. Kind of silly isn't it.
 \end{ex}
```

> *Example* 3.1 (An example example). This is an example of including an example. Kind of silly isn't it.

3.5 PUTTING CODE IN THE MAIN BODY OF THE THESIS

There is one last textual item which Computer Science majors and probably some Mathematics majors will need to incorporate, pseudocode. To do this I would suggest using the \lstlisting environment. Below is an example set up for the listings package. You could put your modifications to this set up into the personal.tex file in the styles folder. Documentation on the listings package can be found in the doc folder with the documentation for the other packages.

```
\lstset{
        language =Pascal, % pick a language style
        emph={return,natural, numbers, integers, increasing},
        emphstyle={\bfseries},% choose other keywords and a format
        linewidth=.95{\textwidth}, breaklines=true,commentstyle=\textit,
        stringstyle=\upshape,showspaces=false,numbers=left,
        numberstyle=\tiny,basicstyle=\small,xleftmargin=30pt,
        breakautoindent=true,captionpos=b
        }
```

The listing in Listing 3.1 gives an algorithm for finding the largest even integer in a given list of n integers. I have used the mathescape option to be able to incorporate mathematics in the listing. The actual code put in the thesis is given first and the formatted output follows.

```
\begin{lstlisting}[mathescape, caption= Find the location
of the largest even integer in a list,label=largesteven]
procedure $largestevenlocation$($a_1, a_2, \ldots, a_n$: integers)
$k$:=0
$largest$:=-$\infty$
for $i$:=1 to $n$
  if ($a_i$ is even and $a_i>largest$) then
  begin
    $k$:=$i$
    $largest$:=$a_i$
  end
end
return $k$
\end{lstlisting}
```

```
1   procedure largestevenlocation(a_1, a_2, ..., a_n: integers)
2   k:=0
3   largest:=-∞
4   for i:=1 to n
5     if (a_i is even and a_i > largest) then
```

```
  6       begin
  7         k:=i
  8         largest:=aᵢ
  9       end
 10    end
 11    return  k
```

Listing 3.1: Find the location of the largest even integer in a list

The code in Listing 3.2 is an improvement on Binary search. The algorithm reduces the size of the search by a factor of four at each iteration. It provides another example of using the \lstlisting environment.

```
\begin{lstlisting}[mathescape,caption=Quartary search,
label=quartsearch]
procedure $quartarysearch$($x$: integer, $a_1, a_2,
 \ldots, a_n$: increasing integers)
$i$:=$1$
$j$:=$n$
while $i<j-2$
begin
  $l:=\lfloor(i+j)/4\rfloor$
  $m:=\lfloor(i+j)/2\rfloor$
  $u:=\lfloor3(i+j)/4\rfloor$
  if $x>a_m$ then
    if $x\leq a_u$ then
    begin
      $i:=m+1$
      $j:=u$
    end
    else
     $i:=u+1$
  else if $x>a_l$ then
    begin
      $i:=l+1$
      $j:=m$
    end
    else $j:=l$
end
if $x=a_i$ then $location:= i$
else if $x=a_j$ then $location:= j$
else if $x=a_{\lfloor(i+j)/2\rfloor}$ then
 $location:= \lfloor(i+j)/2\rfloor$
else $location:= 0$
return $location$
\end{lstlisting}
```

```
  1    procedure  quartarysearch (x :  integer ,  a₁, a₂, . . . , aₙ :  increasing  integers )
  2    i:=1
  3    j:=n
  4    while  i < j − 2
  5    begin
  6       l := ⌊(i + j)/4⌋
  7       m := ⌊(i + j)/2⌋
  8       u := ⌊3(i + j)/4⌋
```

```
 9      if  x > a_m  then
10         if  x ≤ a_u  then
11         begin
12             i := m + 1
13             j := u
14         end
15         else
16         i := u + 1
17      else if  x > a_l  then
18         begin
19             i := l + 1
20             j := m
21         end
22         else  j := l
23   end
24   if  x = a_i  then  location := i
25   else  if  x = a_j  then  location := j
26   else  if  x = a_⌊(i+j)/2⌋  then  location := ⌊(i + j)/2⌋
27   else  location := 0
28   return  location
```
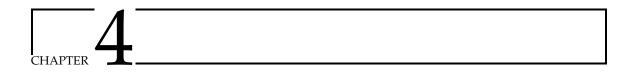
Listing 3.2: Quartary search

3.6 WHAT IS IN `USERNAME.TEX`

Before we move on let's talk a little bit about what is at the beginning of `username.tex`. The file starts with `\documentclass{woosterthesis}`, which must be at the beginning of every IS. In the brackets are options for the woosterthesis class. The options are the same as for the `book` class with some additional options `abstractonly`, `alltt`, `blacklinks`, `code`, `dropcaps`, `euler`, `guass`, `index`, `kaukecopyright`, `palatino`, `picins`, `verbatim`, and `xetex`. The `kaukecopyright` option will put the arch symbol with the word mark on the copyright page. The `blacklinks` option will make the hyperlinks in the PDF version of the thesis black and suitable for printing; normally the links are colored to provide visual clues to the reader. The `code` option will use `listings` style to format program code examples. The `abstractonly` option will allow you to print just the Abstract. The `palatino` option will use the `pxfonts` package which uses the Palatino fonts. The `picins` option will use the `floatflt` package to allow text to wrap around images. `index` will allow the `makeidx` package to be loaded so that if you have index entries they will be added to an index (this reqires additional steps). `dropcaps` loads the `letterine` package for doing dropped capitals and `alltt` loads the `alltt` for using typewriter type in various ways. `verbatim` allows one to set verbatim what is entered. `euler` and `guass` load the `woofncychap` package with the named option which will change the look of chapter headings. Finally `xetex` will allow you to use the XeTeX extension of TEX for easy use of system fonts. Adding or deleting options from the comma separated list will change

the appearance of the document and some options should only be used after consulting your advisor.

Now let's move on to some other things that you'll need to deal with: figures, pictures, and tables.

CHAPTER 4

WORKING WITH FIGURES AND TABLES

4.1 GETTING A SIMPLE FIGURE IN THE DOCUMENT

In this chapter we want to talk about including figures and tables in the document. To insert a simple figure you can enter something like

```
\begin{figure}[!ht]
\begin{center}
\woopic{picture3}{.8}
\end{center}
\caption{Our first
 picture}\label{first}
\end{figure}
```
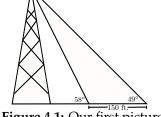

Figure 4.1: Our first picture

The !ht tell LaTeX to try and place the figure here no matter what or at the top of the next page. The \woopic command takes the name of the picture as the first argument and the scaling factor as the second argument. The scaling factor must be between zero and one and the figure name must have *no spaces*. Your figures can be in one of three formats: jpg, tif, or pdf. Captions are placed below the figure and your label should be placed after the caption.

In the next example we are using the woosterthesis option picins to typeset a picture inside a paragraph and have the text wrap around the figure. This option loads the wrapfig package. One thing to note is that the figures placed in this manner do not float with the other figures and as such numbering could get out of sequence. Keep an eye out for such behavior. This technique should be used sparingly in your thesis.

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```
\newcommand{\sample}{Some text that is reused over and over
 again in the example. }
\begin{wrapfigure}{r}{2.2in}
\woopic{picture2}{.4}
\caption{Conchoid.}
\end{wrapfigure}
\sample\sample\sample\sample
```

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.

Some text that is reused over and over again in the example.
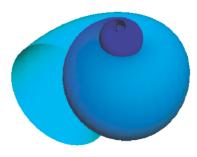

Figure 4.2: Conchoid.

4.1.1 MINIPAGES

You can also create minipages in your documents to accomplish more complicated formatting. For example you could try the following which produces Figure 4.3.

```
\begin{minipage}[t][3 in][t]{1 in}
This is a minipage which is 3 in tall and 1 in wide.
 Top Text Text Text Text.\end{minipage}\hfill
\begin{minipage}[t][3 in][c]{1 in}
This is a minipage which is 3 in tall and 1 in wide.
 Center Text Text Text Text.\end{minipage}\hfill
\begin{minipage}[t][3 in][b]{1 in}
This is a minipage which is 3 in tall and 1 in wide.
 Bottom Text Text Text Text.\end{minipage}
```

In the example above, the syntax `\begin{minipage}[t][3 in][t]{1 in}` follows the convention

`\begin{minipage}[minipageposition][height][textposition]{width}`

4.1.1.1 HOW TO GET MORE THAN ONE PICTURE IN THE SAME FIGURE

You can use minipages to put more than one picture in a figure. Here is an example of how to do this.

```
\begin{minipage}[!ht]{6cm}
\woopic{picture1}{.4}
```

This is a mini-
page which is 3
in tall and 1 in
wide. Top Text
Text Text Text.

This is a mini-
page which is
3 in tall and 1
in wide. Cen-
ter Text Text Text
Text.

This is a mini-
page which is 3
in tall and 1 in
wide. Bottom
Text Text Text
Text.

Figure 4.3: Minipage example

```
\par
\caption[What goes in the List of Figures]{Left}
\end{minipage}
\hfill
\begin{minipage}[!ht]{6cm}
\woopic{picture2}{.4}
\end{picture}\par
\caption{Right}
\end{minipage}
```
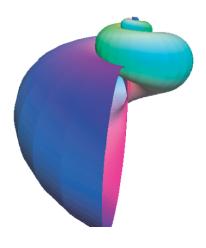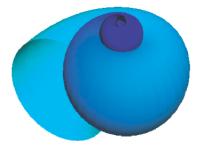

Figure 4.4: Left

Figure 4.5: Right

You can also use the `subfigure` package to do this.

```
\begin{figure}[!ht]\centering
\subfigure[What goes in the List][Large conchoid]
{\woopic{picture1}{.4}\label{fig3:left}}
\qquad
\subfigure[What goes in the List][Small conchoid]
{\woopic{picture2}{.4}\label{fig3:right}}
\caption{Two pictures in one figure}\label{fig3}
\end{figure}
```
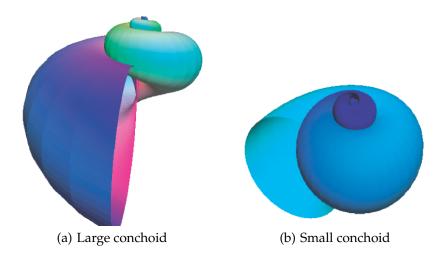

(a) Large conchoid   (b) Small conchoid

Figure 4.6: Two pictures in one figure

We should now be able to refer to either Figure 4.6 (a) or Figure 4.6 (b) using the labels we gave to the left and right images.

The reader is referred to Chapters 8, 9, and 16 of **?**] or to Chapters 6 and 10 of **?**] for a complete discussion of figures and graphics.

4.2 TABLES

Tables are fairly easy to set up. Here is a simple table

```
\begin{table}[!ht]
\begin{center}
\begin{tabular}{r l}
  $\underline{\textnormal{District}}$ &
  $\underline{\textnormal{Population}}$\\
   Applewood & 8280 \\
   Boxwood & 4600  \\
   Central & 5220
   \end{tabular}\caption{Our first table}
   \end{center}
\end{table}
```

District	Population
Applewood	8280
Boxwood	4600
Central	5220

Table 4.1: Our first table

In \begin{tabular}{r l} the two "r" and "l" indicate that we have two columns with right and left aligned entries and no lines dividing cells or around the table. I can make the table look more like a spreadsheet by doing

```
\begin{table}[!ht]
\begin{center}
\begin{tabular}{|r|l|}
\hline
  {\textnormal{District}} &
  {\textnormal{Population}}\\ \hline
   Applewood & 8280 \\ \hline
   Boxwood & 4600  \\ \hline
   Central & 5220\\ \hline
   \end{tabular}\caption{Our first table again}
   \end{center}
\end{table}
```

District	Population
Applewood	8280
Boxwood	4600
Central	5220

Table 4.2: Our first table again

Here is a more complicated example of a table.

```
\begin{table}[!ht]
\centerline{
\begin{tabular}{|l||r|r|r|r|} \hline
\emph{Reprojection} & \multicolumn{3}{|c|}{\emph{Largest
 Reduction of Curvature}}
  & \emph{Average} \\ \cline{2-4}
\emph{Method} & \emph{Original} & \emph{Reprojected} &
 \emph{at} &
  \emph{Reduction} \\
 & \emph{Curvature} & \emph{Curvature} &
  \emph{Rotation} & \emph{of Curvature} \\
  \hline \hline
ZEEL & 0.0358 & 0.0245 &
 $\degree{45}$ & 0.0050 \\ \hline
```

```
ZEEL ext.\ & 0.0358 & 0.0245 &
 $\degree{45}$ & 0.0059 \\ \hline
Regridding & 0.0428 & 0.0166 &
 $\degree{75}$ & 0.0159 \\ \hline
Block & 0.0358 & 0.0103 &
 $\degree{45}$ & 0.0163 \\ \hline
\end{tabular}}
\caption{Reduction of curvature by each
 reprojection method\label{tbl:kreduce}}
\end{table}
```

| *Reprojection* | *Largest Reduction of Curvature* | | | *Average* |
| *Method* | *Original* | *Reprojected* | *at* | *Reduction* |
	Curvature	*Curvature*	*Rotation*	*of Curvature*
ZEEL	0.0358	0.0245	45°	0.0050
ZEEL ext.	0.0358	0.0245	45°	0.0059
Regridding	0.0428	0.0166	75°	0.0159
Block	0.0358	0.0103	45°	0.0163

Table 4.3: Reduction of curvature by each reprojection method

Please refer to Chapter 6 of **?**] for a complete discussion of tables and tabular environments.

5

CHAPTER

WORKING WITH BIBLIOGRAPHIES AND INDICIES

I would highly recommend that you use BibTEX to create your bibliography. BibTEX processes a special .bib file. The .bib file is where you enter your bibliographic information. A sample entry looks something like

```
@article{feu02,
author= {Thomas~Feuerstack},
title= {Introduction to pdf{\TeX{}}},
journal= {TUGboat},
volume= {23},
pages= {329--334},
number= {3/4},
url= {http://www.tug.org/TUGboat/Articles/tb23-3-4/tb75feu.pdf},
year= 2002}
```

or

```
@book{mgbcr04,
author= {Frank~Mittelbach and Michel~Goossens and
Johannes~Braams and David~Carlisle and Chris~Rowley},
title= {The \LaTeX\ Companion},
publisher= {Addison Wesley Professional},
edition= {2nd},
address= {New York},
year= 2004}
```

For a Web site I would recommend the following

```
@misc{brei04,
author =   {Jon~Breitenbucher},
title =   {{W}ooster related {L}a{T}e{X} files},
url =   {http://jbreitenbuch.wooster.edu/~jonb/latex/},
howpublished= {World Wide Web},
year= 2004,
note =   {Accessed on 03/11/2004}}
```

You can make a reference by typing `\citet{mgbcr04}` to produce **?**]. Other forms for citation include `\citep{mgbcr04}` or `\citeauthor {mgbcr04}` to produce [**?**] or **?** respectively. You can consult **?**] or **?**] to find out how to format entries in the .bib file and what options each reference type has.[1]

Indicies are also relatively easy to create. If I wanted to have Wooster show up in the index, I would enter `Wooster\index{Wooster}` in my source file. I could create a subentry for User Services by entering `User Services\index{Wooster!User Services}`. A subsubentry for Help Desk would be entered as `\index{Wooster!User Services!Help Desk}`.

To create the index one needs to make sure to uncomment the `\makeindex` command in the `username.tex` file. One also needs to uncomment the makeidx entry in the `styles/packages.tex` file and then run the Makeindex program. Consult **?**] or **?**] for further information.

---

[1]You could also use footnotes if your department called for that.

REFERENCES

1. George Berkeley. *A treatise concerning the principles of human knowledge*. Dover Publications, Mineola, N.Y, 2003. ISBN 978-0486432533. 4

2. David Lewis. *On the plurality of worlds*. B. Blackwell, Oxford, UK New York, NY, USA, 1986. ISBN 0631139931. 5

3. Mark Siderits. *Buddhism as philosophy : an introduction*. Ashgate Hackett Pub. Co, Aldershot, England Indianapolis, IN, 2007. ISBN 978-0872208735. 5, 6, 7

4. Norman Wang and Wendy Doube. How real is really? a perceptually motivated system for quantifying visual realism in digital images. In *Proceedings of the 2011 International Conference on Multimedia and Signal Processing - Volume 02*, CMSP '11, pages 141–149, Washington, DC, USA, 2011. IEEE Computer Society. ISBN 978-0-7695-4356-7. doi: 10.1109/CMSP.2011.172. URL http://dx.doi.org/10.1109/CMSP.2011.172. 9