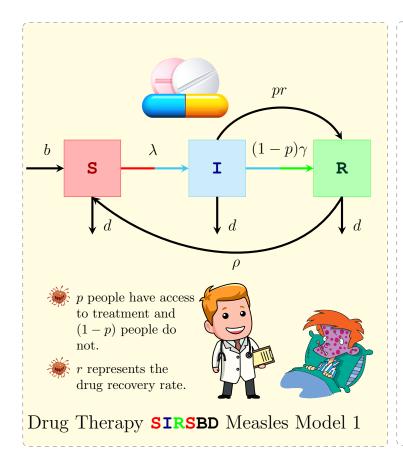


## System of ODEs

$$\frac{d\mathbf{S}}{dt} = b\mathbf{N} - \beta\mathbf{IS} - d\mathbf{S} + \rho\mathbf{R} \tag{1.1}$$

$$\frac{d\mathbf{I}}{dt} = \beta \mathbf{IS} - \gamma \mathbf{I} - d\mathbf{I} \tag{1.2}$$

$$\frac{d\mathbf{R}}{dt} = \gamma \mathbf{I} - d\mathbf{R} - \rho \mathbf{R} \tag{1.3}$$



## System of ODEs

We define the parameter  $\mu = d = b$ .

$$\frac{d\mathbf{S}}{dt} = \mu \mathbf{N} - \beta \mathbf{IS} - \mu \mathbf{S} + \rho \mathbf{R}$$

$$(1.4)$$

$$\frac{d\mathbf{I}}{dt} = \beta \mathbf{IS} - pr\mathbf{I} - \mu \mathbf{I}$$
$$- (1-p)\gamma \mathbf{I}$$
(1.5)

$$\begin{split} \frac{d\mathbf{R}}{dt} &= pr\mathbf{I} - \mu\mathbf{R} - \rho\mathbf{R} \\ &+ (1-p)\gamma\mathbf{I} \end{split} \tag{1.6}$$