

Name: \_\_\_\_\_

Date: \_\_\_\_\_

## Class/Home worksheet: Alg2H

## Quadratic equation: using factoring and completing the square.

(book chapter 8, page 342 to 345)

An equation of the type

$$ax^2 + bx + c = 0$$

where a, b, and c are constants, and  $a \neq 0$ , is called **standard form of the quadratic equation**.

Solve:

$$3x^2 + 5x = 0$$

$$x(3x+5)=0$$

$$x=0 \text{ or } x=-\frac{5}{3}$$

\*

Solve:

$$2x^2 + 7x = 0$$

$$x(2x+7)=0$$

$$x=0 \text{ or } x=-\frac{7}{2}$$

Solve:

$$5x^2 - 7 = 0$$

$$5x^2 = 7$$

$$x^2 = \frac{7}{5} \Rightarrow x = \pm\sqrt{\frac{7}{5}}$$

\*

Solve:

$$3x^2 - 6 = 0$$

$$3x^2 = 6$$

$$x^2 = 2 \Rightarrow x = \pm\sqrt{2}$$

Solve:

$$6x^2 - 7x + 2 = 0$$

M	A	T
12	-7	-4-3

$$6x^2 - 3x - 4x + 2 = 0$$

$$3x(2x-1) - 2(2x-1) = 0$$

$$(3x-2)(2x-1) = 0$$

$$x = \frac{2}{3} \text{ or } x = \frac{1}{2}$$

\*

Solve:

$$14x^2 + 2 = 11x$$

$$14x^2 - 11x + 2 = 0$$

M	A	T
28	-11	-4-7

$$14x^2 - 7x - 4x + 2 = 0$$

$$7x(2x-1) - 2(2x-1) = 0$$

$$(7x-2)(2x-1) = 0$$

$$x = \frac{2}{7} \text{ or } x = \frac{1}{2}$$

## Completing the Square (P. 343)

$$A^2 + 2AB + B^2 = (A + B)^2$$

Solve by completing the square:

$$x^2 - 2x - 8 = 0$$

$$\begin{aligned} x^2 - 2x &= 8 \\ x^2 - 2x + 1 &= 8 + 1 \\ (x - 1)^2 &= 9 \end{aligned}$$

$$\begin{aligned} x - 1 &= 3 \quad \text{or} \quad x - 1 = -3 \\ \boxed{x = 4 \quad \text{or} \quad x = -2} \end{aligned}$$

Solve by completing the square:

$$4x^2 + 12x - 7 = 0$$

$$\begin{aligned} 4x^2 + 12x &= 7 \\ x^2 + 3x &= \frac{7}{4} \\ x^2 + 3x + \left(\frac{3}{2}\right)^2 &= \frac{7}{4} + \left(\frac{3}{2}\right)^2 \\ \left(x + \frac{3}{2}\right)^2 &= \frac{7}{4} + \frac{9}{4} \end{aligned}$$

$$\begin{aligned} \left(x + \frac{3}{2}\right)^2 &= 4 \\ x + \frac{3}{2} &= 2 \quad \text{or} \quad x + \frac{3}{2} = -2 \\ \boxed{x = 0.5 \quad \text{or} \quad x = -3.5} \end{aligned}$$

Solve by completing the square:

$$3x^2 + 18x + 24 = 0$$

$$\begin{aligned} x^2 + 6x + 8 &= 0 \\ x^2 + 6x &= -8 \\ x^2 + 6x + 9 &= -8 + 9 \\ x^2 + 6x + 9 &= 1 \end{aligned}$$

$$\begin{aligned} (x + 3)^2 &= 1 \\ x + 3 &= 1 \quad \text{or} \quad x + 3 = -1 \\ \boxed{x = -2 \quad \text{or} \quad x = -4} \end{aligned}$$

From the book, Page 345-6

(1) Solve:  $7x^2 - 3x = 0$

$$x(7x-3)=0$$

$$\boxed{x=0 \text{ or } x=\frac{3}{7}}$$

(6) Solve:  $6x^2 - x - 2 = 0$

M	A	T
-12	-1	-4, 3

$$(3x-4)(2x+1)=0$$

$$6x^2 + 3x - 4x - 2 = 0$$

$$3x(2x+1) - 2(2x+1) = 0$$

$$\boxed{x=\frac{2}{3} \text{ or } x=-\frac{1}{2}}$$

(11) Solve:  $3x^2 + 7x = 20$

$$3x^2 + 7x - 20 = 0$$

M	A	T
-60	7	42, -5

$$\boxed{x=-4 \text{ or } x=\frac{5}{3}}$$

$$3x^2 + 12x - 5x - 20 = 0$$

$$3x(x+4) - 5(x+4) = 0$$

$$(3x-5)(x+4) = 0$$

(18) Solve:  $4x^2 = 20$

$$x^2 = 5$$

$$\boxed{x=\sqrt{5} \text{ or } x=-\sqrt{5}}$$

(42) Solve by completing the square:

$$x^2 - 4x + 1 = 0$$

$$x^2 - 4x = -1$$

$$x^2 - 4x + 4 = -1 + 4$$

$$(x-2)^2 = +3$$

$$(x-2)^2 = \sqrt{3}$$

$$x-2 = +\sqrt{3} \text{ or } x-2 = -\sqrt{3}$$

$$\boxed{x=2+\sqrt{3} \text{ or } x=2-\sqrt{3}}$$

(43) Solve by completing the square:

$$y^2 + 6y - 3 = 0$$

$$y^2 + 6y = 3$$

$$y^2 + 6y + 9 = 3 + 9$$

$$(y+3)^2 = 12$$

$$y+3 = \pm\sqrt{12}$$

$$\boxed{y = -3 + \sqrt{12} \text{ or } y = -3 - \sqrt{12}}$$