

En el análisis de algunos circuitos eléctricos se utiliza la fórmula $I = \frac{V}{\sqrt{R^2 + L^2 \omega^2}}$, donde I es la corriente, V la tensión o voltaje, R la resistencia, L la inductancia y ω una constante positiva. Calcule e interprete $\frac{\partial I}{\partial R}$ y $\frac{\partial I}{\partial L}$

$$I = \frac{V}{\sqrt{R^2 + L^2 \omega^2}}$$

$$U = R^2 + L^2 \omega^2 \quad \sqrt{U} = (U)^{1/2} \quad \wedge \quad \frac{d}{dR} \sqrt{U} = \frac{1}{2} U^{-1/2} \cdot \frac{dU}{dR}$$

$$U \quad R : \frac{dU}{dR} = 2R$$

$$\frac{d}{dR} \sqrt{R^2 + L^2 \omega^2} = \frac{1}{2} (R^2 + L^2 \omega^2)^{-1/2} \cdot 2R = \frac{R}{\sqrt{R^2 + L^2 \omega^2}}$$

$$\frac{\partial I}{\partial R} = \frac{0 \cdot \sqrt{R^2 + L^2 \omega^2} - V \cdot \frac{R}{\sqrt{R^2 + L^2 \omega^2}}}{R^2 + L^2 \omega^2} = - \frac{V R}{(R^2 + L^2 \omega^2)^{3/2}}$$

$$\frac{\partial I}{\partial R} = \frac{V R}{(R^2 + L^2 \omega^2)^{3/2}}$$

$$\frac{\partial I}{\partial L} \quad L : \frac{dU}{dL} = 2L \omega^2$$

$$\frac{d}{dL} \sqrt{R^2 + L^2 \omega^2} = \frac{1}{2} (R^2 + L^2 \omega^2)^{-1/2} \cdot 2L \omega^2 = \frac{L \omega^2}{\sqrt{R^2 + L^2 \omega^2}}$$

$$\frac{\partial I}{\partial L} = \frac{0 \cdot \sqrt{R^2 + L^2 \omega^2} - V \cdot \frac{L \omega^2}{\sqrt{R^2 + L^2 \omega^2}}}{R^2 + L^2 \omega^2} = - \frac{V L \omega^2}{(R^2 + L^2 \omega^2)^{3/2}}$$

$$\boxed{\frac{\partial I}{\partial L} = - \frac{V L \omega^2}{(R^2 + L^2 \omega^2)^{3/2}}}$$