

Evalúe el límite de $f(x, y) = \frac{y^3}{5x^4 + y^2}$ cuando (x, y) tiende a $(0, 0)$

$$x = 0$$

$$f(0, y) = \frac{y^3}{5 \cdot 0^4 + y^2} = \frac{y^3}{y^2} = y$$

$$\lim_{y \rightarrow 0} y = 0$$

$$y = 0$$

$$f(x, 0) = \frac{0^3}{5x^4 + 0^2} = 0$$

$$\lim_{(x \rightarrow 0)} 0 = 0$$

$$x = x^2$$
$$f(x, x^2) = \frac{(x^2)^3}{5x^4 + (x^2)^2} = \frac{x^6}{5x^4 + x^4} = \frac{x^6}{6x^4} = \frac{x^2}{6}$$

$$\lim_{x \rightarrow 0} \frac{x^2}{6} = 0$$

$$\lim f(x, y) = \frac{y^3}{5x^4 + y^2} \text{ cuando } (x, y) \rightarrow (0, 0) \text{ no está definido}$$