

LAB #12 - RECURSION

PART 1: Exercises

1. Add whatever necessary to fix the following method so that $f(3)$ equals 10.

```
public static int f(int n) {  
    return f(n - 1) + 3;  
}
```

```
if (n == 0)  
    return 1;  
else  
    return f(n-1) + 3;
```

$f(3) + 3$

$f(2) + 3$

$f(1) + 3$

$f(0) + 1$

2. If the following method is called with a value of 73 for n , what is the resulting output?

```
public static void f(int n) {  
    if (n > 0) {  
        f(n / 5);  
        System.out.print(n % 5);  
    }  
}
```

2 4 3

$f(73)$ 3

$f(14)$ 4

$f(2)$ 2

(0)

3. In problems 1 - 3, show the output that will be displayed by the call $f(123)$;

```
1. public static void f(int n) {  
    if (n != 0)  
        f(n / 10);  
    System.out.print(n % 10);  
}
```

1 2 3

$f(123)$ 3

$f(12)$ 2

$f(1)$ 1

$f(0)$

```
2. public static void f(int n) {  
    System.out.print(n % 10);  
    if (n != 0)  
        f(n / 10);  
}
```

3 2 1

$f(123)$ 3

$f(12)$ 2

$f(1)$ 1

$f(0)$

```
3. public static void f(int n) {  
    System.out.print(n % 10);  
    if (n != 0)  
        f(n / 10);  
    System.out.print(n % 10);  
}
```

3 2 1 1 2 3

4. Given the following recursive method:

```
public static int f(int num) {  
    if (num == 0)  
        return 0;  
    else  
        return num + f(num + 1);  
}
```

$f(-5)$ -5

$f(-4)$ -4

$f(-3)$ -3

$f(-2)$ -1

$f(-1)$ -1

$f(0)$ 0

- Is there a constraint on the values that can be passed as parameters for this function?
- Is $f(7)$ a good call? If so, what is returned from the function?
- Is $f(0)$ a good call? If so, what is returned from the function?
- Is $f(-5)$ a good call? If so, what is returned from the function?

Only negatives.

Infinite

0

-14

5. Given the recursive method (base and limit are nonnegative numbers):

```
public static int f(int base, int limit){
    if(base > limit)
        return -1;
    else if (base == limit)
        return 1;
    else
        return base * f(base + 1, limit);
}
```

Base

Recursive

a) Identify the base case(s) for this method. Identify the recursive case(s) for this method.

b) Show what would be displayed by the following calls.

```
System.out.println(f(14,10));
System.out.println(f(4,7));
System.out.println(f(0,0));
```

-1
120
1

f(4, 7) *4
f(5, 7) *5
f(6, 7) *6
f(7, 7) *-1

6. Consider the method below:

```
public static void f(char param1, char param2) {
    if (param1 != param2) {
        param1++;
        param2--;
        f(param1, param2);
        System.out.print(param1);
        System.out.print(param2);
    }
}
```

f(A, G)
f(B, F) BF
f(C, E) CE
f(D, D) DD

Show all output resulting from the method call `f('A', 'G');`

DDCEBF

7. Given the following recursive method:

```
public static int f(int num) {
    if(num < 2)
        return 1;
    else if(num % 2 == 0)
        return f(num / 2);
    else
        return f(3 * num + 1);
}
```

f(7)
f(22)
f(11)
f(34)
f(17)
...

f(8)
f(4)
f(2)
f(1)

1. What problems come up in verifying this method? Odd numbers may be infinite.

2. How many recursive calls are made by the following initial calls?

```
System.out.println(f(7));
System.out.println(f(8));
System.out.println(f(15));
System.out.println(f(16));
```

Infinite
3
Infinite
4

8. Given the following recursive method:

```
public static int f(int num) {
    if(num == 1)
        return 0;
    else if(num % 2 == 1)
        return 1 + f(3 * num + 1);
    else
        return 100 + f(num / 2);
}
```

f(3)
f(10) +1
f(5) +100
f(16) +1
f(8) +100
f(4) +100
f(2) +100
f(0) +100

What is returned from the method after the call for `f(3)`?

9. Given the following recursive method:

```
public static int f(int x, int y) { // x > y
    if(x % y == 0)
        return y;
    else
        return f(y, x % y);
}
```

f(36, 16)
f(16, 4) 4

What is returned from the method after the call for f(36, 16)?

4

10. Given the following recursive method:

```
public static int f(int num) {
    if(num != 5)
        return 3 + f(num + 1);
    else
        return 5;
}
```

f(1) +3
f(2) +3
f(3) +3
f(4) +3
f(5) +5

What is returned from the method after the call for f(1)?

17

11. Given the following recursive method:

```
public static void f(int x) {
    if(x > 0 && x < 10){
        System.out.print(x + " ");
        f(x + 1);
    }
}
```

Nothing, 5 6 7 8 9, Nothing, Nothing

What will be the output for the calls: f(0), f(5), f(10), and f(-5)?

12. Given the following recursive method:

```
public static int f(int x, int y) {
    if(x == y)
        return x;
    else if (x > y)
        return x + y;
    else
        return f(x + 1, y - 1);
}
```

f(5, 10)
f(6, 9)
f(7, 8)
f(8, 7) 15

f(3, 9)
f(4, 8)
f(5, 7)
f(6, 6) 6

What will be the output for the calls: f(5, 10), and f(3, 9)?

13. Given the following recursive method:

```
public static int f(int x, int y) {
    if(x < y)
        return x;
    else
        return f(x - y, y);
}
```

7, 0, 6, 3, 9

For each call below, indicate the value returned: f(7, 10), f(16, 2), f(15, 9), f(27, 4), f(59, 10)
This method does.... what? Subtracts the second number from the first until the first is less than the first.

14. Given the following recursive method:

```
public static void f(int x) {  
    if(x <= 1)  
        System.out.print(x + " ");  
    else {  
        f(x / 2);  
        System.out.print(x + " ");  
    }  
}
```

What will be the output for the call: $f(7)$? **1**

PART 2: Programming

Write a program to do the testing for the following methods. Make sure you also have a method to handle input validation (positive integer, $n > 0$).

1. A method to find the sum of digits in any integer (iterative method)
2. A method to find the sum of digits in any integer (recursive method)
3. A method to display a number in binary (iterative method)
4. A method to display a number in binary (recursive method)
5. A method to return the string representation of a number in any base (iterative method)
6. A method to return the string representation of a number in any base (recursive method)

SAMPLE OUTPUT:

```
Enter a positive integer: weqrwer  
WRONG TYPE! Not a positive integer! REENTER: 123.45  
WRONG TYPE! Not a positive integer! REENTER: -12345  
INVALID! Should be positive! REENTER: 1024  
Enter a positive integer for base: 2  
Sum of digits for 1024 is 7 (iterative solution)  
Sum of digits for 1024 is 7 (recursive solution)  
1024 in binary code is 10000000000 (iterative solution)  
1024 in binary code is 10000000000 (recursive solution)  
1024 in base 2 is 10000000000 (iterative solution)  
1024 in base 2 is 10000000000 (recursive solution)  
Do you want to continue (y/Y): y  
Enter a positive integer: 256  
Enter a positive integer for base: 4  
Sum of digits for 256 is 13 (iterative solution)  
Sum of digits for 256 is 13 (recursive solution)  
256 in binary code is 100000000 (iterative solution)  
256 in binary code is 100000000 (recursive solution)  
256 in base 4 is 10000 (iterative solution)  
256 in base 4 is 10000 (recursive solution)  
Do you want to continue (y/Y): y  
Enter a positive integer: 123456789  
Enter a positive integer for base: 1234  
Sum of digits for 123456789 is 45 (iterative solution)  
Sum of digits for 123456789 is 45 (recursive solution)  
123456789 in binary code is 111010110111100110100010101 (iterative solution)  
123456789 in binary code is 111010110111100110100010101 (recursive solution)  
123456789 in base 1234 is 819225 (iterative solution)  
123456789 in base 1234 is 819225 (recursive solution)  
Do you want to continue (y/Y): y  
Enter a positive integer: 257  
Enter a positive integer for base: 4  
Sum of digits for 257 is 14 (iterative solution)  
Sum of digits for 257 is 14 (recursive solution)  
257 in binary code is 100000001 (iterative solution)
```

```
257 in binary code is 100000001(recursive solution)
257 in base 4 is 10001 (iterative solution)
257 in base 4 is 10001 (recursive solution)
Do you want to continue (y/Y): n
```

Notes:

- A.** The lab will NOT be graded, but you have to submit good quality work in order to get credit.
- B.** The lab should be completed by the start of the next scheduled lab class. Save the **.java** files on your disk and e-mail them (attachments) to Rohan Patel (rpatel27@students.towson.edu)
- Very important:** Make sure that you have COSC 237.section, your name, and Lab#12 in the *Subject* box of your e-mail.
- C.** In case you have any problems, contact the instructor or the TA for assistance.