Experiments and Events:

Def: An experiment is a process whose outcome is not known in advance with certainy.

Sample Space: Collection of all possible outcomes of an experiment. S or Ω . Each outcome is an element of the sample space $s \in S$.

Operations:

Union:
$$x \in S : A \cup B = \{x \in A \text{ or } x \in B\}$$

$$A \cup B = B \cup A$$

$$A \cup A = A$$

$$A \cup \emptyset = A$$

$$A \cup S = S$$

$$A \subset B \Rightarrow A \cup B = B$$

$$A_1, A_2, \dots, A_n \Rightarrow A_1 \cup A_2 \cup \dots \cup A_n = \bigcup_{i=1}^{i=n} A_i$$

$$\bigcup_{i=1}^{\infty} A_i \rightarrow \bigcup_{i \in I} A_i$$

$$(A \cup B) \cup C = A \cup (B \cup C) = A \cup B \cup C$$

Intersections: $A \cap B = \{x \in A \text{ and } x \in B\} = AB$